

Actinide embedded nearly planner gold superatom: structural properties and applications in surface- enhanced Raman scattering (SERS)

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Part 1: Coordinates of the optimized structures.

Table S1. Coordinates of An@Au₆ (An = Ac⁻¹, Th, Pa⁺¹) and their corresponding adsorption complexes.

Structure	Number	Atom	x (Å)	y (Å)	z (Å)
[Ac@Au ₆] ⁻	1	Ac	-0.000001	0.000003	1.162790
	2	Au	0.000021	2.805040	0.101657
	3	Au	2.429440	1.402610	0.102270
	4	Au	2.429360	-1.402540	0.101955
	5	Au	-0.000029	-2.805070	0.101692
	6	Au	-2.429410	-1.402590	0.102223
	7	Au	-2.429380	1.402550	0.102001
Structure	Number	Atom	x (Å)	y (Å)	z (Å)
Th@Au ₆	1	Th	0.000000	0.000003	0.687325
	2	Au	-0.000011	2.780150	-0.000116
	3	Au	2.407600	1.390030	-0.000530
	4	Au	2.407670	-1.390100	-0.000072
	5	Au	0.000008	-2.780140	-0.000167
	6	Au	-2.407600	-1.390030	-0.000524
	7	Au	-2.407670	1.390080	-0.000122
Structure	Number	Atom	x (Å)	y (Å)	z (Å)
[Pa@Au ₆] ⁺	1	Pa	0.000011	-0.000002	0.002544
	2	Au	0.000055	2.765890	-0.000395
	3	Au	-2.400990	1.385140	-0.000439
	4	Au	-2.400970	-1.385110	-0.000420
	5	Au	2.400940	1.385060	-0.000454
	6	Au	2.400880	-1.385020	-0.000409
	7	Au	0.000062	-2.765960	-0.000428
Structure	Number	Atom	x (Å)	y (Å)	z (Å)
[Ac@Au ₆] ⁻ +Pyridine	1	Au	1.118850	2.634870	-0.357089
	2	Au	2.752690	0.328769	-0.367115
	3	Au	1.607140	-2.247430	-0.369267

4	Au	-1.681140	2.334290	-0.530085
5	Au	-1.197730	-2.545680	-0.453127
6	Au	-2.824770	-0.240494	-0.613826
7	Ac	-0.084212	0.046006	0.598093
8	C	-0.078404	1.203100	4.051200
9	C	-0.130734	1.252480	5.444910
10	C	-0.386365	-1.093250	4.045790
11	C	-0.451570	-1.133880	5.438960
12	C	-0.320967	0.061601	6.149880
13	N	-0.203319	0.052795	3.360910
14	H	-0.601338	-2.085730	5.948500
15	H	0.069028	2.109130	3.458020
16	H	-0.023871	2.208120	5.958100
17	H	-0.483007	-2.002390	3.447020
18	H	-0.366250	0.066063	7.240190

Structure	Number	Atom	x (Å)	y (Å)	z (Å)
Th@Au ₆ +Pyridine	1	Au	1.106180	2.606990	-0.284348
	2	Au	2.732110	0.327410	-0.267760
	3	Au	1.591270	-2.227100	-0.284178
	4	Au	-1.673730	2.315470	-0.439455
	5	Au	-1.191960	-2.518200	-0.374012
	6	Au	-2.811740	-0.238383	-0.516181
	7	Th	-0.071306	0.045411	0.321450
	8	C	-0.071101	1.211290	3.539240
	9	C	-0.126484	1.253640	4.928800
	10	C	-0.351619	-1.106320	3.532840
	11	C	-0.416898	-1.141960	4.922350
	12	C	-0.302725	0.057621	5.630590
	13	N	-0.181978	0.050649	2.853750
	14	H	-0.554937	-2.094230	5.432780
	15	H	0.065859	2.114630	2.939070
	16	H	-0.033298	2.208130	5.445250

17	H	-0.436397	-2.013170	2.928300
18	H	-0.350633	0.060654	6.720510

Structure	Number	Atom	x (Å)	y (Å)	z (Å)
[Pa@Au ₆] ⁺ +Pyridine	1	Au	1.089920	2.564900	-0.289647
	2	Au	2.700650	0.324244	-0.153565
	3	Au	1.570300	-2.198080	-0.219278
	4	Au	-1.657890	2.286600	-0.373395
	5	Au	-1.174930	-2.476160	-0.379239
	6	Au	-2.790400	-0.234649	-0.396285
	7	Pa	-0.062690	0.044914	0.132049
	8	C	-0.071437	1.219680	3.210270
	9	C	-0.128886	1.257270	4.597220
	10	C	-0.328900	-1.115230	3.205370
	11	C	-0.393765	-1.145680	4.592570
	12	C	-0.292398	0.057509	5.298890
	13	N	-0.170169	0.049995	2.525490
	14	H	-0.521633	-2.098650	5.104190
	15	H	0.056657	2.124320	2.610770
	16	H	-0.046283	2.212810	5.113260
	17	H	-0.404461	-2.023740	2.602760
	18	H	-0.339816	0.062664	6.388400

Part 2. Calculated relative energies for An@Au₆ (An = Ac⁻, Th, Pa⁺).

Table S2. Relative bonding energies for An@Au₆ calculated based on different functionals and basis sets.

System	Functional /Basis set	Multiplicity	ΔE (eV)
[Ac@Au ₆] ⁻		1(C _{6v})	0
	BP86/TZP	3(C _{6v})	1.54
		5(C _{3v})	2.7
	PBE/TZP	1(C _{6v})	0
		3(C _{6v})	1.56
		5(C _{3v})	2.68
Th@Au ₆		1(C _{6v})	0
	BP86/TZP	3(C _{6v})	1.59
		5(C _{3v})	2.97
	PBE/TZP	1(C _{6v})	0
		3(C _{6v})	1.61
		5(C _{3v})	2.95
[Pa@Au ₆] ⁻		1(D _{6h})	0
	BP86/TZP	3(C _{6v})	0.18
		5(C _{3v})	1.18
	PBE/TZP	1(D _{6h})	0
		3(C _{6v})	0.22
		5(C _{3v})	1.38

Part 3. Calculated geometry information of An@Au₆.

Table S3. Symmetry, gold-gold bond (nm), metal-gold bond (nm), gold-metal-gold angle (°), HOMO-LUMO gap (eV), bond energy (eV) of [Ac@Au₆]⁻, Th@Au₆ and [Pa@Au₆]⁺, respectively.

	[Ac@Au ₆] ⁻	Th@Au ₆	[Pa@Au ₆] ⁺
Symmetry	C _{6v}	C _{6v}	D _{6h}
Au-Au (Å)	2.81 (2.79)	2.78 (2.77)	2.77 (2.76)
An-Au (Å)	3.00 (3.01)	2.86 (2.87)	2.77 (2.76)
Au-An-Au angle (°)	138.8 (136.5)	152.1 (151.5)	180.0 (180.0)
HOMO-LUMO Gap (eV)	1.98 (1.91)	1.80 (1.70)	0.15 (0.0)
Bond Energy (eV)	-21.36 (-48.41)	-21.00 (-49.15)	-13.91 (-42.69)

The data in parenthesis were obtained with SOC (spin-orbit coupling) effects included.

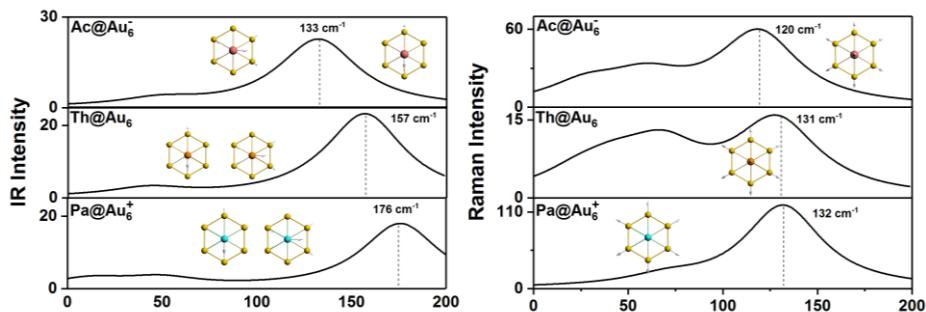
Part 4. Charge analysis for An@Au₆

Table S4. Hirshfeld Charge Analysis and VDD analysis.

Part 5. The vibrational modes and the vibrational spectra for An clusters

To facilitate future experimental characterizations, we also computed the vibrational spectra of An@Au₆ (An = Ac⁻, Th, Pa⁺). The results show that breathing vibration mode at 120 cm⁻¹, 131 cm⁻¹ and 132 cm⁻¹ for [Ac@Au₆]⁻, Th@Au₆ and [Pa@Au₆]⁺ are Raman-active but IR-inactive. But actinide translation vibration mode at 133 cm⁻¹, 157 cm⁻¹ and 176 cm⁻¹ for [Ac@Au₆]⁻, Th@Au₆ and [Pa@Au₆]⁺ are IR-active but Raman-inactive.

Figure 1. IR and Raman vibration modes of An@Au₆ (An = Ac⁻, Th, Pa⁺) clusters.



Part 6. Energy decomposition analysis for An@Au₆.

Table S5. Bond energy decomposition (eV).

Bond energy decomposition (eV)			
	[Ac@Au ₆] ⁻ (Case 6)	Th@Au ₆ (Case 2)	[Pa@Au ₆] ⁺ (Case 10)
ΔE _{int}	-11.7045	-10.8909	-3.4128
ΔE _{pauli}	32.7356	53.5959	48.5546
ΔE _{orb}	-20.0051	-33.4525	-16.7198
	45.02%	51.87%	32.17%
ΔE _{elestat}	-24.4349	-31.0343	-35.2476
	54.98%	48.13%	67.83%
	Ac@Au ₆ (Case 7)	Th@Au ₆ (Case 2)	Pa@Au ₆ (Case 11)
ΔE _{int}	-8.3811	-10.8909	-10.109
ΔE _{pauli}	32.7356	53.5959	48.5546
ΔE _{orb}	-16.6818	-33.4525	-23.416
	40.57%	51.87%	39.92%
ΔE _{elestat}	-24.4349	-31.0343	-35.2476
	59.43%	48.13%	60.08%

Table S6. The various cases for fragment electron configurations assumed for EDA.

#Default closed shell singlet state for each fragment. Au₆* is the ground state for Au₆ ring.

	ΔE in eV	ΔE _{int}	ΔE _{Pauli}	ΔE _{ele}	ΔE _{orb} (percentage of total attractive)
Case 1	#	-12.09	59.01	-29.99	-41.11 (57.82%)
Case 2	Th↑↑+Au₆*	-10.89	53.6	-31.03	-33.45 (51.87%)
Case 3	Th↑↑↑+Au ₆ ↓↓↓	-14.56	28.26	-25.02	-17.8 (41.56%)
Case 4	Th↑↑+Au ₆ ↓↓↓	-12.95	41.41	-30.72	-23.64 (43.49%)
Case 5	[#] ⁻¹	-11.81	44.36	-24.43	-31.74 (56.50%)
Case 6	[Ac↑+Au₆]*⁻¹	-11.7	32.74	-24.43	-20.01 (45.02%)
Case 7	[Ac↑+Au₆]*	-8.38	32.74	-24.43	-16.68 (40.57%)
Case 8	Ac↑↑↑+Au ₆ ↓↓↓	-16.38	28.29	-28.5	-16.17 (36.21%)

Case 9	$[#]^{+1}$	-5.23	49.36	-32.69	-21.89	40.11% ()
Case 10	$[Pa7s\downarrow 6d\uparrow 5f\uparrow\uparrow + Au_6^+]^{+1}$	-3.41	48.55	-35.25	-16.72 (32.17%)	
Case 11	$[Pa7s\uparrow\downarrow 6d\uparrow 5f\uparrow\uparrow + Au_6^+]^{+1}$	-10.11	48.55	-35.25	-23.42 39.92% ()	
Case 12	$[Pa6d\uparrow\uparrow\uparrow + Au_6\downarrow\downarrow\downarrow]^{+1}$	-15.8	29.17	-20.04	-24.93 (55.45%)	
Case 13	$[Pa6d\uparrow\uparrow\uparrow + Au_6^+]^{+1}$	-13.74	27.62	-20.6	-20.76 (50.18%)	
Case 14	$[Pa7s\uparrow\downarrow 5f\uparrow\downarrow + Au_6^+]^{+1}$	-9.81	40.87	-26.3	-24.37 (48.09%)	

Total interaction can be decomposed as:

$$\Delta E_{int} = \Delta E_{elestat} + \Delta E_{Pauli} + \Delta E_{orbital}$$

where $\Delta E_{elestat}$ is the electrostatic interaction term; ΔE_{Pauli} is the Pauli repulsion term; $\Delta E_{orbital}$ is the orbitals interaction term. Within this energy decomposition scheme the attractive and repulsive terms are negative and positive, respectively.

Part 7. UV-visible absorption spectra.

The absorption spectrum can be an effective identification method to test the validity of the specific superatom, especially in the low-energy range. The allowed transitions involve mainly the SAMOs.¹⁻³ The first peak near 435 nm originates from 1P to 1D transition. The next peak near 462 nm arises from the 1D to 1F transition. And the weak peak around 518 nm arises from 1D to (1F, 5f) transition. The last peak around 571 nm arises from 1D to 1D transition. For [Ac@Au₆]⁻ clusters, the weak peak at 383 nm arises from 1P to 1D transition. The next peak around 412 nm originates from 1P to orbital dominated by 7s of Ac. Strong peak near 465 nm arises from 1D to 1F transition and the last one at 498 arises from 1D to 1D transition. Inclusion of SOC effects causes all peaks shifting to red.

Table S7. Calculated wavelength (λ in nm), oscillator strength, and weights of Th@Au₆ and [Ac@Au₆]⁻ clusters at BP86/TZP including scalar relativistic effects.

	state	λ	f	transition	weight
Th@Au ₆	5E ₁	435	0.0134	1P _x 1P _y	1D _{z²} 0.9230
	4E ₁	462	0.0700	1D _{xy} 1D _{x²-y²}	1F _x 0.4602
				1D _{xy} 1D _{x²-y²}	1F _y 0.3417
	1A ₁	516	0.0022	1D _{xy} 1D _{x²-y²}	5f [Th 91.37%] 0.9947
	3E ₁	523	0.0013	1D _{xy} 1D _{x²-y²}	1F _y 0.4982
				1D _{xy} 1D _{x²-y²}	1F _x 0.4659
	1E ₁	571	0.0147	1D _{xy} 1D _{x²-y²}	1D _{xz} 1D _{yz} 0.9651
	1A ₁	357	0.0200	1P _x 1P _y	1D _{xz} 1D _{yz} 0.9244
	4E ₁	383	0.0048	1P _x 1P _y	1D _{z²} 0.9773
	[Ac@Au ₆] ⁻	3E ₁	412	0.0609	1P _x 1P _y 7s [Ac 79.60%] 0.9237
	2E ₁	465	0.1930	1D _{xy} 1D _{x²-y²}	1F _y 0.8547
	1E ₁	498	0.0226	1D _{xy} 1D _{x²-y²}	1D _{xz} 1D _{yz} 0.9663

Note: Th@Au₆: P_x [Au 6s 46.28%, 5d 42.76%; Th 7p 4.47%]; P_y [Au 6s 46.28%, 5d 42.76%; Th 7p 4.47%]; D_{xy} [Au 7s 49.39%, 5d 21.30%, 6p 13.61%; Th 6d 13.63%]; D_{x²-y²} [Au 7s 49.39%, 5d 21.30%, 6p 13.61%; Th 6d 13.63%]; D_{z²} [Th 6d 63.99%, 7s 19.59%, 5f 5.52%; Au 5d 4.68%]; F_x [Th 5f 79.60%; Au 6p 14.80%, 5d 4.82%]; F_y [Au 6s 45.00%, 5d 13.87%; Th 5f 41.45%];

[Ac@Au₆]: P_x [Au 5d 51.09%, 6s 40.87%; Ac 7p 1.79%]; P_y [Au 5d 51.09%, 6s 40.87%; Ac 7p 1.79%]; D_{xy} [Au 6s 58.13%, 6p 12.86%, 5d 16.39%; Ac 6d 11.27%]; D_{x²y²} [Au 6s 58.13%, 6p 12.86%, 5d 16.39%; Ac 6d 11.27%]; D_{xz} [Ac 6d 68.66%; Au 6p 10.97%, 7s 7.37%]; D_{yz} [Ac 6d 68.66%; Au 6p 10.97%, 7s 7.37%]; D_{z²} [Ac 6d 62.38%; Au 6p 23.06%]; F_y [Au 6s 98.29%; Ac 5f 1.93%].

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