

# Supporting Information

Yet again, new compounds found in systems with known binary phase diagrams. Synthesis, crystal and electronic structure of  $\text{Nd}_3\text{Bi}_7$  and  $\text{Sm}_3\text{Bi}_7$

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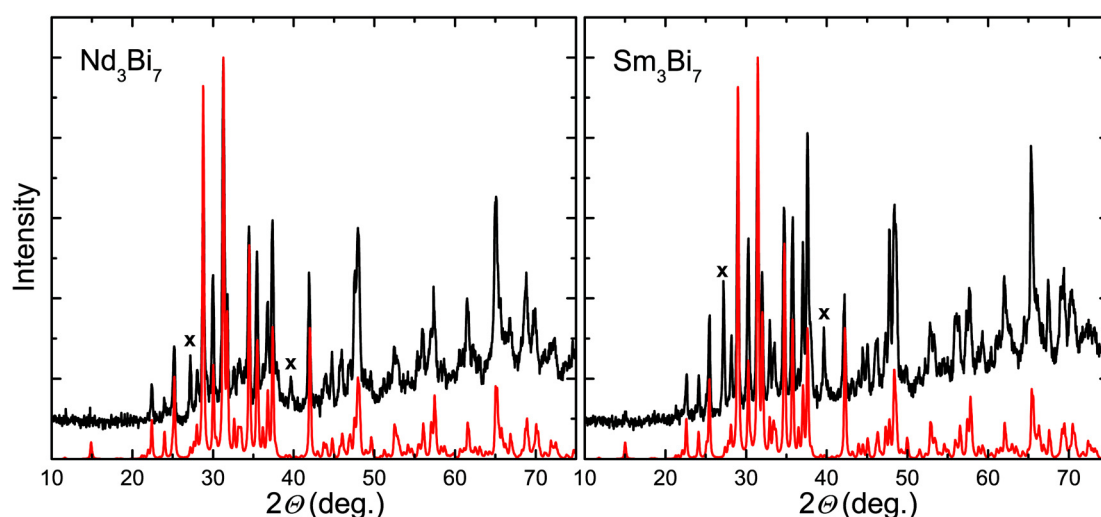
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## 1. Synthesis details

All operations except heat treatment were performed inside an argon-filled glovebox with oxygen and water contents below 0.1 ppm and 0.5 ppm, respectively.

### 1.1. Powder samples

Single phase powder samples of  $\text{Nd}_3\text{Bi}_7$  and  $\text{Sm}_3\text{Bi}_7$  were prepared by a direct combination of elements (Alfa, all with purity >99.9 wt. %). First, small pieces of the rare-earth metal and Bi were mixed in the stoichiometric ratio and placed in an alumina crucible sealed inside an evacuated fused silica tube. The total mass of the pellet was 500 mg. The reaction mixture was annealed at 450 °C for four days. After that, the resulting solid product was finely ground and pelletized. The pellet was annealed for additional two weeks at the same temperature.



**Figure S1.** Experimental (black) and theoretical (red) PXR patterns for  $\text{RE}_3\text{Bi}_7$  ( $\text{RE} = \text{Nd}, \text{Sm}$ ). Crosses mark the positions of the most intense Bragg peaks of the elemental Bi.

Powder X-ray diffraction patterns were collected on a Rigaku Miniflex diffractometer ( $\text{Cu K}_\alpha$  radiation,  $\lambda = 1.5418 \text{ \AA}$ ) in a  $\theta-\theta$  mode between  $10^\circ$  and  $75^\circ$  with a step size of  $0.05^\circ$  and 2 s/step counting time. Theoretical patterns were generated using the structural parameters obtained from the refinement of the single-crystal X-ray diffraction data.

The synthetic procedure described above yielded almost single-phase samples of  $\text{RE}_3\text{Bi}_7$  ( $\text{RE} = \text{Nd}, \text{Sm}$ ) as indicated by PXR analysis (Figure S1). The only observed impurity was the elemental Bi that must have formed on the grain boundaries upon short exposure of the

finely ground powders to air. Attempts were undertaken to obtain the  $RE_3Bi_7$  phases for  $RE = La-Pr, Eu$  and  $Gd$  using the same synthetic protocol, but these reactions failed to yield the desired products. The reaction outcomes are given in Table S1.

**Table S1.** Products of the reaction  $3 \times RE + 7 \times Bi$  (450 °C, 18 days with an intermediate regrinding) for  $RE = La-Pr, Eu$  and  $Gd$

<i>RE</i>	Products
La	LaBi <sub>2</sub> , Bi
Ce	CeBi <sub>2</sub> , Bi
Pr	PrBi <sub>2</sub> , Bi
Eu	EuBi <sub>2</sub> , EuBi <sub>3</sub>
Gd	GdBi, Bi

## 1.2. Single crystal growth procedure

For the single-crystal growth of  $Nd_3Bi_7$  and  $Sm_3Bi_7$ , the corresponding rare-earth metals (*RE*) were mixed with Bi in the ratio  $RE : Bi = 1 : 100$ . The mixture (total mass of ca. 3 g) was placed in an alumina crucible and topped with a piece of quartz wool acting as a filter. The crucible was enclosed in an evacuated fused silica tube and heated up to 1000 °C with 200 °C/h. After homogenization at this temperature for 5 h, the mixture was cooled down to 700 °C with 50 °C/h, and then to 400 °C with 5 °C/h. At this temperature, the reaction tube was taken out from the furnace, flipped over, and the excess of molten Bi was removed by centrifugation.

The large excess of Bi in comparison with the stoichiometric composition was necessary to assure complete dissolution of the rare-earth metal and to prevent the formation of the binary bismuthides  $REBi_2$ . The liquidus line for the latter apparently extends to high Bi concentrations, resulting in the precipitation of these undesired binary phases even from rather Bi-rich compositions, e.g.  $RE : Bi = 1 : 20$ .

The reaction tubes were crack-opened inside the glovebox. Single crystals of  $RE_3Bi_7$  ( $RE = Nd, Sm$ ) were the only product observed in the alumina crucible and on the quartz wool filter. Both  $Nd_3Bi_7$  and  $Sm_3Bi_7$  grow with a needle-like morphology. Smaller needles tend to form agglomerates, whereas larger needles with linear dimensions up to 4 mm appear as individual single crystals upon inspection under an optical microscope. PXRD patterns of the ground crystals were consistent with those of the powder samples produced at 450 °C.

## 2. Single-crystal X-ray diffraction (SCXRD)

Single-crystals suitable for X-ray diffraction were cut in dry Paratone-N oil from individual flux-grown needles. Data collection was done at  $T = 200$  K on a Bruker SMART CCD-diffractometer equipped with monochromated Mo  $K_{\alpha}$  radiation ( $\lambda = 0.71073$  Å). The raw data were integrated using the program SAINT.<sup>1</sup> Semiempirical absorption corrections were applied with the SADABS software.<sup>2</sup> Crystal structures were solved by direct methods and refined by full matrix least-squares methods on  $F^2$  using SHELXL.<sup>3</sup> Generating of the initial model in space group  $Immm$  (No. 71) and further refinements were straightforward. All atoms were refined anisotropically. The largest residual electron density peaks were located in the vicinity of the heavy Bi atoms—an apparent artifact of the semi-empirical absorption corrections (N.B. the absorption coefficients are extremely high, exceeding  $1000$  cm<sup>-1</sup>).

**Table S2.** Data collection details and selected crystallographic data for  $RE_3Bi_7$  ( $RE = Nd, Sm$ ; space group  $Immm$ ,  $Z = 4$ ,  $T = 200$  K, Mo  $K_{\alpha}$   $\lambda = 0.71073$  Å)

Refined composition	Nd <sub>3</sub> Bi <sub>7</sub>	Sm <sub>3</sub> Bi <sub>7</sub>
Molecular weight/ g mol <sup>-1</sup>	1895.58	1913.91
$a$ / Å	4.2996(6)	4.2762(8)
$b$ / Å	15.200(2)	15.050(3)
$c$ / Å	19.121(3)	19.034(4)
$V$ / Å <sup>3</sup>	1249.6(3)	1225.0(4)
$\rho_{\text{calc}}$ / g cm <sup>-3</sup>	10.076	10.378
$\mu_{\text{MoK}\alpha}$ / cm <sup>-1</sup>	1103.4	1142.2
$R_1$ [ $I > 2\sigma(I)$ ] <sup>a</sup>	0.040	0.043
$wR_2$ [ $I > 2\sigma(I)$ ] <sup>a</sup>	0.082	0.086
$R_1$ [all data] <sup>a</sup>	0.056	0.058
$wR_2$ [all data] <sup>a</sup>	0.089	0.092
$\Delta\rho_{\text{max,min}}$ / e Å <sup>-3</sup>	3.21, -3.89	3.04, -4.51

<sup>a</sup> $R_1 = \sum ||F_o| - |F_c|| / \sum |F_o|$ ;  $wR_2 = [\sum [w(F_o^2 - F_c^2)^2] / \sum [w(F_o^2)^2]]^{1/2}$ , where  $w = 1/[\sigma^2 F_o^2 + (0.0248P)^2]$  for Nd<sub>3</sub>Bi<sub>7</sub>, and  $w = 1/[\sigma^2 F_o^2 + (0.0221P)^2]$  for Sm<sub>3</sub>Bi<sub>7</sub>.  $P = (F_o^2 + 2F_c^2)/3$ ; CIFs have been deposited with reference numbers CCDC 1833009 for Nd<sub>3</sub>Bi<sub>7</sub>, and CCDC 1833010 for Sm<sub>3</sub>Bi<sub>7</sub>.

**Table S3.** Atomic coordinates and equivalent isotropic displacement parameters ( $\text{\AA}^2$ ) for  $\text{Nd}_3\text{Bi}_7$ 

Atom	Site	$x$	$y$	$z$	$U_{\text{eq}}^a$
Nd1	8l	0	0.13913(7)	0.36829(6)	0.0158(2)
Nd2	4i	0	0	0.17266(8)	0.0160(3)
Bi1	8l	0	0.21176(5)	0.19682(4)	0.0170(2)
Bi2	8l	0	0.36019(5)	0.41198(4)	0.0190(2)
Bi3	4j	1/2	0	0.30090(6)	0.0164(2)
Bi4	4g	0	0.33521(7)	0	0.0179(2)
Bi5	2c	1/2	1/2	0	0.0191(3)
Bi6	2a	0	0	0	0.0213(3)

<sup>a</sup> $U_{\text{eq}}$  is defined as one third of the trace of the orthogonalized  $U_{ij}$  tensor.

**Table S4.** Anisotropic displacement parameters ( $\text{\AA}^2$ ) for  $\text{Nd}_3\text{Bi}_7$ 

Atom	$U_{11}$	$U_{22}$	$U_{33}$	$U_{12}$	$U_{13}$	$U_{23}$
Nd1	0.0153(5)	0.0173(5)	0.0148(5)	0	0	0.0009(4)
Nd2	0.0173(8)	0.0162(6)	0.0144(7)	0	0	0
Bi1	0.0171(4)	0.0175(3)	0.0163(4)	0	0	0.0001(3)
Bi2	0.0189(4)	0.0200(4)	0.0182(4)	0	0	-0.0004(3)
Bi3	0.0151(5)	0.0179(5)	0.0162(5)	0	0	0
Bi4	0.0165(5)	0.0230(5)	0.0142(5)	0	0	0
Bi5	0.0248(9)	0.0184(7)	0.0139(7)	0	0	0
Bi6	0.0192(8)	0.0288(8)	0.0158(7)	0	0	0

**Table S5.** Atomic coordinates and equivalent isotropic displacement parameters ( $\text{\AA}^2$ ) for  $\text{Sm}_3\text{Bi}_7$ 

Atom	Site	$x$	$y$	$z$	$U_{\text{eq}}^a$
Sm1	8l	0	0.13886(8)	0.36812(8)	0.0156(3)
Sm2	4i	0	0	0.1731(1)	0.0145(4)
Bi1	8l	0	0.21180(6)	0.19686(5)	0.0154(3)
Bi2	8l	0	0.36056(6)	0.41167(6)	0.0179(3)
Bi3	4j	1/2	0	0.30095(7)	0.0152(3)
Bi4	4g	0	0.33396(9)	0	0.0170(3)
Bi5	2c	1/2	1/2	0	0.0168(4)
Bi6	2a	0	0	0	0.0195(4)

<sup>a</sup> $U_{\text{eq}}$  is defined as one third of the trace of the orthogonalized  $U_{ij}$  tensor.

**Table S6.** Anisotropic displacement parameters ( $\text{\AA}^2$ ) for  $\text{Sm}_3\text{Bi}_7$ 

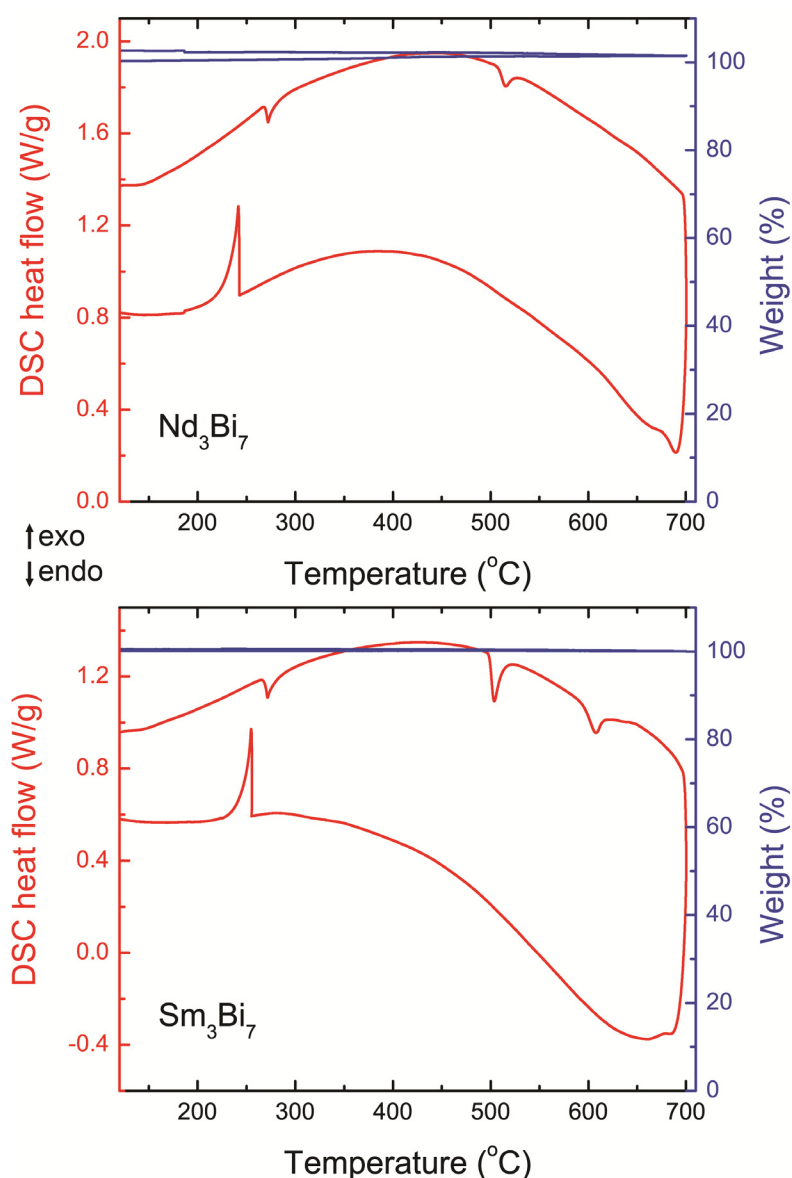
Atom	$U_{11}$	$U_{22}$	$U_{33}$	$U_{12}$	$U_{13}$	$U_{23}$
Sm1	0.0169(6)	0.0121(6)	0.0179(7)	0	0	0.0008(5)
Sm2	0.0173(9)	0.0119(8)	0.015(1)	0	0	0
Bi1	0.0174(5)	0.0124(5)	0.0166(5)	0	0	0.0004(3)
Bi2	0.0192(5)	0.0152(5)	0.0193(6)	0	0	-0.0001(4)
Bi3	0.0155(6)	0.0138(6)	0.0162(7)	0	0	0
Bi4	0.0157(7)	0.0189(7)	0.0163(8)	0	0	0
Bi5	0.023(1)	0.0141(9)	0.014(1)	0	0	0
Bi6	0.021(1)	0.023(1)	0.014(1)	0	0	0

**Table S7.** Selected interatomic distances ( $\text{\AA}$ ) in  $RE_3\text{Bi}_7$  ( $RE = \text{Nd}, \text{Sm}$ )

Atoms	Nd	Sm
$RE1-\text{Bi}3 \times 2$	3.2793(9)	3.252(1)
$RE1-\text{Bi}5$	3.289(1)	3.266(1)
$RE1-\text{Bi}4 \times 2$	3.3341(9)	3.323(1)
$RE1-\text{Bi}1 \times 2$	3.363(1)	3.340(1)
$RE1-\text{Bi}1$	3.460(1)	3.438(2)
$RE1-\text{Bi}2$	3.463(1)	3.440(2)
$RE2-\text{Bi}1 \times 2$	3.2517(9)	3.220(1)
$RE2-\text{Bi}3 \times 2$	3.261(2)	3.239(2)
$RE2-\text{Bi}6$	3.301(2)	3.295(2)
$RE2-\text{Bi}2 \times 4$	3.429(1)	3.403(1)
$\text{Bi}1-\text{Bi}1 \times 2$	3.180(1)	3.160(2)
$\text{Bi}1-\text{Bi}2 \times 2$	3.1851(9)	3.166(1)
$\text{Bi}2-\text{Bi}2$	3.366(2)	3.363(2)
$\text{Bi}2-\text{Bi}6 \times 2$	3.4597(7)	3.4354(9)
$\text{Bi}4-\text{Bi}5 \times 2$	3.3009(9)	3.289(1)

### 3. Differential scanning calorimetry (DSC)

Simultaneous differential scanning calorimetry thermogravimetric (DSC/TG) analysis was carried out using a SDT Q600 analyzer, supplied by TA Instruments, under a constant flow of high-purity argon (100 ml/min). Polycrystalline  $RE_3Bi_7$  intergrowths ( $RE = Nd, Sm$ ) produced by the Bi flux method were loaded in capped alumina pans. After equilibration at 100 °C, the temperature was raised to 700 °C with 10 °C/min, kept at this point for 1 min, and lowered to 100 °C with 10 °C/min. The results of the DSC/TG measurements are shown in Figure S2. No significant mass changes were observed in any of the runs.

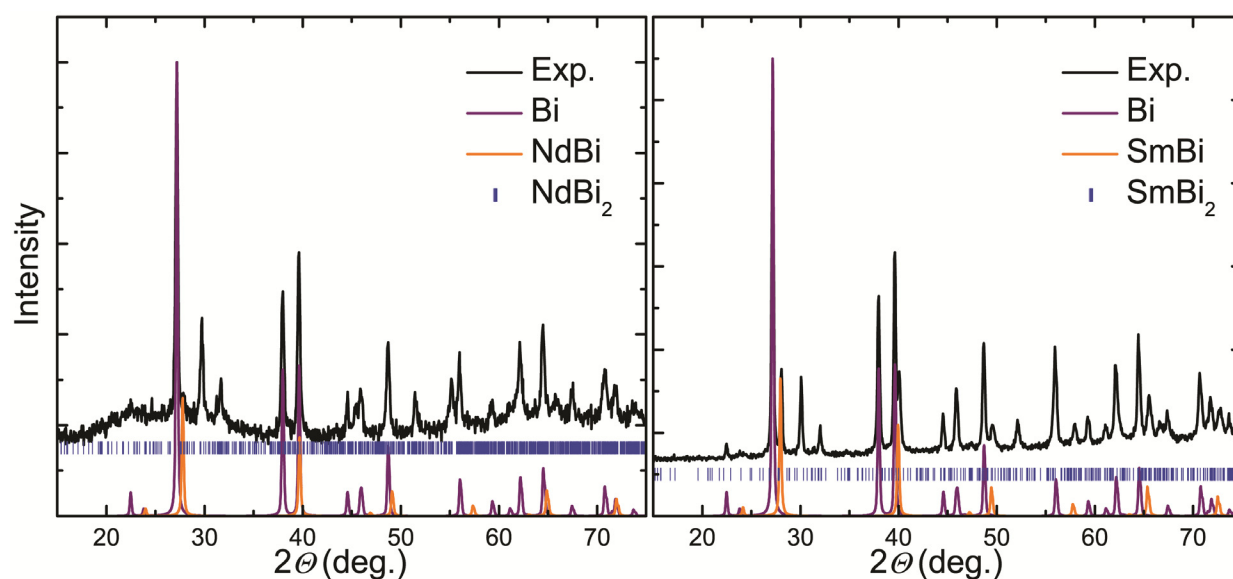


**Figure S2.** Results from the DSC/TG analysis for  $Nd_3Bi_7$  (top) and  $Sm_3Bi_7$  (bottom).

In both samples, a small endothermic peak is visible around 270 °C upon heating, indicating the melting of the residual Bi flux trapped between the individual crystals.

For  $\text{Nd}_3\text{Bi}_7$ , one intrinsic endothermic effect is observed upon heating at 508 °C. In the case of  $\text{Sm}_3\text{Bi}_7$ , two endothermic peaks are visible in the heating curve at 499 °C and 594 °C. PXRD analysis of the  $\text{RE}_3\text{Bi}_7$  ( $\text{RE} = \text{Nd}, \text{Sm}$ ) samples annealed at 650 °C for 30 min and air-quenched to room temperature revealed the presence of  $\text{REBi}$  and elemental Bi along with another product (Figure S3). The latter can be identified as  $\text{REBi}_2$ , although, since no structural data are available for the  $\text{NdBi}_2$  and  $\text{SmBi}_2$  phases, only a rough match with the reported Bragg peak positions was possible.<sup>4,5</sup>

Annealing of the  $\text{Sm}_3\text{Bi}_7$  sample at 520 °C yielded a powder pattern similar to that obtained after annealing at 650 °C. Thus, the nature of the second endothermic event at 594 °C remains unclear. The decomposition of  $\text{Sm}_3\text{Bi}_7$  with the onset temperature of 499 °C likely proceeds through an intermediate amorphous phase, which itself undergoes an endothermic transformation at 594 °C.



**Figure S3.** PXRD patterns of decomposition products (650 °C, 30 min) of  $\text{Nd}_3\text{Bi}_7$  (left) and  $\text{Sm}_3\text{Bi}_7$  (right).

Interestingly, dwelling of the decomposition products at 650 °C for five days does not result in significant changes of the PXRD patterns. According to the available phase diagrams,<sup>5-7</sup> for the composition  $\text{RE} : \text{Bi} = 3 : 7$  at this temperature, the  $\text{REBi}_2$  phases are expected to be in equilibrium with liquid Bi. Apparently, a high stability of the equiatomic  $\text{REBi}$  cubic phases,



which form upon decomposition of  $RE_3Bi_7$ , prohibits further transformation to  $REBi_2$  despite the presence of the excessive Bi metal.

The cooling DSC curves display the solidification of Bi as the only thermal event. PXRD patterns of the slowly cooled DSC samples are identical to those of the air-quenched products. Although the back-formation of  $RE_3Bi_7$  does not occur within the timeframe of the DSC experiment, annealing of the decomposition products at 450 °C for four days recovers the  $RE_3Bi_7$  phases, suggesting that these compounds are thermodynamically stable at this temperature.

#### 4. Physical property measurements

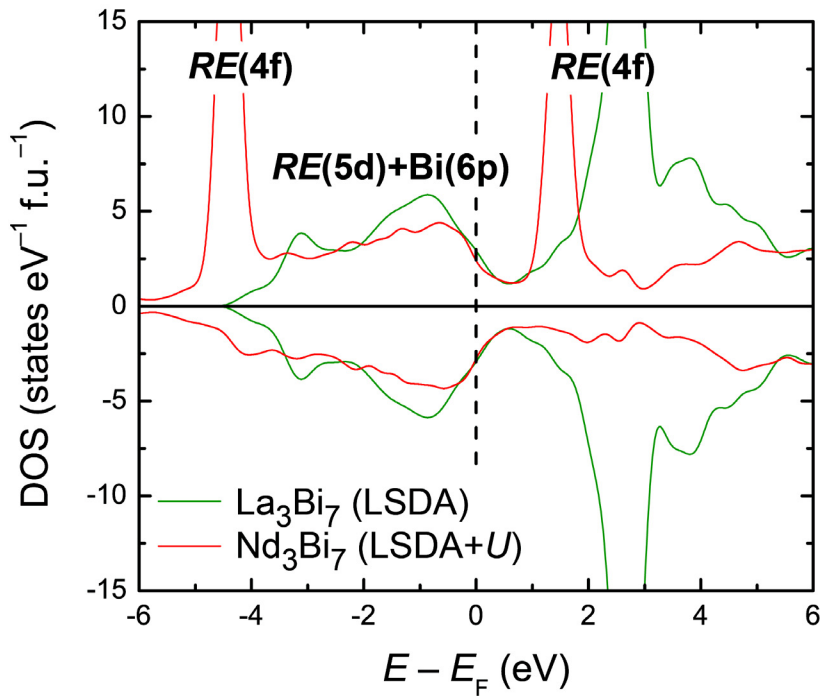
Temperature dependent electrical resistivity was measured from 5 to 300 K with an excitation current of 10 mA using a Quantum Design Physical Property Measurement System (PPMS). Four platinum wires were connected to single crystals of  $RE_3Bi_7$  ( $RE = Nd, Sm$ ) using EPO TEK H20E silver epoxy. The measurements were carried out on both heating and cooling for two different crystals to ensure reproducibility. Field-cooled direct current magnetization was measured on a collection of hand-picked single crystals using the PPMS in the temperature range  $T = 5\text{--}300$  K under an applied field of 5000 Oe. The measurements were done for two different batches to ensure reproducibility.

#### 5. First-principle calculations

Electronic structure calculations were performed for  $Nd_3Bi_7$  with the SIESTA code<sup>8</sup> employing the LSDA+ $U$  approach to take into account strong correlations on the Nd 4f-orbitals. The rotationally invariant scheme was applied with  $U_{\text{eff}} = 4.0$  eV, which is a typical value for rare-earth elements.<sup>9</sup> The Brillouin zone was sampled by a 6x6x6  $k$ -point grid and the Perdew-Zunger variant of the exchange-correlation functional was used. The mesh cutoff was set to 200 Ry after checking for convergence. For simplicity, we only considered a ferromagnetically ordered structure.

In addition, we conducted first-principle calculations for the hypothetical nonmagnetic compound  $La_3Bi_7$ . The initial structure was generated by extrapolating the unit cell parameters of  $RE_3Bi_7$  ( $RE = Nd, Sm$ ) for  $RE = La$ , while keeping the atomic coordinates of  $Nd_3Bi_7$ . At the next stage, the unit cell vectors and atomic coordinates were relaxed using the

Broyden–Fletcher–Goldfarb–Shanno (BFGS) algorithm implemented in the Quantum Espresso package.<sup>10</sup> The Perdew-Burke-Ernzerhof (PBE) flavor of the exchange-correlation functional was applied and the Brillouin zone was sampled by a  $4 \times 4 \times 4$   $k$ -point grid. Kinetic energy cutoff for wavefunctions was set to 100 Ry after checking for convergence. The forces were converged to less than 0.003 Ry/a.u.



**Figure S4.** Electronic density of states (DOS) for  $\text{Nd}_3\text{Bi}_7$  and  $\text{La}_3\text{Bi}_7$ . Positive and negative values correspond to majority and minority spin directions, respectively. Main contributions to the DOS are indicated (see the main text for details).

Aside from the differences in the 4f-states distribution arising from the magnetism in  $\text{Nd}_3\text{Bi}_7$ , the overall appearance of the electronic densities of states (Figure S4) is very similar for the two bismuthides. Since detailed analysis of the  $\text{Nd}_3\text{Bi}_7$  electronic structure requires establishing the magnetic ground state, we continue discussion of the electron counting and chemical bonding for the nonmagnetic  $\text{La}_3\text{Bi}_7$ .

**Table S8.** Atomic coordinates of the optimized  $\text{La}_3\text{Bi}_7$  structure ( $Immm$ ,  $a = 4.4848 \text{ \AA}$ ,  $b = 15.7190 \text{ \AA}$ ,  $c = 19.2754 \text{ \AA}$ )

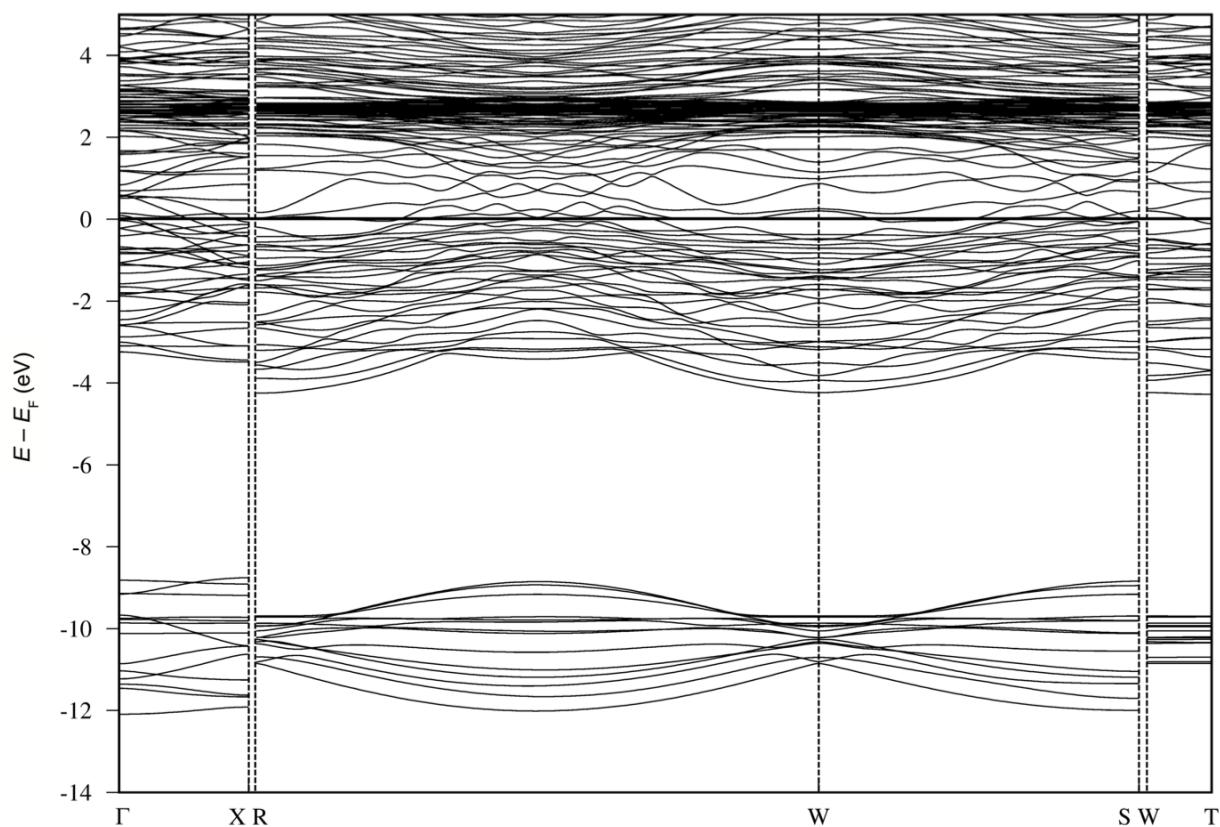
Atom	Site	$x$	$y$	$z$
La1	8l	0	0.13812	0.36784
La2	4i	0	0	0.17306
Bi1	8l	0	0.21351	0.19658
Bi2	8l	0	0.35920	0.41354
Bi3	4j	1/2	0	0.30123
Bi4	4g	0	0.34295	0
Bi5	2c	1/2	1/2	0
Bi6	2a	0	0	0

The optimized  $\text{La}_3\text{Bi}_7$  structure (Table S8) was used as an input for the all-electron TB-LMTO-ASA code.<sup>11</sup> For the latter, the von-Barth-Hedin functional was employed and a  $16 \times 16 \times 16$   $k$ -point grid was used to sample the Brillouin zone. To satisfy the atomic sphere approximation (ASA), an introduction of empty spheres was necessary. Chemical bonding was interrogated using the Crystal Orbital Hamilton Population (COHP) analysis.

The electronic band structure for  $\text{La}_3\text{Bi}_7$  is shown in Figure S5. The bands in the vicinity of the Fermi level ( $E_F$ ) have mainly La(5d) and Bi(6p) character. Above the Fermi level, a dense manifold of the La(4f) states is located, resulting in a peak in the density of states (Figure 2 in the main text). Localized bands below circa  $E - E_F = -8.0$  eV stem from the Bi(6s) states and hallmark the lone pair effect.

The COHP and integrated COHP (ICOHP) curves for selected symmetrically independent interactions are displayed in Figure S6. The pattern of interconnecting Bi atoms forming the anionic subunits in  $RE_3\text{Bi}_7$  is shown in Figure S7 for reference.

The La–Bi interactions in  $\text{La}_3\text{Bi}_7$  show bonding character below the Fermi level. Small peaks of bonding states also extend above  $E_F$ , making these interactions slightly underoptimized. A band of unoccupied antibonding states is located at  $E - E_F > 1.8$  eV.

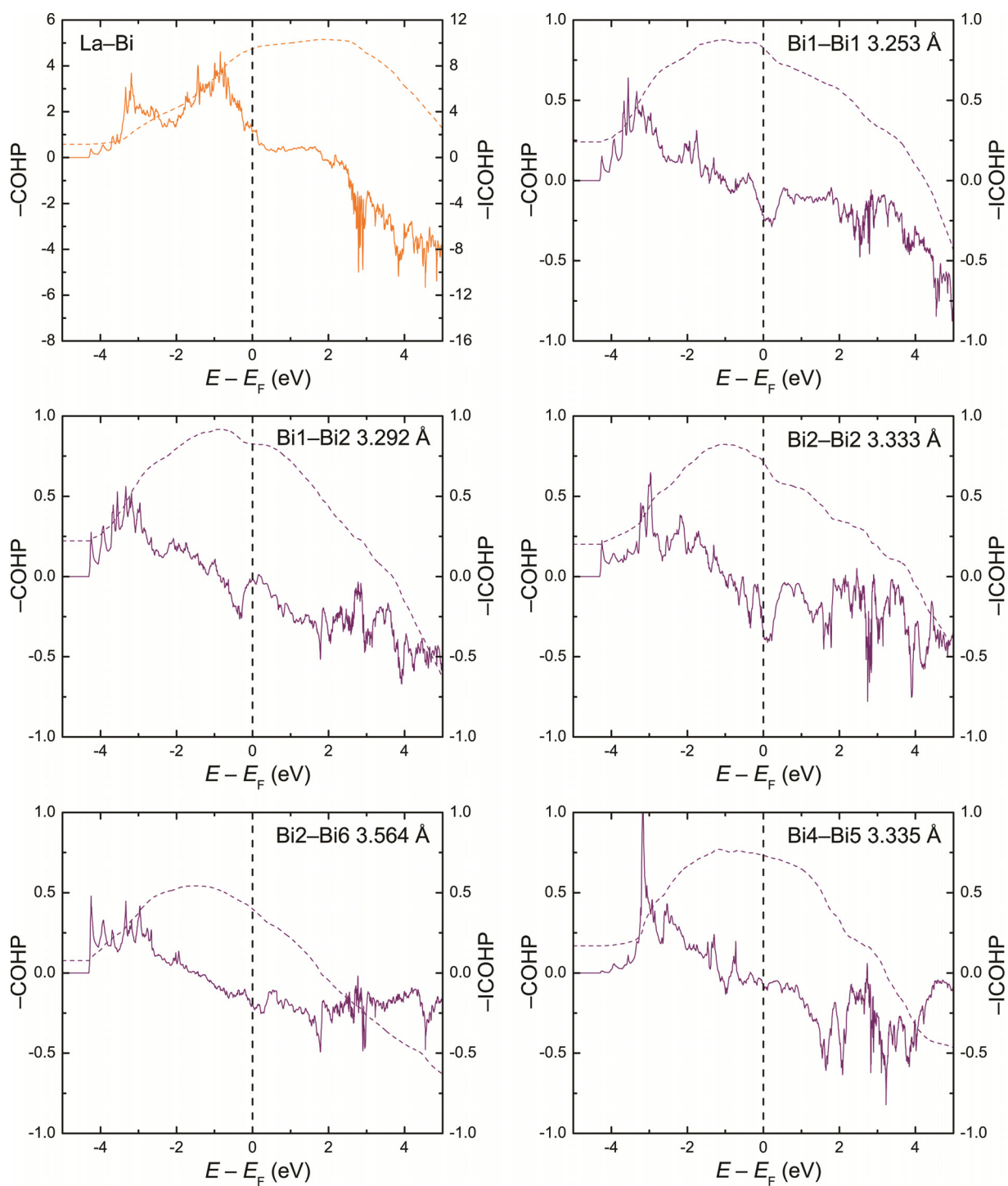


**Figure S5.** Electronic band structure along selected directions for the hypothetical  $\text{La}_3\text{Bi}_7$  compound.

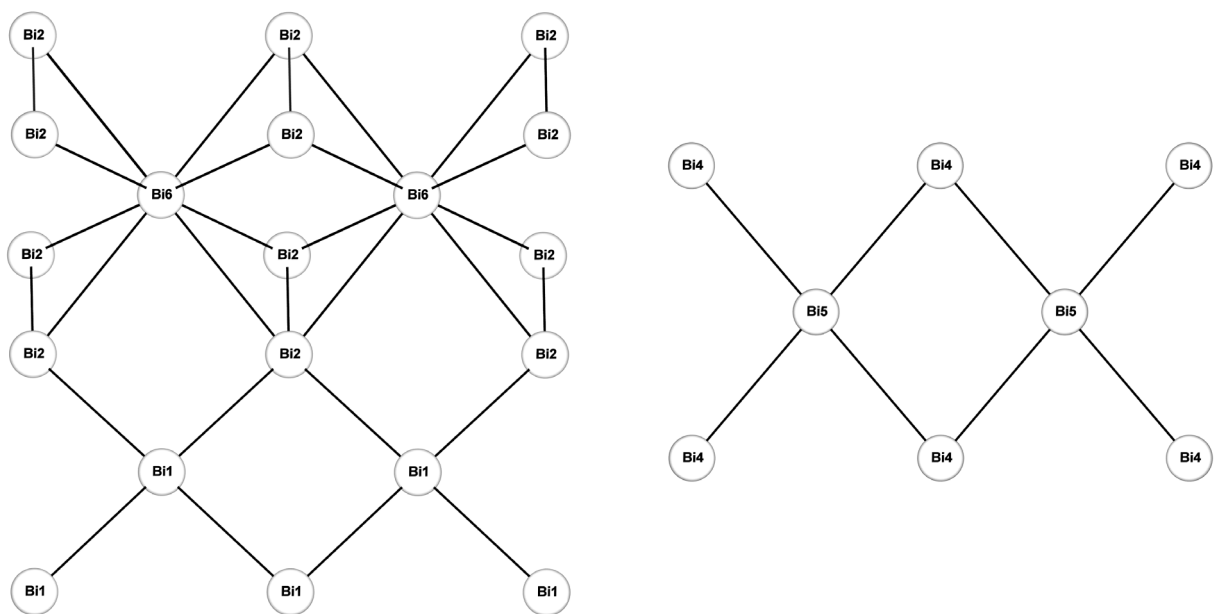
All Bi–Bi contacts show a combination of low-lying bonding states and smaller peaks of antibonding character located just below the Fermi level. Such a pattern of electronic state distribution along with the overall underoptimized bonding interaction is typical for hypervalent  $Pn$ – $Pn$  bonds.<sup>12,13</sup> Indeed, the interatomic Bi–Bi distances in the optimized  $\text{La}_3\text{Bi}_7$  structure, as well as in  $\text{RE}_3\text{Bi}_7$  ( $\text{RE} = \text{Nd}, \text{Sm}$ ), appear to be longer than single Bi–Bi bonds, but fall in the range of bonding contacts in electron-rich (hypervalent) bismuthides.<sup>14–15</sup> The –ICOHP values for the individual Bi–Bi interactions range from about 0.4 to 0.8 eV/bond. Taken as a measure of the strength of chemical interactions, these values expectedly increase with decreasing Bi–Bi interatomic separation. It is therefore reasonable to assume that for  $\text{RE}_3\text{Bi}_7$  ( $\text{RE} = \text{Nd}, \text{Sm}$ ), the contribution of the Bi–Bi interactions to the stability of the structure will be more substantial due to the shorter Bi–Bi bonds, whereas for earlier rare-earth metals, the large size of the  $\text{RE}$  cation leads to the expansion of the unit cell and weakening of the hypervalent bonding.

For the Bi1–Bi1 and Bi2–Bi2 interactions, the Fermi level crosses broad peaks of antibonding character, indicating possible electronic instability. Raising the electron count by about two electrons per formula unit will shift the Fermi level to a hollow in the density of states located  $\approx 0.5$  eV above the original  $E_F$  and to the base of the antibonding peaks. Besides lifting the electronic instability, such electron doping results in population of the bonding La–Bi states, although at the expense of the Bi–Bi interactions. The latter, being already electron-rich, suffer from further underoptimization when the number of electrons increases. Such an unfavorable effect can be counterbalanced by additional bonding interaction, as in the case of  $RE_6Zn_{1+x}Sb_{14}$  ( $RE = Sm, Gd-Ho$ )<sup>16</sup> and  $Ce_6ZnBi_{14}$ ,<sup>17</sup> representing stuffed variants of the  $(U_{0.5}Ho_{0.5})_3Sb_7$  structure. These compounds appear to be stabilized by additional Zn–Pn ( $Pn = Sb, Bi$ ) interactions, whereas the binary phases  $Ce_6Bi_{14}$  ( $\equiv Ce_3Bi_7$ ) and  $RE_6Sb_{14}$  ( $\equiv RE_3Sb_7$ ;  $RE = Sm, Gd-Ho$ ) are not known. The idealized composition  $RE_6Zn_2Pn_{14}$  ( $\equiv RE_3ZnPn_7$ ) corresponds to exactly two extra electrons added to the  $RE_3Pn_7$  formula unit. In line with our calculations, which predict shifting of the Fermi level to a minimum in the DOS, the hypothetical  $Gd_6Zn_2Sb_{14}$  displays a pseudogap at the Fermi level.<sup>16</sup>

Similarly, the prototypic  $(U_{0.5}Ho_{0.5})_3Sb_7$ , reportedly containing  $U^{4+}$ ,<sup>18</sup> possesses 1.5 extra electrons per formula unit in comparison with the hypothetical  $Ho_3Sb_7$ , with additional stabilization coming presumably from shorter  $RE-Sb$  bonds ( $RE = U/Ho$ ). Thus,  $Nd_3Bi_7$  and  $Sm_3Bi_7$  appear so far to be the only truly binary compounds of the  $(U_{0.5}Ho_{0.5})_3Sb_7$  structure type stable without electron doping.



**Figure S6.** COHP curves for selected interatomic contacts in  $\text{La}_3\text{Bi}_7$ .



**Figure S7.** Labeling of the Bi atoms in the anionic subunits of  $RE_3Bi_7$ .

## 6. References

- 1 SAINT; Bruker AXS Inc., Madison, Wisconsin, USA, 2014.
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