

Supplementary Information for

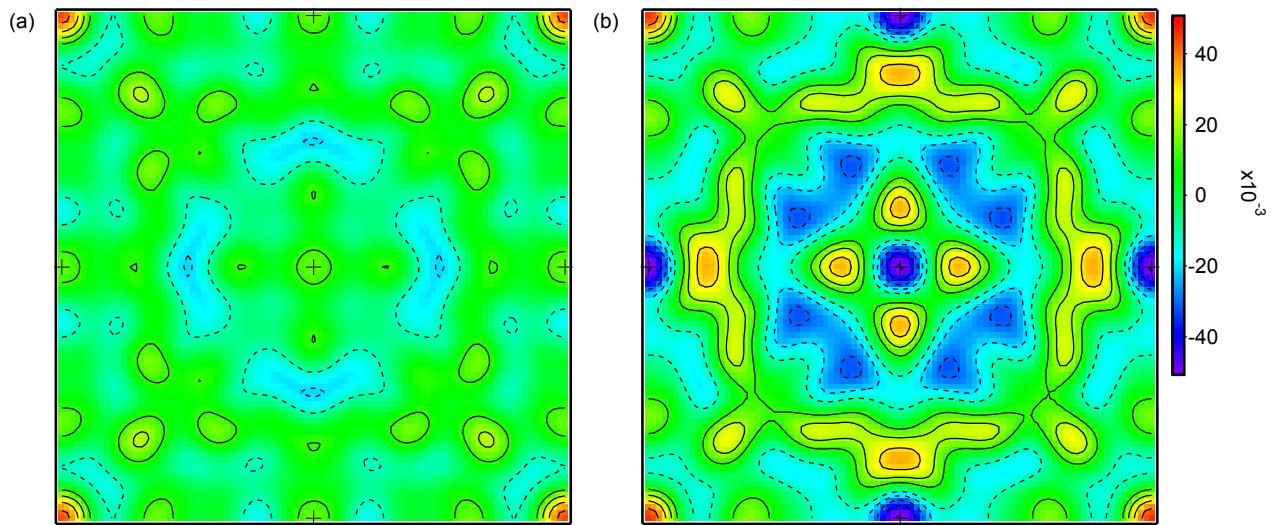
# Crystal Structure of High-temperature Polymorph $\beta$ -Na<sub>3</sub>PS<sub>4</sub>

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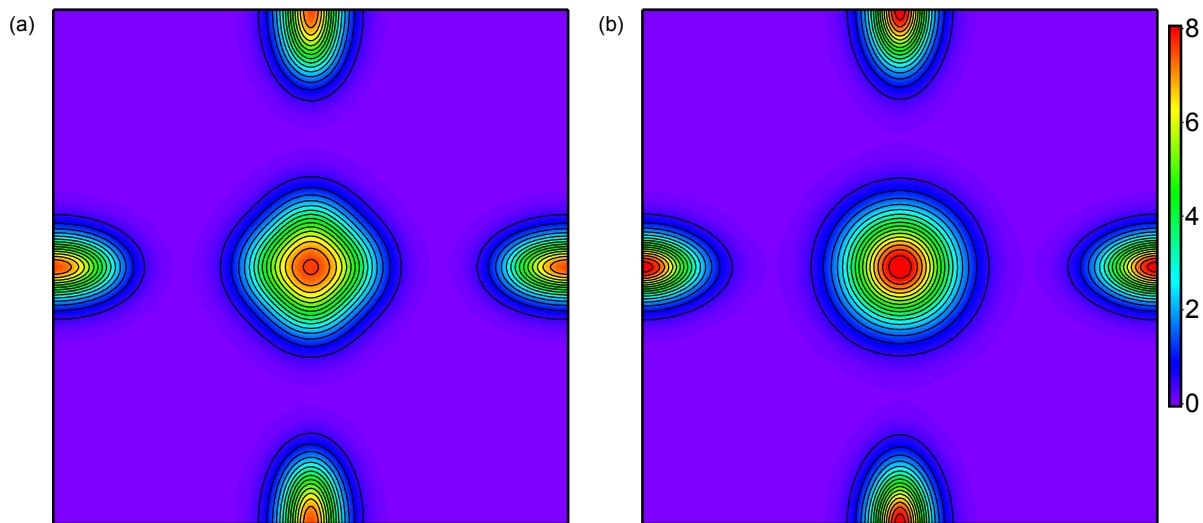
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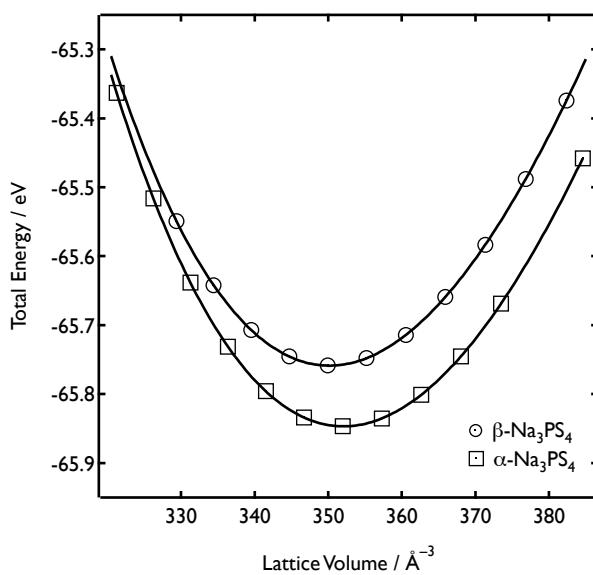
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**Figure S1** Difference Fourier map at (100) plane ( $x = 0$ ) for  $\beta\text{-Na}_3\text{PS}_4$  at 600 K with (a) and without (b) the site splitting of Na. The contour level spacing is  $0.01 \text{ \AA}^{-3}$ . Solid and broken lines represent positive and negative values respectively, while zero contours are not drawn. The average sodium positions (6b) are plotted as crosses.



**Figure S2** Electron density distribution at (001) plane ( $x = 0$ ) about Na sites calculated from refined structural parameters of  $\beta\text{-Na}_3\text{PS}_4$  at 600 K with (a) and without (b) the site splitting. The contours are drawn up to  $8 \text{ \AA}^{-3}$  with intervals of  $0.5 \text{ \AA}^{-3}$ . Electron density from phosphorus and sulphur are omitted for clarity.



**Figure S3 Total energy versus lattice volume for  $\alpha$ - and  $\beta$ - $\text{Na}_3\text{PS}_4$ .**

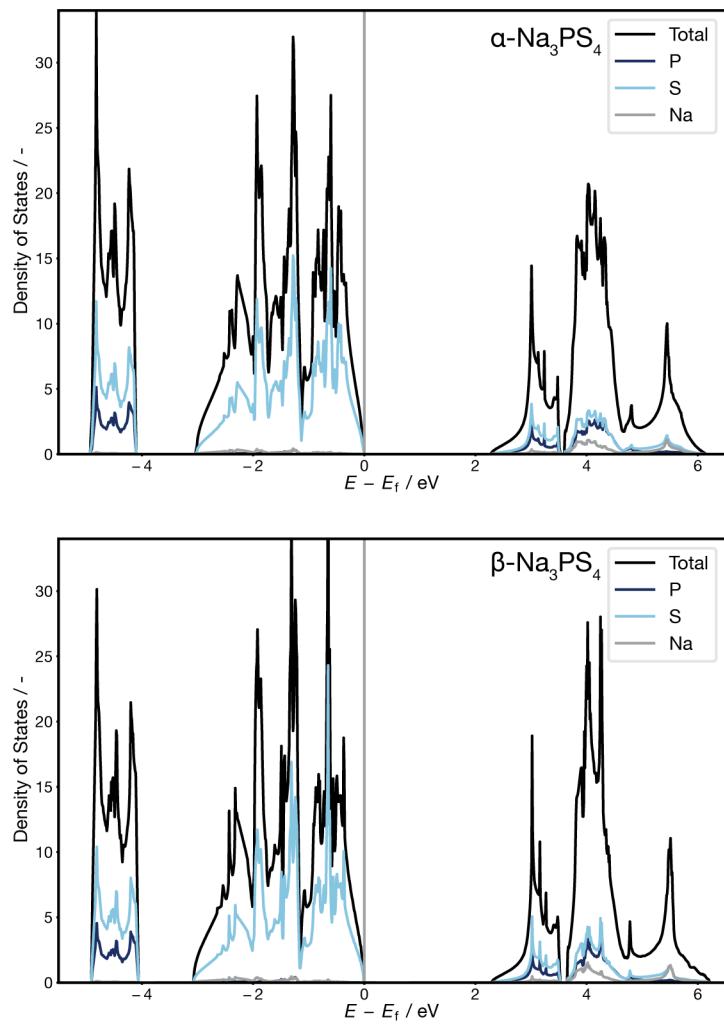


Figure S4 Electronic density of states of  $\alpha$ - and  $\beta\text{-Na}_3\text{PS}_4$ .

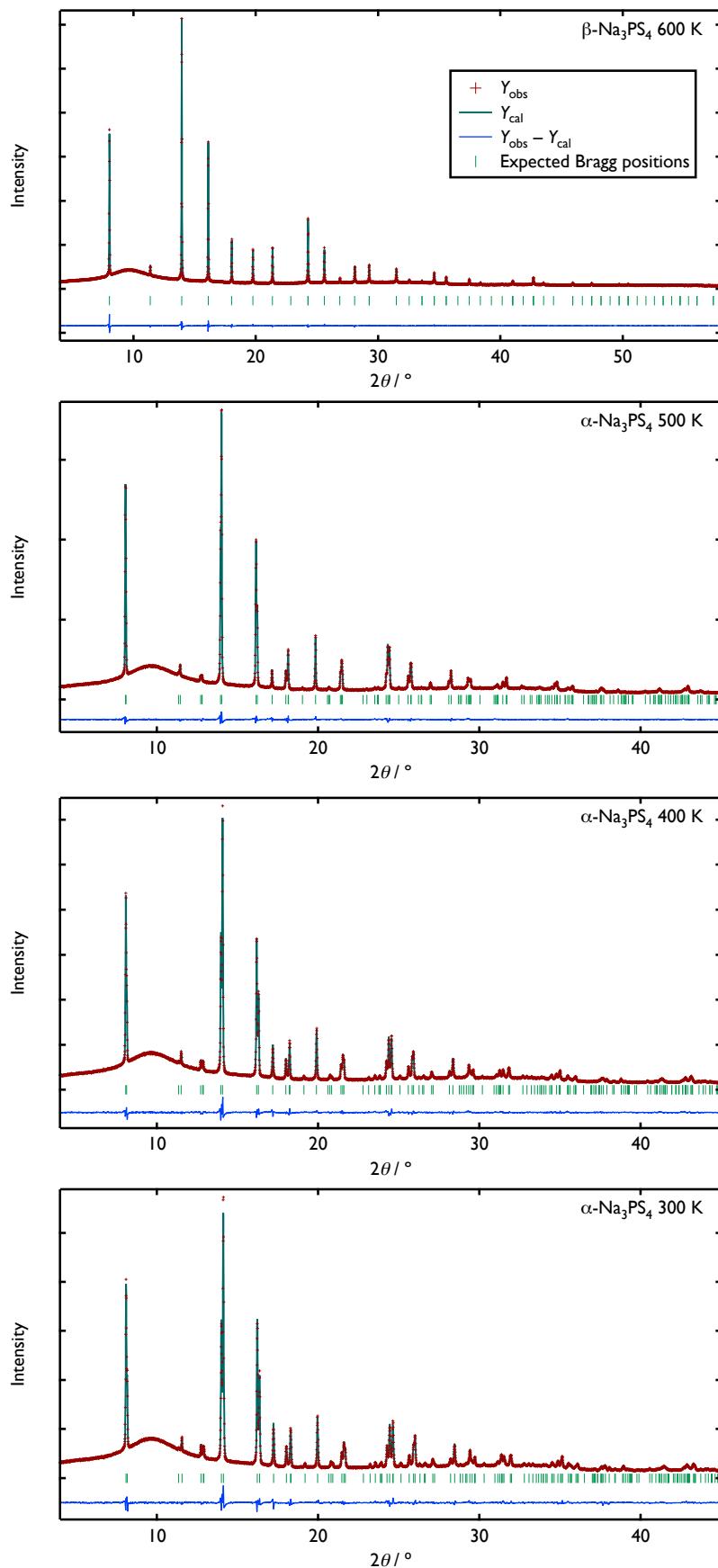


Figure S5 Rietveld refinement patterns of  $\text{Na}_3\text{PS}_4$  at 300, 400, 500, and 600 K.

**Table S1 Crystal data for  $\alpha\text{-Na}_3\text{PS}_4$  at 300 K and  $\beta\text{-Na}_3\text{PS}_4$  at 600 K.**

Chemical formula	$\text{Na}_3\text{PS}_4$	
Z	2	
Mr	228.20	
T (K)	300	600
Crystal system	Tetragonal	Cubic
Space group	$P\bar{4}2_1c$	$\bar{I}43m$
a (Å)	6.9587(13)	7.06985(4)
c (Å)	7.0832(9)	—
V (Å <sup>3</sup> )	342.99(12)	353.370(7)
$R_{\text{wp}}$	0.0364	0.0293
$R_{\text{p}}$	0.0264	0.0221
$R_{\text{Bragg}}$	0.0158	0.00678

**Table S2 Fractional coordinates, isotropic atomic displacement parameters (ADPs) and occupancies for  $\alpha\text{-Na}_3\text{PS}_4$  at 300 K.**

	x	y	z	$B_{\text{iso}}$ (Å <sup>2</sup> )
Na1	0	1/2	0.4281 (4)	
Na2	0	0	0	
P	0	0	1/2	1.14 (5)
S	0.31409 (17)	0.34547 (15)	0.16605 (18)	

**Table S3 Anisotropic ADPs for  $\alpha\text{-Na}_3\text{PS}_4$  at 300 K. (Å<sup>2</sup>)**

	$U_{11}$	$U_{22}$	$U_{33}$	$U_{12}$	$U_{13}$	$U_{23}$
Na1	0.045 (3)	0.017 (2)	0.086 (3)	0	0	0
Na2	0.092 (3)	= $U_{11}$	0.011 (3)	0	0	0
S1	0.0261 (12)	0.0169 (12)	0.0259 (8)	-0.0054 (8)	0.0044 (11)	-0.0011 (11)

**Table S4 Fractional coordinates, isotropic ADPs and occupancies for  $\beta\text{-Na}_3\text{PS}_4$  at 600 K.**

	x	y	z	$B_{\text{iso}}$ (Å <sup>2</sup> )	Occ. (<1)
Na	0.0626 (14)	0	1/2		1/4
P	0	0	0	2.25 (3)	
S	0.16738 (6)	= x	= x		

**Table S5 Anisotropic ADPs for  $\beta\text{-Na}_3\text{PS}_4$  at 600 K. (Å<sup>2</sup>)**

	$U_{11}$	$U_{22}$	$U_{33}$	$U_{12}$	$U_{13}$	$U_{23}$
S	0.0484 (3)	= $U_{11}$	= $U_{11}$	-0.0107 (4)	= $U_{12}$	= $U_{12}$
Na	0.110 (6)	0.098 (7)	0.0418 (18)	0	0	0