Supplementary Information for

## Valley-selective circular dichroism and high carrier mobility of graphene-like BC<sub>6</sub>N

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Figure S1. Phonon spectrum of g-BC<sub>6</sub>N monolayer calculated from first-principles



**Figure S2**. Electronic band structure of g-BC<sub>6</sub>N monolayer calculated by using DFT-PBE. The energy at the Fermi level is set to zero. The direct band gap at the K point is about 1.276 eV, which is smaller than that (1.833 eV) obtained from the HSE06 functional.



(a) AB-I



(b)AB-II

**Figure S3.** Two stable staking patterns of g-BC<sub>6</sub>N bilayer. (a) AB-I, (b) AB-II. The two patterns are almost energetically degenerate with AB-I slightly stable than AB-II by about  $0.58 \times 10^{-4}$  eV/atom. The interlayer distance is about 3.50Å. The VDW interaction energy between the two layers is about 16.4 meV/Å<sup>2</sup>.



**Figure S4.** Electronic band structure of g-BC<sub>6</sub>N bilayers calculated by using DFT-PBE. The energy at the Fermi level is set to zero. The direct band gap at the K point are about 1.251 eV for AB-I and 1.202 eV for AB-II, both of which are smaller than that (1.276 eV) for monolayer obtained by using the same strategy.



**Figure S5.** The electronic band lines of g-B<sub>3</sub>C obtained at the DFT-PBE level (solid lines) and TB model (dotted lines). The parameters employed in the TB models are  $t_1$ =-3.2 eV,  $t_2$ = $t_3$ =-2.0 eV,  $\varepsilon_1$ =  $\varepsilon_2$ = 2.35 eV. The onsite energy of carbon atom is set to zero.



**Figure S6.** The electronic band lines of g-C<sub>3</sub>N obtained at the DFT-PBE level (solid lines) and TB model (dotted lines). The parameters employed in the TB models are  $t_1$ =-3.2 eV,  $t_2$ = $t_3$ =-2.0 eV,  $\varepsilon_1$ = $\varepsilon_2$ = -2.35 eV. The onsite energy of carbon atom is set to zero.