

Theoretical Study of Radiative and Nonradiative Decay Rates for Cu(I) Complexes with Double Heteroleptic Ligands

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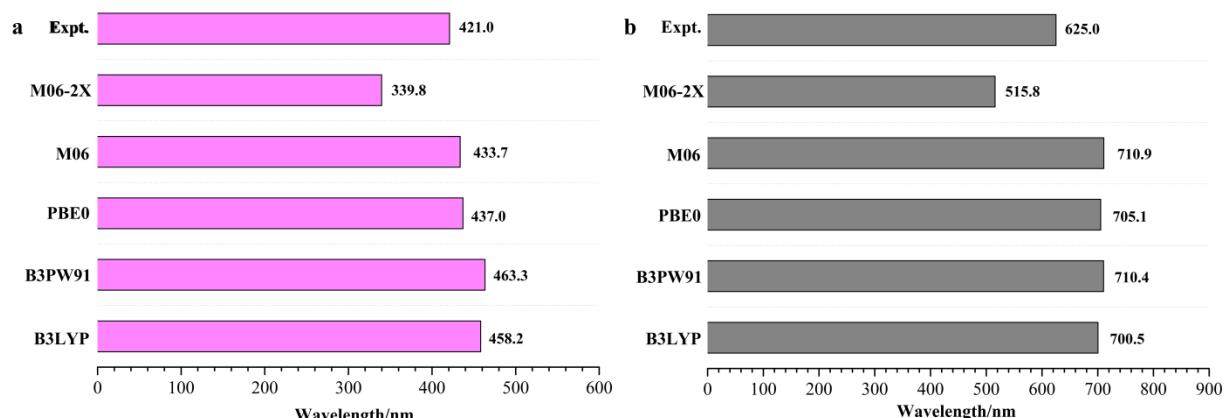


Fig. S1. Absorption(a) and emission(b) spectra obtained by TDDFT method with different functionals for **3**, together with experimentally (unit: nm).

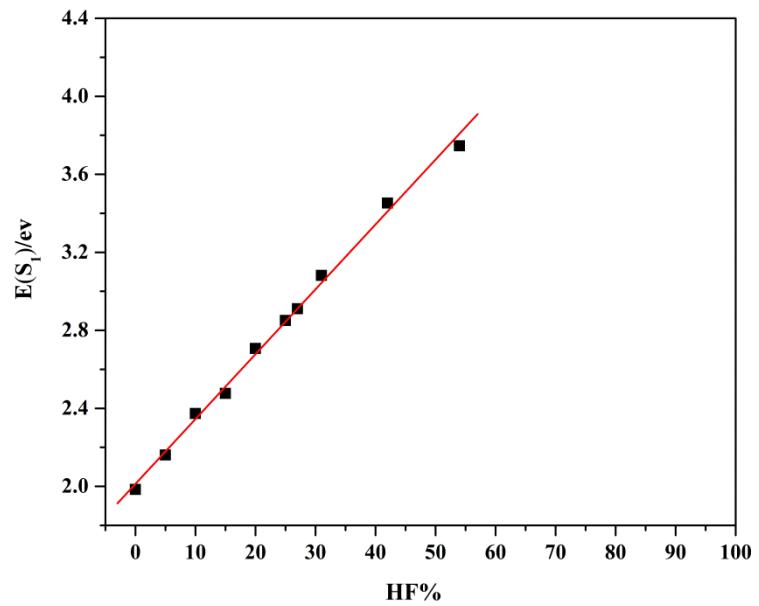


Fig. S2. Dependence of $E(S_1)$ of **3** on the HF% in TD-DFT functionals.

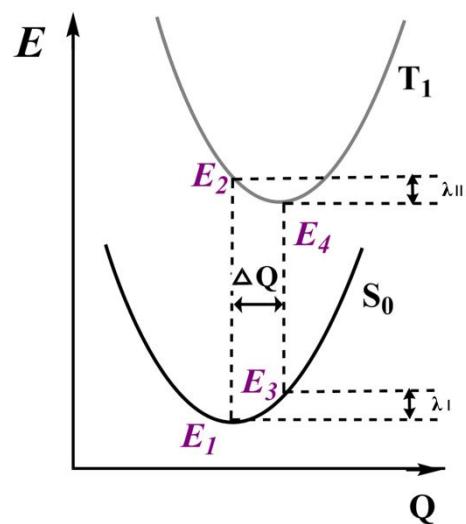


Fig. S3. *Dushin* program to deal with changes in the electronic state process of reorganization energy diagram.

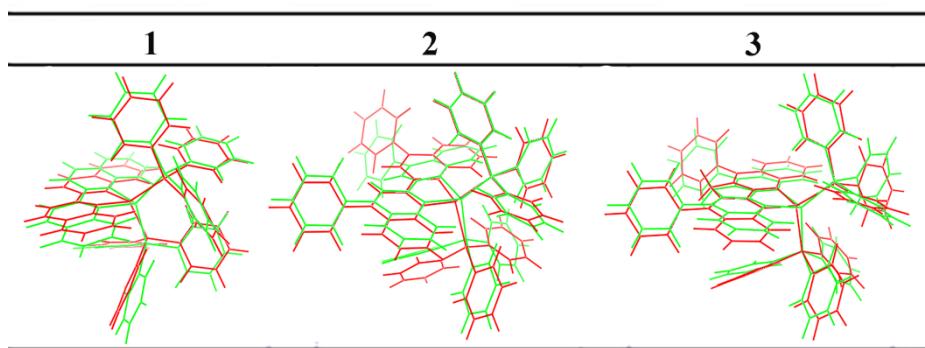


Fig. S4. Super imposed structures of S_0 (green) and T_1 (red) states of the studied complexes.

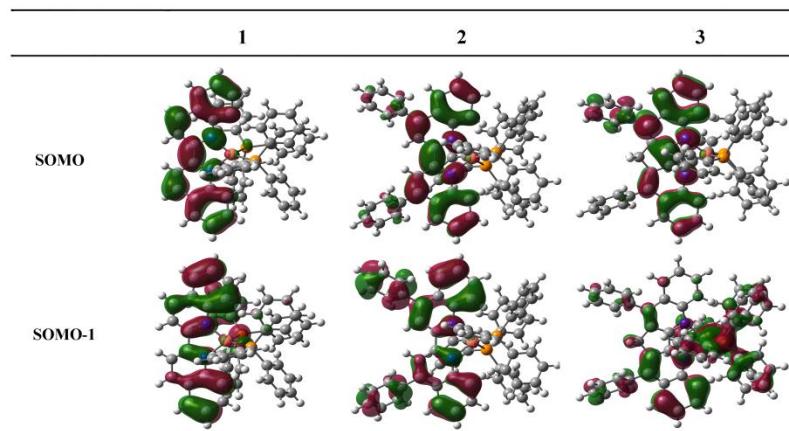
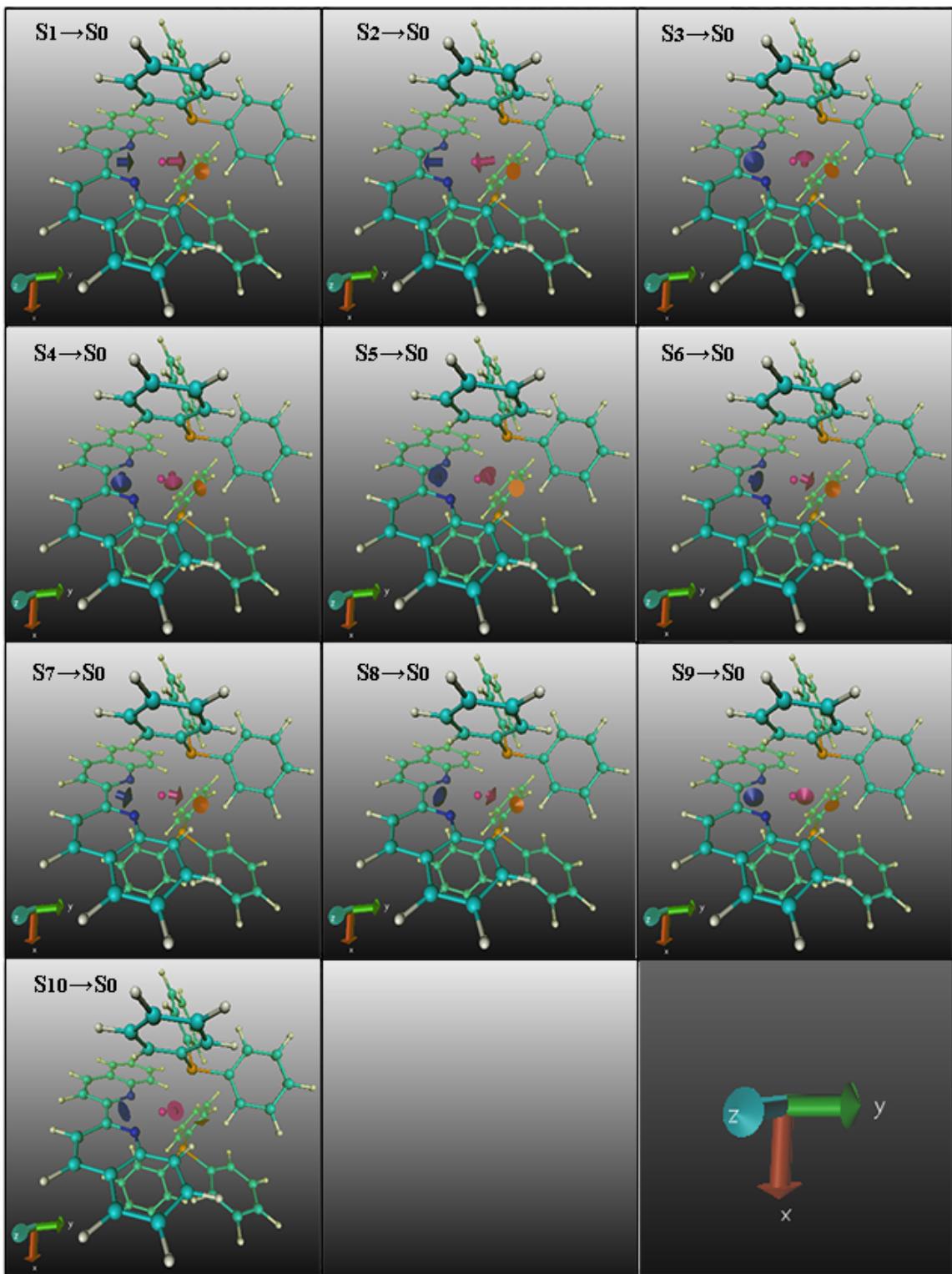
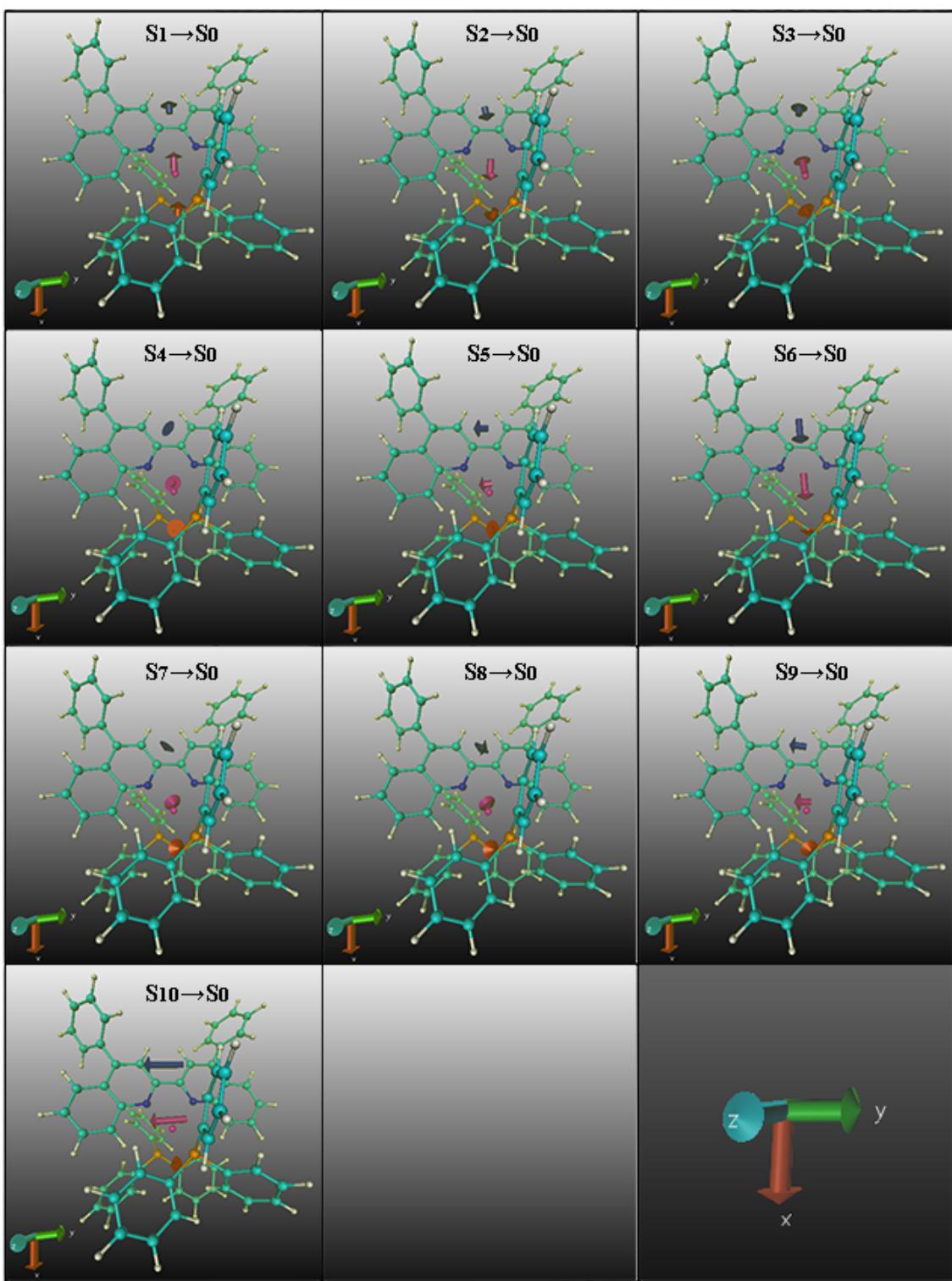


Fig. S5. Spin density plot for the lowest T_1 state for the complexes.

1



2



3

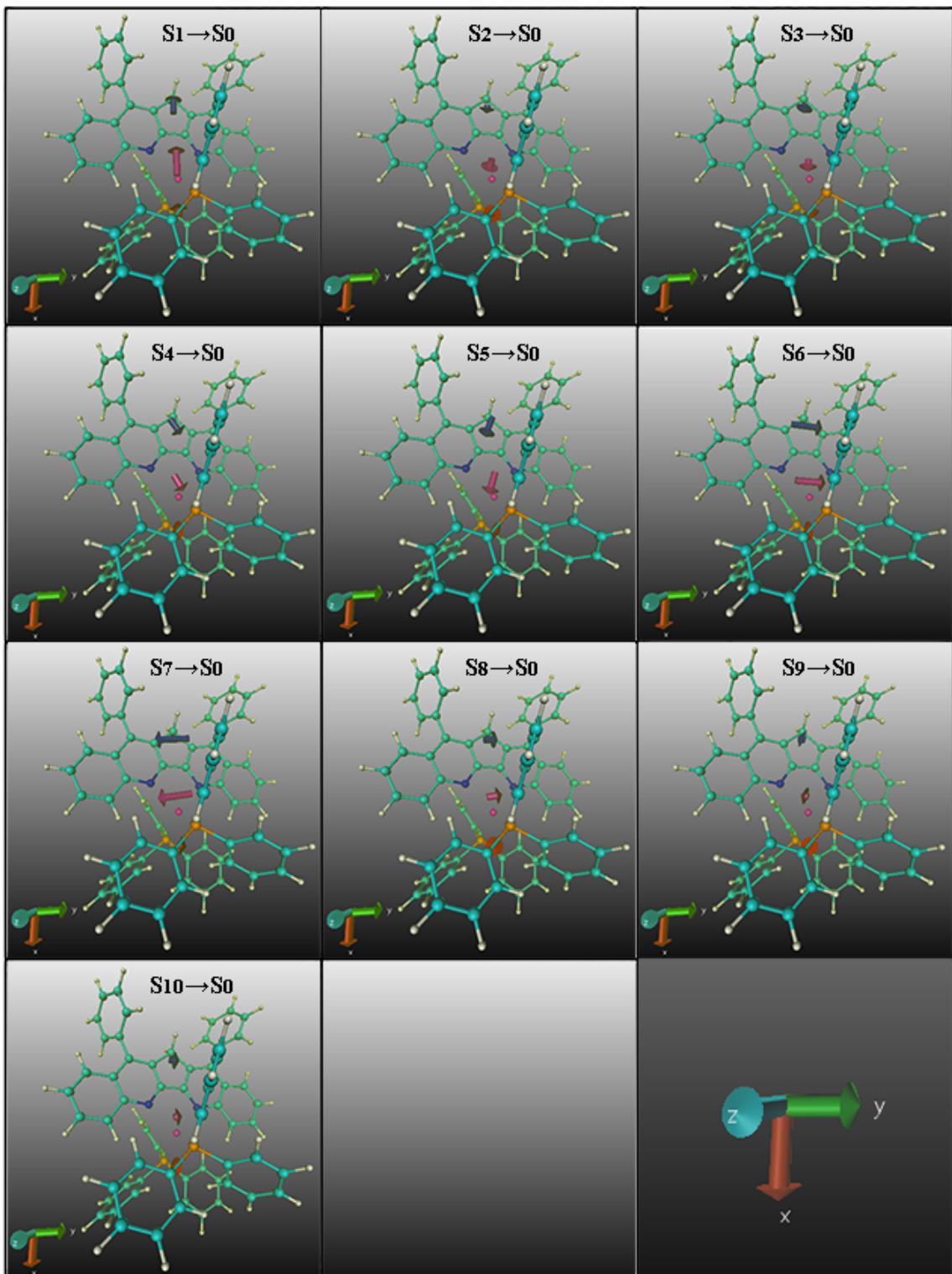
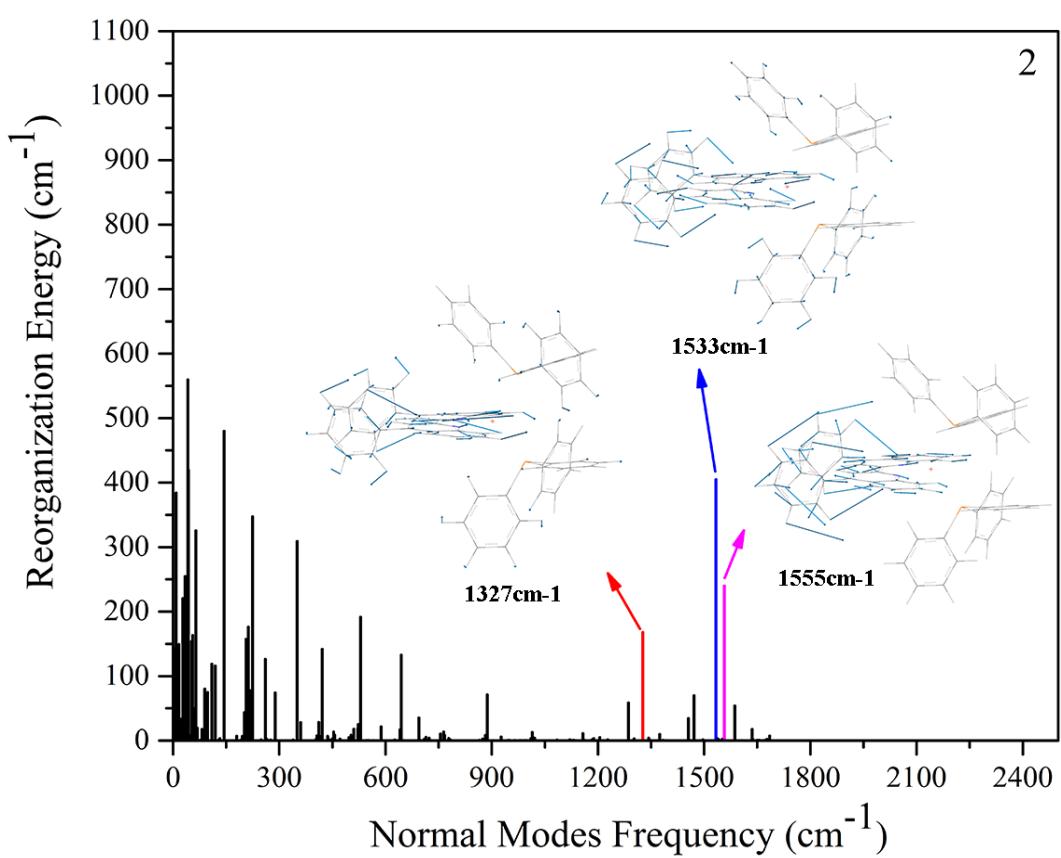
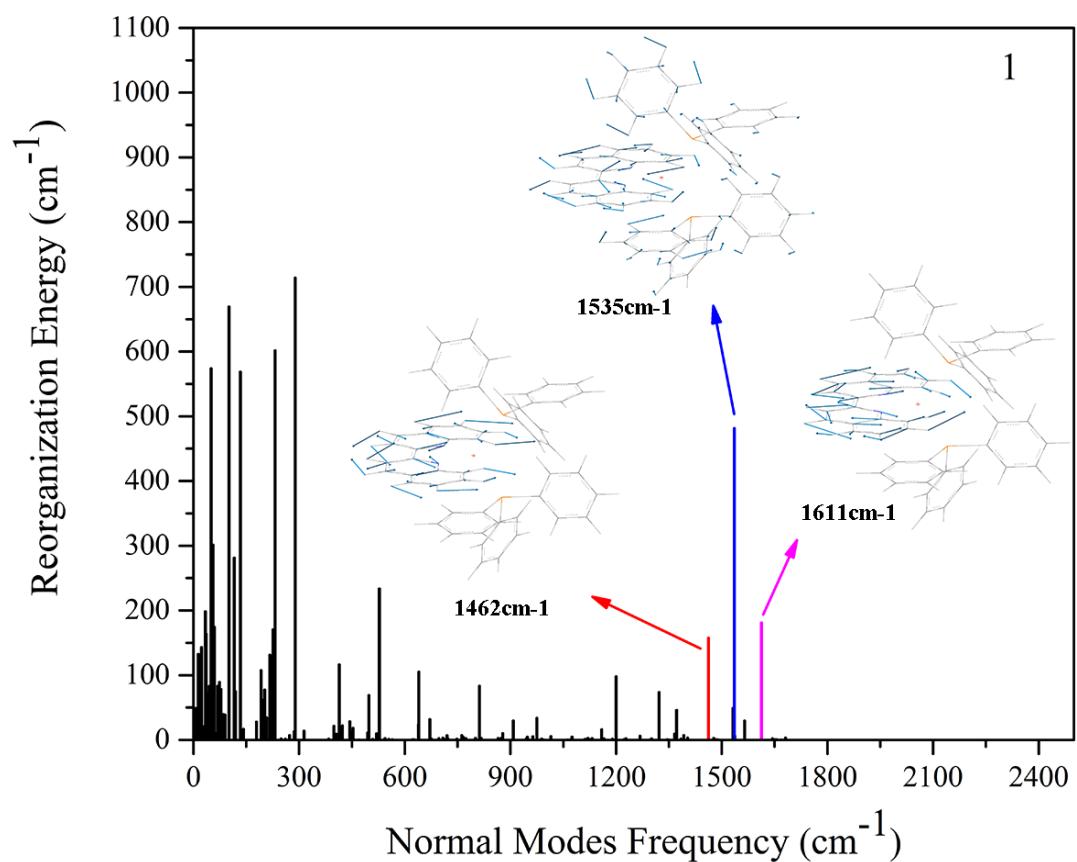


Fig. S6. The transition dipole moment vector of the contribution from N^N ligand, P^P ligand and the whole complex is described by the blue, orange and purple arrows, respectively.



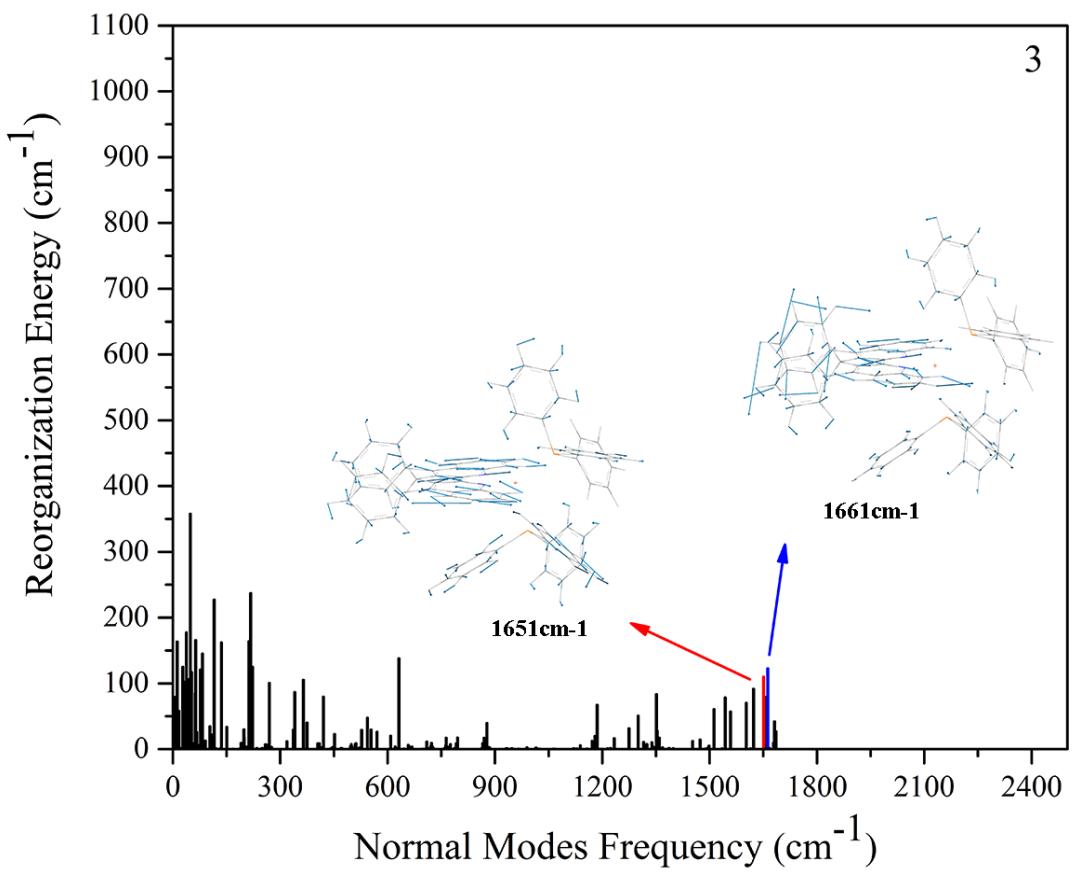
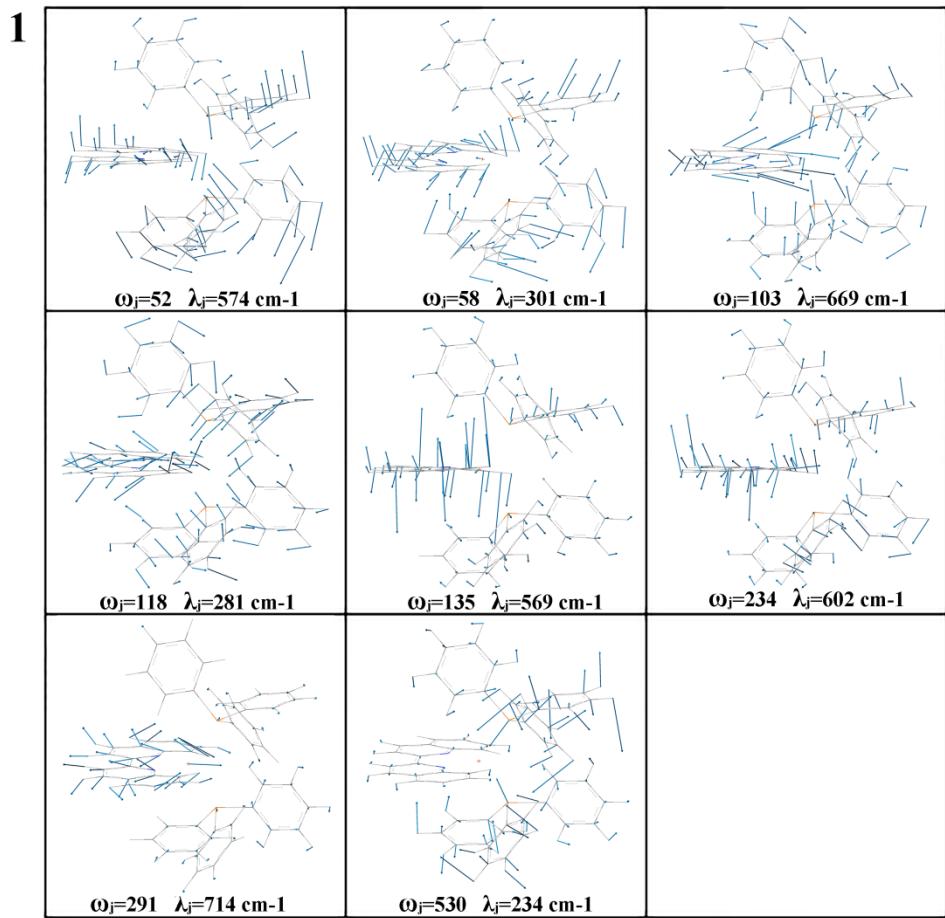


Fig. S7. Calculated reorganization energies and the displacement vectors for the normal modes with the largest reorganization energies over 100 cm^{-1} at high-frequency (inset).



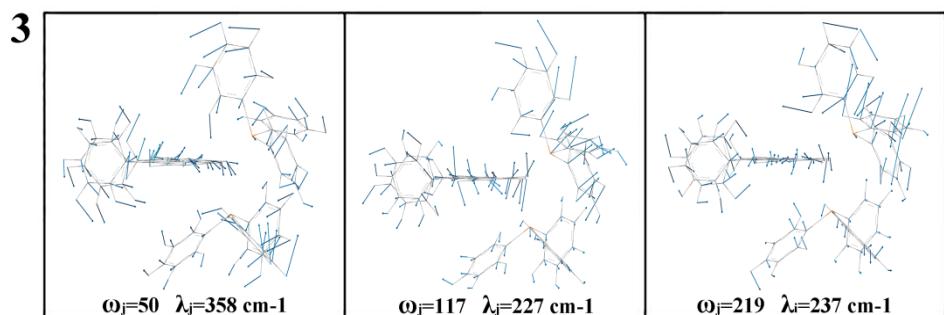
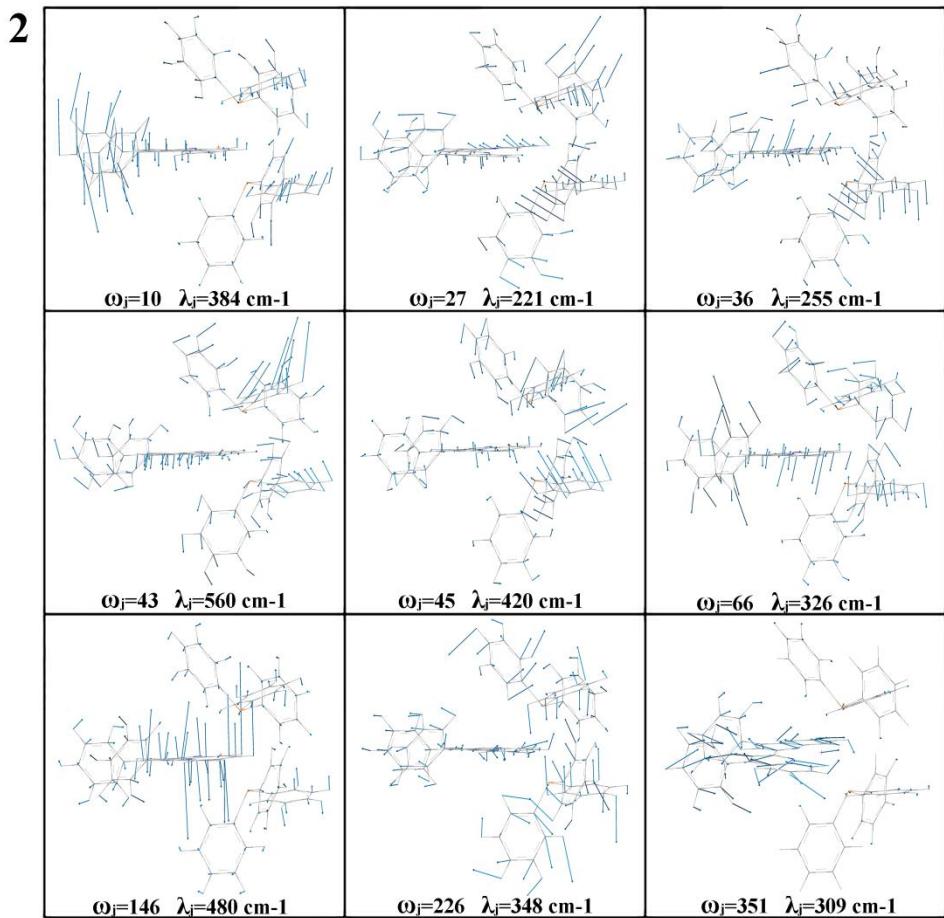


Fig. S8. Calculated reorganization energies and the displacement vectors for the normal modes with the reorganization energies over 200 cm^{-1} at low-frequency(inset).

Table S1 Partial optimized geometric structural parameters of **3** in the ground state by B3LYP, B3PW91, PBE0, M06 and M06-2X functionals, together with the observed experimentally.

	B3LYP	B3PW91	PBE0	M06	M06-2X	Expt.
Cu-N ₁	2.2870	2.2620	2.2196	2.2216	2.2582	2.2275
Cu-N ₂	2.2388	2.2220	2.2349	2.2116	2.2056	2.1372
Cu-P ₁	2.4094	2.3828	2.3649	2.3297	2.3700	2.2851
Cu-P ₂	2.3932	2.3693	2.3327	2.2768	2.4497	2.2319
N ₁ -Cu-P ₁	109.25	109.13	104.93	102.35	103.24	101.95
N ₁ -Cu-P ₂	110.44	110.39	114.13	114.15	116.13	112.77
N ₂ -Cu-P ₁	106.02	105.68	100.60	97.84	94.15	98.24
N ₂ -Cu-P ₂	114.56	114.41	116.80	121.28	129.71	120.26
N ₁ -Cu-N ₂	80.37	80.80	81.11	81.35	81.33	82.58
P ₁ -Cu-P ₂	126.61	126.88	128.64	128.85	122.97	130.05
DHA ₁	1.15	1.33	0.90	2.34	0.74	0.62

Table S2 The maximum absorption spectra $\lambda_{\max(\text{nm})}$ (oscillator strengths), emission spectra and experimental values of **3** calculated by different functionals.

	B3LYP	B3PW91	PBE0	M06	M06-2X	Expt
	λ_{\max}/f	λ_{\max}/f	λ_{\max}/f	λ_{\max}/f	λ_{\max}/f	λ_{\max}
S ₀ →S ₁	458.2/ 0.0892	463.3/ 0.0930	437.0/ 0.0975	433.7/ 0.0964	339.8/ 0.1490	421
T ₁ →S ₀	684.6	698.4	748.8	719.2	426.9	631

Table S3 Calculated E(S₁)/ev using various functionals and LANL2DZ/6-31G(d) basis set in DCM solution for **3**.

	BLYP	MPWLYP1M	TPSSH	B3LYP*	B3LYP	PBE0	M06	MPW1B95	BMK	M062X
HF%	0	5	10	15	20	25	27	31	42	54
E(S ₁)	1.9841	2.1605	2.3735	2.4763	2.7063	2.8500	2.9104	3.0813	3.4524	3.7458

Table S4 Absorption and emission values obtained by TD-DFT method with PBE0 and M06 for all, together with experimental values (unit: nm).

	PBE0		M06	
	$\lambda^{\text{Abs}}_{\text{max}}/\text{Expt}$	$\lambda^{\text{Em}}_{\text{max}}/\text{Expt}$	$\lambda^{\text{Abs}}_{\text{max}}/\text{Expt}$	$\lambda^{\text{Em}}_{\text{max}}/\text{Expt}$
1	430.2/420 ^a	834.2/646 ^a	429.2 /420 ^a	851.5/646 ^a
2	437.6/425 ^a	811.9/648 ^a	435.1/425 ^a	742.8/648 ^a
3	437.0/421 ^a	705.1/625 ^a	433.7/421 ^a	719.2/625 ^a

Table S5 Negative value of the HOMO ($-\epsilon_{\text{HOMO}}$) and LUMO ($-\epsilon_{\text{LUMO}}$) energies, HOMO-LUMO gaps calculated by DFT, and the lowest singlet energies ($E_{\text{S}1}$) calculated by TDDFT in eV for these complexes.

	$-\epsilon_{\text{HOMO}}$	$-\epsilon_{\text{LUMO}}$	$\Delta E_{\text{H-L}}$	$E_{\text{S}1}$
1	6.44	2.76	3.68	2.88
2	6.40	2.76	3.64	2.83
3	6.41	2.81	3.60	2.84

Table S6 Molecular orbital compositions of Cu at the optimized S_0 geometries in solvent DCM.

	MO	Energy(eV)	Cu contribution (%)
1	LUMO	-2.76	2.1(0.90d _{xz} +0.42d _z ²)
	HOMO	-6.44	34.0(19.77 d _{xz} +4.25 d _z ² +0.86d _{x-y} ²)
	HOMO-1	-6.79	42.2(4.78 d _{xz} +0.95 d _{yz} +2.85 d _{xy} +3.03 d _z ² +21.45d _{x-y} ²)
	HOMO-2	-7.01	50.7 (38.61 d _{yz} +6.31 d _{xy} +0.77d _{xz} +2.09 d _{x-y} ²)
	HOMO-3	-7.08	27.4(24.64d _{yz} +0.16d _{xz} +0.25d _z ² +0.77d _{x-y} ²)
	HOMO-4	-7.29	2.3(0.45d _{xz} +0.20d _{yz})
2	LUMO	-2.76	2.0 (0.53d _{xz})
	HOMO	-6.40	33.3(11.07 d _{xz} +10.15 d _z ² +2.52d _{x-y} ²)
	HOMO-1	-6.80	41.8(5.38 d _{yz} +2.64 d _{xy} +9.63d _{xz} +13.21 d _z ² +1.86d _{x-y} ²)
	HOMO-2	-6.93	11.7 (7.54 d _{xy} +2.04d _{xz} + 1.37 d _z ²)
	HOMO-3	-7.03	51.5(3.91 d _{yz} +40.23 d _{xy} +3.49d _{xz} +0.74 d _z ² +0.60d _{x-y} ²)
	HOMO-4	-7.14	21.2(0.66 d _{yz} +13.87d _{xy} +1.69d _{xz} +1.06 d _z ² +0.65d _{x-y} ²)

3	LUMO+1	-1.66	0.2(0.09d _{yz})
	LUMO	-2.81	1.4(0.61d _{xz})
	HOMO	-6.41	31.9(10.68d _{xz} +10.37 d _z ² +1.48d _{x-y} ²)
	HOMO-1	-6.67	58.2 (18.35d _z ² +9.85 d _{xz} +3.89d _{x-y} ²)
	HOMO-2	-6.95	5.0(2.95 d _{yz} +1.83 d _{yz})
	HOMO-3	-7.04	3.4(1.84d _{x-y} ²)
	HOMO-4	-7.23	66.4(4.92 d _{yz} +1.15d _{xz} +58.03d _{xy} + 0.05d _z ²)

Table S7 Molecular orbital compositions of Cu at the optimized S₀ geometries in gas phase.

	MO	Energy(eV)	Cu contribution (%)
1	LUMO	-4.66	2.1(0.96d _{xz} +0.44d _z ²)
	HOMO	-8.21	32.6(18.55 d _{xz} +3.80 d _z ² +0.62d _{x-y} ²)
	HOMO-1	-8.58	39.39(3.43 d _{xz} +2.34d _{xy} +3.05 d _z ² +20.58d _{x-y} ²)
	HOMO-2	-8.86	55.6 (43.22d _{yz} +6.57d _{xy} +1.29d _{xz} + 1.47d _{x-y} ²)
	HOMO-3	-8.94	21.0(18.89d _{yz})
	HOMO-4	-9.09	1.54(0.77d _{xz})
2	LUMO	-4.47	2.0 (0.54d _{xz})
	HOMO	-8.07	33.5(10.63 d _{xz} + 1.27d _{yz} +2.46d _z ² +9.80d _{x-y} ²)
	HOMO-1	-8.47	40.5(5.25d _{yz} +2.26d _{xy} +9.54d _{xz} +12.49d _z ² +1.80d _{x-y} ²)
	HOMO-2	-8.61	9.63(5.94d _{xy} +1.69d _{xz} +1.29d _z ²)
	HOMO-3	-8.73	46.73(3.37d _{yz} +36.81d _{xy} +3.06d _{xz})
	HOMO-4	-8.82	28.7(19.97d _{xy} +2.39d _{xz} + 1.36d _z ²)
3	LUMO+1	-3.36	0.21(0.09d _{yz})
	LUMO	-4.51	1.4(0.34d _z ²)
	HOMO	-8.07	31.3(10.53d _{xz} +0.63d _{xy} +9.72d _z ² +1.51d _{x-y} ²)
	HOMO-1	-8.35	41.1(17.98d _z ² +9.18 d _{xz} +1.23d _{yz} +3.65d _{x-y} ²)
	HOMO-2	-8.63	4.7(2.70d _{xy} +1.80 d _{yz})
	HOMO-3	-8.72	2.9(0.13d _{xy} + 0.12d _{x-y} ²)
	HOMO-4	-8.92	64.9(4.70 d _{yz} +1.05d _{xz} +56.97d _{xy})

Table S8 Molecular orbital compositions of Cu at the optimized T₁ geometries in solvent DCM.

	MO	Energy(eV)	Cu contribution (%)
1	LUMO	-3.10	3.8(0.96 d _z ² +0.87d _{yz})
	HOMO	-5.80	36.1(19.78 d _{xy} +9. 85d _{xz})
	HOMO-1	-6.76	41.3(1.23d _z ² +2.18d _{xy} +7.27 d _{xz} +2.20d _{yz} +10.91d _{x-y} ²)
	HOMO-2	-6.82	53.5 (15.60d _z ² +14.37 d _{xz} +9.80 d _{x-y} ²)
	HOMO-5	-7.41	9.5(1.79d _z ² +2.80d _{xz} +2.18d _{xy} +2.20d _{yz})
2	LUMO	-3.12	3.7(2.37 d _{xz})
	HOMO	-5.83	36.7(25.39 d _{xy} +5.55d _{xz})
	HOMO-1	-6.68	36.0(7.64d _z ² +1.35d _{xy} +0.85 d _{xz} +17.23d _{yz})
	HOMO-2	-6.76	58.4(33.26 d _{xy} +19.69 d _{xz})
	HOMO-5	-7.42	0.2(0.06 d _{x-y} ² +0.04d _{xz})
3	LUMO+1	-1.82	0.3(0.14d _{yz})
	LUMO	-3.09	2.3(1.48d _{xz})
	HOMO	-6.16	30.9 (15.39d _{xz} +6.64 d _{xy} +2.68d _z ²)
	HOMO-1	-6.63	39.3(11.58d _{yz} +1.37d _{xz} +16.75d _z ² +2.21 d _{x-y} ²)
	HOMO-2	-6.81	5.6 (0.05d _z ²)
	HOMO-5	-7.33	0.1(3.17d _{yz} +3.11d _z ²)

Table S9 Frontier molecular orbital energies(eV) and compositions (%) of different fragments in the ground state for the complexes.

MO	E/eV	MO composition (%)			Assign
		Cu	N^N	P^P	
1					
LUMO+5	-0.95	5.5	4.3	90.2	$\pi^*(P^P)$
LUMO+4	-1.09	3.3	1.8	95.0	$\pi^*(P^P)$
LUMO+3	-1.15	3.2	2.6	94.2	$\pi^*(P^P)$
LUMO+2	-1.42	1.6	94.5	3.9	$\pi^*(N^N)$
LUMO+1	-1.71	0.3	96.6	3.1	$\pi^*(N^N)$
LUMO	-2.76	2.1	94.2	3.7	$\pi^*(N^N)$
HOMO	-6.44	34.0	5.6	60.4	d(Cu)+ $\pi(P^P)$

HOMO-1	-6.79	42.2	11.7	46.1	$d(Cu)+\pi(N^N+P^P)$
HOMO-2	-7.01	50.7	43.8	5.6	$d(Cu)+\pi(N^N)$
HOMO-3	-7.08	27.4	67.2	5.4	$d(Cu)+\pi(N^N)$
HOMO-4	-7.29	2.3	72.	25.7	$\pi(N^N+P^P)$
HOMO-5	-7.42	0.5	91.1	8.5	$\pi(N^N)$
2					
LUMO+5	-0.951	5.5	5.1	89.4	$\pi^*(P^P)$
LUMO+4	-1.05	1.9	14.8	83.3	$\pi^*(N^N)+\pi^*(P^P)$
LUMO+3	-1.17	2.1	6.0	92.0	$\pi^*(P^P)$
LUMO+2	-1.44	1.8	94.0	4.2	$\pi^*(N^N)$
LUMO+1	-1.86	0.5	97.7	1.7	$\pi^*(N^N)$
LUMO	-2.76	2.0	95.5	2.5	$\pi^*(N^N)$
HOMO	-6.40	34.1	9.7	56.1	$d(Cu)+\pi(P^P)$
HOMO-1	-6.79	41.8	16.3	41.9	$d(Cu)+\pi(N^N+P^P)$
HOMO-2	-6.93	11.7	83.9	4.3	$d(Cu)+\pi(N^N)$
HOMO-3	-7.03	51.5	44.7	3.8	$d(Cu)+\pi(N^N)$
HOMO-4	-7.14	21.2	66.6	12.2	$d(Cu)+\pi(N^N+P^P)$
HOMO-5	-7.38	0.4	95.1	4.5	$\pi(N^N)$
3					
LUMO+5	-0.95	5.8	3.4	90.9	$\pi^*(P^P)$
LUMO+4	-1.05	2.0	2.9	95.1	$\pi^*(P^P)$
LUMO+3	-1.15	1.4	2.9	95.7	$\pi^*(P^P)$
LUMO+2	-1.30	1.9	92.5	5.6	$\pi^*(N^N)$
LUMO+1	-1.66	0.2	98.6	1.2	$\pi^*(N^N)$
LUMO	-2.81	1.4	96.2	2.4	$\pi^*(N^N)$
HOMO	-6.41	31.9	10.5	57.6	$d(Cu)+\pi(N^N+P^P)$
HOMO-1	-6.67	42.3	14.1	43.6	$d(Cu)+\pi(N^N+P^P)$
HOMO-2	-6.95	5.0	92.9	2.1	$\pi(N^N)$
HOMO-3	-7.04	3.4	84.0	12.6	$\pi(N^N+P^P)$
HOMO-4	-7.23	66.4	27.2	6.3	$d(Cu)+\pi(N^N)$
HOMO-5	-7.27	4.6	92.5	2.9	$\pi(N^N)$

Table S10 Frontier molecular orbital energies (eV) and compositions (%) of different fragments in the triplet state for the complexes.

MO	E/eV	MO composition (%)			Assign
		Cu	N [^] N	P [^] P	
1					
LUMO+5	-0.92	5.0	4.1	90.8	$\pi^*(P^P)$
LUMO+4	-1.02	1.6	1.5	97.0	$\pi^*(P^P)$
LUMO+3	-1.12	5.5	3.9	90.7	$\pi^*(P^P)$
LUMO+2	-1.45	1.5	91.8	6.8	$\pi^*(N^N)$
LUMO+1	-1.78	0.6	96.3	3.1	$\pi^*(N^N)$
LUMO	-3.10	3.8	90.9	5.3	$\pi^*(N^N)$
HOMO	-5.80	36.1	14.4	49.5	d(Cu)+ $\pi(N^N+P^P)$
HOMO-1	-6.76	41.3	15.7	43.0	d(Cu)+ $\pi(N^N+P^P)$
HOMO-2	-6.83	53.5	25.7	20.8	d(Cu)+ $\pi(N^N+P^P)$
HOMO-3	-7.00	9.0	78.6	12.4	$\pi(N^N+P^P)$
HOMO-4	-7.29	7.2	63.3	29.5	$\pi(N^N+P^P)$
HOMO-5	-7.41	9.5	47.4	43.1	$\pi(N^N+P^P)$
2					
LUMO+5	-0.96	3.6	13.9	82.5	$\pi^*(N^N)+\pi^*(P^P)$
LUMO+4	-0.99	2.6	20.3	77.1	$\pi^*(N^N)+\pi^*(P^P)$
LUMO+3	-1.10	5.9	6.5	87.6	$\pi^*(P^P)$
LUMO+2	-1.51	1.6	94.0	4.4	$\pi^*(N^N)$
LUMO+1	-1.91	0.5	97.8	1.7	$\pi^*(N^N)$
LUMO	-3.12	3.7	92.2	4.1	$\pi^*(N^N)$
HOMO	-5.83	36.7	16.5	46.8	d(Cu)+ $\pi(N^N+P^P)$
HOMO-1	-6.68	36.0	17.3	46.7	d(Cu)+ $\pi(N^N+P^P)$
HOMO-2	-6.76	58.4	28.3	13.3	d(Cu)+ $\pi(N^N+P^P)$
HOMO-3	-6.88	7.8	83.5	8.7	$\pi(N^N)$
HOMO-4	-7.13	7.2	75.7	17.1	$\pi(N^N+P^P)$
HOMO-5	-7.42	0.2	95.8	4.1	$\pi(P^P)$
3					
LUMO+5	-0.94	2.5	2.7	94.9	$\pi^*(P^P)$
LUMO+4	-1.02	1.8	3.9	94.3	$\pi^*(P^P)$
LUMO+3	-1.04	3.3	4.1	92.6	$\pi^*(P^P)$

LUMO+2	-1.33	2.7	91.6	5.8	$\pi^*(N^N)$
LUMO+1	-1.82	0.3	98.9	0.8	$\pi^*(N^N)$
LUMO	-3.09	2.3	94.5	3.2	$\pi^*(N^N)$
HOMO	-6.16	30.9	15.1	54.0	$d(Cu)+\pi(N^N+P^P)$
HOMO-1	-6.63	39.3	13.5	47.2	$d(Cu)+\pi(N^N+P^P)$
HOMO-2	-6.81	5.6	85.3	9.0	$\pi(N^N)$
HOMO-3	-7.01	11.3	82.0	6.7	$d(Cu)+\pi(N^N)$
HOMO-4	-7.05	65.7	26.3	8.0	$d(Cu)+\pi(N^N)$
HOMO-5	-7.33	0.1	99.5	0.5	$\pi(N^N)$

Table S11 SOC matrix elements $\langle T_1^a | H_{SOC} | S_m \rangle (\text{cm}^{-1})$, the transition dipole moment $M_{S_{m,j}}$ of **1** calculated at the T_1^{opt} optimized geometry with DCM included. The radiative decay rate constant (k_r/s^{-1}) is also given.

$E(T_1)=11988\text{cm}^{-1}$									
S_m	$M_{S_{m,j}}$	$M_{S_{m,j}}$	$M_{S_{m,j}}$	$\langle T_1^x H_{SOC} S_m \rangle$		$\langle T_1^y H_{SOC} S_m \rangle$		$\langle T_1^z H_{SOC} S_m \rangle$	
				Re	Im	Re	Im	Im	
S_1	0.0008	-0.6330	-0.4067	-8.0561	-30.8048	-8.0561	30.8048	8.8035	
S_2	0.0773	0.5922	0.5199	127.6256	-8.6501	127.6256	8.6501	-55.9092	
S_3	0.1912	-0.5392	-0.0193	57.2251	-58.3964	57. 2251	58.3964	166.6064	
S_4	-0.6639	-0.2856	0.1479	0.8508	-8.9057	0.8508	8.9057	-3.7694	
S_5	-0.6324	-0.3100	0.3045	10.0211	-88.8470	10.0211	88.8470	-104.9409	
S_6	0.0419	0.4374	0.0835	4.5139	9.8495	4.5139	-9.8495	15.8400	
S_7	-0.7361	0.0936	0.4877	89.0185	174.5850	89.0185	-174.5850	426.6527	
S_8	0.1658	0.2371	-0.0366	76.1690	-11.8938	76.1690	11.8938	-0.8565	
S_9	-0.1707	-0.2073	0.1563	0.6071	-52.4358	0.6071	52.4358	4.0796	
S_{10}	1.2138	0.9098	-0.7204	-16.4388	-9.8422	-16.4388	9.8422	6.4022	
k_m^x				5985.70					
k_m^y					5985.70				
k_m^z						2568.82			
k_r					4846.74				

a $M_{S_{m,j}}$ is the j -axis ($j \in x, y, z$) projection of the $S_m \rightarrow S_0$ transition dipole moment .

b the superscript α denotes the spin sub-level (x , y , or z) of the T_1 excited state.

c $k_r(T_1 \rightarrow S_0) = \frac{1}{3} \sum_{\alpha} k_r^{\alpha}$

d (T_1^{α}) is the energy shift (cm^{-1}) of the spin sub-level α ($\alpha = x$, y , or z) due to SOC with the S_m excited state. $E(T_1)$ is taken as the reference point.

Table S12 SOC matrix elements $\langle T_1^{\alpha} | H_{\text{SOC}} | S_m \rangle (\text{cm}^{-1})$, the transition dipole moment $M_{S_{m,j}}$ of **2** calculated at the T_1^{opt} optimized geometry with DCM included. The radiative decay rate constant

(k_r/s^{-1}) is also given.

$E(T_1) = 12371 \text{ cm}^{-1}$

S_m	$M_{S_{m,j}}$	$M_{S_{m,j}}$	$M_{S_{m,j}}$	$\langle T_1^x H_{\text{SOC}} S_m \rangle$		$\langle T_1^y H_{\text{SOC}} S_m \rangle$		$\langle T_1^z H_{\text{SOC}} S_m \rangle$	
				Re	Im	Re	Im	Re	Im
S_1	-1.0561	0.0438	0.0486	32.0066	4.1489	32.0066	-4.1489	2.7563	
S_2	1.2269	0.0339	0.0725	15.8802	-136.1803	15.8802	136.1803	41.6169	
S_3	0.5371	-0.1055	-0.3296	105.6034	21.3574	105.6034	-21.3574	-81.2957	
S_4	0.1742	-0.1292	-0.2380	-2.4138	2.1208	-2.4138	-2.1208	21.2989	
S_5	0.0610	-0.7402	0.0191	-39.1828	-79.6429	-39.1828	79.6429	-174.1596	
S_6	-1.2169	-0.0655	-0.0502	-2.4743	-1.1103	-2.4743	1.1103	-2.4205	
S_7	0.4284	-1.2015	0.2444	42.5899	42.7375	42.5899	-42.7375	514.7130	
S_8	0.1043	1.0373	-0.2440	37.2695	-22.2640	37.2695	22.2640	9.3032	
S_9	-0.0062	1.3071	-0.2028	-9.1107	-20.0546	-9.1107	20.0546	60.8538	
S_{10}	0.1307	1.2340	-0.1321	-0.4287	-10.5200	-0.4287	10.5200	-9.6280	
k_m^x				4908.30					
k_m^y					4908.30				
k_m^z						9514.32			
k_r							6443.64		

Table S13 SOC matrix elements $\langle T_1^a | H_{SOC} | S_m \rangle (\text{cm}^{-1})$, the transition dipole moment $M_{S_{m,j}}$ of **3** calculated at the T_1^{opt} optimized geometry with DCM included. The radiative decay rate constant (k_r/s^{-1}) is also given.

$E(T_1) = 14182\text{cm}^{-1}$								
S_m	$M_{S_{m,j}}$	$M_{S_{m,j}}$	$M_{S_{m,j}}$	$\langle T_1^x H_{SOC} S_m \rangle$	$\langle T_1^y H_{SOC} S_m \rangle$	$\langle T_1^z H_{SOC} S_m \rangle$		
				Re	Im	Re	Im	Im
S_1	-1.5978	0.0092	-0.1665	88.6776	-49.0399	88.6776	49.0399	-7.9374
S_2	0.3655	-0.1326	-0.3594	12.2639	114.9570	12.2639	-144.9570	-52.7289
S_3	0.4827	-0.0437	0.0686	114.9070	-61.8399	114.9070	61.8399	18.5976
S_4	0.7062	0.4484	-0.0807	65.3256	-24.8984	65.3256	24.8984	-198.1577
S_5	1.0978	-0.4620	0.1104	12.0904	-165.7141	12.0904	165.7141	-365.5163
S_6	0.0497	2.1554	-0.4749	-2.4853	-5.6882	-2.4853	5.6882	8.3283
S_7	0.3610	-1.4467	0.3576	-2.1243	-4.1736	-2.1243	4.1736	-1.5673
S_8	0.0026	-0.0263	0.0119	-12.9428	14.8570	-12.9428	-14.8570	-23.4307
S_9	0.0550	-0.4595	0.0008	-14.0689	14.1006	-14.0689	-14.1006	11.3669
S_{10}	0.0697	-0.2017	0.1314	-9.9454	-19.9932	-9.9454	19.9932	50.9251
k_m^x				6565.84				
k_m^y					6565.84			
k_m^z						35154.51		
k_r						16095.39		