

Electron correlation effects of the ThO and ThS molecules in the spinor basis. A relativistic coupled cluster study of the ground and excited states properties.

Paweł Tecmer^{a 1} and
Cristina E. Gonzalez Espinoza^b

^a Institute of Physics, Faculty of Physics, Astronomy and Informatics, Nicolaus Copernicus University in Torun, Grudziadzka 5, 87-100 Torun, Poland

^b Department of Chemistry and Chemical Biology, McMaster University, Hamilton, 1280 Main Street West, L8S 4M1, Canada

Supplementary Information

¹ Author to whom correspondence should be sent; email: ptecmer@fizyka.umk.pl

1 Fock space coupled cluster: computational details

In both molecules the $7s$, $6d$, and $7p$ spinors were included in the model (P_i) space.

Table S1: A detailed description of active spaces used in the IH-FSCCSD calculations for the ThO molecule.

Method/ basis	inactive occupied	active occupied	active virtual	inactive virtual	P_i occupied (E_h)	P_i virtual(E_h)
IHFSCC(1,1)/dyall.v3z	18	16	22	354	$[-10.00; -0.30]$	$[0.08; 0.011]$
IHFSCC(0,2)/dyall.v3z	36	0	24	350	—	$[-0.30; -0.20]$

Table S2: A detailed description of active spaces used in the IH-FSCCSD calculations for the ThS molecule.

Method/ basis	inactive occupied	active occupied	active virtual	inactive virtual	P_i occupied (E_h)	P_i virtual (E_h)
IHFSCC(1,1)/dyall.v3z	18	16	12	352	$[-7.0; -0.30]$	$[0.07; 0.13]$
IHFSCC(0,2)/dyall.v3z	36	0	15	348	—	$[-0.30; -0.20]$

2 IHFSCC total energies

Table S3: IHFSCC total energies for ThO (in E_h).

τ_e [Å]	X	0 ⁺	1 (H)	2 (Q)	3 (W)	0 ⁻	0 ⁺ (A)	1 (B)	2	1 (C)	2	1 (D)	0 ⁻	0 ⁺ (E)
IHFSCC(1,1)														
1.74	-26592.427902	-26592.397888	-26592.393839	-26592.386774	-26592.371454	-26592.369036								
1.76	-26592.427902	-26592.402037	-26592.397962	-26592.390850	-26592.375748	-26592.373304			-26592.364276		-26592.352366			
1.78	-26592.430582	-26592.405243	-26592.401143	-26592.393985	-26592.379109	-26592.376642			-26592.368181		-26592.356637			
1.80	-26592.432383	-26592.407580	-26592.403458	-26592.396253	-26592.381788	-26592.377489			-26592.371157		-26592.359975			
1.82	-26592.433377	-26592.409121	-26592.404975	-26592.397724	-26592.383517	-26592.379131			-26592.373280	-26592.364213	-26592.362451			
1.84	-26592.433629	-26592.409029	-26592.405760	-26592.398463	-26592.384527	-26592.380057			-26592.374620	-26592.366105	-26592.364140			-26592.366351
1.86	-26592.433202	-26592.410063	-26592.405872	-26592.398530	-26592.384877	-26592.380327			-26592.375202	-26592.367767	-26592.365395			-26592.367567
1.88	-26592.432152	-26592.409579	-26592.405366	-26592.397979	-26592.384623	-26592.379998			-26592.374560	-26592.367651	-26592.365075			-26592.368117
1.90	-26592.430532	-26592.408529	-26592.404294	-26592.396861	-26592.383818	-26592.379121			-26592.373366	-26592.366973	-26592.364191			-26592.368055
1.92	-26592.428391	-26592.406958	-26592.402702	-26592.395225	-26592.382511	-26592.377746			-26592.371669	-26592.365782	-26592.362790			-26592.367432
1.94	-26592.425773	-26592.404913	-26592.400637	-26592.393115	-26592.380745	-26592.375918			-26592.369513	-26592.364120	-26592.360915			-26592.366295
1.96	-26592.422723	-26592.402435	-26592.398137	-26592.390571	-26592.378563	-26592.373680			-26592.366940	-26592.362030	-26592.358604			-26592.364690
														-26592.362658
														-26592.353056
IHFSCC(0,2)														
1.76	-26592.379733	-26592.350318	-26592.346563	-26592.339663	-26592.327650	-26592.325918	-26592.322197	-26592.320304	-26592.302628	-26592.311241	-26592.296273	-26592.298483	-26592.297258	-26592.297258
1.78	-26592.382462	-26592.353548	-26592.349768	-26592.342811	-26592.330959	-26592.329225	-26592.325553	-26592.323395	-26592.306129	-26592.314532	-26592.299725	-26592.301806	-26592.300021	-26592.300021
1.80	-26592.384399	-26592.355913	-26592.352108	-26592.345094	-26592.333402	-26592.331668	-26592.328043	-26592.325628	-26592.308756	-26592.316956	-26592.302310	-26592.304272	-26592.305948	-26592.305948
1.82	-26592.385525	-26592.357480	-26592.353651	-26592.346580	-26592.335046	-26592.333312	-26592.329735	-26592.327072	-26592.310596	-26592.318581	-26592.304095	-26592.306896	-26592.308932	-26592.308932
1.84	-26592.385905	-26592.358314	-26592.354461	-26592.347335	-26592.335954	-26592.334221	-26592.330693	-26592.327791	-26592.311706	-26592.319470	-26592.305144	-26592.307174	-26592.309377	-26592.309377
1.86	-26592.385601	-26592.358473	-26592.354597	-26592.347416	-26592.336187	-26592.334453	-26592.330975	-26592.327842	-26592.312141	-26592.319683	-26592.305516	-26592.307526	-26592.309777	-26592.309777
1.88	-26592.384669	-26592.358012	-26592.354114	-26592.346878	-26592.335796	-26592.334063	-26592.330634	-26592.327280	-26592.311955	-26592.319274	-26592.305266	-26592.306837	-26592.308714	-26592.308714
1.90	-26592.383163	-26592.356982	-26592.353061	-26592.345772	-26592.334834	-26592.333101	-26592.329721	-26592.326155	-26592.311197	-26592.318291	-26592.304442	-26592.305932	-26592.307981	-26592.307981
1.92	-26592.381129	-26592.355428	-26592.351486	-26592.344144	-26592.333345	-26592.331613	-26592.328282	-26592.324513	-26592.309913	-26592.316783	-26592.304507	-26592.306507	-26592.308192	-26592.308192

Table S4: IHFSCC total energies for ThS (in E_h).

r_e [Å]	X 0^+	1	2	3	0^-	0^+	1	2	2	1	0^-	0^+
IHFSCC(1,1)												
2.28	-26915.941297	-26915.927207	-26915.922587	-26915.915034					-26915.887693	-26915.879239		
2.30	-26915.942500	-26915.928946	-26915.924316	-26915.916720					-26915.889502	-26915.881375		
2.32	-26915.943257	-26915.930235	-26915.925594	-26915.917957	-26915.901068				-26915.899224	-26915.890884	-26915.883037	-26915.866635
2.34	-26915.943601	-26915.931106	-26915.926454	-26915.918774	-26915.902298				-26915.900493	-26915.891877	-26915.884282	-26915.868110
2.36	-26915.943561	-26915.931587	-26915.926924	-26915.919200	-26915.903146				-26915.901383	-26915.892810	-26915.885118	-26915.869188
2.38	-26915.943164	-26915.931705	-26915.927031	-26915.919263	-26915.903638				-26915.901919	-26915.892813	-26915.885566	-26915.869896
2.40	-26915.942435	-26915.931484	-26915.926800	-26915.918986	-26915.903797				-26915.902125	-26915.892813	-26915.885648	-26915.870259
2.42	-26915.941399	-26915.930950	-26915.926255	-26915.918396	-26915.903646				-26915.902023	-26915.892535	-26915.885384	-26915.870300
2.44	-26915.940079	-26915.930125	-26915.925418	-26915.917513	-26915.903206				-26915.901634	-26915.892000	-26915.884795	-26915.870042
IHFSCC(0,2)												
2.26	-26916.085623	-26916.062365	-26916.058120	-26916.050957	-26916.037115	-26916.035657	-26916.032240	-26916.027437	-26916.019367	-26916.014250	-26916.009399	-26916.004987
2.28	-26916.087272	-26916.064475	-26916.060217	-26916.053006	-26916.039408	-26916.037942	-26916.034586	-26916.029575	-26916.021660	-26916.016769	-26916.011982	-26916.007547
2.30	-26916.088434	-26916.066095	-26916.061823	-26916.054565	-26916.041204	-26916.039730	-26916.036436	-26916.031229	-26916.023457	-26916.018787	-26916.014068	-26916.009604
2.32	-26916.089145	-26916.067256	-26916.062972	-26916.055668	-26916.042535	-26916.041054	-26916.037820	-26916.032428	-26916.024791	-26916.020834	-26916.015691	-26916.011191
2.34	-26916.089442	-26916.068109	-26916.063809	-26916.056449	-26916.043591	-26916.042100	-26916.038942	-26916.033333	-26916.025853	-26916.021655	-26916.017109	-26916.012560
2.36	-26916.089327	-26916.068323	-26916.064013	-26916.056620	-26916.043923	-26916.042426	-26916.039312	-26916.033581	-26916.026188	-26916.022142	-26916.017656	-26916.013075
2.38	-26916.088855	-26916.068282	-26916.063960	-26916.056523	-26916.044033	-26916.042530	-26916.039476	-26916.033588	-26916.026307	-26916.022457	-26916.018053	-26916.013428
2.40	-26916.088042	-26916.067892	-26916.063558	-26916.056078	-26916.043790	-26916.042279	-26916.039284	-26916.033249	-26916.026073	-26916.022414	-26916.018092	-26916.013421
2.42	-26916.086912	-26916.067177	-26916.062831	-26916.055309	-26916.043217	-26916.041699	-26916.038761	-26916.032587	-26916.025511	-26916.022037	-26916.017797	-26916.013079
2.44	-26916.085487	-26916.066157	-26916.061800	-26916.054236	-26916.042335	-26916.040810	-26916.037930	-26916.031623	-26916.024642	-26916.021348	-26916.017189	-26916.012425

Table S5: Composition of the wave function for the ThO model IHFSCC(1,1) and IHFSCC(0,2) spaces. The assignment to the σ , π , δ , etc. is based on the Mullikan population analysis of the DHF spinors and should be considered as very approximate.

State	IHFSCC(1,1)	IHFSCC(0,2)
1 (H)	99% $\frac{1}{2}\sigma\frac{3}{2}\delta$	99% $\frac{1}{2}\sigma\frac{3}{2}\delta$
2 (Q)	69% $\frac{1}{2}\sigma\frac{3}{2}\delta + 29\%\frac{1}{2}\sigma\frac{5}{2}\delta$	71% $\frac{1}{2}\sigma\frac{3}{2}\delta + 28\%\frac{1}{2}\sigma\frac{5}{2}\delta$
3 (W)	100% $\frac{1}{2}\sigma\frac{5}{2}\delta$	99% $\frac{1}{2}\sigma\frac{5}{2}\delta$
0 ⁻	42% $\frac{1}{2}\sigma\frac{1}{2}\pi + 40\%\frac{1}{2}\sigma\frac{1}{2}\pi'$	98% $\frac{1}{2}\sigma\frac{1}{2}\delta$
0 ⁺ (A)	56% $\frac{1}{2}\sigma\frac{1}{2}\pi + 42\%\frac{1}{2}\sigma\frac{1}{2}\pi'$	98% $\frac{1}{2}\sigma\frac{1}{2}\delta$
2	66% $\frac{1}{2}\sigma\frac{3}{2}\delta + 24\%\frac{1}{2}\sigma\frac{3}{2}\delta'$	62% $\frac{1}{2}\sigma\frac{5}{2}\delta + 20\%\frac{1}{2}\sigma\frac{3}{2}\delta$
1 (C)	73% $\frac{1}{2}\sigma\frac{1}{2}\sigma' + 9\%\frac{1}{2}\sigma\frac{1}{2}\delta''$	77% $\frac{1}{2}\sigma\frac{1}{2}\delta + 17\%\frac{1}{2}\sigma\frac{3}{2}\delta'$
2	52% $\frac{1}{2}\sigma\frac{3}{2}\delta + 36\%\frac{1}{2}\sigma\frac{3}{2}\delta'$	89% $\frac{1}{2}\sigma\frac{3}{2}\delta$
0 ⁻	85% $\frac{1}{2}\sigma\frac{1}{2}\delta'$	98% $\frac{1}{2}\sigma\frac{1}{2}\delta'$
0 ⁺ (E)	84% $\frac{1}{2}\sigma\frac{1}{2}\delta'$	48% $\frac{1}{2}\sigma\frac{3}{2}\delta + 45\%\frac{1}{2}\sigma\frac{1}{2}\delta'$

Table S6: Composition of the wave function for the ThS model IHFSCC(1,1) and IHFSCC(0,2) spaces. The assignment to the σ , π , δ , etc. is based on the Mullikan population analysis of the DHF spinors and should be considered as very approximate.

State	IHFSCC(1,1)	IHFSCC(0,2)
1	97% $\frac{1}{2}\sigma\frac{3}{2}\delta$	99% $\frac{1}{2}\sigma\frac{3}{2}\delta$
2	66% $\frac{1}{2}\sigma\frac{3}{2}\delta + 31\%\frac{1}{2}\sigma\frac{5}{2}\delta$	69% $\frac{1}{2}\sigma\frac{3}{2}\delta + 30\%\frac{1}{2}\sigma\frac{5}{2}\delta$
3	100% $\frac{1}{2}\sigma\frac{5}{2}\delta$	100% $\frac{1}{2}\sigma\frac{5}{2}\delta$
0 ⁻	70% $\frac{1}{2}\sigma\frac{1}{2}\pi + 26\%\frac{1}{2}\sigma\frac{1}{2}\pi'$	97% $\frac{1}{2}\sigma\frac{1}{2}\sigma'$
0 ⁺	67% $\frac{1}{2}\sigma\frac{1}{2}\pi + 25\%\frac{1}{2}\sigma\frac{1}{2}\pi'$	97% $\frac{1}{2}\sigma\frac{1}{2}\sigma'$
2	53% $\frac{1}{2}\sigma\frac{3}{2}\delta' + 16\%\frac{1}{2}\sigma\frac{3}{2}\pi + 12\%\frac{1}{2}\sigma\frac{3}{2}\delta''$	56% $\frac{1}{2}\sigma\frac{5}{2}\delta + 21\%\frac{1}{2}\sigma\frac{3}{2}\delta + 12\%\frac{1}{2}\sigma\frac{3}{2}\delta'$
2	35% $\frac{1}{2}\sigma\frac{3}{2}\delta' + 32\%\frac{1}{2}\sigma\frac{3}{2}\pi + 12\%\frac{1}{2}\sigma\frac{3}{2}\delta''$	85% $\frac{1}{2}\sigma\frac{3}{2}\delta'$
0 ⁻	56% $\frac{1}{2}\sigma\frac{1}{2}\sigma' + 38\%\frac{1}{2}\sigma\frac{1}{2}\sigma''$	68% $\frac{3}{2}\delta\frac{3}{2}\delta + 21\%\frac{1}{2}\sigma\frac{1}{2}\sigma'$
0 ⁺	50% $\frac{1}{2}\sigma\frac{1}{2}\sigma' + 38\%\frac{1}{2}\sigma\frac{1}{2}\sigma''$	98% $\frac{1}{2}\sigma\frac{1}{2}\sigma'$