Supporting Information

Protection of COOH and OH Groups in Acid, Base and Salt Free Reactions

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Materials and methods

All reactions were carried out under an atmosphere of air in glassware with magnetic stirring unless otherwise indicated. Commercially purchased reagents were used as received. Solvents were dried by Innovative Technology Solvent Purification System. Liquids and solutions were transferred via syringe. All reactions were monitored by thin-layer chromatography. GC data were recorded on Thermo TRACE 1300. GC-MS data were recorded on Thermo ISQ QD. ¹H and ¹³C NMR spectra were recorded on Bruker-BioSpin AVANCE III HD. Data for ¹H NMR spectra are reported relative to chloroform as an internal standard (7.26 ppm) and are reported as follows: chemical shift (ppm), multiplicity (m), coupling constant (Hz), and integration. Data for ¹³C NMR spectra are reported relative to chloroform as an internal standard (77.23 ppm) and are reported in terms of chemical shift (ppm). HRMS data were recorded on Thermo Finnigan Impact II UHR-TOF. Melting point was obtained from Shanghai Shengguang SGW X-4.

General procedure

General procedure A for Table 1: Catalyst, benzoic acid (0.4 mmol, 1.0 equiv.), and MTBE (1.0 mL) were added into the Schlenk tube with a stirring bar, and then the reaction mixture was heated at 90 $^{\circ}$ C for 8 hours. The mixture was filtered by a short silica gel column (about 3 g) or a short activated carbon column (about 2 g), which was washed by EA (10 mL). After added the 1,4-dimethoxybenzene into the solvent as the internal standard, the yield of product **3a** could be detected by GC analysis.

General procedure B for Table 2: $Fe(OTf)_3$ (0.05 mmol, 1 mol%), carboxylic acid 1 (5.0 mmol, 1.0 equiv.), and MTBE 2 (2.5 mL) were added into the Schlenk tube with a stirring bar, and then the reaction mixture was heated at 90 °C for 48 hours. The mixture was filtered by a short silica gel column (about 5 g) or a short activated carbon column (about 3 g), which was washed by EA (30 mL). The solvent was removed by rotary evaporation under vacuum and products **3** were attained directly without further purification.

General procedure C for Table 2: $Fe(OTf)_3$ (0.01 mmol, 0.1 mol%), phenol **4** (10 mmol, 1.0 equiv.) and IPA 5 (2.5 mL) were added into the Schlenk tube with a stirring bar, and then the reaction mixture was stirred at room temperature for 5 hours. The mixture was filtered by a short silica gel column (about 5 g) or a short activated carbon column (about 2 g), which was washed by EA (30 mL). The solvent was removed by rotary evaporation under vacuum and products **6** were attained directly without further purification.

General procedure D for Table 3: $Fe(OTf)_3$ (0.025 mmol, 0.5 mol%), alcohol **4** (5 mmol, 1.0 equiv.) and IPA **5** (2.5 mL) were added into the Schlenk tube with a stirring bar, and then the reaction mixture was stirred at room temperature for 5 hours. The solvent was removed by rotary evaporation under vacuum and the residue was chromatographed on silica gel to give the product **6**.

Efficiency of catalyst

Figure S1:

	о 0 ⁻ Н + 2	Fe(OTf) ₃	→ OMe	
	1a	2	3a	
Entry	Fe(OTf) ₃ (mol%)	MTBE (mL)	Yield $(\%)^b$	TON
1	1	10	90	90
2	0.5	10	87	174
3	0.1	10	53	265
4	1	3.5	81	81
5	1	2.2	72	72
6	0.5	3.5	73	146
7	0.1	3.5	49	490
8	0.05	3.5	44	880
9	0.01	3.5	23	2300

^{*a*} Reaction conditions: benzoic acid **1a** (20 mmol, 1 equiv), MTBE, 48 h. ^{*b*} Yields of product **3a** were determined by GC analysis with 1,4-dimethoxybenzene as the internal standard.

General procedure for Figure S1: $Fe(OTf)_3$, benzoic acid 1a (20.0 mmol, 1.0 equiv.), and MTBE 2 were added into the Schlenk tube with a stirring bar, and then the reaction mixture was heated at 90 °C for 48 hours. The mixture was filtered by a short silica gel column, which was washed by EA (30 mL). After added the 1,4-dimethoxybenzene into the solvent as the internal standard, the yield of product methyl benzoate **3a** could be detected by GC analysis.

Figure S2:

	OF	+	Fe(OTf) ₃ rt, Time	OAc	
	4a	5		6a	
Entry	Fe(OTf) ₃ (mol%)	IPA (mL)	Time (h)	Yield $(\%)^b$	TON
1	1	8	5	89	89
2	0.5	8	5	93	186
3	0.1	8	5	90	900
4	0.1	5	5	92	920
5	0.05	5	5	83	1660
6	0.01	5	24	67	6700
7^c	10	2.5	24	NR	/

^{*a*} Reaction conditions: phenol **4a** (20 mmol, 1 equiv), IPA **5**, room temperature. ^{*b*} Yields of product **6a** were determined by ¹H NMR analysis with 1,4-dimethoxybenzene as the internal standard. ^{*c*} Phenol **4a** (1 mmol, 1 equiv), IPA **5** (2.5 mL), room temperature, 24 h.

General procedure for Figure S2: $Fe(OTf)_3$, phenol **4a** (20 mmol, 1.0 equiv) and IPA **5** were added into the Schlenk tube with a stirring bar, and then the reaction mixture was stirred at room temperature. The mixture was filtered by a short silica gel column, which was washed by EA (30 mL). After added the 1,4-dimethoxybenzene into the solvent as the internal standard, the yield of product methyl benzoate **6a** could be detected by ¹H NMR.

Characterization data for the products





Following the general procedure B (967.5 mg, 90% yield, a pale yellow solid (m.p.: 75.1-75.6 °C)). ¹H NMR (400 MHz, CDCl₃) δ 7.90 (d, J = 7.7 Hz, 2H), 7.58 (d, J = 6.8 Hz, 2H), 3.91 (s, 3H). ¹³C NMR (101 MHz, CDCl₃) δ 166.36, 131.71, 131.11, 129.03, 128.03, 52.30.



3c¹

Following the general procedure B (2.0 mmol, Fe(OTf)₃ (5 mol %), MTBE (2.0 mL), 445.4 mg, 85% yield, product **3c** was chromatographed on silica gel as a clear oil). ¹H NMR (400 MHz, CDCl₃) δ 7.99 (d, *J* = 7.9 Hz, 1H), 7.80 (d, *J* = 7.7 Hz, 1H), 7.40 (t, *J* = 7.5 Hz, 1H), 7.15 (t, *J* = 8.4 Hz, 1H), 3.93 (s, 3H). ¹³C NMR (101 MHz, CDCl₃) δ 166.96, 141.32, 135.07, 132.66, 130.95, 127.90, 94.10, 52.52.



3d²

Following the general procedure B (853.6 mg, 88% yield, a white solid (m.p.: 64.0-64.6 °C)). ¹H NMR (400 MHz, CDCl₃) δ 8.68 (t, J = 1.8 Hz, 1H), 8.22 (dd, J = 7.8, 1.8 Hz, 2H), 7.53 (t, J = 7.8 Hz, 1H), 3.95 (s, 6H). ¹³C NMR (101 MHz, CDCl₃) δ 166.18, 133.76, 130.67, 130.56, 128.59, 52.33.



3e¹

Following the general procedure B (2.0 mmol, Fe(OTf)₃ (5 mol %), MTBE (2.0 mL), 333.1 mg, 92% yield, , product **3e** was chromatographed on silica gel as a white solid (m.p.: 91.5-92.2 °C)). ¹H NMR (400 MHz, CDCl₃) δ 8.29 (d, *J* = 6.2 Hz, 2H), 8.22 (d,

J = 6.3 Hz, 2H), 3.99 (s, 3H). ¹³C NMR (101 MHz, CDCl₃) δ 165.15, 150.51, 135.47, 130.70, 123.53, 52.83.





Following the general procedure B (2.0 mmol, Fe(OTf)₃ (5 mol %), MTBE (2.0 mL), 288.8 mg, 87% yield, , product **3f** was chromatographed on silica gel as a white solid (m.p.: 44.0-44.8 °C)). ¹H NMR (400 MHz, CDCl₃) δ 7.99 (d, *J* = 8.8 Hz, 2H), 6.92 (d, *J* = 8.8 Hz, 2H), 3.88 (s, 3H), 3.86 (s, 3H). ¹³C NMR (101 MHz, CDCl₃) δ 166.87, 163.31, 131.58, 122.58, 113.59, 55.42, 51.88.



3g

Following the general procedure B (676.4 mg, 89% yield, a white solid (m.p.: 66.9-68.0 °C)). ¹H NMR (400 MHz, CDCl₃) δ 7.70 – 7.55 (m, 2H), 7.31 (t, *J* = 7.8 Hz, 1H), 7.13 – 7.04 (m, 1H), 6.44 (br, 1H), 3.92 (s, 3H). ¹³C NMR (101 MHz, CDCl₃) δ 167.49, 155.96, 131.25, 129.76, 121.86, 120.41, 116.40, 52.43. Compound **3g** is commercially available.



3h³

Following the general procedure B (2.0 mmol, Fe(OTf)₃ (5 mol %), MTBE (2.0 mL), 275.4 mg, 85% yield, product **3h** was chromatographed on silica gel as a clear oil). ¹H NMR (400 MHz, CDCl₃) δ 7.99 (d, *J* = 8.1 Hz, 2H), 7.46 (d, *J* = 8.1 Hz, 2H), 6.75 (dd, *J* = 17.6, 10.9 Hz, 1H), 5.86 (d, *J* = 17.6 Hz, 1H), 5.38 (d, *J* = 10.9 Hz, 1H), 3.91 (s, 3H). ¹³C NMR (101 MHz, CDCl₃) δ 166.87, 141.91, 136.01, 129.89, 129.26, 126.11, 116.49, 52.10.



3i⁴

Following the general procedure B (729.0 mg, 90% yield, a clear oil). ¹H NMR (400 MHz, CDCl₃) δ 7.69 (d, J = 16.0 Hz, 1H), 7.55 – 7.45 (m, 2H), 7.37 (t, J = 3.8 Hz,

3H), 6.44 (d, J = 16.0 Hz, 1H), 3.80 (s, 3H). ¹³C NMR (101 MHz, CDCl₃) δ 167.41, 144.87, 134.38, 130.30, 128.89, 128.07, 117.80, 51.70.



3j⁵

Following the general procedure B (541.8 mg, 86% yield, a clear oil). ¹H NMR (400 MHz, CDCl₃) δ 7.26 (dd, J = 15.3, 9.8 Hz, 1H), 6.30 – 6.06 (m, 2H), 5.78 (d, J = 15.4 Hz, 1H), 3.73 (s, 3H), 1.85 (d, J = 5.5 Hz, 3H). ¹³C NMR (101 MHz, CDCl₃) δ 167.64, 145.12, 139.37, 129.72, 118.50, 51.34, 18.58.



3k

Following the general procedure B (1097.5 mg, 98% yield, a white solid (m.p.: 34.7-35.4 °C)). ¹H NMR (400 MHz, CDCl₃) δ 6.82 – 6.77 (m, 1H), 6.77 – 6.70 (m, 2H), 3.87 (s, 3H), 3.85 (s, 3H), 3.67 (s, 3H), 2.90 (t, *J* = 7.8 Hz, 2H), 2.66 – 2.57 (t, *J* = 7.8 Hz, 2H). ¹³C NMR (101 MHz, CDCl₃) δ 173.39, 148.83, 147.45, 133.11, 120.06, 111.57, 111.22, 55.89, 55.80, 51.63, 36.01, 30.60. HRMS (ESI) m/z calcd. for (C₁₂H₁₆O₄) [M+ Na]⁺: 247.0941, found: 247.0942.



Following the general procedure B (598.0 mg, 92% yield, a clear oil). ¹H NMR (400 MHz, CDCl₃) δ 3.60 (s, 3H), 2.70 (m, 2H), 2.51 (t, *J* = 6.1 Hz, 2H), 2.12 (s, 3H). ¹³C NMR (100 MHz, CDCl₃) δ 206.62, 173.12, 51.65, 37.81, 29.70, 27.62.



Following the general procedure B (809.1 mg, 93% yield, a clear oil). ¹H NMR (400 MHz, CDCl₃) δ 3.67 (s, 6H), 2.40 – 2.28 (m, 4H), 1.72 – 1.59 (m, 4H). ¹³C NMR (101 MHz, CDCl₃) δ 173.61, 51.39, 33.52, 24.25.





Following the general procedure B (762.6 mg, 93% yield, a clear oil). ¹H NMR (400 MHz, CDCl₃) δ 7.34 – 7.26 (m, 4H), 7.26 – 7.19 (m, 1H), 3.71 (q, *J* = 7.2 Hz, 1H), 3.63 (s, 3H), 1.49 (d, *J* = 7.2 Hz, 3H). ¹³C NMR (101 MHz, CDCl₃) δ 174.99, 140.60, 128.68, 127.50, 127.18, 52.02, 45.44, 18.65.



30

Following the general procedure B (644.0 mg, 92% yield, a clear oil). ¹H NMR (400 MHz, CDCl₃) δ 5.75 – 5.58 (m, 2H), 3.69 (s, 3H), 2.62 – 2.51 (m, 1H), 2.30 – 2.21 (m, 2H), 2.15 – 2.05 (m, 2H), 2.05 – 1.95 (m, 1H), 1.75 – 1.61 (m, 1H). ¹³C NMR (101 MHz, CDCl₃) δ 176.24, 126.61, 125.14, 51.57, 39.18, 27.42, 25.05, 24.41. Compound **30** is commercially available.



sp^r og the genera

Following the general procedure B (1303.5 mg, 79% yield, product **3p** was chromatographed on silica gel as a white solid (m.p.: 116.5-117.2 °C)). ¹H NMR (400 MHz, CDCl₃) δ 5.73 (s, 1H), 3.68 (s, 3H), 2.48 – 2.24 (m, 5H), 2.21 – 2.10 (m, 1H), 2.08 – 1.98 (m, 2H), 1.91 – 1.67 (m, 4H), 1.64 – 1.50 (m, 2H), 1.48 – 1.38 (m, 1H), 1.35 – 1.23 (m, 2H), 1.19 (s, 3H), 1.16 – 1.02 (m, 2H), δ 1.02 – 0.93 (m, 1H), 0.71 (s, 3H). ¹³C NMR (101 MHz, CDCl₃) δ 199.40, 174.31, 170.99, 123.88, 55.24, 55.06, 53.69, 51.27, 43.87, 38.59, 38.02, 35.70, 35.68, 33.93, 32.78, 31.91, 24.42, 23.57, 20.85, 17.35, 13.43.



Following the general procedure B (911.8 mg, 94% yield, a clear oil). ¹H NMR (400 MHz, CDCl₃) δ 3.65 (s, 3H), 2.05 – 1.97 (m, 3H), 1.93 – 1.84 (m, 6H), 1.77 – 1.65 (m, 6H). ¹³C NMR (101 MHz, CDCl₃) δ 178.18, 51.52, 40.68, 38.84, 36.48, 27.93.



Following the general procedure C (10 mmol, 1361.5 mg, 99% yield, a clear oil). ¹H NMR (400 MHz, CDCl₃) δ 7.38 – 7.31 (m, 2H), 7.22 – 7.16 (m, 1H), 7.10 – 7.03 (m, 2H), 2.25 (s, 3H). ¹³C NMR (101 MHz, CDCl₃) δ 169.52, 150.74, 129.48, 125.87, 121.64, 21.14.



6b

Following the general procedure C (10 mmol, 2150.5 mg, 99% yield, a clear oil). ¹H NMR (400 MHz, CDCl₃) δ 7.30 – 7.25 (m, 1H), 7.20 (t, J = 2.1 Hz, 1H), 7.15 (t, J = 8.1 Hz, 1H), 6.98 – 6.92 (m, 1H), 2.19 (s, 3H). ¹³C NMR (101 MHz, CDCl₃) δ 168.98, 151.18, 130.49, 129.01, 125.12, 122.35, 120.50, 21.03. Compound **6b** is commercially available.



6c

Following the general procedure C (10 mmol, 2939.4 mg, 99% yield, a white solid (m.p.: 48.7-49.2 °C)). ¹H NMR (400 MHz, CDCl₃) δ 7.45 (t, *J* = 1.7 Hz, 1H), 7.16 (d, *J* = 1.7 Hz, 2H), 2.20 (s, 3H). ¹³C NMR (101 MHz, CDCl₃) δ 168.52, 151.38, 131.65, 124.13, 122.75, 20.96. Compound **6c** is commercially available.



Following the general procedure C (1801.6 mg, 99% yield, a clear oil). ¹H NMR (400 MHz, CDCl₃) δ 6.76 (d, *J* = 8.3 Hz, 1H), 6.60 (d, *J* = 2.3 Hz, 1H), 6.51 (dd, *J* = 8.4, 2.3 Hz, 1H), 5.95 (s, 2H), 2.25 (s, 3H). ¹³C NMR (101 MHz, CDCl₃) δ 169.79, 147.99, 145.35, 144.99, 113.91, 107.96, 103.73, 101.71, 20.98.



6e¹²

Following the general procedure C (5 mmol, Fe(OTf)₃ (0.2 mol %), IPA (2.5 mL), 931.1 mg, 99% yield, a white solid (m.p.: 62.3-63.5 °C)). ¹H NMR (400 MHz, CDCl₃) δ 7.88 – 7.74 (m, 3H), 7.55 (d, *J* = 2.4 Hz, 1H), 7.52 – 7.40 (m, 2H), 7.22 (dd, *J* = 8.9, 2.3 Hz, 1H), 2.34 (s, 3H). ¹³C NMR (101 MHz, CDCl₃) δ 169.68, 148.34, 133.77, 131.49, 129.44, 127.79, 127.67, 126.58, 125.74, 121.15, 118.56, 21.23.



Following the general procedure C (5 mmol, Fe(OTf)₃ (0.2 mol %), IPA (2.5 mL), DCM (1.0 mL) 1251.3 mg, 99% yield, a white solid (m.p.: 118.4-119.2 °C)). ¹H NMR (400 MHz, CDCl₃) δ 7.64 (d, *J* = 15.9 Hz, 1H), 7.14 – 7.08 (m, 2H), 7.04 (d, *J* = 8.3 Hz, 1H), 6.39 (d, *J* = 15.9 Hz, 1H), 3.84 (s, 3H), 3.80 (s, 3H), 2.32 (s, 3H). ¹³C NMR (101 MHz, CDCl₃) δ 168.77, 167.23, 151.36, 144.13, 141.40, 133.31, 123.23, 121.18, 117.99, 111.24, 55.86, 51.74, 20.63.



6g¹⁴

Following the general procedure C (5 mmol, Fe(OTf)₃ (0.2 mol %), IPA (2.5 mL), 1562.0 mg, 99% yield, a white solid (m.p.: 142.5-143.7 °C)). ¹H NMR (400 MHz, Chloroform-*d*) δ 7.31 – 7.27 (m, 1H), 6.85 (dd, *J* = 8.4, 2.7 Hz, 1H), 6.81 (d, *J* = 2.6 Hz, 1H), 2.95 – 2.87 (m, 2H), 2.51 (dd, *J* = 18.8, 8.4 Hz, 1H), 2.45 – 2.37 (m, 1H), 2.33 – 2.24 (m, 4H), 2.20 – 1.94 (m, 4H), 1.69 – 1.41 (m, 6H), 0.91 (s, 3H). ¹³C NMR (101 MHz, CDCl₃) δ 220.75, 169.84, 148.56, 138.02, 137.41, 126.42, 121.60, 118.76, 50.44, 47.95, 44.16, 38.00, 35.87, 31.56, 29.41, 26.35, 25.75, 21.60, 21.14, 13.84.



Following the general procedure D (5 mmol, Fe(OTf)₃ (0.5 mol %), IPA (2.5 mL), 0.83 g, 94% yield, a clear oil). ¹H NMR (400 MHz, CDCl₃) δ 7.40 – 7.35 (m, 2H), 7.34 – 7.28 (m, 2H), 7.27 – 7.21 (m, 1H), 6.64 (dt, *J* = 15.8, 1.3 Hz, 1H), 6.27 (dt, *J* = 15.9, 6.4 Hz, 1H), 4.72 (dd, *J* = 6.4, 1.4 Hz, 2H), 2.08 (s, 3H). ¹³C NMR (101 MHz, CDCl₃) δ 170.81, 136.22, 134.20, 128.62, 128.08, 126.62, 123.19, 65.08, 20.99.



Following the general procedure D (5 mmol, Fe(OTf)₃ (0.5 mol %), IPA (2.5 mL), 0.78 g, 95% yield, a clear oil). ¹H NMR (400 MHz, CDCl₃) δ 7.31 – 7.24 (m, 2H), 7.23 – 7.16 (m, 3H), 4.26 (t, *J* = 7.1 Hz, 2H), 2.91 (t, *J* = 7.1 Hz, 2H), 1.99 (s, 3H). ¹³C NMR (101 MHz, CDCl₃) δ 170.98, 137.86, 128.93, 128.54, 126.60, 64.96, 35.12, 20.96.



Following the general procedure D (5 mmol, Fe(OTf)₃ (0.5 mol %), IPA (2.5 mL), 0.78 g, 92% yield, a clear oil). ¹H NMR (400 MHz, CDCl₃) δ 5.77 – 5.62 (m, 1H), 5.20 – 5.11 (m, 2H), 5.08 (d, *J* = 10.5 Hz, 1H), 1.99 (s, 3H), 1.61 – 1.46 (m, 2H), δ 1.29 – 1.19 (m, 6H), 0.80 (t, *J* = 6.8 Hz, 3H). ¹³C NMR (101 MHz, CDCl₃) δ 170.30, 136.63, 116.43, 74.83, 34.12, 31.52, 24.69, 22.48, 21.19, 13.94.



6k¹⁸

Following the general procedure D (2.5 mmol, Fe(OTf)₃ (1.0 mol %), IPA (2.5 mL), 0.50 g, 66% yield, a clear oil). ¹H NMR (400 MHz, CDCl₃) ¹H NMR (400 MHz, CDCl₃) δ 8.84 (br, 1H), 6.82 (s, 1H), 5.71 (s, 1H), 5.34 – 5.14 (m, 2H), 2.86 (d, J = 18.9 Hz, 1H), 2.39 (d, J = 18.8 Hz, 1H), 2.10 – 1.99 (m, 9H). ¹³C NMR (101 MHz, CDCl₃) δ 177.00, 170.14, 170.07, 169.84, 134.66, 130.75, 67.54, 66.77, 66.03, 28.07, 20.95, 20.72, 20.70.



6I¹⁹

Following the general procedure D (2.5 mmol, Fe(OTf)₃ (1.0 mol %), IPA (2.5 mL), 0.86 g, 90% yield, a white solid (m.p.: 142.2-143.1 °C)). ¹H NMR (400 MHz, CDCl₃) δ 7.33 – 7.26 (m, 1H), 6.84 (dd, *J* = 8.4, 2.7 Hz, 1H), 6.79 (d, *J* = 2.6 Hz, 1H), 2.91 – 2.82 (m, 2H), 2.85 – 2.73 (m, 1H), 2.63 (s, 1H), 2.43 – 2.32 (m, 1H), 2.33 – 2.22 (m, 4H), 2.13 – 1.97 (m, 5H), 1.94 – 1.78 (m, 3H), 1.80 – 1.67 (m, 1H), 1.59 – 1.34 (m,

4H), 0.90 (s, 3H). ¹³C NMR (101 MHz, CDCl₃) δ 169.86, 169.60, 148.45, 138.17, 137.78, 126.45, 121.52, 118.62, 84.45, 83.37, 74.95, 47.87, 47.84, 43.63, 38.78, 37.37, 33.12, 29.54, 27.11, 26.18, 23.32, 21.47, 21.15, 13.41.



6m

Following the general procedure D (2.5 mmol, Fe(OTf)₃ (1.0 mol %), IPA (2.5 mL), 0.86 g, 87% yield, a white solid). ¹H NMR (400 MHz, CDCl₃) δ 5.70 (s, 1H), 5.39 (t, J = 5.2, 1H), 2.79 – 2.70 (m, 1H), 2.60 (s, 1H), 2.52 – 2.41 (m, 1H), 2.24 – 2.11 (m, 5H), 2.07 – 2.02 (m, 4H), 1.92 – 1.82 (m, 2H), 1.78 – 1.66 (m, 5H), 1.64 – 1.50 (m, 2H), 1.39 – 1.31 (m, 2H), 1.12 – 1.01 (m, 4H), 0.92 – 0.88 (m, 3H). ¹³C NMR (101 MHz, CDCl₃) δ 169.61, 169.37, 147.07, 139.39, 123.44, 116.91, 84.50, 83.36, 74.85, 49.20, 47.55, 47.52, 37.40, 34.91, 33.76, 32.91, 32.16, 31.42, 24.80, 23.62, 21.46, 21.10, 20.84, 18.87, 13.43. MS (EI): 396 [M⁺].



Following the general procedure D (2.5 mmol, Fe(OTf)₃ (1.0 mol %), IPA (2.5 mL), 0.93 g, 70% yield, a clear oil). ¹H NMR (400 MHz, CDCl₃) δ 5.10 (d, *J* = 2.9 Hz, 1H), 4.91 (q, *J* = 3.1 Hz, 1H), 4.58 (tt, *J* = 11.3, 4.3 Hz, 1H), 2.44 – 2.34 (m, 1H), 2.29 – 2.20 (m, 1H), 2.14 (s, 3H), 2.10 (s, 3H), 2.06 (s, 3H), 2.02 – 1.75 (m, 7H), 1.74 – 1.29 (m, 13H), 1.17 – 1.03 (m, 2H), 0.92 (s, 3H), 0.82 (d, *J* = 6.3 Hz, 3H), 0.73 (s, 3H). ¹³C NMR (101 MHz, CDCl₃) δ 179.68, 170.68, 170.63, 170.52, 75.41, 74.13, 70.74, 47.32, 45.05, 43.39, 40.90, 37.71, 34.67, 34.59, 34.54, 34.32, 31.23, 30.83, 30.53, 28.88, 27.16, 26.88, 25.57, 22.79, 22.57, 21.65, 21.52, 21.46, 17.48, 12.24. HRMS (ESI) m/z calcd. for (C₃₀H₄₆O₆Na) [M+Na]⁺: 557.3085, found: 557.3081.



Following the general procedure D (2.5 mmol, Fe(OTf)₃ (1.0 mol %), IPA (2.5 mL), 0.81 g, 90% yield, a white solid (m.p.: 144.0-144.9 °C)). ¹H NMR (400 MHz, CDCl₃) δ 5.35 (d, *J* = 3.8 Hz, 1H), 4.64 – 4.52 (m, 1H), 2.51 (t, *J* = 8.8 Hz, 1H), 2.35 – 2.25 (m, 2H), 2.23 – 2.13 (m, 1H), 2.10 (s, 3H), 2.05 – 1.93 (m, 5H), 1.85 (d, *J* = 11.3 Hz, 2H), 1.72 – 1.54 (m, 5H), 1.52 – 1.42 (m, 3H), 1.24 – 1.11 (m, 3H), 1.04 – 0.94 (m, 4H), 0.61 (s, 3H). ¹³C NMR (101 MHz, CDCl₃) δ 209.49, 170.51, 139.65, 122.32, 73.83, 63.67, 56.83, 49.89, 43.97, 38.79, 38.07, 37.00, 36.60, 31.82, 31.76, 31.54, 27.73, 24.48, 22.83, 21.42, 21.03, 19.30, 13.22.





Following the general procedure D (2.5 mmol, Fe(OTf)₃ (1.0 mol %), IPA (2.5 mL), 0.93 g, 87% yield, a clear oil). ¹H NMR (400 MHz, CDCl₃) δ 6.15 (d, *J* = 11.2 Hz, 1H), 5.96 (d, *J* = 11.4 Hz, 1H), 4.99 (d, *J* = 2.4 Hz, 1H), 4.87 (tt, *J* = 8.0, 3.9 Hz, 1H), 4.77 (d, *J* = 2.4 Hz, 1H), 2.79 – 2.70 (m, 1H), 2.50 (dd, *J* = 13.5, 4.1 Hz, 1H), 2.37 – 2.25 (m, 2H), 2.18 – 2.12 (m, 1H), 1.97 (s, 3H), 1.91 – 1.77 (m, 3H), 1.71 – 1.60 (m, 2H), 1.50 – 1.37 (m, 4H), 1.32 – 1.16 (m, 9H), 1.10 – 1.02 (m, 3H), 0.85 (d, *J* = 6.4 Hz, 3H), 0.80 (d, *J* = 1.9 Hz, 3H), 0.79 (d, *J* = 1.9 Hz, 3H), 0.47 (s, 3H). ¹³C NMR (101 MHz, CDCl₃) δ 170.65, 144.62, 142.50, 134.30, 122.46, 117.46, 112.74, 71.81, 56.59, 56.38, 45.93, 42.15, 40.55, 39.51, 36.15, 32.20, 31.98, 29.73, 29.08, 28.04, 27.69, 23.88, 23.59, 22.85, 22.59, 22.24, 21.44, 18.86, 12.00.



Following the general procedure D (1.0 mmol, Fe(OTf)₃ (10 mol %), IPA (2.5 mL), 0.5 h, 160 mg, 41% yield, a white solid (m.p.: 97.6-99.2 °C)). ¹H NMR (400 MHz, CDCl₃) δ 6.33 (d, J = 3.7 Hz, 1H), 5.51 – 5.44 (m, 1H), 5.18 – 5.07 (m, 2H), 4.30 – 4.24 (m, 1H), 4.16 – 4.07 (m, 2H), 2.19 (s, 3H), 2.10 (s, 3H), 2.05 (s, 3H), 2.03 (s, 3H), 2.02 (s, 3H). ¹³C NMR (101 MHz, CDCl₃) δ 170.59, 170.18, 169.63, 169.37, 168.73, 89.02, 69.79, 69.16, 67.85, 61.43, 20.83, 20.65, 20.62, 20.52, 20.41. .OAc

AcO

6r²²

Following the general procedure D (1.0 mmol, Fe(OTf)₃ (10 mol %), IPA (2.5 mL), 0.5 h, 156.5 mg, 91% yield, a clear oil). ¹H NMR (400 MHz, CDCl₃) δ 5.78 – 5.73 (m, 2H), 4.68 (d, J = 5.2 Hz, 4H), 2.07 (s, 6H). ¹³C NMR (101 MHz, CDCl₃) δ 170.62, 127.99, 59.92, 20.80.



Following the general procedure D (1.0 mmol, Fe(OTf)₃ (10 mol %), IPA (2.5 mL), 0.5 h, 178.4 mg, 90% yield, a clear oil). ¹H NMR (400 MHz, CDCl₃) δ 4.76 – 4.58 (m, 1H), 2.03 (s, 3H), 2.01 – 1.94 (m, 1H), 1.91 – 1.82 (m, 1H), 1.73 – 1.62 (m, 2H), 1.54 -1.42 (m, 1H), 1.40 - 1.30 (m, 1H), 1.26 (d, J = 4.2 Hz, 1H), 1.13 - 1.02 (m, 1H), 1.01 - 0.94 (m, 1H), 0.91 (d, J = 2.4 Hz, 3H), 0.89 (d, J = 2.9 Hz, 3H), 0.77 (d, J =7.0 Hz, 3H). ¹³C NMR (101 MHz, CDCl₃) δ 170.56, 74.07, 46.97, 40.90, 34.23, 31.33, 26.28, 23.46, 21.96, 21.23, 20.68, 16.33.



Following the general procedure D (1.0 mmol, Fe(OTf)₃ (10 mol %), IPA (2.5 mL), 0.5 h, 146.2 mg, 58% yield, a white solid (m.p.: 104.5-101.9 °C)). ¹H NMR (400 MHz, CDCl₃) δ 6.84 (s, 3H), 2.27 (s, 9H). ¹³C NMR (101 MHz, CDCl₃) δ 168.59, 151.09, 112.78, 21.07.



6u

Following the general procedure D (1.0 mmol, Fe(OTf)₃ (10 mol %), IPA (2.5 mL), 24 h, 114.8 mg, 85% yield, a pale yellow solid (m.p.: 114.8-145.7 °C)). ¹H NMR (400 MHz, CDCl₃) δ 7.60 (s, 1H), 7.53 – 7.46 (m, 2H), 7.35 – 7.27 (m, 2H), 7.14 – 7.05 (m,

1H), 2.16 (s, 3H). ¹³C NMR (101 MHz, CDCl₃) δ 168.59, 137.94, 128.97, 124.31, 119.98, 24.55. Compound **6q** is commercially available.



6v

Following the general procedure D (1.0 mmol, Fe(OTf)₃ (10 mol %), IPA (2.5 mL), 24 h, 119.0 mg, 73% yield, a pale yellow solid (m.p.: 49.5-50.5 °C)). ¹H NMR (400 MHz, CDCl₃) δ 7.34 – 7.28 (m, 2H), 7.27 – 7.22 (m, 1H), 7.21 – 7.17 (m, 2H), 5.66 (s, 1H), 3.51 (td, *J* = 7.0, 5.7 Hz, 2H), 2.81 (t, *J* = 7.0 Hz, 2H), 1.93 (s, 3H). ¹³C NMR (101 MHz, CDCl₃) δ 170.15, 138.89, 128.74, 128.64, 126.52, 40.69, 35.63, 23.30. Compound **6r** is commercially available.



6w

Following the general procedure D (1.0 mmol, Fe(OTf)₃ (10 mol %), IPA (2.5 mL), 24 h, 82.0 mg, 55% yield, a pale yellow solid (m.p.: 99.3-100.2 °C)). ¹H NMR (400 MHz, CDCl₃) δ 7.46 – 7.39 (m, 2H), 7.37 – 7.30 (m, 1H), 7.23 – 7.16 (m, 2H), 3.27 (s, 3H), 1.87 (s, 3H). ¹³C NMR (101 MHz, CDCl₃) δ 170.58, 144.62, 129.73, 127.71, 127.08, 37.17, 22.42. Compound **6s** is commercially available.

Following the general procedure D (1.0 mmol, Fe(OTf)₃ (10 mol %), IPA (2.5 mL), 24 h, 151.0 mg, 74% yield, a yellow solid (m.p.: 94.1-94.9 °C)). ¹H NMR (400 MHz, CDCl₃) δ 7.33 – 7.25 (m, 2H), 6.97 – 6.88 (m, 3H), 3.77 (t, *J* = 5.2 Hz, 2H), 3.61 (t, *J* = 5.2 Hz, 2H), 3.16 (dt, *J* = 13.1, 5.3 Hz, 4H), 2.14 (s, 3H). ¹³C NMR (101 MHz, CDCl₃) δ 169.02, 150.92, 129.25, 120.56, 116.67, 49.70, 49.37, 46.23, 41.35, 21.36. Compound **6t** is commercially available.

Sequential protection of COOH and OH in a one-pot reaction



Fe(OTf)₃ (0.05 mmol, 10 mol%), lithocholic acid **7** (0.5 mmol, 1.0 equiv.), and MTBE (1 mL) were added into the Schlenk tube with a stirring bar. The reaction mixture was heated for 5 hours, and then cooled to room temperature. After remove the solvent under vacuum, IPA (1 mL) were added into the Schlenk tube. The reaction mixture was stirred at room temperature for 30 minutes. The mixture was filtered by a short silica gel column, which was washed by EA (30 mL). The solvent was removed by rotary evaporation under vacuum and the residue was chromatographed on silica gel to give the product **8** (164.4 mg, 76% yield, a white solid (m.p.: 126.5-126.9 °C)).



¹H NMR (400 MHz, CDCl₃) δ 4.71 (td, J = 11.3, 5.6 Hz, 1H), 3.66 (s, 3H), 2.41 – 2.30 (m, 1H), 2.27 – 2.17 (m, 1H), 2.03 (s, 3H), 1.99 – 1.93 (m, 1H), 1.91 – 1.75 (m, 5H), 1.72 – 1.65 (m, 1H), 1.61 – 1.50 (m, 2H), 1.49 – 1.21 (m, 11H), 1.19 – 0.98 (m, 6H), 0.96 – 0.88 (m, 6H), 0.64 (s, 3H). ¹³C NMR (101 MHz, CDCl₃) δ 174.75, 170.64, 74.38, 56.49, 55.98, 51.48, 42.72, 41.88, 40.40, 40.13, 35.77, 35.36, 35.03, 34.57, 32.23, 31.04, 30.99, 28.19, 27.01, 26.62, 26.32, 24.18, 23.34, 21.48, 20.83, 18.27, 12.03.



Fe(OTf)₃ (0.05 mmol, 10 mol%), deoxycholic acid **9** (0.5 mmol, 1.0 equiv.), and MTBE (1 mL) were added into the Schlenk tube with a stirring bar. The reaction mixture was heated for 5 hours, and then cooled to room temperature. After remove the solvent under vacuum, IPA (1 mL) were added into the Schlenk tube. The reaction mixture was stirred at room temperature for 30 minutes. The mixture was filtered by a short silica gel column, which was washed by EA (30 mL). The solvent was removed by rotary evaporation under vacuum and the residue was chromatographed on silica gel to give the product **10** (168.7 mg, 69% yield, a clear oil).



¹H NMR (400 MHz, CDCl₃) δ 5.11 – 5.05 (m, 1H), 4.76 – 4.64 (m, 1H), 3.66 (s, 3H), 2.39 – 2.28 (m, 1H), 2.25 – 2.15 (m, 1H), 2.10 (s, 3H), 2.03 (s, 3H), 1.93 – 1.76 (m, 4H), 1.74 – 1.53 (m, 8H), 1.51 – 1.23 (m, 9H), 1.22 – 1.01 (m, 3H), 0.91 (s, 3H), 0.81 (d, *J* = 6.4 Hz, 3H), 0.73 (s, 3H). ¹³C NMR (101 MHz, CDCl₃) δ 174.56, 170.53, 170.44, 75.88, 74.17, 51.48, 49.43, 47.56, 44.99, 41.81, 35.66, 34.71, 34.69, 34.38, 34.02, 32.24, 30.95, 30.82, 27.33, 26.87, 26.61, 25.85, 25.63, 23.42, 23.06, 21.44, 21.35, 17.49, 12.39. HRMS (ESI) m/z calcd. for (C₂₉H₄₆O₆Na) [M+Na]⁺: 513.3187, found: 513.3185.

Mechanistic study



Fe(OTf)₃ (0.1 mmol, 10 mol%), benzoic acid (1.0 mmol, 1.0 equiv.), and MTBE (2.5 mL) were added into the Schlenk tube with a stirring bar, and then the reaction mixture was heated at 90 °C for 1 hour. The mixture was filtered by a short silica gel column, which was washed by EA (30 mL). After added the 1,4-dimethoxybenzene into the solvent as the internal standard, the yield of product **3a** could be detected by GC-MS. Isobutene (MS (Ion trap, EI): m/z (%) = 56.07 [M⁺] (100.00)) and H₂O (MS (Ion trap, EI): m/z (%) = 18.07 [M⁺] (100.00)) could be detected by GC-MS.



Fe(OTf)₃ (0.1 mmol, 10 mol%), phenol (1.0 mmol, 1.0 equiv.) and IPA (2.5 mL) were added into the Schlenk tube with a stirring bar, and then the reaction mixture was stirred at room temperature for 10 minutes. The reaction mixture was stirred at room temperature for 10 minutes. The mixture was filtered by a short silica gel column, which was washed by EA (30 mL). After added the 1,4-dimethoxybenzene into the solvent as the internal standard, the yield of product **3a** could be detected by GC-MS. Acetone (MS (Ion trap, EI): m/z (%) = 58.04 [M⁺] (100.00)) could be detected by GC-MS.

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NMR spectra

















- 3.989





- 52.830



200 190 180 170 160 150 140 130 120 110 100 90 80 f1 (ppm) 0 -





















































-3.672 3.672 2.355 2.349 2.332 2.332 2.332 1.666 1.666









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2.046 2.042 2.011 1.926 1.717 1.717 1.714 1.714 1.710 1.677 -- 3.649









10 200 190 180 170





160 150 140 130 120 110 100 90 f1 (ppm) 0 -80 70 60 50 40 30 20 10

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- 2.246



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- 20.977





6d





- 2.340











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6h











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6.335 6.434 6.444 6.5446 6.446 6.1470 6.1470 6.1470 6.1470 6.1470 6.1470 6.144 7.284 4.284 4.284 4.284 4.284 4.284 4.284 4.284 4.284 4.120 6.1014 1.466 7.1016 7.10



























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74.380 76.387 65.438 65.438 65.438 65.438 65.438 65.438 65.438 65.438 65.438 65.438 65.438 65.438 65.438 65.438 65.438 65.438 73.537 73.534 73.533 73.0393 73.0393 73.0393 73.0393 73.0393 73.0393 73.03093 73.03093 73.03093 73.03093 73.03093 72.0419 72.0419 72.0419 72.0419 72.0419 72.0419 72.0419 72.0410 72.0410 72.0411 72.0411 72.0411 72.0411 72.0411 72.0411



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6.088 6.088 6.078 8.6078 8.6078 8.6078 8.6178 8.6173 8.6111 8.6273 8.6273 8.6474</





76.875 74.173 74.173 74.173 74.173 74.173 74.173 74.173 74.173 74.173 74.173 73.173 73.173 73.21416 73.21416 73.21416 73.21416 73.21416 73.21416 73.21416 73.21416 73.21416 73.21416 73.21416 72.1352 71.5174777 71.5174777777777777777777777







 $10 \hspace{0.2cm} 200 \hspace{0.2cm} 190 \hspace{0.2cm} 180 \hspace{0.2cm} 170 \hspace{0.2cm} 160 \hspace{0.2cm} 150 \hspace{0.2cm} 140 \hspace{0.2cm} 130 \hspace{0.2cm} 120 \hspace{0.2cm} 110 \hspace{0.2cm} 100 \hspace{0.2cm} 90 \hspace{0.2cm} 80 \hspace{0.2cm} 70 \hspace{0.2cm} 60 \hspace{0.2cm} 50 \hspace{0.2cm} 40 \hspace{0.2cm} 30 \hspace{0.2cm} 20 \hspace{0.2cm} 10 \hspace{0.2cm} 0 \hspace{0.2cm} - \hspace{0cm} 0 \hspace{0.2cm} - \hspace{0.2cm} 0 \hspace{0.2cm} - \hspace{0cm} 0 \hspace{0.2cm} - \hspace{0cm} 0 \hspace{0.2cm} - \hspace{0.2cm} 0 \hspace{0.2cm} 0 \hspace{0.2cm} 0 \hspace{0.2cm} - \hspace{0.2cm} 0 \hspace{0$