## ELECTRONIC SUPPLEMENTARY INFORMATION

# Doping engineering of thermoelectric transport in BNC heteronanotubes

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## **1** Electron transport properties

We have computed the projected electronic density of states (EDOS) of (6,6)-BNC heteronanotubes as implemented in DFTB+ code.



**Figure S 1** Orbital-resolved of projected electronic density of states of helical (6,6)-BNC heteronanotubes. We show the contributions of C and BN domains.



**Figure S 2** Orbital-resolved projected electronic density of states of helical, horizontal, and random (6,6)-BNC heteronanotubes with a BN concentration of 50%. We show the contributions of C and BN domains.



**Figure S 3** Variation of the M parameter with the BN concentration in helical (6,6)-BNC heteronanotubes. M is defined as  $M = \int |\tau_{el}(E > E_F) - \tau_{el}(E < E_F)| dE$ , with  $\tau_{el}$  as the electron transmission function. Insets: comparison of the transmission probability for the conduction (black solid lines) and valence (red dashed lines) bands of helical (6,6)-BNC heteronanotubes at different doping concentrations.



**Figure S 4** Electron transmission function for the different atomic configurations of horizontal (6,6)-BNC heteronanotubes with c = 50%. We compare the results with those corresponding to a (6,6)-CNT and full helical (6,6)-BNCNT with the same concentration. The atomic configurations for each case are also shown.

#### 2 Phonon transport properties

The phonon density of states per atomic site has been calculated by using Green's function formalism as

$$\eta(\omega) = \frac{i(G^r - G^a)\omega}{\pi L}.$$
(1)

Then, we defined the ratio between the phonon DOS corresponding to C and BN domains with the following expression

$$R_{DOS} = \frac{\eta_X(\omega)}{\eta_{Total}(\omega)} \tag{2}$$

where *X* can be either C or BN.



**Figure S 5** Variation of  $R_{DOS}$  as a function of the vibrational frequency for helical (6,6)-BNC heteronanotubes with different concentrations. We show the values corresponding to (a) carbon and (b) boron-nitride domains.



**Figure S 6** Variation of  $R_{DOS}$  as a function of the vibrational frequency for helical, horizontal, and random (6,6)-BNC heteronanotubes with a BN concentration of 50%. We show the values corresponding to (a) carbon and (b) boron-nitride domains.



## **3** Thermoelectric transport properties

**Figure S 7** Variation of the Power Factor (PF) as a function of the chemical potential for helical, horizontal, and random (6,6)-BNC heteronanotubes with a BN concentration of (a) 16% (c = 11% for helical case) and (b) 66%. Figure of merit ZT as a function of the temperature and chemical potential  $\mu$  for (6,6)-BNC heteronanotubes with (c) horizontal and (d) random doping distribution at c = 50%.



**Figure S 8** Temperature dependence of the (a,b) electrical conductance G and the (c,d) Seebeck coefficient S for (6,6)-BNC heteronanotubes at a doping concentration of 50 %. We show the results for helical and horizontal doping distributions.

## 4 CNT - helical BNCNT - CNT system



**Figure S 9** (a) electron and (b) phonon transmission functions for the two cases of helical (6,6)-BNC heteronanotubes. We compare the results to the corresponding functions for (6,6)-CNT. BN concentration dependence of (c) Seebeck coefficient and (d) Power Factor for helical (6,6)-BNCNTs connected to (6,6)-CNT electrodes. (e) Variation of the Figure of merit as a function of the BN concentration for CNT-helical BNCNT - CNT system at 300 K and 800 K.