

Supplementary File 3

Model Assumptions and Constraints

1. Cell metabolism reached isotopic pseudo-steady state under cell growth phase and 3HB production phase. This assumption is supported by our observations that ^{13}C -enrichment of proteinogenic amino acids are consistent in these two phases.
2. In our model, CO_2 exchange reaction with atmospheric $^{12}\text{CO}_2$ was not included since we use screwed flasks to prevent unlabeled atmospheric CO_2 diluting the tracer system. Supply of substrates ($\text{NaH}^{13}\text{CO}_3$ and glucose) is sufficient in both cell growth and 3HB production phases.
3. Our previous research¹ demonstrates that addition of ^{13}C -glutamate to the *Synechocystis* culture in the light leads to the labeling of succinate but not fumarate, suggesting a very low activity of succinate dehydrogenase under our experimental conditions. Therefore, we introduce the following constraint for succinate dehydrogenase reaction:

$$V_{(\text{SUC} \rightarrow \text{FUM})} = 0$$

4. You et al.² reported that feeding glyoxylate into the *Synechocystis* culture resulted in altered labeling pattern in glycine, but had little effects on serine and other proteinogenic amino acids. Accordingly, we set:

$$V_{(\text{GOX} + \text{GOX} \rightarrow \text{GA} + \text{CO}_2)} = 0$$

Reactions and Carbon Transitions for ^{13}C -MFA

1. Glucose (abcdef) \rightarrow G6P (abcdef)
2. G6P (abcdef) \leftrightarrow F6P (abcdef)
3. F6P (abcdef) \leftrightarrow FBP (abcdef)
4. FBP (abcdef) \leftrightarrow DHAP (cba) + GAP (def)
5. DHAP (abc) \leftrightarrow GAP (abc)
6. GAP (abc) \leftrightarrow 3PGA (abc)
7. 3PGA (abc) \leftrightarrow 2PGA (abc)
8. 2PGA (abc) \leftrightarrow PEP (abc)
9. PEP (abc) \leftrightarrow PYR (abc)
10. PYR (abc) \rightarrow ACA (bc) + CO_2 (a)
11. $2.47 \cdot \text{ACA}(\text{ab}) + 1.47 \cdot \text{ACA}(\text{cd}) \rightarrow \text{AC}(\text{ab}) + 0.735 \cdot 3\text{HB}(\text{abcd}) + 0.735 \cdot 3\text{HB}(\text{cdab})$
12. OAA (abcd) + ACA (ef) \rightarrow CIT (dcbfea)
13. CIT (abcdef) \leftrightarrow ICI (abcdef)
14. ICI (abcdef) \leftrightarrow AKG (abcde) + CO_2 (f)
15. AKG (abcde) \rightarrow SUC (bcde) + CO_2 (a)
16. SUC (abcd) \leftrightarrow FUM (abcd)
17. FUM (abcd) \leftrightarrow MAL (abcd)
18. MAL (abcd) \leftrightarrow OAA (abcd)

19. MAL (abcd) → PYR (abc) + CO₂ (d)
20. PEP (abc) + CO₂ (d) → OAA (abcd)
21. G6P (abcdef) → RU5P (bcdef) + CO₂ (a)
22. RU5P (abcde) → RUBP (abcde)
23. RUBP (abcde) + CO₂ (f) → 3PGA (cde) + 3PGA (fba)
24. RU5P (abcde) ↔ X5P (abcde)
25. RU5P (abcde) ↔ R5P (abcde)
26. X5P (abcde) ↔ GAP (cde) + EC₂ (ab)
27. F6P (abcdef) ↔ E4P (cdef) + EC₂ (ab)
28. X5P (abcde) → GAP (cde) + ACA (ab)
29. F6P (abcdef) → E4P (cdef) + ACA (ab)
30. S7P (abcdefg) ↔ R5P (cdefg) + EC₂ (ab)
31. F6P (abcdef) ↔ GAP (def) + EC₃ (abc)
32. S7P (abcdefg) ↔ E4P (defg) + EC₃ (abc)
33. DHAP (cba) + E4P (defg) → SBP (abcdefg)
34. SBP (abcdefg) → S7P (abcdefg)
35. RUBP (abcde) → 3PGA (cde) + 2PG (ba)
36. 2PG (ab) → GLC (ab)
37. GLC (ab) → GOX (ab)
38. GOX (ab) + GOX (cd) → GA (abd) + CO₂ (c)
39. GA (abc) ↔ 2PGA (abc)
40. AKG (abdce) → GLU (abcde)
41. GLU (abdce) → GLN (abcde)
42. GLU (abcde) → PRO (abcde)
43. GLU (abdce) + CO₂ (f) + GLN (ghijk) + ASP (lmno) → ARG (abcdef) + AKG (ghijk) + FUM (lmno)
44. OAA (abcd) + GLU (efghi) → ASP (abcd) + AKG (efghi)
45. ASP (abcd) → ASN (abcd)
46. PYR (abc) + GLU (defgh) → ALA (abc) + AKG (defgh)
47. 3PGA (abc) + GLU (defgh) → SER (abc) + AKG (defgh)
48. SER (abc) → GLY (ab) + MTHF (c)
49. GLY (ab) → MTHF (b) + CO₂ (a)
50. GOX (ab) → GLY (ab)
51. SER (abc) → CYS (abc)
52. ASP (abcd) → THR (abcd)
53. ASP (abcd) + PYR (efg) + GLU (hijkl) → 0.5*LYS (bcdgfe) + 0.5*LYS (fgdcba) + 0.5*CO₂ (a) + 0.5*CO₂ (e) + AKG (hijkl)
54. ASP (abcd) + MTHF (e) + CYS (fgh) → MET (abcde) + PYR (fgh)
55. PYR (abc) + PYR (def) + GLU (ghijk) → VAL (abefc) + AKG (ghijk) + CO₂ (d)
56. ACA (ab) + PYR (cde) + PYR (fgh) + GLU (ijklm) → LEU (abdghe) + AKG (ijklm) + CO₂ (c) + CO₂ (f)
57. THR (abcd) + PYR (efg) + GLU (hijkl) → ILE (abfcdg) + AKG (hijkl) + CO₂ (e)
58. PEP (abc) + PEP (def) + E4P (ghij) + GLU (klmno) → PHE (abcefg hij) + AKG (klmno) + CO₂ (d)
59. PEP (abc) + PEP (def) + E4P (ghij) + GLU (klmno) → TYR (abcefg hij) + AKG (klmno) + CO₂ (d)

60. SER (abc) + R5P (defgh) + PEP (ijk) + PEP (lmn) + E4P (opqr) + GLN (stuvw) -> TRP (abcdkopqrij) + GAP (fgh) + PYR (lmn) + GLU (stuvw) + CO2 (i)
61. R5P (abcde) + MTHF (f) + GLN (ghijk) + ASP (lmno) -> HIS (edcbaf) + AKG (ghijk) + FUM (lmno)
62. 0.284*G6P + 0.495*R5P + 0.046*GAP + 0.173*DHAP + 0.046*PYR + 3.707*ACA + 0.366*MTHF + 0.53*GLY + 0.158*PRO + 0.387*ALA + 0.201*VAL + 0.31*LEU + 0.171*ILE + 0.048*MET + 0.03*CYS + 0.087*PHE + 0.058*TYR + 0.027*TRP + 0.043*HIS + 0.105*LYS + 0.104*ARG + 0.136*GLN + 0.11*ASN + 0.2*GLU + 0.657*ASP (abcd) + 0.199*SER + 0.165*THR -> Biomass + 0.210*FUM (abcd)

***Notes:** 1. Reaction 11 is used for 3HB production. TesB uses both Acetyl CoA and 3-hydroxybutyryl CoA as the substrates and produces acetate and 3HB, respectively. We lumped the two reactions for simplicity. The stoichiometry for acetate and 3HB production is based on experimental measurements, which is 1:1.47. 2. Reaction 62 is biomass formation based on a previous report³ and adopted for ¹³C-MFA².

****Abbreviations:** 2PGA, 2-phosphoglyceric acid; 2PG, 2-phosphoglycolate; 3HB, 3-hydroxybutyrate; 3PGA, 3-phosphoglyceric acid; AC, acetate; ACA, acetyl-CoA; AKG, α -ketoglutarate; ALA, alanine; ARG, arginine; ASN, asparagine; CIT, citrate; CYS, cysteine; DHAP, dihydroxyacetone phosphate; E4P, erythrose 4-phosphate; F6P, fructose 6-phosphate; FBP, fructose-1,6-bisphosphate; FUM, fumarate; G6P, glucose 6-phosphate; GA, glycerate; GAP, glyceraldehyde 3-phosphate; GLC, glycolate; GLN, glutamine; GLX, glyoxylate; GLY, glycine; GLU, glutamate; HIS, histidine; ICI, isocitrate; ILE, isoleucine; LEU, leucine; MAL, malate; MTHF, 5,10-Methylenetetrahydrofolate (5,10-CH₂-THF); OAA, oxaloacetate; PEP, phosphoenolpyruvate; PHE, phenylalanine; PRO, proline; PYR, pyruvate; R5P, ribose 5-phosphate; Ru5P, ribulose-5-phosphate; RuBP, ribulose-1,5-diphosphate; S7P, sedoheptulose-7-phosphate; SBP, sedoheptulose-1,7-bisphosphate; SER, serine; SUC, succinate; SucCoA, succinyl-CoA; THR, threonine; TRP, tryptophan; VAL, valine; X5P, xylulose-5-phosphate.

References:

1. W. Xiong, D. Brune and W. F. J. Vermaas, *Molecular Microbiology*, 2014, **93**, 786-796.
2. L. You, B. Berla, L. He, H. B. Pakrasi and Y. J. Tang, *Biotechnology Journal*, 2014, **9**, 684-692.
3. R. Saha, A. T. Verseput, B. M. Berla, T. J. Mueller, H. B. Pakrasi and C. D. Maranas, *PLoS One*, 2012, **7**, e48285.