

**Supplementary material for “Potential energy surface and rovibrational bound states  
of the  $\text{H}_2\text{-C}_3\text{N}^-$  van der Waals complex”**

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TABLE S1. Asymptotic form of the leading expansion coefficients for long-range interaction contributions.  $q$  is the charge,  $\mu$  and  $\Theta$  are the dipole and quadrupole moment respectively.  $\alpha = (\alpha_{\parallel} + 2\alpha_{\perp})$  and  $\Delta\alpha = (\alpha_{\parallel} - \alpha_{\perp})$  are the isotropic and anisotropic polarizabilities where  $\alpha_{\parallel}$  and  $\alpha_{\perp}$  are dipole polarizabilities.  $A_{\parallel}$  and  $A_{\perp}$  are dipole-quadrupole polarizabilities and  $U$  the ionization energies. Subscripts  $a$  and  $b$  refer to molecules  $\text{H}_2$  and  $\text{C}_3\text{N}^-$  respectively.

| $v_{l_1, l_2}^m$ | Electrostatic                                     | Induction                                                                                                                                                                   | Dispersion                                                                                                   |
|------------------|---------------------------------------------------|-----------------------------------------------------------------------------------------------------------------------------------------------------------------------------|--------------------------------------------------------------------------------------------------------------|
| $v_{00}^0$       |                                                   | $-\frac{\alpha_a q_b^2}{R^4} - \frac{1}{3} \frac{\mu_b^2 \Delta\alpha_a}{R^6} - \frac{\mu_b^2 \alpha_a}{R^6} + \dots$                                                       | $-3 \frac{U_a U_b}{U_a + U_b} \frac{\alpha_a \alpha_b}{R^6} + \dots$                                         |
| $v_{01}^0$       |                                                   | $-\frac{4\sqrt{3}}{3} \frac{\alpha_a \mu_b q_b}{R^5} - \frac{12\sqrt{3}}{5} \frac{\alpha_a \mu_b \Theta_b}{R^7} + \dots$                                                    | $-\frac{6\sqrt{3}}{5} \frac{U_a U_b}{U_a + U_b} \frac{\alpha_a (A_{\parallel} + 2A_{\perp})_b}{R^7} + \dots$ |
| $v_{02}^0$       |                                                   | $-\frac{6\sqrt{5}}{5} \frac{\alpha_a q_b \Theta_b}{R^6} - \frac{2\sqrt{5}}{5} \frac{\alpha_a \mu_b^2}{R^6} - \frac{\sqrt{5}}{5} \frac{\Delta\alpha_a \mu_b^2}{R^6} + \dots$ | $-\frac{\sqrt{5}}{5} \frac{U_a U_b}{U_a + U_b} \frac{\alpha_a \Delta\alpha_b}{R^6} + \dots$                  |
| $v_{20}^0$       | $\frac{2\sqrt{5}}{5} \frac{q_b \Theta_a}{R^3}$    | $-\frac{2\sqrt{5}}{15} \frac{\alpha_a q_b^2}{R^4} - \frac{4\sqrt{5}}{15} \frac{\alpha_a q_b \mu_b}{R^5} - \frac{\sqrt{5}}{15} \frac{\Delta\alpha_a \mu_b^2}{R^6} + \dots$   | $-\frac{\sqrt{5}}{5} \frac{U_a U_b}{U_a + U_b} \frac{\alpha_b \Delta\alpha_a}{R^6} + \dots$                  |
| $v_{21}^0$       | $\frac{2\sqrt{15}}{5} \frac{\Theta_a \mu_b}{R^4}$ | $-\frac{4\sqrt{15}}{45} \frac{\Delta\alpha_a q_b \mu_b}{R^5} + \dots$                                                                                                       |                                                                                                              |
| $v_{21}^1$       | $-\frac{4\sqrt{5}}{5} \frac{\Theta_a \mu_b}{R^4}$ | $-\frac{2\sqrt{15}}{15} \frac{\Delta\alpha_a q_b \mu_b}{R^5} + \dots$                                                                                                       |                                                                                                              |
| $v_{22}^0$       | $\frac{15}{5} \frac{\Theta_a \Theta_b}{R^5}$      | $-\frac{2}{5} \frac{\Delta\alpha_a \mu_b^2}{R^6} - \frac{4}{5} \frac{\Delta\alpha_a q_b \Theta_b}{R^6} + \dots$                                                             |                                                                                                              |
| $v_{22}^1$       | $-\frac{16}{5} \frac{\Theta_a \Theta_b}{R^5}$     | $\frac{8}{15} \frac{\Delta\alpha_a \mu_b^2}{R^6} + \frac{12}{5} \frac{\Delta\alpha_a q_b \Theta_b}{R^6} + \dots$                                                            |                                                                                                              |
| $v_{22}^2$       | $\frac{4}{5} \frac{\Theta_a \Theta_b}{R^5}$       | $-\frac{4}{15} \frac{\Delta\alpha_a \mu_b^2}{R^6} + \dots$                                                                                                                  |                                                                                                              |

TABLE S2. Character table of the  $G_4$  group .

|       | $E$ | $(12)$ | $E^*$ | $(12)^*$ |
|-------|-----|--------|-------|----------|
| $A_1$ | 1   | 1      | 1     | 1        |
| $A_2$ | 1   | 1      | -1    | -1       |
| $B_1$ | 1   | -1     | -1    | 1        |
| $B_2$ | 1   | -1     | 1     | -1       |

TABLE S3. Complete list of the  $H_2-C_3N^-$  calculated rovibrational energy levels for total angular momentum  $J = 0$ .

| $\Gamma_i$ | Energy ( $cm^{-1}$ ) |         |         |         |         |         |         |         |
|------------|----------------------|---------|---------|---------|---------|---------|---------|---------|
| $A_1$      | -257.22              | -232.95 | -216.34 | -203.00 | -189.93 | -174.95 | -174.76 | -160.57 |
|            | -157.08              | -153.89 | -146.80 | -137.43 | -134.08 | -125.76 | -120.79 | -113.17 |
|            | -109.80              | -99.17  | -98.14  | -85.24  | -84.18  | -83.73  | -80.74  | -74.97  |
|            | -70.38               | -67.58  | -66.14  | -61.66  | -56.92  | -52.83  | -50.61  | -48.28  |
|            | -42.22               | -38.52  | -34.73  | -33.05  | -32.10  | -30.46  | -29.16  | -25.80  |
|            | -24.16               | -20.47  | -19.33  | -17.55  | -13.91  | -13.50  | -11.01  | -10.26  |
|            | -8.96                | -7.47   | -6.43   | -5.92   | -3.85   | -2.83   | -1.33   |         |
| $B_2$      | -242.50              | -214.84 | -193.29 | -174.67 | -156.44 | -141.71 | -137.29 | -125.74 |
|            | -120.00              | -116.38 | -101.76 | -101.45 | -95.02  | -84.47  | -82.69  | -71.89  |
|            | -66.53               | -59.89  | -51.15  | -45.22  | -39.41  | -35.86  | -33.47  | -33.16  |
|            | -26.59               | -17.30  | -15.93  | -15.81  | -10.40  | -8.41   | -4.45   | -0.85   |

TABLE S4. Complete list of the  $\text{H}_2\text{-C}_3\text{N}^-$  calculated rovibrational energy levels for total angular momentum  $J = 1$ .

| $\Gamma_i$ | Energy ( $\text{cm}^{-1}$ ) |         |         |         |         |         |         |         |
|------------|-----------------------------|---------|---------|---------|---------|---------|---------|---------|
| A1         | -242.83                     | -223.06 | -208.68 | -195.80 | -181.75 | -166.14 | -164.81 | -153.36 |
|            | -146.75                     | -141.94 | -135.81 | -125.96 | -124.16 | -114.41 | -110.69 | -103.42 |
|            | -95.94                      | -90.43  | -80.05  | -77.96  | -75.99  | -71.58  | -68.35  | -61.83  |
|            | -60.69                      | -60.17  | -52.03  | -50.92  | -43.09  | -41.82  | -39.71  | -32.49  |
|            | -28.83                      | -28.50  | -27.64  | -23.40  | -22.31  | -22.10  | -17.94  | -16.33  |
|            | -13.91                      | -11.10  | -8.60   | -7.77   | -6.94   | -5.01   | -3.33   | -1.74   |
|            | -0.48                       |         |         |         |         |         |         |         |
| A2         | -256.89                     | -242.84 | -232.60 | -223.07 | -215.96 | -208.72 | -202.58 | -195.85 |
|            | -189.46                     | -181.81 | -174.42 | -174.17 | -166.13 | -164.96 | -159.46 | -157.26 |
|            | -153.43                     | -152.30 | -148.90 | -143.57 | -141.96 | -139.17 | -133.60 | -132.71 |
|            | -127.83                     | -125.98 | -120.29 | -120.21 | -115.08 | -114.38 | -109.34 | -106.18 |
|            | -103.48                     | -100.72 | -97.43  | -91.22  | -89.96  | -85.42  | -83.68  | -83.41  |
|            | -80.24                      | -78.19  | -77.05  | -74.12  | -72.53  | -71.59  | -71.16  | -67.46  |
|            | -66.28                      | -65.61  | -63.35  | -60.33  | -57.68  | -56.38  | -54.35  | -54.02  |
|            | -52.02                      | -49.65  | -48.15  | -46.95  | -44.10  | -42.70  | -37.84  | -35.83  |
|            | -34.76                      | -34.29  | -32.72  | -32.36  | -31.21  | -29.21  | -29.18  | -28.84  |
|            | -26.83                      | -25.45  | -25.31  | -23.45  | -22.42  | -20.96  | -20.70  | -19.72  |
|            | -18.48                      | -16.35  | -15.23  | -13.78  | -12.48  | -11.91  | -9.99   | -9.93   |
|            | -9.22                       | -8.67   | -8.38   | -8.23   | -7.88   | -6.60   | -6.47   | -6.23   |
|            | -5.35                       | -4.73   | -4.08   | -3.28   | -3.12   | -1.15   | -0.97   | -0.36   |
| B1         | -242.15                     | -226.67 | -214.46 | -202.63 | -192.86 | -182.99 | -174.13 | -164.63 |
|            | -155.64                     | -145.80 | -141.02 | -135.96 | -129.45 | -125.20 | -125.07 | -119.43 |
|            | -113.96                     | -111.62 | -109.40 | -103.09 | -100.82 | -100.21 | -94.30  | -90.48  |
|            | -89.29                      | -84.97  | -81.92  | -77.33  | -73.36  | -72.89  | -65.58  | -64.03  |
|            | -59.08                      | -57.28  | -49.78  | -49.40  | -45.20  | -40.80  | -39.56  | -37.08  |
|            | -35.14                      | -31.99  | -31.32  | -28.72  | -23.89  | -23.83  | -23.24  | -21.85  |
|            | -15.85                      | -15.06  | -12.96  | -11.84  | -9.12   | -8.22   | -7.02   | -6.70   |
|            | -4.88                       | -3.37   | -2.21   |         |         |         |         |         |
| B2         | -226.66                     | -202.62 | -182.98 | -164.61 | -145.79 | -129.45 | -125.08 | -111.61 |
|            | -109.44                     | -102.53 | -92.32  | -90.48  | -80.63  | -73.35  | -68.85  | -57.41  |
|            | -54.49                      | -41.55  | -39.83  | -34.64  | -23.83  | -23.27  | -21.85  | -17.33  |
|            | -9.72                       | -7.72   | -6.71   | -2.99   | -2.81   | -2.26   |         |         |