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## **Electronic Supporting Information**

# Utilizing formation of dye aggregates with aggregation-induced emission characteristics for enhancement of two-photon absorption

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#### **Techniques and instrumentation**

<sup>1</sup>H, <sup>13</sup>C{<sup>1</sup>H}, <sup>31</sup>P{<sup>1</sup>H} NMR spectra were recorded either on a Jeol JNM-ECZ 400S Research FT NMR spectrometer (JEOL Ltd., Tokyo, Japan) operating at 400 MHz (for <sup>1</sup>H), or with the use of a Bruker Avance 600 spectrometer operating at 600 MHz (for <sup>1</sup>H). Mid-infrared (MIR) and far-infrared (FIR) spectra were obtained on a VERTEX 70V FT-IR spectrometer (Bruker Optik GmbH, Ettlingen, Germany) in attenuated total reflection (ATR) measurement mode at room temperature. Absorption spectra in the UV–Vis region were acquired in 1 cm quartz cuvettes using a Jasco V-670 spectrophotometer.

#### **Synthetic procedures**

Starting materials were of reagent grade purity and were obtained from commercial sources and used without further purification. Dioxane and DMF were kept over 3Å Aldrich molecular sieves.

#### Synthesis of *N*-hexylcarbazole (1):

In two-neck flask were placed carbazole (5.00 g, 0.0299 mol), 1-bromohexane (5.52 cm<sup>3</sup>, 0.0389 mol), KOH (2.18 g, 0.0389 mol), TBAB (tetrabutylammonium bromide, 0.967 g, 0.00299 mol), and DMF (50 cm<sup>3</sup>). Obtained mixture was stirred at 70 deg. C for 24 hours. After cooling down, water and chloroform were added (each 100 cm<sup>3</sup>) and thoroughly shaken. Organic layer was separated, and inorganic layer was extracted again with chloroform (100 cm<sup>3</sup>). Combined organic extracts were washed with water (100 cm<sup>3</sup>), two times with NaCl saturated solution (2 x 100 cm<sup>3</sup>) and finally dried with anhydrous Na<sub>2</sub>SO<sub>4</sub>. Yellowish oil was subjected to column chromatography on silica gel, using hexane as a mobile phase. Colorless oil, yield 7.51 g, 84 %.

<sup>1</sup>H NMR (600 MHz, CDCl<sub>3</sub>, 300K) δ 8.12 (d, J = 7.7 Hz, 2H), 7.48 (t, J = 7.6 Hz, 2H), 7.42 (d, J = 8.1 Hz, 2H), 7.24 (t, J = 7.4 Hz, 2H), 4.31 (t, J = 7.3 Hz, 2H), 1.88 (dt, J = 15.0, 7.5 Hz, 2H), 1.44-1.35 (m, 2H), 1.35-1.22 (m, 4H), 0.88 (t, J = 7.0 Hz, 3H).

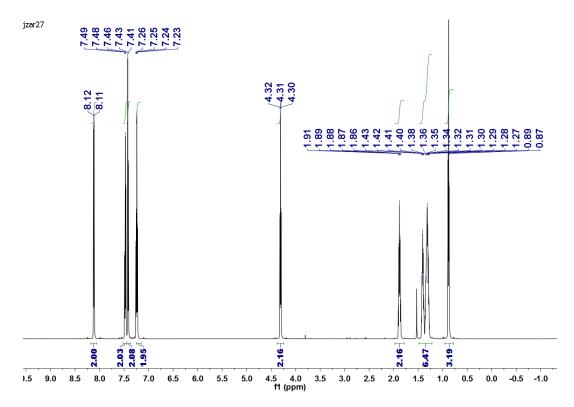


Fig. S1. <sup>1</sup>H NMR (600 MHz, CDCl<sub>3</sub>) spectrum of of N-hexylcarbazole (1)

#### Synthesis of 3-formyl-9-(*N*-hexyl)carbazole (2):

In two-neck flask was placed DMF (1.133 g, 0.0155 mol). Next, POCl<sub>3</sub> (2.30 g, 15.00 mmol) under the atmosphere of nitrogen was added in small portion at 0 deg. C. The mixture was stirred till the glassy solid was obtained. It was heated to 80 deg. C and *N*-hexylcarbazole (1) was added in one portion (3.00 g, 0.0119 mmol). Initially, dark green coloration is observed, which with time turns to dark brown (heating 4 hours, under nitrogen).

After cooling, the mixture was transferred to the large excess of 10% aqueous solution of sodium acetate. Obtained brown solid was filtered out, washed with water and dried in air. Crude product was subjected to column chromatography on silica gel, using chloroform / hexane = 1:1 (v/v) as a mobile phase. Yellowish oil, crystallizing after some time, was obtained. Yield:  $2.69 \, g$ ,  $81 \, \%$ .

<sup>1</sup>H NMR (600 MHz, CDCl<sub>3</sub>) δ 9.85 (s, 1H), 8.30 (s, 1H), 7.88 (d, J = 7.8 Hz, 1H), 7.75 (d, J = 8.5 Hz, 1H), 7.32 (m, 1H), 7.19 (d, J = 8.2 Hz, 1H), 7.15 (d, J = 8.5 Hz, 1H), 7.10 (m, 1H), 3.97 (t, J = 7.2 Hz, 2H), 1.68-1.47 (m, 2H), 1.20-0.95 (m, 6H), 0.68 (t, J = 5.9 Hz, 3H).

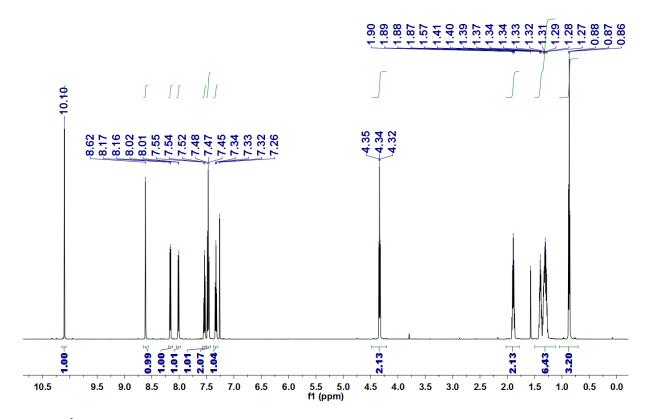


Fig. S2. <sup>1</sup>H NMR (600 MHz, CDCl<sub>3</sub>) spectrum of 3-formyl-9-(N-hexyl)carbazole (2)

#### Synthesis of 9,10-bis(chloromethyl)antracene (3):

In two-neck flask were placed anthracene (9.79 g, 0.055 mol), paraformaldehyde (3.795 g, 0.1265 mol), CTAB (cetyltrimethylammonium bromide, 2.00 g, 0.0055 mol), dioxane (100 cm³), and 36% HCl (100 cm³). The obtained heterogenous mixture was heated at 100 deg. C for 3 hours. During heating 36% HCl (50 cm³) was slowly dropped to the mixture, in order to maintain high concentration of HCl in the reaction system. After cooling down, the fluffy yellow precipitate was gravity filtered, washed with large amount of water and dried in air. Crude product has been crystallized from toluene twice, giving light yellow small needles as the product. Yield: 7.41 g, 49 %.

<sup>1</sup>**H NMR** (400 MHz, DMSO-d<sub>6</sub>) δ 8.50-8.53 (m, 4H), 7.71-7.73 (m, 4H), 5.87(s, 4H).

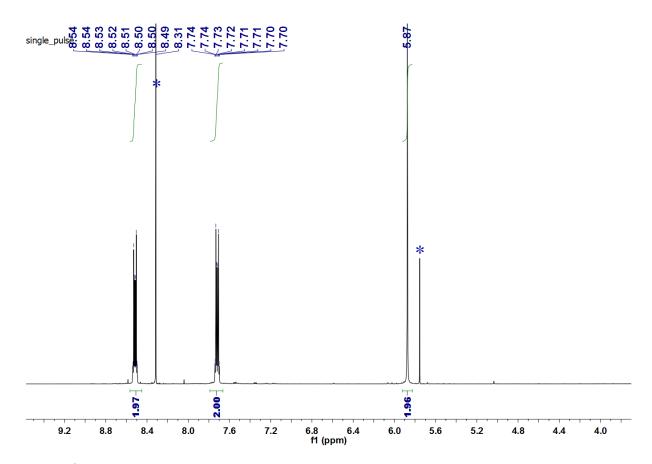


Fig. S3. <sup>1</sup>H NMR (400 MHz, DMSO-d<sub>6</sub>) of 9,10-bis(chloromethyl)antracene (3)

#### Synthesis of 9,10-bis(dietoxyphosphorylmethyl)antracene (4):

In a two-neck flask were placed 9,10-bis(chloromethyl)antracene (2.50 g, 0.0091 mol), and triethyl phosphite (6 cm³, 0.0350 mol). The mixture was heated to 150 deg. C under constant flow of nitrogen in order to remove ethyl chloride (which is necessary for high yield of reaction, since ethyl chloride, can consume triethyl phosphite in consecutive Arbuzov reaction). After four hours the volatiles were distilled off under reduced pressure at the same temperature. Orange-colored crude product was crystallized from the ethyl acetate / cyclohexane mixture. Light yellow crystals, 2.837 g. Another crop

of compound is obtained from column chromatography of supernatant from crystallization (silica-gel, eluent: chloroform / methanol = 10:1 (v/v)), 0.822 g. Total yield: 3.659 g, 84 %.

<sup>1</sup>**H NMR** (400 MHz, CDCl<sub>3</sub>) δ 8.38-8.36 (m, 4H), 7.58-7.55 (m, 4H), 4.23 (d, 4H,  $J_{H-P}$  = 19.8 Hz), 3.91- 3.86 (m, 4H), 3.82-3.78(m, 4H), 1.06 (t, 12H, J = 7.2 Hz).

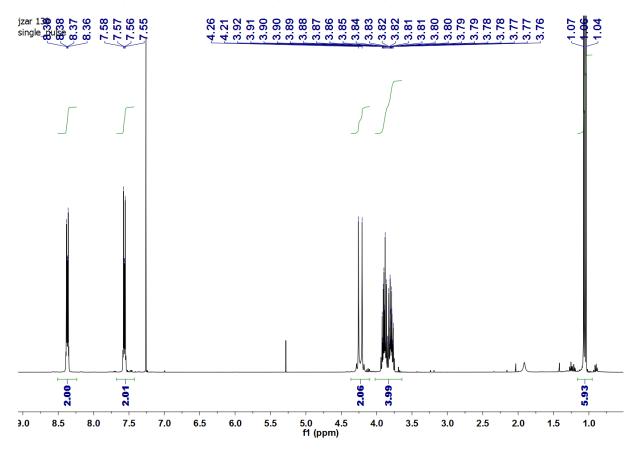


Fig. S4. <sup>1</sup>H NMR (400 MHz, CDCl<sub>3</sub>) spectrum of 9,10-bis(dietoxyphosphorylmethyl)antracene (4) Synthesis of 9,10-bis(*N*-hexylcarbazol-3-yl-vinyl-2)antracene (5):

In the flask was placed 9,10-bis(dietoxyphosphorylmethyl)antracene (1.000 g, 0.0021 mol), 3-formyl-9-(N-hexyl)carbazole (1.518 g, 0.0054 mol), and dioxane (60 cm<sup>3</sup>). After dissolution of those reagents potassium tertbutanolate was added (0.90 g, 0.008 mol). Reaction was stirred at room temperature for 12 hours. After that time an excess of water was added (approx. 200 cm<sup>3</sup>). The orange precipitate was filtered out and dried. Crude product was extracted three times with boiling methanol (3 x 50 cm<sup>3</sup>). Light-orange methanolic extracts were discarded; the remaining yellow solid was subjected to column chromatography on silica gel two times, using chloroform / hexane = 4:1 (v/v) as an eluent. Yellow solid, yield: 0.902 g, 59 %.

<sup>1</sup>**H NMR** (600 MHz, CDCl<sub>3</sub>) δ 8.60 – 8.48 (m, 4H), 8.40 (d, J = 1.2 Hz, 2H), 8.18 (d, J = 7.7 Hz, 2H), 7.99 (d, J = 16.4 Hz, 2H), 7.88 (dd, J = 8.4, 1.5 Hz, 2H), 7.55 – 7.47 (m, 8H), 7.45 (d, J = 8.2 Hz, 2H), 7.28 (t, J = 7.3 Hz, 2H), 7.16 (d, J = 16.4 Hz, 2H), 4.36 (t, J = 7.2 Hz, 4H), 2.01 – 1.88 (m, 4H), 1.50 – 1.39 (m, 4H), 1.39 – 1.19 (m, 8H), 0.90 (t, J = 7.1 Hz, 6H).

<sup>13</sup>C NMR (151 MHz, CDCl<sub>3</sub>) δ 140.97, 140.47, 138.27, 133.07, 129.83, 128.64, 126.73, 125.89, 125.10, 124.45, 123.33, 122.97, 122.33, 120.57, 119.08, 118.78, 109.01, 108.94, 43.29, 31.65, 29.04, 27.03, 22.60, 14.07.

**MS** (ESI) m/z (M<sup>+</sup>) calc. 728.4130, found 728.4098.

### NMR spectra of BHCVA

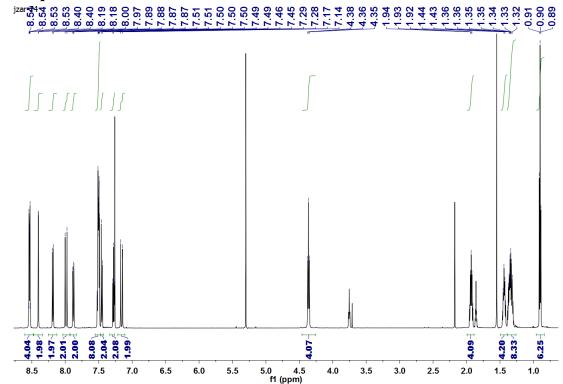


Fig. S5. BHCVA <sup>1</sup>H NMR spectrum

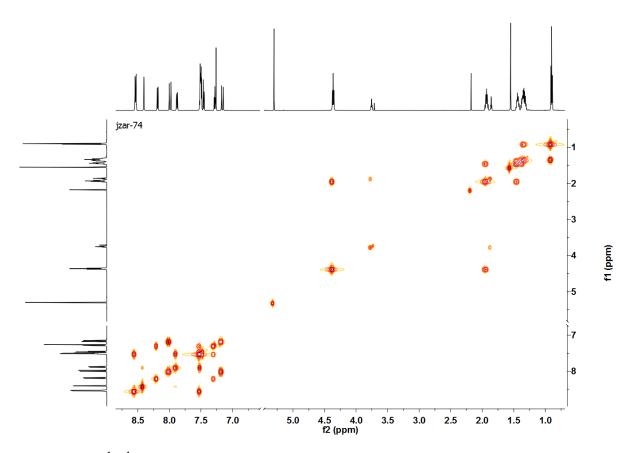


Fig. S6. BHCVA <sup>1</sup>H-<sup>1</sup>H COSY correlation spectrum

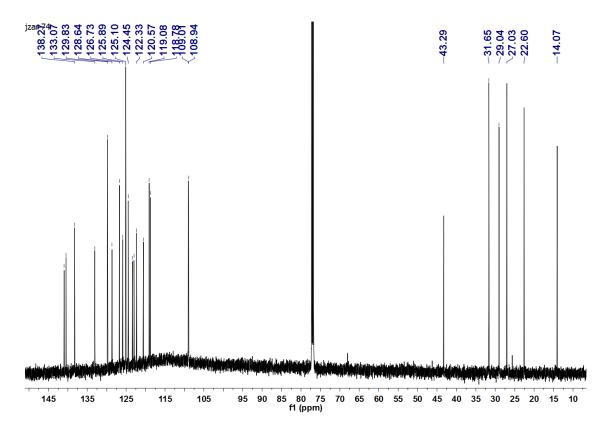


Fig. S7. BHCVA <sup>13</sup>C NMR spectrum

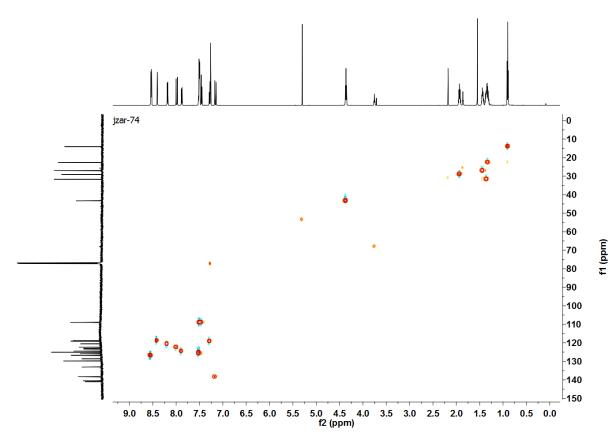


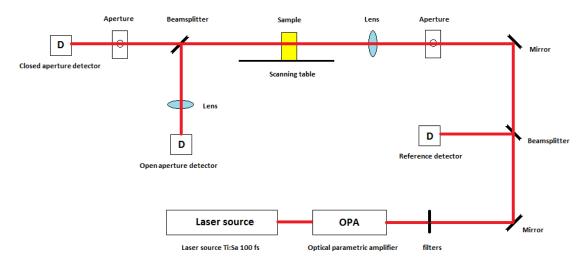
Fig. S8. BHCVA <sup>1</sup>H-<sup>13</sup>C HSQC correlation spectrum

#### **Z-scan experiment details**

The Z-scan technique is used to measure nonlinear refractive index  $(n_2)$  and nonlinear absorption coefficient  $(\beta)$ . Both quantities can be measured simultaneously by monitoring changes in laser power of a focused laser beam on open aperture (OA) and closed aperture (CA) detectors placed in the far field, as the sample travels in the z direction.

The Z-scan measurements were performed as previously described, with some modifications<sup>1</sup>. In order to exclude the contributions of solvent and cuvette cell to the values of NLO parameters, we have used a calculation method, in which the real and imaginary parts of the cubic hyperpolarizability,  $\gamma$ , or the corresponding two-photon cross sections, ( $\sigma_2$ ), are derived from the difference between the Z-scan traces obtained for the cell filled with solvent(s) and the cell with the solution (of the same solvent composition) of **BHCVA** aggregates.

Z-scan studies were performed using a femtosecond laser system comprising a Quantronix Integra-C regenerative amplifier operating as an 800 nm pump and a Quantronix-Palitra-FS optical parametric amplifier. The latter was used to deliver wavelength tunable pulses (available range from 500 up to 2000 nm) with the duration <130 fs, and a repetition rate of 1 kHz. For investigations of **BHCVA** aggregates we used the range of 625 – 1350 nm. The Z-scan setup is presented in Scheme S1.



Scheme S1. Setup for Z-scan experiment

Aggregate samples for NLO studies were prepared in exactly the same way as for one-photon experiments, however, samples in which microcrystal precipitation of **BHCVA** occurred were not investigated (due to excessive scattering). The concentration for each solution was set to 2.74 mM which allowed to have sufficiently strong signals in the Z-scan measurements as well as allowed to obtain stable solutions of aggregates in THF-acetone and chloroform-acetone solvent systems.

Experimental open aperture (OA) and closed aperture (CA) traces were fitted using theoretical expressions derived by Sheikh-Bahae et al.<sup>2</sup>

#### Fluorescence lifetime

The nanosecond fluorescence kinetics was investigated with the use of Time-Correlated Single-Photon Counting (TCSPC) method. For TCSPC measurements we used a Becker&Hickl system constructed from a TCSPC Module (SPC-130-EM) and a hybrid PMT detector (HPM-100-06) with detector control card (DCC 100) mounted to a Princeton Instruments spectrograph (Acton SpectraPro-2300i).

The sample was excited with a 375 nm picosecond laser diode (BDL-375-SMC) in the 20MHz repetition mode (which corresponds to 50 ns collection time window). The fluorescence lifetime values were calculated, after elimination of the instrument response function (IRF) contribution, which accounted for  $200 \, \mathrm{ps}$ .

#### **Excited state dynamics**

The femtosecond pump-probe setup is based on a Legend Elite Duo (Coherent, Inc.) Ti:sapphire regenerative amplifier delivering 800 nm pulses at a repetition rate of 5 kHz, the output of which is divided and routed into two independent Noncollinear Optical Parametric Amplifiers (NOPA, TOPAS-White, Light Conversion) yielding 20–30 µJ pulses tunable from 500 to 750 nm. Outputs from the NOPAs are attenuated, to approximately 800 nJ in the case of the pump beam, and to 60 nJ in the case of the probe. A mechanical chopper, synchronized with the amplifier, blocks every second pump pulse, allowing fast switching between pumping and non-pumping regimes. The probe beam traverses a delay line consisting of a corner-cube retroreflector mounted on a motorized linear stage which can provide up to 2 ns delay between pump and probe pulses. An achromatic half-wave plate mounted after the last routing mirror is used to rotate the polarization of the probe beam to 45° with respect to the pump. A polarizing beam splitting cube separates the probe beam after the sample into two polarization components, parallel and perpendicular to the polarization of the excitation. Both components are recorded by two photodiodes so that the magic angle signal (independent of rotational diffusion of molecules in the sample) can be subsequently calculated.

The pump NOPA output was tuned to 680 nm, either to excite the sample directly in a two-photon process or, when using a frequency doubling BBO crystal in the pump beam path, to provide one-photon excitation at 340 nm. This wavelength was selected to match the lowest-energy absorption peak in the samples. The probe pulses were in both cases centered at 580 nm (the setup does not allow broad-band probing, so only kinetics at selected wavelengths can be recorded). Samples were placed in quartz cells with optical path length of 2 mm. Temporal resolution of the setup was better than 100 fs for excitation at 680 nm and degraded to approx. 200 fs with frequency-doubled excitation pulses. In any case the temporal resolution was much shorter than timescale of processes seen in the samples: in the range of tens of picoseconds for the initial rise of the signal and of the order of 100 ps for its decay. For this reason the data were analyzed simply by fitting with exponential functions because any deconvolution procedures were not needed with so well separated timescales of the instrumental response and studied processes. system that has larger density of excited-states. Stabilization of the relative orientation between donor and acceptor moieties can substantially shorten the non-radiative relaxation.

#### Fluorescence decay and excited state dynamics for aggregates

Fluorescence decay show significant influence of aggregation degree on excited states. Typically, the emission lifetime increases upon aggregation of AIE compounds. Indeed, fluorescence lifetime in the presence of acetone (non-solvent) becomes longer (0.58 ns and 0.71 ns for 10% and 20% acetone respectively) than in pure chloroform (0.26 ns) and THF (0.45 ns). This phenomenon is well-explained by the restriction of molecular motion, due to formation of more dense, structurally confined structures, therefore limiting non-radiative relaxation pathways. Similar behavior is observed for AIE compounds in systems with gradually changed viscosity of solution.

With the use of pump-probe experiments we have found that the increase of aggregation degree (by addition of acetone) affects significantly the excited state dynamics of BHCVA. In the presence of two

different THF/acetone volume ratios (Fig. S9b) the absorption decay times were equal to 106 ps and 88 ps, about twice shorter than in pure solvents: 267 ps in chloroform and 205 ps in THF. These results were concentration independent suggesting internal processes occurring in the chromophore. Possible explanation could be the steric hindrance of the chromophores in the aggregate that may affect the charge and energy transfers in the confined molecular that has larger density of excited states.

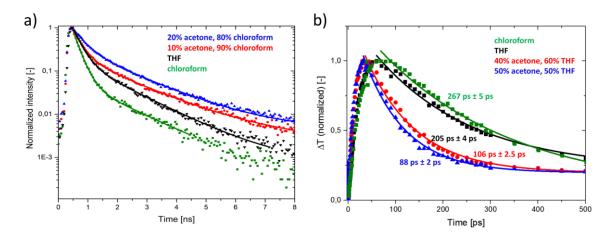


Fig. S9. (a) Fluorescence decays of BHCVA (ex. 377 nm em. 560 nm) in pure chloroform, mixtures of chloroform and acetone (10% and 20% v/v) and pure THF (b) TA dynamics monitored at 580 nm (excitation 340 nm and 680 nm) for pure chloroform, pure THF, and mixtures of THF and acetone.

#### Mechanochromism and termochromism study

The influence of structural changes of BHCVA on its fluorescence was investigated in solid state. It was shown by Bu et al.<sup>3</sup> that analogous compounds exhibit mechanochromism (methyl, propyl, pentyl, and dodecyl). Here we took a closer look at mechanochromic property of a derivative with a hexyl chain substituted at *N*-position of carbazole. The mechanochromic property of **BHCVA** was investigated through grinding a dose of pristine powder with a pestle in a mortar for several minutes. Pristine compound emits at 538 nm, with a long tail at the red side of spectrum. After grinding the emission spectrum shifts to a maximum at 598 nm, which is an effect of disturbance of a crystalline phase and formation of amorphous phase. Mechanochromism can be treated as a common property of 9,10-divinyl substituted derivatives of anthracene.<sup>4</sup>

Mechanochromism is often assisted by so-called vapochromism, i.e. the change of the optical properties upon exposure to certain vapors. To test response of **BHCVA** to organic vapors, a ground sample of BHCVA was introduced into a desiccator with atmosphere of dichloromethane. The sample was excited with a UV lamp (365 nm) after 5 min and 3 h of exposure to vapors (Fig.S10)

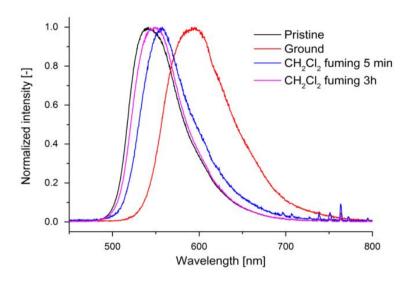


Fig. S10. UV-Vis emission spectra of BHCVA before and after grinding (black and red line, respectively). Exposure to fumes of ground BHCVA was performed with dichloromethane for 5 min and 3 h (blue and pink line, respectively).

Under such conditions an immediate response is observed: the fluorescence maximum shifts by 40 nm to the value of 558 nm. Further exposure for a total of 3 h results in a shift of 46 nm from the starting point to the value of 552 nm.

To complete mechanochromic study we have performed FT-IR studies on crystalline and ground materials (Fig. S11). Broadening and change of the relative intensity of signals suggests disruption of crystal packing (amorphization) upon grinding. Especially affected seem to be the signals corresponding to the rocking vibrations of the methylene fragments of the hexyl chains (~720 cm<sup>-1</sup>)

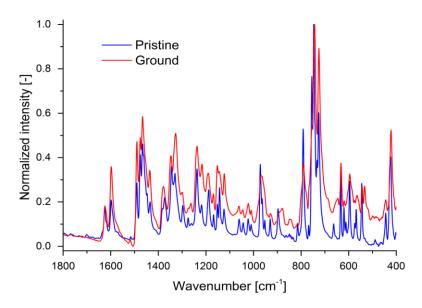


Fig. S11. A comparison of mid-IR spectra (ATR method) for pristine and ground BHCVA.

We have also investigated response of fluorescence of bulk **BHCVA** to temperature changes (thermochromism) as shown in Fig. S12 and S13. Pristine powder of **BHCVA** was deposited on a heating plate covered with glass substrate to prevent rapid temperature decay. Temperature of the

plate was changed from 23  $^{0}$ C to 180  $^{0}$ C (with 4 ± 1  $^{0}$ C step), controlled with thermocouple. The stabilization time was 2 minutes. The spectrum was measured on illumination of the powder with a UV lamp (365 nm). Emitted radiation was collected using an Ocean Optics spectrometer, collection time 1000 ms, averaged 5 times. Spectral red shift of the maximum in the temperature range between 25 $^{0}$ C and 150 $^{0}$ C is approximately linear (Fig. S13). It is reasonable to assume that temperature influences orientation of molecules and results in continuous transition from crystalline toward disordered, amorphous phase. Further increase of temperature above 150 $^{0}$ C results in rapid decrease in fluorescence intensity, deviation from linear trend in emission shift and visible decomposition of material.

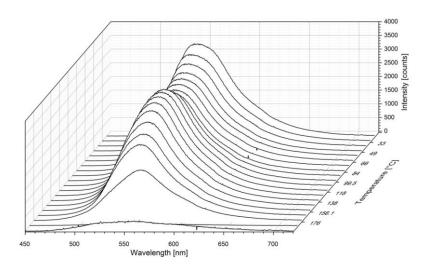


Fig. S12. Emission spectra of BHCVA collected during thermochromic experiment.

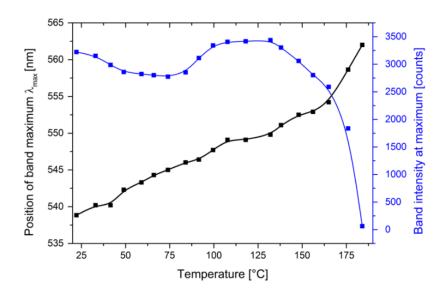


Fig. S13. Change of fluorescence maximum for BHCVA powder against temperature. The black dots represent position of intensity maximum and blue dots represent value of maximum intensity. Excitation was performed with 365 nm. Lines are used to guide eyes.

#### **Confirmation of the AIE property**

AIE nature of **BHCVA** was confirmed through gradual addition of water as non-solvent to solution of **BHCVA** in THF. Final concentration of **BHCVA** is 5  $\mu$ M in each probe, with assumption that volume contraction is neglected. For low water content in solution **BHCVA** exhibits only weak fluorescence. After reaching a point when the water content comprises 50% in solution, **BHCVA** starts to bulk precipitate out of solution with fluorescence maximum at 529 nm, the same as freshly crystallized **BHCVA**. Further increase of water fraction above 70% results in formation of highly dispersive aggregates whose fluorescence maximum is shifted to 561 nm and increased in intensity (Fig. S14).

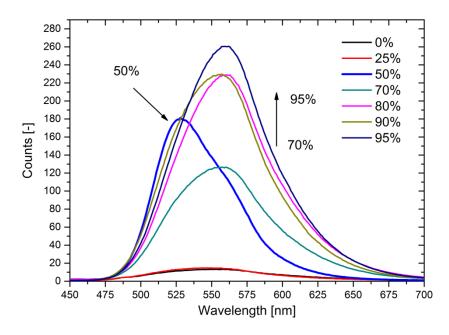


Fig. S14. Fluorescence of BHCVA in diluted THF solution (black line) subsequently titrated with water. In all samples the final molar concentration is  $5~\mu M$ .

# Open aperture Z-scan traces in the three-photon region and degradation experiment

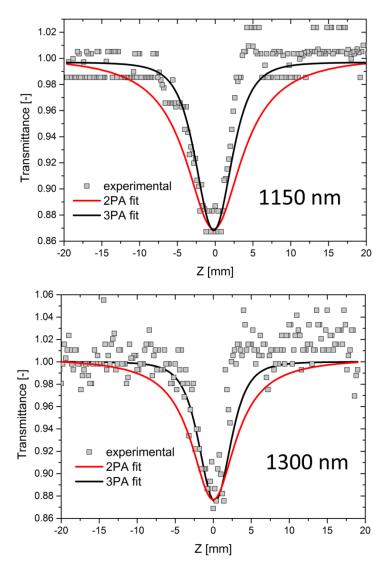


Fig. S15. Z-scan measurement traces at 1150 and 1300 nm for BHCVA in chloroform/acetone solution with 10% volume of acetone along with two-photon theoretical fit (red lines) and three-photon theoretical fit. In the case of no photochemical change the experimental traces should be vertically symmetric vs. Z=0.

The degradation of the dye upon prolonged irradiation was confirmed in a separate experiment, in which we irradiated the chloroform solution of **BHCVA** with high power (1W) 800 nm laser light directly from the regenerative amplifier for 3 hours. The photodegradation was evident, as judged from <sup>1</sup>H NMR spectroscopy (Fig. S16).

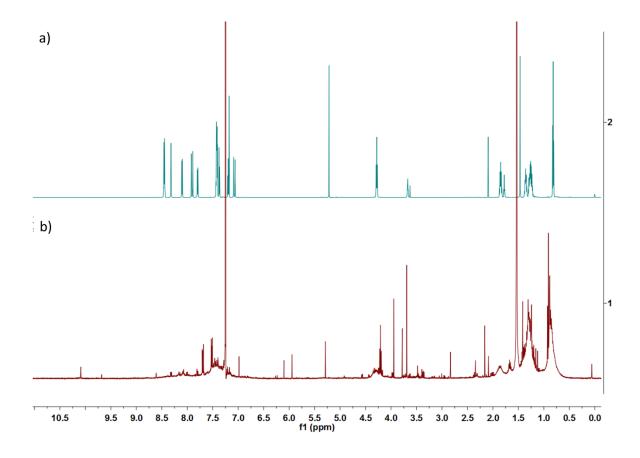


Fig. S16. A comparison of  $^1H$  NMR (400 MHz, CDCl<sub>3</sub>) spectra of a) pure BHCVA (before 800 nm irradiation), b) photochemically degraded BHCVA (after 800 nm irradiation).

#### Three-photon absorption cross section spectrum

Evaluation of nonlinear absorption properties in a range of wavelenghts corresponding to the three-photon absorption (1100 – 1350 nm) was performed by obtaining a Z-scan from a selected region of solution twice. The second scan was obtained right after the first one to minimize effects resulting from diffusion of possible products of photochemical reactions. The OA traces obtained in the first scan were always asymmetric, strongly suggesting the presence of photochemically induced changes in the solution, whereas the OA traces obtained in the second scan were symmetric. Those symmetric traces were fitted with theoretical three-photon absorption curves. The three-photon absorption cross section spectra obtained in this manner for chloroform and chloroform/acetone mixtures did not exhibit any significant differences (Fig. S17). This result may indicate that the three-photon induced photochemical changes may influence the degree of aggregation but further comment is not possible without knowing the actual chemical identity of species that are produced upon irradiation in the 1100-1350 nm region and that give rise to the spectra in Fig. S17.

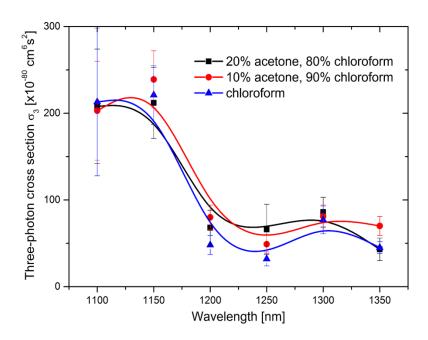


Fig. S17. Apparent three-photon cross section spectra of BHCVA in chloroform and chloroform/acetone solutions (10%, 20%). Full lines are drawn just to guide the eyes.

#### Aggregation motifs of molecules structurally related to BHCVA

Although at present it is not clear whether the structure of AIE aggregates corresponds to the structure of the crystalline solid, the X-ray crystal structures of AIE compounds, such as **BHCVA**, could be used as a valuable source of information on general trends on molecular self-assembly. Accordingly, a determination of recurrent structural motifs may allow for drawing probable aggregation models, necessary as starting points for electronic structure calculations of spectroscopic properties. Despite numerous trials, however, we were not able to obtain single crystals of **BHCVA** that could be used for X-ray diffraction studies. As a result, instead we surveyed CSD database (Web-based interface, February 2018) to establish what are structural preferences of molecules structurally related to **BHCVA**. Since a distinct feature of **BHCVA** is the protruding hexyl substituent, perpendicular to the main axis of the compound, we searched for crystal structures of similar compounds possessing functional group at the 3 position of the styryl fragment and/or ring expansion (see Scheme S1).

Scheme S1. Molecular structure used for CSD search. In blue are indicated atoms for which substructure search was performed

Database survey shows that there are no direct alkyl analogues of **BHCVA** deposited in the CSD. The most closely related compound to **BHCVA** is 3,3'-(anthracene-9,10-diyldiethene-2,1-diyl)bis(10-hexyl-10*H*-phenothiazine), CSD refcode: VASKIL, which contains *N*-hexylphenothiazine fragment instead of *N*-hexylcarbazole one. As can be seen in Figure S18a there is a partial overlap between anthracene planes, which results in the stacking with offset along the anthracene fragment.

Exploration of crystal structures of the other 3-substituted styryl derivatives such as 9,10-bis(3,5-difluorostyryl)anthracene (ZEDJOJ), 9,10-bis(3,5-bis(trifluoromethyl)styryl)anthracene (ZEDJUP), 9,10-bis(3,5-dimethylstyryl)anthracene (ZEDKAW), 3,3'-(anthracene-9,10-diyldiethene-2,1-diyl)dibenzaldehyde (OPUGIR), 9,10-bis(2-(3-propoxyphenyl)vinyl)anthracene (DIGMAJ) shows formation of extensive offset  $\pi$ - $\pi$  stacking as well. In those cases, also peripheral substituted styryl fragments are positioned in parallel (shown in Figure S18b, c, and d for selected examples). Note that all molecules are shifted along the short axis of the anthracene fragment. Taken together, we assumed that **BHCVA** molecule may assemble in the solid state according to the same pattern. The model based on the above analysis, used for electronic structure calculations, is referred to as "type B" in the main text of this paper.

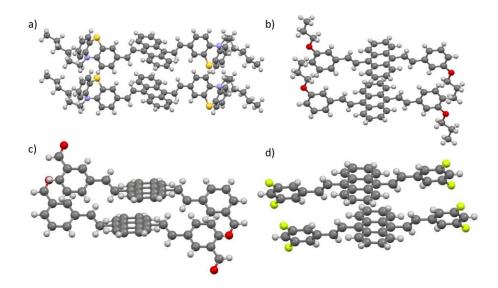


Figure S18. Visualizations of stacking patterns for structures of CSD reference codes a) VASKIL, b) DIGMAJ, c) OPUGIR and d) ZEDJUP.

#### Theoretical calculations

In this work we studied the electronic structure of monomer, dimer and trimer of 9,10-bis(N-hexylcarbazol-2-yl-vinyl-2)anthracene (hereafter abbreviated as BHCVA) using slightly simplified model (ethyl group instead of hexyl). Moreover, for aggregates we used two different types, denoted as A and B (see Fig. S19). All geometries were optimized *in vacuo* assuming  $C_i$  symmetry point group using 6-31G(d,p) basis set and B3LYP functional for monomer and BLYP-D2 functional for dimer and trimer. The GAUSSIAN program was used for this purpose. All geometries shown in Fig. S19 were confirmed to be true minima by evaluation of hessian.

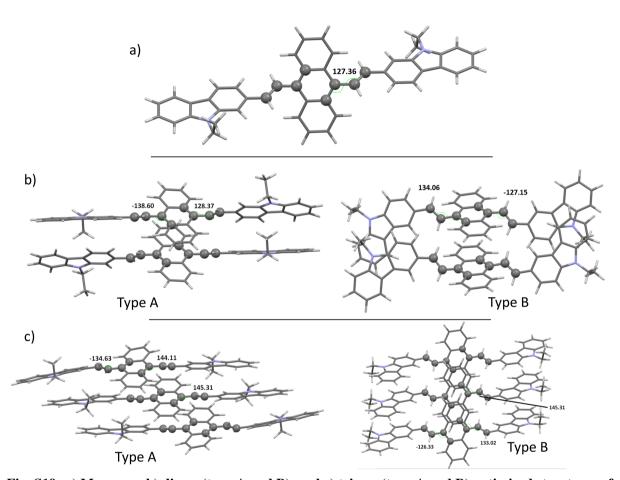


Fig. S19: a) Monomer, b) dimer (type A and B), and c) trimer (type A and B) optimized structures of BHCVA with indicated dihedral angles  $\varphi$ .

The results of electronic structure calculations, performed employing density functional theory for monomer, dimer and trimer assuming  $C_i$  symmetry point group and using the GAUSSIAN program, are reported in Tables S1–S17 (model A) and in Tables S22 and S23 (model B). When analyzing the performance of various density functionals (within model A) one can see that for each of the studied systems the range-separated functionals yield similar results and they predict, unlike B3LYP functional, that the maximum of one-photon excitation wavelength does not exceed 473 nm. The predictions of B3LYP are significantly overestimated. Hence, for further analysis, the CAM-B3LYP functional shall be employed. Moreover, there is only insignificant influence of solution environment on the optical spectra and the solvent-induced shifts for all electronic states do not exceed 12 nm. For this reason, gas-phase data are used to analyze electronic structure and two-photon absorption properties. The aggregation-induced changes in electronic structure are discussed in the manuscript.

We have also calculated the two-photon properties (TPA activity and TPA cross section) of the monomer, dimer and trimer using the DALTON program<sup>8</sup>. In the case of linearly polarized light, two-photon activity is given by:

$$\delta_{\text{TPA}} = \frac{1}{30} \sum_{\alpha\beta} \left[ 2S_{\alpha\alpha} S_{\beta\beta}^* + 2S_{\alpha\beta} S_{\alpha\beta}^* + 2S_{\alpha\beta} S_{\beta\alpha}^* \right],\tag{1}$$

where two-photon matrix elements,  $S_{\alpha\alpha}$ , for energy of incident photon  $\omega_i$  are described as a summation running over intermediate states, i:

$$S_{\alpha\beta} = \sum_{i} \left( \frac{\langle 0|\mu_{\alpha}|i\rangle\langle i|\mu_{\beta}|f\rangle}{\omega_{i} - \frac{\omega_{f}}{2}} + \frac{\langle 0|\mu_{\beta}|i\rangle\langle i|\mu_{\alpha}|f\rangle}{\omega_{i} - \frac{\omega_{f}}{2}} \right)$$
(2)

Note that by symmetry:

$$\langle \mathbf{A}_g | \hat{\mu} | \mathbf{A}_g \rangle = 0$$
  
 $\langle \mathbf{A}_g | \hat{\mu} | \mathbf{A}_u \rangle \neq 0$ 

 $\delta_{\text{TPA}}$  can be related to experimentally measured TPA cross sections using the following equation:

$$\sigma_2(\omega) = \frac{4\pi^3 \alpha a_0^5 \omega^2}{c} g(2\omega) \delta_{\text{TPA}}$$
(3)

where  $g(2\omega)$  is the line shape function,  $a_0$  is the Bohr radius,  $\alpha$  is the fine structure constant, c is the speed of the light. In our studies we used a normalized Gauss function as a line shape function with a broadening parameter,  $\Gamma_f$ , equal to 0.50 eV. The final expression of TPA cross section in the maximum of the band reads:

$$\sigma_2(\omega = \frac{1}{2}\omega_f) = \frac{8\pi^3 \sqrt{2\ln 2\alpha a_0^5 \omega^2}}{c\Gamma_f \sqrt{2\pi}} \delta_{\text{TPA}}.$$
(4)

The results of calculations of two-photon absorption properties are presented in Tables S18–S20 (model A) and in Tables S24 and S25 (model B). In order to gain an insight into aggregation-induced increase in TPA intensity we performed an analysis of electronic structure parameters (transition moments and excitation energies) for monomer and dimer (model A), and the data are collected in Table S21. The obtained results are discussed in the manuscript.

Table S1: One-photon absorption spectra of monomer *in vacuo* determined at the B3LYP/6-31G(d,p) level of theory.

	Symmetry	$\Delta E_{\mathrm{vert}}$ [eV]	$\lambda_{\mathrm{vert}}$ [nm]	f
1	$A_u$	2.5842	479.78	1.0695
2	$A_q$	3.1979	387.70	0.0000
2	$A_u$	3.1996	387.50	0.0136
3	$A_g$	3.2068	386.63	0.0000
3	$A_u$	3.2867	377.23	0.0187
4	$A_q$	3.3804	366.78	0.0000
4	$A_u$	3.4789	356.39	0.3195
5	$A_u$	3.6867	336.30	0.0002
6	$A_u$	3.8385	323.00	0.0404
5	$A_q$	3.8386	323.00	0.0000
7	$A_u^{\circ}$	4.1283	300.33	0.8100
6	$\mathrm{A}_q$	4.1918	295.78	0.0000
7	$\mathbf{A}_{g}^{s}$	4.1939	295.63	0.0000
8	$A_u^{"}$	4.1946	295.58	0.0079
8	$A_g$	4.2366	292.65	0.0000

Table S2: One-photon absorption spectra of monomer in vacuo determined at the  $\omega$ B97X-D/6-31G(d,p) level of theory.

	Symmetry	$\Delta E_{\mathrm{vert}}$ [eV]	$\lambda_{\mathrm{vert}}$ [nm]	f
1	$A_u$	3.0305	409.12	1.1367
2	$A_u$	3.9325	315.28	0.0006
2	$A_g$	4.1279	300.36	0.0000
3	$A_u$	4.1284	300.32	0.0737
3	$A_g$	4.1545	298.43	0.0000
4	$A_u$	4.1600	298.04	1.2118
5	$A_u$	4.4748	277.07	0.0649
4	$A_g$	4.5250	274.00	0.0000
6	$A_u$	4.8367	256.34	0.0106
5	$A_g$	4.8644	254.88	0.0000
6	$A_g$	5.0038	247.78	0.0000
7	$A_u$	5.1798	239.36	1.2193
7	$A_g$	5.2441	236.43	0.0000
8	$A_u$	5.2670	235.40	0.0793
8	$A_g$	5.2733	235.12	0.0000

Table S3: One-photon absorption spectra of monomer  $in\ vacuo$  determined at the BHandHLYP/6-31G(d,p) level of theory.

	Symmetry	$\Delta E_{\mathrm{vert}}$ [eV]	$\lambda_{\mathrm{vert}}$ [nm]	f
1	$A_u$	2.9826	415.70	1.2110
2	$A_u$	4.0120	309.03	0.0113
2	$A_q$	4.0430	306.66	0.0000
3	$A_u$	4.0659	304.94	0.9357
3	$A_{g}$	4.1638	297.77	0.0000
4	$A_u$	4.1645	297.72	0.0830
4	$A_g$	4.2095	294.53	0.0000
5	$A_u$	4.2567	291.27	0.0865
6	$A_u$	4.7410	261.51	0.1852
5	$A_{g}$	4.7858	259.07	0.0000
7	$A_u$	4.8446	255.92	0.0506
6	$A_{g}$	4.8471	255.79	0.0000
7	$A_g^{\circ}$	5.0068	247.63	0.0000
8	$A_u$	5.1957	238.63	1.0881
8	$A_g$	5.2098	237.98	0.0000

Table S4: One-photon absorption spectra of monomer  $in\ vacuo$  determined at the CAM-B3LYP/6-31G(d,p) level of theory.

	Symmetry	$\Delta E_{ m vert}$ [eV]	$\lambda_{\mathrm{vert}}$ [nm]	f	orb. transitions
1	$A_u$	2.9932	414.22	1.1547	HOMO→LUMO
2	$A_u$	3.9210	316.21	0.0012	HOMO-5→LUMO, HOMO→LUMO+3
2	$A_g$	4.0679	304.79	0.0000	HOMO-3→LUMO, HOMO→LUMO+1
3	$A_{g}^{\circ}$	4.0796	303.92	0.0000	HOMO-2→LUMO+1, HOMO-1→LUMO
3	$A_u^{\circ}$	4.0797	303.90	0.1229	HOMO-2→LUMO, HOMO-1→LUMO+1
4	$A_u$	4.0864	303.41	0.9782	HOMO→LUMO+2,
4	$\mathrm{A}_q$	4.2911	288.93	0.0000	HOMO-3→LUMO, HOMO→LUMO+1
5	$\mathbf{A}_u^{"}$	4.3054	287.97	0.0883	HOMO-4→LUMO
6	$A_u$	4.7452	261.28	0.0756	HOMO-4→LUMO+2, HOMO-3→LUMO+1
5	$A_g$	4.7764	259.58	0.0000	HOMO-4→LUMO+1, HOMO-3→LUMO+2
7	$A_u^{\circ}$	4.9330	251.34	0.0788	HOMO-2→LUMO
6	$A_q$	4.9363	251.17	0.0000	HOMO-1→LUMO
7	$\mathbf{A}_q^{\scriptscriptstyle J}$	4.9703	249.45	0.0000	HOMO-6→LUMO
8	$\mathbf{A}_u^{"}$	5.1416	241.14	1.1409	HOMO-5→LUMO, HOMO→LUMO+3
8	$\mathbf{A}_g$	5.1557	240.48	0.0000	HOMO→LUMO+8

Table S5: One-photon absorption spectra of monomer in  $CHCl_3$  solution determined at the CAM-B3LYP/6-31G(d,p) level of theory. Solvent effects were included using PCM method.

	Symmetry	$\Delta E_{\mathrm{vert}}$ [eV]	$\lambda_{\mathrm{vert}}$ [nm]	f
1	$A_u$	2.9281	423.43	1.2751
2	$A_u$	3.9223	316.10	0.0032
2	$A_q$	3.9818	311.38	0.0000
3	$A_{g}^{\circ}$	4.0359	307.20	0.0000
3	$A_u$	4.0361	307.19	0.1343
4	$A_u$	4.0484	306.26	1.2070
4	$A_{g}$	4.2947	288.69	0.0000
5	$A_u$	4.3002	288.32	0.0313
6	$A_u$	4.7200	262.68	0.0968
5	$A_q$	4.7522	260.90	0.0000
7	$A_u$	4.8669	254.75	0.1039
6	$A_{g}$	4.8707	254.55	0.0000
8	$A_u^{"}$	4.9581	250.06	1.5224
7	$A_{g}$	4.9619	249.87	0.0000
7	$A_g^{\scriptscriptstyle S}$	5.1462	240.92	0.0000

Table S6: Frontier orbitals involved in one-photon transitions. All calculations were performed at the CAM-B3LYP level of theory. See Table 4 for orbital assignments.

НОМО LUMO HOMO-1 LUMO+1 HOMO-2 LUMO+2 HOMO-3 LUMO+3 HOMO-4 LUMO+4 HOMO-5 LUMO+5

Table S7: One-photon absorption spectra of dimer (model A)  $in\ vacuo$  determined at the B3LYP/6-31G(d,p) level of theory.

	Symmetry	$\Delta E_{ m vert}$ [eV]	$\lambda_{\mathrm{vert}}$ [nm]	f
2	$A_q$	2.0978	591.02	0.0000
1	$\mathbf{A}_u^{_\mathcal{J}}$	2.1250	583.45	0.2809
3	$A_{g}$	2.3604	525.27	0.0000
2	$A_u$	2.5337	489.34	1.7911
4	$A_{g}$	2.9416	421.48	0.0000
3	$A_u$	2.9560	419.43	0.0061
4	$A_u$	2.9602	418.84	0.0097
5	$A_q$	2.9739	416.91	0.0000
5	$A_u$	2.9746	416.81	0.0013
6	$A_{g}$	2.9942	414.08	0.0000
6	$A_u$	3.0110	411.77	0.0136
7	$A_{g}$	3.0305	409.12	0.0000
8	$A_{g}$	3.0508	406.40	0.0000
7	$A_u$	3.0535	406.04	0.0358
8	$A_u$	3.1318	395.89	0.1404
9	$A_{g}$	3.1326	395.79	0.0000
9	$A_u$	3.1686	391.29	0.0059
10	$A_g$	3.1688	391.27	0.0000
10	$A_u$	3.2028	387.11	0.0051
11	$A_g$	3.2057	386.77	0.0000

Table S8: One-photon absorption spectra of dimer (model A) in vacuo determined at the  $\omega$ B97X-D/6-31G(d,p) level of theory.

	Symmetry	$\Delta E_{ m vert}$ [eV]	$\lambda_{\mathrm{vert}}$ [nm]	f
2	$A_q$	2.6695	464.44	0.0000
1	$\mathbf{A}_u^{"}$	2.8233	439.15	1.7717
3	$\mathrm{A}_q$	3.2090	386.36	0.0000
2	$A_u$	3.2488	381.63	0.4603
3	$A_u$	3.7712	328.77	0.0047
4	$A_u$	3.8025	326.06	0.0020
4	$\mathbf{A}_g$	3.8100	325.41	0.0000
5	$\mathbf{A}_{g}$	3.8830	319.30	0.0000
5	$\mathbf{A}_u$	3.9654	312.67	0.0179
6	$\mathbf{A}_g$	3.9666	312.57	0.0000
6	$A_u$	3.9902	310.72	1.1023
7	${ m A}_g$	3.9966	310.22	0.0000
7	$A_u$	4.0262	307.94	0.7325
8	${ m A}_g$	4.0320	307.50	0.0000
9	$\mathbf{A}_g$	4.2544	291.42	0.0000
8	$\mathbf{A}_u$	4.2644	290.74	0.1507
10	$\mathbf{A}_g$	4.2870	289.21	0.0000
9	$\mathbf{A}_u$	4.3032	288.12	0.0084
11	$\mathbf{A}_g$	4.4364	279.47	0.0000
10	$\mathbf{A}_u$	4.4375	279.40	0.0272

Table S9: One-photon absorption spectra of dimer (model A) in vacuo determined at the BHandHLYP/6-31G(d,p) level of theory.

	Symmetry	$\Delta E_{ m vert}$ [eV]	$\lambda_{\mathrm{vert}}$ [nm]	f
2	$A_q$	2.5973	477.36	0.0000
1	$\mathbf{A}_u^{"}$	2.7347	453.37	1.5395
3	$\mathrm{A}_q$	3.0258	409.76	0.0000
2	$A_u$	3.0895	401.30	0.8466
3	$A_u$	3.6528	339.42	0.0045
4	$\mathbf{A}_g$	3.7741	328.51	0.0000
5	$\mathbf{A}_g$	3.8594	321.25	0.0000
4	$\mathbf{A}_u$	3.8602	321.18	0.5082
6	$\mathbf{A}_g$	3.8779	319.72	0.0000
5	$\mathbf{A}_u$	3.8798	319.56	0.6037
7	${ m A}_g$	3.9402	314.66	0.0000
6	$A_u$	3.9500	313.89	0.0140
7	$A_u$	3.9579	313.25	0.0605
8	${ m A}_g$	3.9614	312.98	0.0000
9	$\mathbf{A}_g$	4.0043	309.62	0.0000
8	$\mathbf{A}_u$	4.0065	309.46	0.0814
9	$A_u$	4.0279	307.81	0.2408
10	$\mathbf{A}_g$	4.0315	307.54	0.0000
11	${\rm A}_g$	4.1640	297.76	0.0000
10	$\mathbf{A}_u$	4.1648	297.70	0.0753

Table S10: One-photon absorption spectra of dimer (model A) in vacuo determined at the CAM-B3LYP/6-31G(d,p) level of theory.

	Symmetry	$\Delta E_{ m vert}$ [eV]	$\lambda_{\mathrm{vert}}$ [nm]	f	orb. transitions
2	$A_g$	2.6232	472.65	0.0000	HOMO-1→LUMO, HOMO→LUMO+1
1	$A_u^{\circ}$	2.7625	448.81	1.5832	$HOMO \rightarrow LUMO$
3	${f A}_g$	3.0721	403.58	0.0000	$HOMO-1 \rightarrow LUMO, HOMO \rightarrow LUMO+1$
2	$A_u$	3.1275	396.44	0.6843	HOMO-1→LUMO+1
3	$A_u$	3.6861	336.35	0.0048	$HOMO-2 \rightarrow LUMO+1, HOMO \rightarrow LUMO+3$
4	$A_u$	3.7848	327.58	0.0046	HOMO-11→LUMO+1, HOMO-10→LUMO
					HOMO→LUMO+7
4	$A_g$	3.7855	327.52	0.0000	HOMO→LUMO+5, HOMO→LUMO+6
5	$A_g$	3.8146	325.03	0.0000	HOMO→LUMO+2
6	$A_g$	3.9019	317.75	0.0000	$HOMO-2 \rightarrow LUMO, HOMO \rightarrow LUMO+2$
5	$A_u$	3.9040	317.59	0.3806	HOMO-3→LUMO
6	$A_u$	3.9051	317.49	0.7991	HOMO→LUMO+4
7	$A_g$	3.9070	317.34	0.0000	HOMO-4→LUMO
8	$A_g$	3.9553	313.46	0.0000	HOMO-3→LUMO+1
7	$A_u$	3.9565	313.37	0.2747	HOMO-4→LUMO+1
9	${f A}_g$	4.0393	306.95	0.0000	$HOMO-2 \rightarrow LUMO, HOMO \rightarrow LUMO+2$
8	$A_u$	4.0562	305.67	0.0232	HOMO-2→LUMO+1, HOMO→LUMO+3
10	$A_g$	4.0884	303.26	0.0000	HOMO-5→LUMO+1
9	$A_u$	4.0905	303.10	0.2124	HOMO-5→LUMO
11	$\mathbf{A}_g$	4.2379	292.56	0.0000	HOMO-1→LUMO+3
10	$A_u$	4.2388	292.50	0.0496	HOMO-1→LUMO+2

Table S11: One-photon absorption spectra of dimer (model A) in  $CHCl_3$  solution determined at the CAMB3LYP/6-31G(d,p) level of theory. Solvent effects were included using PCM method.

	Symmetry	$\Delta E_{ m vert}$ [eV]	$\lambda_{\mathrm{vert}}$ [nm]	f
2	$A_q$	2.6033	476.26	0.0000
1	$\mathbf{A}_u^{"}$	2.6961	459.86	2.0863
3	$\mathbf{A}_g$	3.0653	404.48	0.0000
2	$\mathbf{A}_u$	3.1040	399.44	0.6247
3	$\mathbf{A}_u$	3.6632	338.46	0.0058
4	${ m A}_g$	3.7794	328.06	0.0000
4	$A_u$	3.7843	327.63	0.0119
5	${ m A}_g$	3.8066	325.71	0.0000
6	$\mathbf{A}_{g}$	3.8197	324.59	0.0000
5	$\mathbf{A}_u$	3.8701	320.36	0.0901
7	${ m A}_g$	3.8726	320.16	0.0000
6	$A_u$	3.8735	320.08	1.4337
8	${ m A}_g$	3.9140	316.77	0.0000
7	$A_u$	3.9173	316.51	0.3449
9	$\mathbf{A}_g$	4.0386	307.00	0.0000
8	$\mathbf{A}_u$	4.0549	305.76	0.0185
9	$\mathbf{A}_u$	4.0802	303.87	0.1213
10	$\mathbf{A}_g$	4.0805	303.85	0.0000
11	${\rm A}_g$	4.2369	292.63	0.0000
10	$\mathbf{A}_u$	4.2423	292.26	0.0365

Table S12: Frontier orbitals involved in one-photon transitions. All calculations were performed at the CAM-B3LYP level of theory. See Table 10 for orbital assignments.

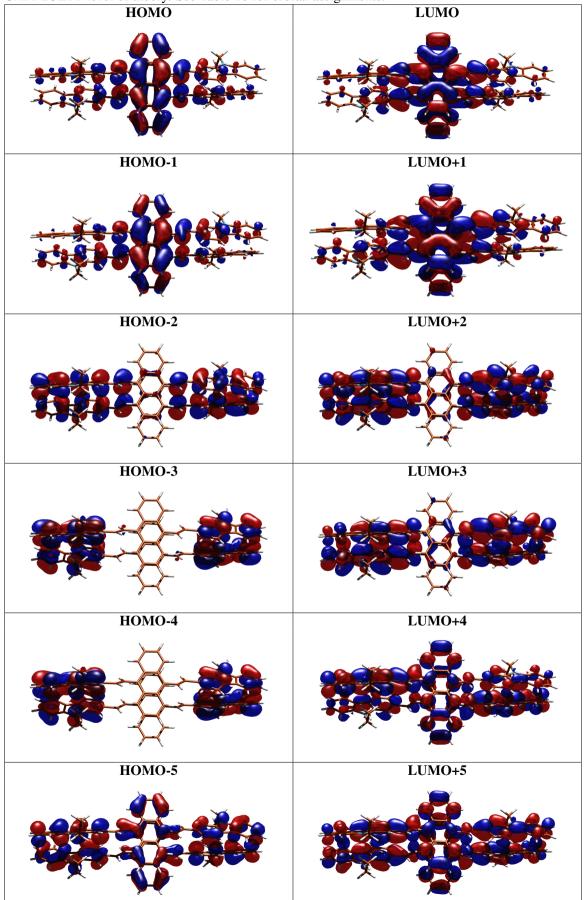


Table S13: One-photon absorption spectra of trimer (model A) *in vacuo* determined at B3LYP/6-31G(d,p) level of theory.

	Symmetry	$\Delta E_{\mathrm{vert}}$ [eV]	$\lambda_{\mathrm{vert}}$ [nm]	f
2	$A_g$	1.9317	641.84	0.0000
1	$A_u^{"}$	1.9326	641.54	0.0104
2	$A_u$	1.9757	627.53	0.3312
3	$A_g$	2.1608	573.79	0.0000
3	$A_u$	2.2826	543.18	0.0724
4	${f A}_g$	2.3134	535.93	0.0000
4	$A_u$	2.3846	519.94	0.3974
5	$A_g$	2.4188	512.58	0.0000
5	$A_u$	2.4906	497.82	1.7054
6	$A_g$	2.6727	463.89	0.0000
6	$A_u$	2.6911	460.71	0.0060
7	$A_g$	2.7022	458.82	0.0000
7	$A_u$	2.7451	451.66	0.0019
8	$A_g$	2.7881	444.69	0.0000
8	$A_u$	2.7956	443.50	0.0126
9	$A_g$	2.7972	443.24	0.0000
9	$A_u$	2.8496	435.09	0.0054
10	$A_g$	2.8527	434.61	0.0000
10	$A_u$	2.8695	432.07	0.0214
11	$A_u$	2.8786	430.71	0.1216

Table S14: One-photon absorption spectra of trimer (model A) in vacuo determined at  $\omega$ B97X-D/6-31G(d,p) level of theory.

	Symmetry	$\Delta E_{\mathrm{vert}}$ [eV]	$\lambda_{\mathrm{vert}}$ [nm]	f
1	$A_u$	2.4839	499.15	0.1482
2	$A_q$	2.6595	466.20	0.0000
2	$A_u^{\scriptscriptstyle J}$	2.7374	452.93	2.0037
3	$A_g$	3.1301	396.10	0.0000
3	$A_u$	3.1362	395.33	0.3657
4	$A_{g}$	3.1999	387.47	0.0000
4	$A_u$	3.2796	378.05	0.2867
5	$A_u$	3.7024	334.88	0.0078
5	$A_g$	3.7147	333.77	0.0000
6	$A_u$	3.7548	330.21	0.0051
6	$A_{g}$	3.7712	328.76	0.0000
7	$A_u$	3.7804	327.96	0.4001
7	$\mathrm{A}_g$	3.8631	320.95	0.0000
8	$A_u$	3.9253	315.86	0.2070
8	$\mathrm{A}_g$	3.9326	315.27	0.0000
9	$A_u$	3.9361	314.99	0.3885
9	$\mathrm{A}_g$	3.9417	314.54	0.0000
10	$A_u$	3.9583	313.22	1.3751
11	$A_u$	3.9694	312.35	0.0612
10	$A_g$	3.9864	311.02	0.0000

Table S15: One-photon absorption spectra of trimer (model A) in vacuo determined at BHandHLYP/6-31G(d,p) level of theory.

	Symmetry	$\Delta E_{\mathrm{vert}}$ [eV]	$\lambda_{\mathrm{vert}}$ [nm]	f
1	$A_u$	2.4059	515.34	0.1469
2	$A_q$	2.5604	484.24	0.0000
2	$A_u^{"}$	2.6240	472.50	1.4906
3	$A_g$	2.8926	428.63	0.0000
3	$A_u$	2.9225	424.25	0.7918
4	$A_g$	2.9715	417.25	0.0000
4	$A_u$	3.0721	403.59	0.5520
5	$A_u$	3.5296	351.27	0.0048
5	${f A}_g$	3.5335	350.88	0.0000
6	$A_g$	3.5363	350.60	0.0000
6	$A_u$	3.5911	345.26	0.1653
7	$A_g$	3.6350	341.09	0.0000
7	$A_u$	3.6902	335.98	0.4026
8	$A_u$	3.7570	330.00	0.0288
9	$A_u$	3.7655	329.27	0.4845
8	$A_g$	3.7907	327.07	0.0000
9	$A_g$	3.8102	325.40	0.0000
10	$A_u$	3.8212	324.46	0.4746
10	$A_g$	3.8256	324.09	0.0000
11	$A_u$	3.8453	322.43	0.1298

Table S16: One-photon absorption spectra of trimer (model A) in vacuo determined at CAM-B3LYP/6-31G(d,p) level of theory.

	Symmetry	$\Delta E_{ m vert}$ [eV]	$\lambda_{\mathrm{vert}}$ [nm]	f
1	$A_u$	2.4338	509.42	0.1449
2	$\mathbf{A}_g$	2.5967	477.47	0.0000
2	$\mathbf{A}_u$	2.6655	465.14	1.6731
3	$\mathbf{A}_g$	2.9619	418.60	0.0000
3	$\mathbf{A}_u$	2.9820	415.77	0.6024
4	${ m A}_g$	3.0361	408.36	0.0000
4	$\mathbf{A}_u$	3.1269	396.51	0.4238
5	${ m A}_g$	3.5932	345.05	0.0000
5	$\mathbf{A}_u$	3.6274	341.80	0.0954
6	$\mathbf{A}_u$	3.6903	335.97	0.2232
6	${ m A}_g$	3.7029	334.83	0.0000
7	$\mathbf{A}_u$	3.7232	333.01	0.0611
7	${ m A}_g$	3.7397	331.54	0.0000
8	$A_g$	3.7581	329.91	0.0000
8	$\mathbf{A}_u$	3.7582	329.90	0.0957
9	$\mathbf{A}_u$	3.7971	326.53	0.2757
10	$\mathbf{A}_u$	3.8283	323.86	0.4384
9	${ m A}_g$	3.8360	323.21	0.0000
10	${ m A}_g$	3.8546	321.65	0.0000
11	$A_u$	3.8712	320.28	0.5482

Table S17: One-photon absorption spectra of trimer (model A) in  $CHCl_3$  determined at CAM-B3LYP/6-31G(d,p) level of theory. Solvent effects were included using PCM method.

	Symmetry	$\Delta E_{\mathrm{vert}}$ [eV]	$\lambda_{\mathrm{vert}}$ [nm]	f
1	$A_u$	2.4192	512.50	0.2884
2	$A_q$	2.5619	483.96	0.0000
2	$A_u^{\scriptscriptstyle J}$	2.6002	476.82	2.1712
3	$A_g$	2.9189	424.76	0.0000
3	$A_u$	2.9308	423.03	0.8430
4	$A_g$	3.0680	404.12	0.0000
4	$A_u$	3.1477	393.89	0.3304
5	$A_{g}$	3.5560	348.66	0.0000
5	$A_u$	3.5869	345.66	0.1150
6	$A_g$	3.6426	340.37	0.0000
6	$A_u$	3.6836	336.59	0.3292
7	$\mathrm{A}_u$	3.7161	333.64	0.1753
7	$\mathrm{A}_g$	3.7371	331.77	0.0000
8	$A_u$	3.7443	331.13	0.0450
8	$\mathrm{A}_g$	3.7477	330.83	0.0000
9	$A_u$	3.7678	329.06	0.4176
10	$A_u$	3.7958	326.64	0.3805
9	$\mathrm{A}_g$	3.8004	326.24	0.0000
10	$A_g$	3.8164	324.87	0.0000
11	$A_u$	3.8282	323.87	0.4157

Table S18: Summary of CAM-B3LYP/6-31G(d,p) calculations of TPA properties for monomer in vacuo.

	Symmetry	$\Delta E_{\mathrm{vert}}$ [eV]	$\lambda_{\mathrm{vert}}$ [nm]	$\delta^{\mathrm{TPA}}$ [au]	$\sigma^{\mathrm{TPA}}$ [GM]
2	$A_g$	4.07	304.79	$0.611 \times 10^3$	2
3	$A_{g}^{\circ}$	4.08	303.92	$0.345 \times 10^4$	12
4	$A_g^{\circ}$	4.29	288.93	$0.446 \times 10^6$	1773
5	$A_g$	4.78	259.58	$0.107 \times 10^4$	5
6	$A_g$	4.94	251.17	$0.222 \times 10^4$	12
7	$A_g$	4.97	249.45	$0.132 \times 10^{5}$	70
8	$A_g$	5.16	240.48	$0.412 \times 10^5$	237

Table S19: Summary of CAM-B3LYP/6-31G(d,p) calculations of TPA properties for dimer (model A) in vacuo.

	Symmetry	$\Delta E_{ m vert}$ [eV]	$\lambda_{\mathrm{vert}}$ [nm]	$\delta^{ ext{TPA}}$ [au]	$\sigma^{\mathrm{TPA}}$ [GM]
2	$A_q$	2.62	472.65	$0.176 \times 10^3$	<1
3	$A_{g}^{J}$	3.07	403.58	$0.117 \times 10^4$	2
4	$A_{g}$	3.79	327.52	$0.235 \times 10^4$	7
5	$A_g$	3.81	325.03	$0.813 \times 10^{3}$	3
6	$A_g$	3.90	317.75	$0.145 \times 10^4$	5
7	$A_g$	3.90	317.34	$0.311 \times 10^4$	10
8	$A_g$	3.95	313.46	$0.167 \times 10^{5}$	56
9	$A_g$	4.04	306.95	$0.784 \times 10^{6}$	2764
10	$A_g$	4.09	303.26	$0.960 \times 10^{3}$	4
11	$A_g$	4.24	292.56	$0.822 \times 10^{3}$	3
12	$A_g$	4.39	282.40	$0.106 \times 10^{5}$	44
13	$A_g$	4.49	276.11	$0.416 \times 10^{3}$	2
14	$A_g$	4.52	274.28	$0.155 \times 10^4$	7
15	$A_{g}^{\circ}$	4.55	272.47	$0.805 \times 10^{3}$	4
16	$\mathbf{A}_g$	4.57	271.28	$0.120 \times 10^5$	54

Table S20: Summary of CAM-B3LYP/6-31G(d,p) calculations of TPA properties for trimer (model A) in vacuo.

	Symmetry	$\Delta E_{ m vert}$ [eV]	$\lambda_{\mathrm{vert}}$ [nm]	$\delta^{ ext{TPA}}$ [au]	$\sigma^{\mathrm{TPA}}$ [GM]
2	$A_g$	2.60	477.47	$1.83 \times 10^{3}$	3
3	${\rm A}_g^{\scriptscriptstyle S}$	2.96	418.60	$4.12 \times 10^{3}$	8
4	${\sf A}_g$	3.04	408.36	$4.87 \times 10^{3}$	10
5	$A_g$	3.59	345.05	$7.06 \times 10^{4}$	197
6	$A_g$	3.70	334.83	$4.71 \times 10^{4}$	139
7	$A_g$	3.74	331.54	$9.74 \times 10^{2}$	3
8	$A_g$	3.76	329.91	$1.29 \times 10^{4}$	39
9	${\sf A}_g$	3.84	323.21	$2.85 \times 10^{3}$	9
10	${\sf A}_g$	3.85	321.65	$7.75 \times 10^{3}$	25
11	$A_g$	3.89	318.57	$9.08 \times 10^{3}$	30
12	$A_g$	3.92	316.26	$3.40 \times 10^5$	1128
13	$A_g$	3.94	314.10	$3.51 \times 10^2$	1
14	$A_g$	3.97	312.14	$9.97 \times 10^{4}$	339
15	$A_g$	4.01	309.14	$1.38 \times 10^{5}$	479
16	$A_g$	4.07	304.94	$6.29 \times 10^{4}$	224
17	$A_g$	4.08	304.02	$2.76 \times 10^{4}$	99
18	${\sf A}_g$	4.12	301.23	$1.30 \times 10^{4}$	47
19	$A_g$	4.16	298.12	$1.27\times10^3$	5
20	$A_g$	4.24	292.16	$2.39\times10^5$	928
21	$A_g$	4.33	286.11	$5.88 \times 10^{2}$	2

Table S21: Unsigned transition moments along cartesian z direction between electronic states for monomer and dimer (model A). All calculations were performed at the CAM-B3LYP/6-31G(d,p) level of theory. Shown are also the diagonal components of second-order transition moment tensor ( $S_{ii}$ ). Key transition moments are marked in red colour.

			I	MONOM	ER $ \langle i \hat{\mu}_z $	$ j\rangle $				
	$S_{xx} = 44 \text{ au.}, S_{yy} = -6 \text{ au.}, S_{zz} = 1449 \text{ au.}$									
	$1 A_q$	$2 A_q$	$3 A_q$	$4 A_q$	$5 A_q$	$6 A_q$	$7 A_q$	$8 A_q$	$9 A_q$	
$1 A_u$	3.9035	0.2015	0.3056	5.1256	0.2461	0.1616	0.2511	0.4076	0.1110	
$2 A_u$	0.1095	0.1055	0.0255	0.1886	0.0955	0.0057	0.0583	0.0729	0.0024	
$3 A_u$	0.7229	0.3330	2.7916	1.4063	0.7657	4.3841	0.0775	0.1356	1.0060	
$4 A_u$	3.1147	0.9531	0.9938	4.2807	1.1222	1.0837	0.4173	0.5619	0.9041	
$5 A_u$	0.9059	5.5311	0.1753	0.9886	4.2448	1.0208	0.5115	1.0782	1.6408	
$6 A_u$	0.8055	0.7183	0.3085	4.7109	1.2498	1.2815	0.3712	0.1682	0.8129	
$7 A_u$	0.7919	0.7144	4.4795	0.8310	1.7749	10.4168	0.2374	0.3450	0.7523	
$8 A_u$	0.2616	0.2085	0.1559	0.7023	0.0056	0.2304	0.0762	0.0284	0.0262	
				DIMEI	$\mathbf{R}  \langle i \hat{\mu}_z j \rangle$	<b>)</b>				
		S	$S_{xx} = 161$	au., $S_{yy}$ =	= 36 au., <i>S</i>	$S_{zz} = 1780$	au.			
	$1 A_g$	$2 A_g$	$3 A_g$	$4 A_g$	$5 A_g$	$6 A_g$	$7 A_g$	$8 A_g$	$9 A_g$	
$1 A_u$	4.5883	0.1298	0.7378	0.3339	0.1472	0.2981	0.2409	0.6507	4.3783	
$2 A_u$	2.7810	0.5008	1.3140	0.0175	0.0814	0.0996	0.0074	0.0314	0.8110	
$3 A_u$	0.0717	0.0678	0.0265	0.5385	0.8002	0.6438	0.0279	0.4220	0.3346	
$4 A_u$	0.2202	0.1168	0.0831	0.1273	0.1417	0.0545	0.0271	0.1791	0.3152	
$5 A_u$	0.3219	0.2038	0.0819	0.0538	0.1997	0.1964	3.0003	0.2294	0.2610	
$6 A_u$	3.2816	0.4887	0.0860	0.1480	0.1837	0.8187	0.0327	1.0181	3.7771	
$7 A_u$	1.6193	0.0400	0.1386	0.2095	0.6029	1.2435	0.2287	2.6266	1.1415	
$8 A_u$	0.4602	4.9968	0.0520	2.1055	2.8189	0.2197	0.1619	0.5511	0.1927	

Table S22: One-photon absorption spectra of dimer (model B) in vacuo determined at the CAM-B3LYP/6-31G(d,p) level of theory.

	Symmetry	$\Delta E_{\mathrm{vert}}$ [eV]	$\lambda_{\mathrm{vert}}$ [nm]	f	orb. transitions
2	$A_g$	2.7456	451.57	0.0000	HOMO-1→LUMO, HOMO→LUMO+1
1	$A_u$	2.7521	450.51	1.2382	$HOMO \rightarrow LUMO$
3	$A_g$	3.2998	375.74	0.0000	HOMO-1→LUMO, HOMO→LUMO+1
2	$A_u$	3.4339	361.05	0.6748	HOMO-1→LUMO+1
3	$A_u$	3.7772	328.25	0.0086	HOMO-10→LUMO, HOMO→LUMO+10
4	$A_u$	3.7958	326.64	0.0154	HOMO-3→LUMO
4	$A_g$	3.8016	326.13	0.0000	HOMO-11→LUMO, HOMO→LUMO+11
5	$A_g$	3.8638	320.89	0.0000	HOMO→LUMO+3
5	$A_u$	3.9162	316.60	0.1927	HOMO-1→LUMO+3
6	${f A}_g$	3.9169	316.53	0.0000	HOMO-1→LUMO+2
6	$A_u$	3.9668	312.55	0.2354	HOMO-3→LUMO, HOMO→LUMO+2
7	$A_g$	3.9975	310.15	0.0000	HOMO-2→LUMO
7	$A_u$	4.0688	304.72	0.4313	HOMO→LUMO+4
8	$A_g$	4.0872	303.35	0.0000	HOMO-2→LUMO
8	$A_u$	4.1385	299.58	0.2815	HOMO-4→LUMO
9	${f A}_g$	4.1687	297.41	0.0000	HOMO-5→LUMO, HOMO→LUMO+9
10	$A_{g}^{\circ}$	4.1829	296.41	0.0000	HOMO→LUMO+5
9	$A_u^{"}$	4.2017	295.08	0.0150	HOMO-1→LUMO+5, HOMO→LUMO+8
10	$A_u$	4.3286	286.43	0.0238	HOMO-7→LUMO+2, HOMO-6→LUMO+3
11	$\mathbf{A}_g$	4.3336	286.10	0.0000	HOMO-7→LUMO+3, HOMO-6→LUMO+2

Table S23: One-photon absorption spectra of trimer (model B) in vacuo determined at CAM-B3LYP/6-31G(d,p) level of theory.

	Symmetry	$\Delta E_{ m vert}$ [eV]	$\lambda_{\mathrm{vert}}$ [nm]	f
1	$A_u$	2.7907	444.28	0.0165
2	$A_g$	2.8116	440.98	0.0000
2	$A_u$	2.8605	433.43	1.5040
3	$A_u$	3.3054	375.10	0.0375
3	${ m A}_g$	3.3070	374.91	0.0000
4	$\mathbf{A}_g$	3.3793	366.90	0.0000
4	$\mathbf{A}_u$	3.4191	362.63	0.7109
5	$A_u$	3.7592	329.81	0.0073
5	$\mathrm{A}_q$	3.8011	326.18	0.0000
6	$A_u$	3.8052	325.83	0.0002
6	$\mathrm{A}_q$	3.8377	323.07	0.0000
7	$A_u$	3.8851	319.13	0.0260
8	$A_u$	3.9307	315.43	0.0237
7	$A_g$	3.9496	313.91	0.0000
8	${\rm A}_g^{\scriptscriptstyle S}$	3.9904	310.71	0.0000
9	$\mathbf{A}_u^{"}$	3.9962	310.26	0.4888
9	$\mathbf{A}_g$	4.0515	306.02	0.0000
10	$\mathbf{A}_u^{^{\mathtt{J}}}$	4.0613	305.28	0.0301
10	$A_g$	4.0856	303.47	0.0000
11	$A_u^{^{^{3}}}$	4.0957	302.72	0.0030

Table S24: Summary of CAM-B3LYP/6-31G(d,p) calculations of TPA properties for dimer (model B) in vacuo.

	Symmetry	$\Delta E_{\mathrm{vert}}$ [eV]	$\lambda_{\mathrm{vert}}$ [nm]	$\delta^{\mathrm{TPA}}$ [au]	$\sigma^{\mathrm{TPA}}$ [GM]
2	$A_g$	2.75	451.57	$4.13 \times 10^{2}$	1
3	$A_g^{\scriptscriptstyle S}$	3.30	375.74	$3.41 \times 10^{3}$	8
4	$A_g$	3.80	326.13	$2.63 \times 10^{2}$	1
5	$A_g$	3.86	320.89	$3.47 \times 10^{3}$	11
6	$A_g$	3.92	316.53	$1.04 \times 10^{4}$	35
7	$A_g$	4.00	310.15	$1.13 \times 10^{5}$	391
8	$A_g$	4.09	303.35	$1.59 \times 10^{5}$	575
9	$A_g$	4.17	297.41	$6.37 \times 10^{3}$	24
10	$A_g$	4.18	296.41	$2.49 \times 10^{5}$	940
11	$A_g$	4.33	286.10	$3.06 \times 10^{3}$	12
12	$A_g$	4.48	276.76	$7.23 \times 10^{2}$	3
13	$A_g$	4.55	272.69	$3.67 \times 10^{3}$	16
14	$A_g$	4.59	270.26	$9.19 \times 10^{2}$	4
15	$A_g$	4.62	268.32	$3.64 \times 10^{3}$	17
16	$A_g$	4.67	265.27	$8.10 \times 10^2$	4

Table S25: Summary of CAM-B3LYP/6-31G(d,p) calculations of TPA properties for trimer (model B) in vacuo.

	Symmetry	$\Delta E_{\mathrm{vert}}$ [eV]	$\lambda_{\mathrm{vert}}$ [nm]	$\delta^{ ext{TPA}}$ [au]	$\sigma^{\mathrm{TPA}}$ [GM]
2	$A_g$	2.81	440.98	$1.20 \times 10^{2}$	< 1
3	${\rm A}_g^{\scriptscriptstyle S}$	3.31	374.91	$5.21 \times 10^{3}$	12
4	$A_g$	3.38	366.90	$4.80 \times 10^{2}$	1
5	$A_g$	3.80	326.18	$2.87 \times 10^{2}$	1
6	$A_g$	3.84	323.07	$1.44 \times 10^{3}$	5
7	$A_g$	3.95	313.91	$1.46 \times 10^{4}$	49
8	$A_g$	3.99	310.71	$5.20 \times 10^4$	179
9	$A_g$	4.05	306.02	$2.63 \times 10^4$	93
10	$A_g$	4.09	303.47	$1.42 \times 10^4$	51
11	$A_g$	4.11	301.87	$7.93 \times 10^4$	289
12	$A_g$	4.14	299.51	$5.78 \times 10^4$	214
13	$A_g$	4.21	294.84	$4.20 \times 10^{3}$	16
14	$A_g$	4.24	292.79	$9.26 \times 10^{2}$	4
15	${ m A}_g$	4.30	288.65	$1.79 \times 10^{5}$	715
16	$A_g$	4.40	281.62	$1.99 \times 10^{4}$	83
17	$A_g$	4.44	279.29	$2.82 \times 10^{3}$	12
18	$A_g$	4.48	276.44	$1.57 \times 10^{2}$	1
19	$A_g$	4.50	275.56	$8.42 \times 10^{2}$	4
20	$A_g$	4.53	273.75	$1.12 \times 10^{3}$	5
21	$A_g$	4.58	270.43	$1.80 \times 10^{3}$	8

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