

## Electronic Supplementary Information

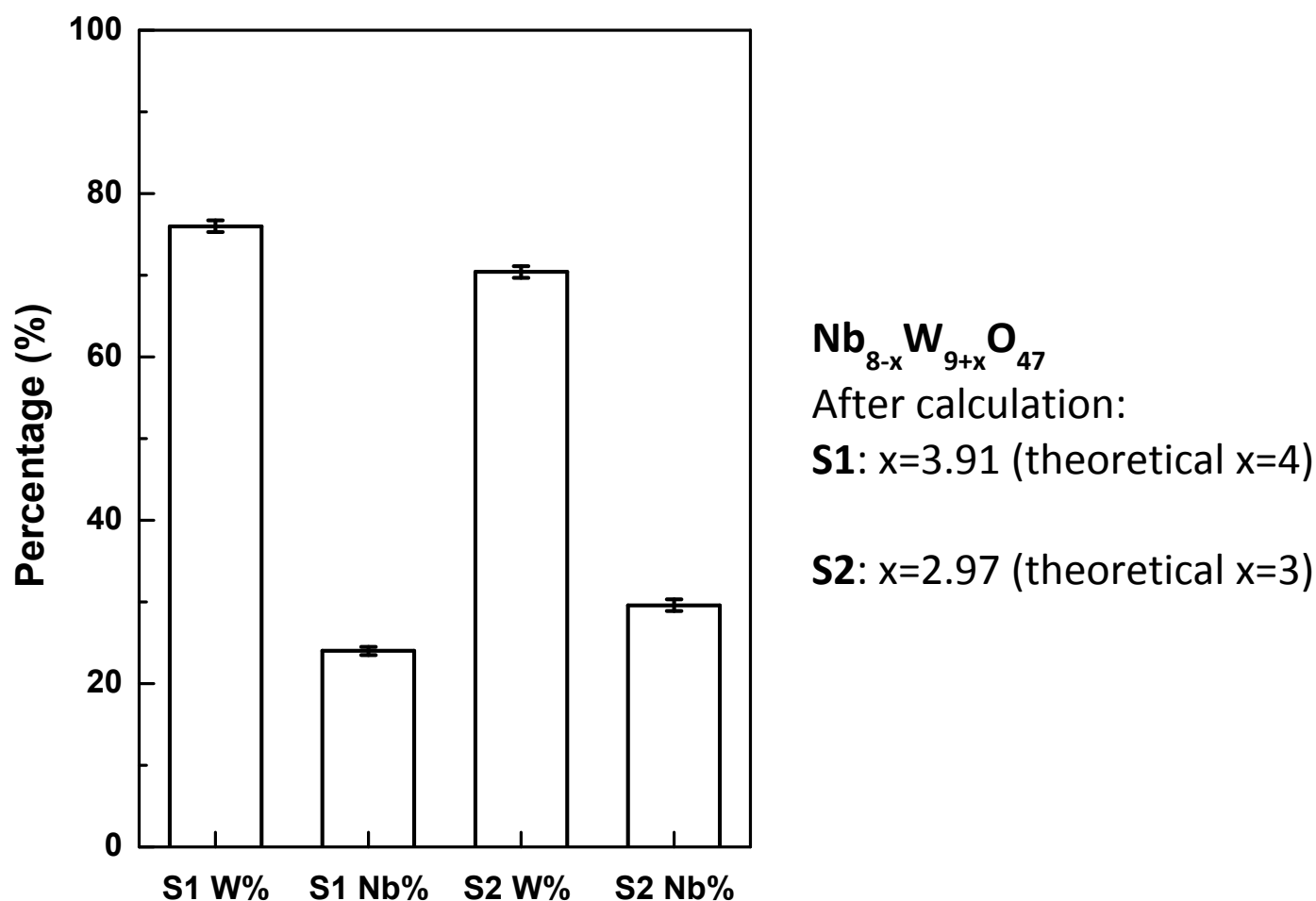
### Thermal stability and enhanced thermoelectric properties of the tetragonal tungsten bronzes $\text{Nb}_{8-x}\text{W}_{9+x}\text{O}_{47}$ ( $0 < x < 5$ )

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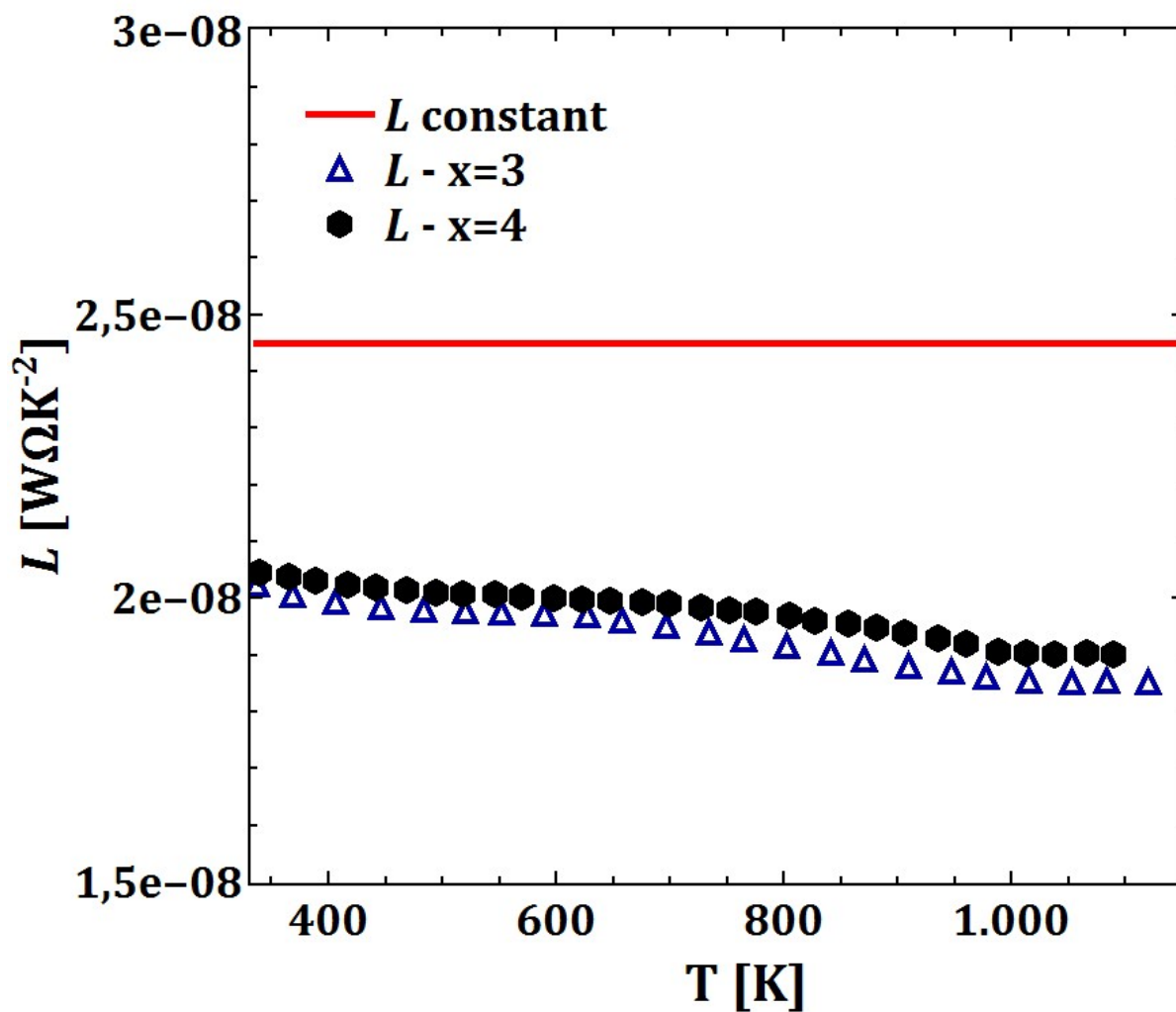
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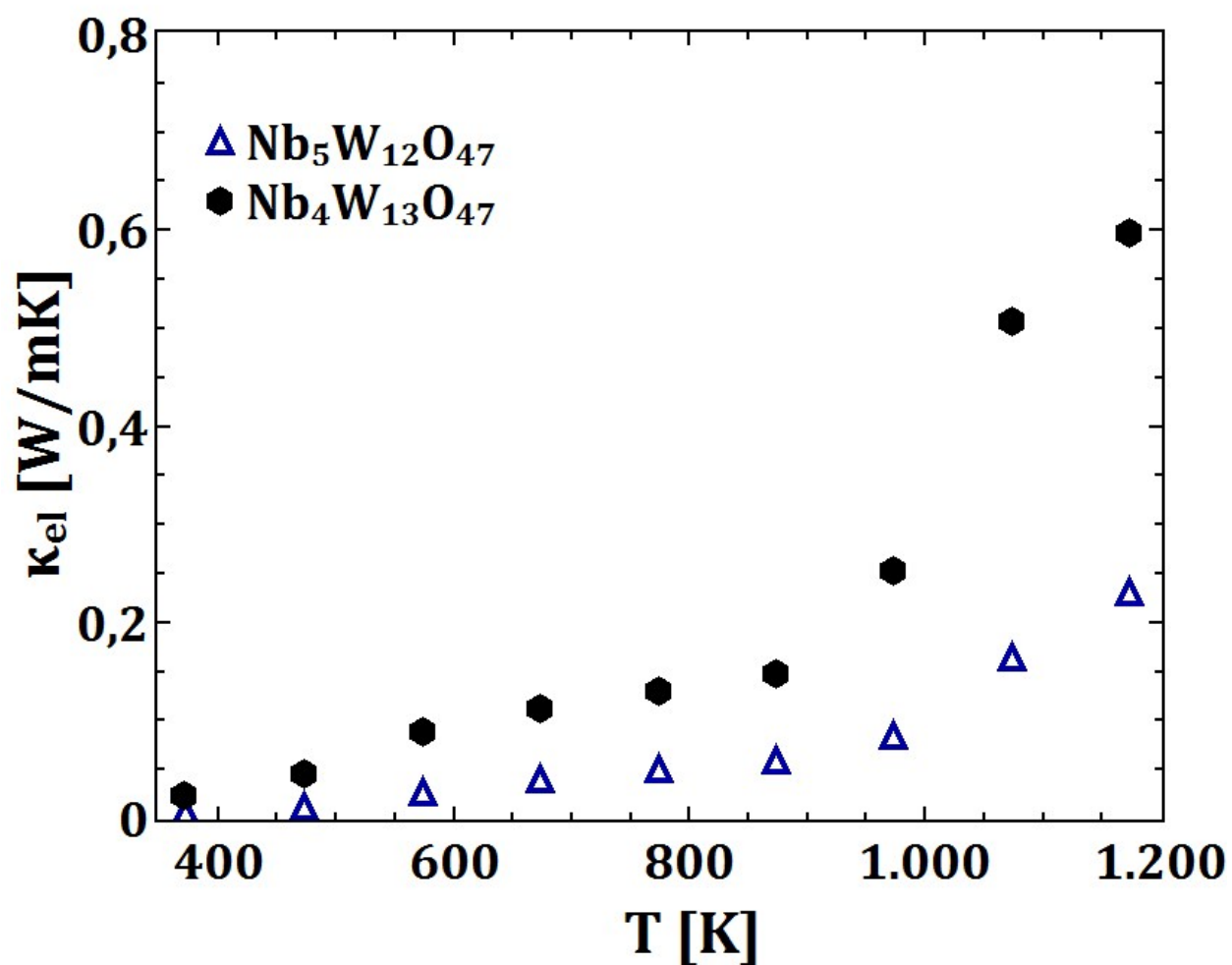
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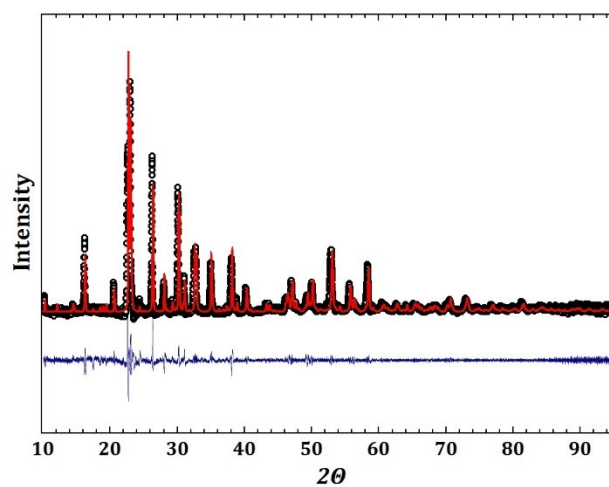
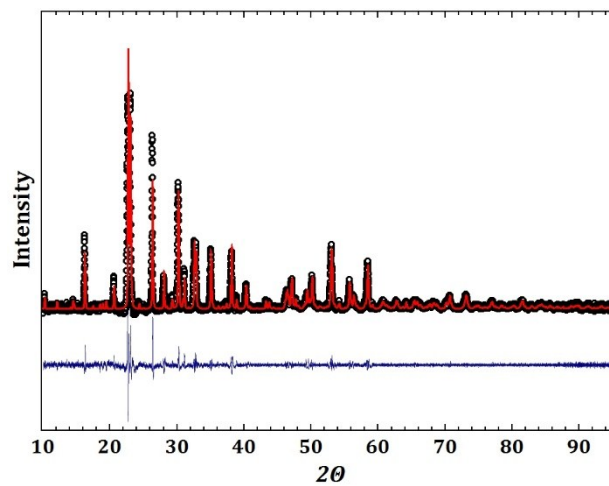
**Fig. S1.** Percentage atomic composition of W and Nb calculated by quantifying the peak intensities of W 4d and N 3d core-level emissions measured with XPS technique. The obtained results confirmed the expected substitution level and therefore the high quality of the synthesized compounds.

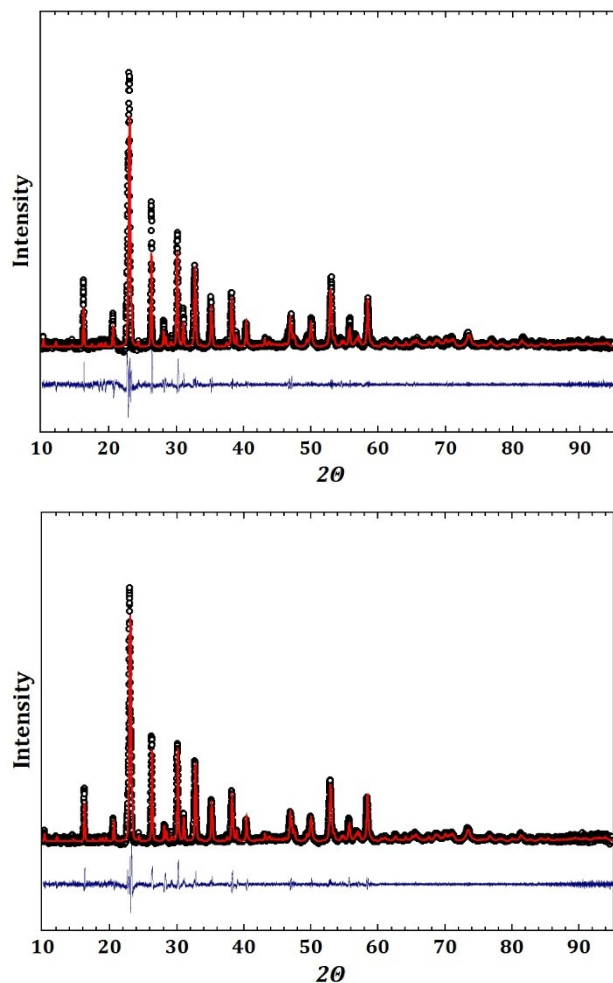


**Fig. S2.** Comparison between the thermopower dependent Lorenz numbers calculated with the formula derived by Kim et al. *APL Mater.* 3, 2015 (points) and the value of the degenerate limit  $2.44 \times 10^{-8} \text{ W}\Omega\text{K}^{-2}$  (red solid line).



**Fig. S3.** Comparison of  $\kappa_{el}$  values as a function of temperature for the sample  $\text{Nb}_5\text{W}_{12}\text{O}_{47}$  ( $x = 3$ ) and  $\text{Nb}_4\text{W}_{13}\text{O}_{47}$  ( $x = 4$ ). The evaluation of  $\kappa_{el}$  has been done using the thermopower dependent values of the Lorenz's number.





**Fig. S4.** X-ray diffractograms of  $\text{Nb}_5\text{W}_{12}\text{O}_{47}$  before (top left) and after (top right) and of  $\text{Nb}_4\text{W}_{13}\text{O}_{47}$  before (bottom left) and after (bottom right) thermal cycling. Experimental (black circles), theoretical profile (red line) and difference between the diffraction patterns (blue line). The compositions and structures of both samples after cycling remained unchanged, confirming their stability.