

Electronic Supplementary Information

**The role of electronegativity on the extent of nitridation
of group 5 metals as revealed
by reactions of tantalum cluster cations with ammonia molecules**

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Table S1. Cartesian coordinates and natural charge distribution of the optimized structures shown in Fig. 4 calculated with TPSSh/def2-TZVP using Stuttgart/Dresden relativistic effective potential (ECP) for tantalum atoms.

Species	Symmetry	Total energy /Hartree	Atom	$x/\text{\AA}$	$y/\text{\AA}$	$z/\text{\AA}$	Natural charge / e
$^3\text{TaNH}^+$	$C_{\infty v}$	-112.025719	Ta	0.000000	0.000000	0.182448	+1.445
			N	0.000000	0.000000	-1.537573	-0.867
			H	0.000000	0.000000	-2.555705	+0.421
$^1\text{Ta}_2\text{N}_2\text{H}_2^+$	C_{2v}	-167.447170	Ta	0.000000	0.205515	0.000000	+1.974
			N	1.428205	-0.825573	0.000000	-0.891
			N	-1.428205	-0.825573	0.000000	-0.891
			H	1.909502	-1.722304	0.000000	+0.404
			H	-1.909495	-1.722307	0.000000	+0.404
$^1\text{Ta}_2\text{N}_2^+$	C_{2v}	-166.135246	Ta	0.000000	0.000000	0.264284	+1.708
			N	0.000000	0.722422	-1.378052	-0.354
			N	0.000000	-0.722422	-1.378052	-0.354
$^4\text{Ta}_2^+$	$D_{\infty h}$	-113.549129	Ta	0.000000	0.000000	1.110866	+0.500
			Ta	0.000000	0.000000	-1.110866	+0.500
$^2\text{Ta}_2\text{NH}^+$	C_{2v}	-169.034315	Ta	0.000000	1.128951	-0.089413	+0.840
			Ta	0.000000	-1.128951	-0.089413	+0.840
			N	0.000000	0.000000	1.504652	-1.083
			H	0.000000	0.000000	2.521668	+0.402
$^2\text{Ta}_2\text{N}_2\text{H}_2^+$	C_{2v}	-224.499393	Ta	1.219799	0.000000	-0.061237	+1.147
			Ta	-1.219799	0.000000	-0.061237	+1.147
			N	0.000000	1.411766	0.514267	-1.047
			N	0.000000	-1.411766	0.514267	-1.047
			H	0.000000	-2.366216	0.870420	+0.400
			H	0.000000	2.366216	0.870420	+0.400
$^4\text{Ta}_2\text{N}_2^+$	D_{2h}	-223.306433	Ta	0.000000	0.000000	1.368087	+1.396
			Ta	0.000000	0.000000	-1.368087	+1.396
			N	0.000000	1.272131	0.000000	-0.896

			N	0.000000	-1.272131	0.000000	-0.896
${}^2\text{Ta}_2\text{N}_3\text{H}^+$	C_s	-278.749802	Ta	-0.839171	-1.209365	0.000000	+1.449
			Ta	0.859938	0.965219	0.000000	+1.809
			N	-0.034478	-0.195351	1.283151	-0.905
			N	-0.034478	-0.195351	-1.283151	-0.905
			N	-0.034478	2.485471	0.000000	-0.846
			H	-0.791974	3.159211	0.000000	+0.397
${}^2\text{Ta}_2\text{N}_4\text{H}_2^+$	C_{2v}	-334.126483	Ta	0.000000	1.406805	-0.159101	+1.746
			Ta	0.000000	-1.406805	0.159101	+1.746
			N	-1.283187	0.000000	-0.271977	-0.853
			N	1.283187	0.000000	-0.271977	-0.853
			N	0.000000	-1.923307	1.563348	-0.784
			N	0.000000	1.923307	1.563348	-0.784
			H	0.000000	-1.839036	2.574756	+0.391
			H	0.000000	1.839036	2.574756	+0.391
${}^2\text{Ta}_2\text{N}_4^+$	C_s	-332.818207	Ta	1.259094	-0.091452	0.017643	+1.632
			Ta	-1.259094	-0.091452	0.017642	+1.632
			N	0.000002	1.847356	0.081255	-0.280
			N	0.000001	-1.225743	-0.862552	-0.827
			N	0.000004	1.230056	-1.019129	-0.419
			N	-0.000005	0.055753	1.432460	-0.737
${}^3\text{Ta}_3^+$	D_{3h}	-170.574764	Ta	0.000000	1.410137	0.000000	+0.334
			Ta	-1.221214	-0.705068	0.000000	+0.333
			Ta	1.221214	-0.705068	0.000000	+0.333
${}^3\text{Ta}_3\text{NH}^+$	C_{2v}	-226.056553	Ta	0.000000	1.436078	-0.567469	+0.746
			Ta	0.000000	0.000000	1.354289	+0.205
			Ta	0.000000	-1.436078	-0.567469	+0.746
			N	0.000000	0.000000	-1.873941	-1.101
			H	0.000000	0.000000	-2.895085	+0.404
${}^1\text{Ta}_3\text{N}_2\text{H}_2^+$	C_s	-281.507448	Ta	-0.936091	1.042542	0.000000	+1.046

			Ta	0.414644	-0.669395	1.268022	+0.657
			Ta	0.414644	-0.669395	-1.268022	+0.657
			N	0.414644	1.259834	-1.456456	-1.070
			N	0.414644	1.259834	1.456456	-1.070
			H	0.995833	1.994203	1.855881	+0.390
			H	0.995833	1.994203	-1.855881	+0.390
${}^1\text{Ta}_3\text{N}_2^+$	C_1	-280.317386	Ta	-1.289395	-0.792519	-0.074956	+1.297
			Ta	1.495937	-0.495086	0.029010	+0.948
			Ta	-0.105682	1.406163	-0.073091	+0.558
			N	-1.337936	0.633936	1.167568	-0.876
			N	0.286115	-1.870330	0.073814	-0.927
${}^1\text{Ta}_3\text{N}_3\text{H}^+$	C_1	-335.779856	Ta	-0.715069	1.275523	0.027251	+0.947
			Ta	-0.752330	-1.221048	0.095574	+1.530
			Ta	1.573311	0.088484	-0.069036	+1.172
			N	-1.956732	0.077156	-0.876960	-1.136
			N	0.866594	-1.431832	-0.873517	-0.867
			N	0.375601	-0.161009	1.408501	-1.039
			H	-2.729839	0.173777	-1.532769	+0.392
${}^1\text{Ta}_3\text{N}_4\text{H}_2^+$	C_s	-391.254162	Ta	0.661134	1.240944	0.000000	+1.481
			Ta	-0.280070	-0.675747	1.359510	+1.559
			Ta	-0.280070	-0.675747	-1.359510	+1.559
			N	1.179214	-0.829285	0.000000	-1.085
			N	-1.481063	-1.195668	0.000000	-0.915
			N	-0.280070	1.304954	-1.765111	-1.183
			N	-0.280070	1.304954	1.765111	-1.183
			H	-0.669329	1.987716	2.412500	+0.384
			H	-0.669329	1.987716	-2.412500	+0.384
${}^1\text{Ta}_3\text{N}_4^+$	C_s	-390.028676	Ta	0.341857	-0.766088	1.263129	+1.584
			Ta	-0.753210	1.529673	0.000000	+1.715
			Ta	0.341857	-0.766088	-1.263129	+1.584
			N	-1.203253	-0.458640	0.000000	-1.033
			N	0.341857	1.189469	-1.440361	-0.942

			N	1.244281	-1.894192	0.000000	-0.965
			N	0.341857	1.189469	1.440361	-0.942
${}^1\text{Ta}_3\text{N}_5\text{H}^+$	C_s	-445.480315	Ta	0.394859	-0.850338	1.419231	+1.739
			Ta	-0.671719	1.433701	0.000000	+1.904
			Ta	0.394859	-0.850338	-1.419231	+1.739
			N	-0.960097	-0.669528	0.000000	-1.023
			N	0.394859	0.953983	-1.638564	-0.927
			N	1.595359	-1.208945	0.000000	-0.919
			N	0.394859	0.953983	1.638564	-0.927
			N	-2.213393	2.348215	0.000000	-0.977
			H	-3.094958	2.845136	0.000000	+0.391
${}^1\text{Ta}_3\text{N}_6\text{H}_2^+$	C_1	-500.831095	Ta	1.571098	0.214116	-0.063606	+1.850
			Ta	-1.184791	1.129503	0.206409	+1.754
			Ta	-0.639736	-1.651277	-0.013042	+1.738
			N	-0.048126	-0.205078	1.189524	-1.068
			N	-1.862148	-0.360354	-0.709414	-0.920
			N	0.877723	-1.447033	-0.977552	-0.894
			N	0.467169	1.763141	-0.695498	-0.611
			N	3.192170	0.216157	0.696176	-0.966
			N	-0.473081	2.782392	-0.770410	-0.650
			H	4.100168	0.195299	1.142729	+0.391
			H	-0.675871	3.019166	-1.745014	+0.376
${}^1\text{Ta}_3\text{N}_6^+$	C_1	-499.543643	Ta	1.597116	0.226288	0.073496	+1.528
			Ta	-0.821295	-1.423571	-0.203984	+1.664
			Ta	-1.058186	1.410431	0.015315	+1.734
			N	-0.165204	0.156989	-1.173182	-1.025
			N	-1.687970	-0.252859	0.887715	-0.878
			N	0.472358	1.809281	0.835466	-0.870
			N	1.091919	-1.733297	0.730760	-0.359
			N	2.822132	0.475519	-1.102330	-0.606
			N	0.411434	-2.678464	1.022662	-0.188

Table S2. Change in relative energy of the reactants and possible products upon reaction of Ta_n^+ with NH_3 molecules. The change in relative energy exhibits the same trend in both calculations employing TPSSh and B3LYP functional.

Species	Formal oxidation number of Ta atoms	Change in relative energy / eV	
		TPSSh	B3LYP
		Stuttgart/Dresden ECP	Stuttgart/Dresden ECP
<i>n</i> = 1			
Ta ⁺ + 2NH ₃	+1	0.00	0.00
TaNH ⁺ + H ₂ + NH ₃	+3	−2.33	−2.24
TaN ₂ H ₂ ⁺ + 2H ₂	+5	−1.19	−1.01
TaN ₂ ⁺ + 3H ₂	+7	+3.89	+4.06
<i>n</i> = 2			
Ta ₂ ⁺ + 4NH ₃	+0.5	0.00	0.00
Ta ₂ NH ⁺ + H ₂ + 3NH ₃	+1.5	−2.92	−2.62
Ta ₂ N ₂ H ₂ ⁺ + 2H ₂ + 2NH ₃	+2.5	−2.38	−2.15
Ta ₂ N ₂ ⁺ + 3H ₂ + 2NH ₃	+3.5	+0.65	+0.74
Ta ₂ N ₃ H ⁺ + 4H ₂ + NH ₃	+4.5	−1.78	−1.65
Ta ₂ N ₄ H ₃ ⁺ + 4H ₂ + H	+5	+0.26	−1.35
Ta ₂ N ₄ H ₂ ⁺ + 5H ₂	+5.5	−0.23	+0.21
Ta ₂ N ₄ ⁺ + 6H ₂	+6.5	+3.79	+4.37
<i>n</i> = 3			
Ta ₃ ⁺ + 6NH ₃	+0.3	0.00	0.00
Ta ₃ NH ⁺ + H ₂ + 5NH ₃	+1	−2.83	−2.64
Ta ₃ N ₂ H ₂ ⁺ + 2H ₂ + 4NH ₃	+1.7	−1.99	−1.70
Ta ₃ N ₂ ⁺ + 3H ₂ + 4NH ₃	+2.3	+0.58	+0.63
Ta ₃ N ₃ H ⁺ + 4H ₂ + 3NH ₃	+3	−2.30	−1.99
Ta ₃ N ₄ H ₂ ⁺ + 5H ₂ + 2NH ₃	+3.7	−2.63	−2.37
Ta ₃ N ₄ ⁺ + 6H ₂ + 2NH ₃	+4.3	+1.54	+1.49
Ta ₃ N ₅ H ⁺ + 7H ₂ + NH ₃	+5	−2.01	−2.00
Ta ₃ N ₆ H ₂ ⁺ + 8H ₂	+5.7	+0.74	+0.87
Ta ₃ N ₆ ⁺ + 9H ₂	+6.3	+1.83	+6.06

Table S3. Cartesian coordinates and natural charge distribution of the optimized structures shown in Fig. 5 calculated with TPSSh/def2-TZVP using Stuttgart/Dresden ECP for vanadium atoms.

Species	Symmetry	Total energy /Hartree	Atom	$x/\text{\AA}$	$y/\text{\AA}$	$z/\text{\AA}$	Natural charge / e
$^4\text{V}_2^+$	$D_{\infty h}$	-141.377560	V	0.000000	0.000000	0.836972	+0.500
			V	0.000000	0.000000	-0.836972	+0.500
$^2\text{V}_2\text{NH}^+$	C_{2v}	-196.786484	V	0.000000	0.872701	-0.254879	+0.725
			V	0.000000	-0.872701	-0.254879	+0.725
			N	0.000000	0.000000	1.338195	-0.842
			H	0.000000	0.000000	2.357049	+0.392
$^6\text{V}_2\text{N}_2\text{H}_2^+$	C_{2v}	-252.250293	V	1.355463	0.000000	-0.035231	+1.107
			V	-1.355463	0.000000	-0.035231	+1.107
			N	0.000000	1.262242	0.114163	-0.981
			N	0.000000	-1.262242	0.114163	-0.981
			H	0.000000	-2.279627	0.011164	+0.374
			H	0.000000	2.279627	0.011164	+0.374
$^4\text{V}_2\text{N}_2^+$	D_{2h}	-251.041795	V	0.000000	0.000000	1.256102	+1.052
			V	0.000000	0.000000	-1.256102	+1.052
			N	0.000000	1.183998	0.000000	-0.552
			N	0.000000	-1.183998	0.000000	-0.552
$^4\text{V}_2\text{N}_3\text{H}^+$	C_1	-306.406515	V	1.365261	0.247314	0.004780	+0.967
			V	-1.023126	-0.664089	0.014412	+1.091
			N	0.712812	-1.271982	-0.025374	-0.598
			N	-0.139176	1.138533	0.012242	-0.333
			N	-1.428876	1.217645	-0.104039	-0.528
			H	-1.882424	1.996459	0.378788	+0.400
$^2\text{V}_2\text{N}_4\text{H}_2^+$	C_1	-361.746380	V	1.308675	-0.565905	0.160696	+1.109
			V	-1.141375	-0.005115	-0.429864	+0.825
			N	0.357517	1.069919	-0.425192	-0.248
			N	-0.188796	-1.417158	-0.015279	-0.500
			N	-2.024359	0.349962	0.884392	-0.492
			N	1.417436	1.460047	0.132449	-0.491

			H	-2.341047	0.434472	1.851661	+0.386
			H	1.560549	2.459600	0.304606	+0.410
${}^1\text{V}_3^+$	D_{3h}	-212.188944	V	0.000000	1.04716	0.000000	+0.333
			V	-0.906867	-0.52358	0.000000	+0.334
			V	0.906867	-0.52358	0.000000	+0.334
${}^3\text{V}_3\text{NH}^+$	C_{2v}	-267.683752	V	0.000000	1.376211	-0.520755	+0.713
			V	0.000000	0.000000	1.687418	+0.273
			V	0.000000	-1.376211	-0.520755	+0.713
			N	0.000000	0.000000	-1.729169	-1.067
			H	0.000000	0.000000	-2.751686	+0.368
${}^1\text{V}_3\text{N}_2\text{H}_2^+$	C_s	-323.041065	V	-0.84920	0.779703	0.000000	+0.701
			V	0.295308	-0.769235	1.062416	+0.531
			V	0.295308	-0.769235	-1.062416	+0.531
			N	0.295308	1.004865	-1.388389	-0.769
			N	0.295308	1.004865	1.388389	-0.769
			H	0.906675	1.691771	1.826561	+0.388
			H	0.906675	1.691771	-1.826561	+0.388
${}^5\text{V}_3\text{N}_2^+$	C_1	-321.869345	V	0.423036	1.363954	-0.115475	+0.946
			V	-1.592672	-0.622484	0.087316	+0.801
			V	1.114097	-1.111850	-0.181644	+0.637
			N	1.463105	0.173177	0.789131	-0.671
			N	-1.280620	1.043787	-0.099780	-0.712
${}^3\text{V}_3\text{N}_3\text{H}^+$	C_1	-377.326275	V	1.409528	-0.930120	-0.034656	+1.006
			V	-0.032351	1.275064	0.311951	+0.937
			V	-1.481764	-0.784819	-0.157985	+0.945
			N	1.591178	0.813387	-0.535055	-0.966
			N	-1.299288	0.958209	-0.693153	-0.524
			N	-0.272479	-0.516698	0.992325	-0.775
			H	2.269624	1.332833	-1.092931	+0.376
${}^1\text{V}_3\text{N}_4\text{H}_2^+$	C_s	-432.752916	V	0.662345	1.027837	0.000000	+0.920

			V	-0.207486	-0.661542	1.237011	+0.901
			V	-0.207486	-0.661542	-1.237011	+0.901
			N	1.134819	-0.834447	0.000000	-0.576
			N	-1.346702	-1.033262	0.000000	-0.387
			N	-0.207486	1.155083	-1.587613	-0.771
			N	-0.207486	1.155083	1.587613	-0.771
			H	-0.650803	1.846731	2.191310	+0.391
			H	-0.650803	1.846731	-2.191310	+0.391
${}^3\text{V}_3\text{N}_4^+$	C_s	-431.537315	V	0.275182	-0.702210	1.292875	+0.900
			V	-0.832198	1.244006	0.000000	+0.901
			V	0.275182	-0.702210	-1.292875	+0.900
			N	-1.030245	-0.586272	0.000000	-0.535
			N	0.275182	1.033556	-1.320523	-0.389
			N	1.405909	-0.953765	0.000000	-0.388
			N	0.275182	1.033556	1.320523	-0.389
${}^1\text{V}_3\text{N}_5\text{H}^+$	C_1	-486.894737	V	1.497568	-0.727400	-0.154846	+0.948
			V	0.286334	1.487554	0.231391	+0.922
			V	-1.055333	-0.921900	0.369353	+0.860
			N	0.479740	-0.108024	1.181549	-0.600
			N	-1.469468	1.055258	-0.349482	-0.269
			N	-0.055139	-1.655677	-0.681105	-0.427
			N	1.485222	0.908517	-0.846089	-0.493
			N	-2.377605	0.249230	-0.607545	-0.337
			H	-3.196351	0.575017	-1.136962	+0.396
${}^3\text{V}_3\text{N}_6\text{H}_2^+$	C_1	-542.254336	V	-1.042144	-0.798859	-0.057799	+0.650
			V	1.499514	-0.009823	0.464353	+0.859
			V	-0.415493	1.692163	-0.075774	+0.865
			N	-0.287406	0.436509	1.144506	-0.503
			N	1.277382	1.357785	-0.513274	-0.389
			N	-1.244708	0.661923	-1.103381	-0.294
			N	0.756447	-1.517561	-0.539501	-0.214
			N	-2.458497	-1.440694	0.411251	-0.436
			N	1.969994	-1.782838	-0.455446	-0.327

			H	−3.392606	−1.710963	0.719828	+0.390
			H	2.336947	−2.614979	−0.936845	+0.397
$^1\text{V}_3\text{N}_6^+$	C_1	−541.044845	V	0.645203	1.209871	−0.135811	+0.653
			V	−1.366851	−0.547473	0.479265	+0.807
			V	1.079806	−1.367486	−0.040147	+0.893
			N	0.372798	−0.26585	1.113443	−0.499
			N	−0.742289	−1.559218	−0.609120	−0.349
			N	1.678979	−0.238950	−0.995307	−0.304
			N	−1.395128	1.300749	−0.580875	−0.124
			N	1.351285	2.242766	0.727544	−0.100
			N	−2.442447	0.837217	−0.652264	−0.023

Table S4. Change in relative energy of the reactants and possible products upon reaction of V_n^+ with NH_3 molecules. The change in relative energy obtained by either of the methods exhibits the same trend for $n = 2$ and 3; the result depends neither on functional nor on the use of ECP. For $n = 1$, the result is dependent on the method; the use of ECP resulted in far off from a previous experiment, where the total energy of $VNH^+ + H_2$ is reported to be about 0.1 eV lower than that of $V^+ + NH_3$.^a

Species	Formal oxidation number of V atoms	Change in relative energy / eV			
		TPSSh Stuttgart/Dresden ECP	TPSSh All electrons	B3LYP Stuttgart/Dresden ECP	B3LYP All electrons
<i>n</i> = 1					
V ⁺ + 4NH ₃	+1	0.00	0.00	0.00	0.00
VNH ⁺ + H ₂ + 3NH ₃	+3	+0.76	+0.01	+0.96	+0.25
VN ₂ H ₂ ⁺ + 2H ₂ + 2NH ₃	+5	+0.04	+0.30	+0.34	−0.01
VN ₂ ⁺ + 3H ₂ + 2NH ₃	+7	+1.61	+1.42	+1.47	+1.91
<i>n</i> = 2					
V ₂ ⁺ + 4NH ₃	+0.5	0.00	0.00	0.00	0.00
V ₂ NH ⁺ + H ₂ + 3NH ₃	+1.5	−0.85	−1.15	−1.33	−0.75
V ₂ N ₂ H ₂ ⁺ + 2H ₂ + 2NH ₃	+2.5	−2.34	−2.32	−2.47	−2.59
V ₂ N ₂ ⁺ + 3H ₂ + 2NH ₃	+3.5	+1.08	+0.89	+1.37	+1.25
V ₂ N ₃ H ⁺ + 4H ₂ + NH ₃	+4.5	+0.71	+0.64	+0.76	+0.70
V ₂ N ₄ H ₂ ⁺ + 5H ₂	+5.5	+0.68	+0.29	+0.81	+0.47
<i>n</i> = 3					
V ₃ ⁺ + 6NH ₃	+0.3	0.00	0.00	0.00	0.00
V ₃ NH ⁺ + H ₂ + 5NH ₃	+1	−3.18	−2.57	−3.80	−2.72
V ₃ N ₂ H ₂ ⁺ + 2H ₂ + 4NH ₃	+1.7	+0.56	−1.21	−0.12	−1.54
V ₃ N ₂ ⁺ + 3H ₂ + 4NH ₃	+2.3	+0.08	+1.15	+0.83	+0.77
V ₃ N ₃ H ⁺ + 4H ₂ + 3NH ₃	+3	−2.15	−2.31	−1.73	−2.06
V ₃ N ₄ H ₂ ⁺ + 5H ₂ + 2NH ₃	+3.7	−1.33	−2.17	−0.82	−1.59
V ₃ N ₄ ⁺ + 6H ₂ + 2NH ₃	+4.3	+1.27	+1.60	+1.94	+1.83
V ₃ N ₅ H ⁺ + 7H ₂ + NH ₃	+5	+0.55	+0.23	+0.31	+0.21
V ₃ N ₆ H ₂ ⁺ + 8H ₂	+5.7	+0.50	+0.26	+0.70	+0.43
VN ₆ ⁺ + 9H ₂	+6.3	+1.10	+1.50	+0.27	−1.39

^a D. E. Clemmer, L. S. Sunderlin and P. B. Armentrout, *J. Phys. Chem.*, 1990, **94**, 208–217.

Table S5. Bond dissociation energies obtained by DFT calculations along with experimental reports.

Species	Bond dissociation energy / eV				Experiment
	TPSSh Stuttgart/Dresden ECP	TPSSh All electrons	B3LYP Stuttgart/Dresden ECP	B3LYP All electrons	
Ta ⁺ –Ta	4.50		4.19		6.87 ^a
Ta ₂ ⁺ –Ta	5.55		4.74		6.60 ^a
Ta ₃ ⁺ –Ta	6.56		5.64		7.60 ^a
V ⁺ –V	2.26	2.88	2.12	1.95	3.14 ^b
V ₂ ⁺ –V	1.67	2.35	0.53	0.37	2.27 ^b

^a P. B. Armentrout, D. A. Hales and D. Lian, in *Advances in Metal and Semiconductor Clusters*, ed. M. A. Duncan, JAI Press, Greenwich, 1994, vol. 2, pp. 1–39.

^b C.-X. Su, D. A. Hales and P. B. Armentrout, *J. Chem. Phys.*, 1993, **99**, 6613–6623.