

Supplementary Information

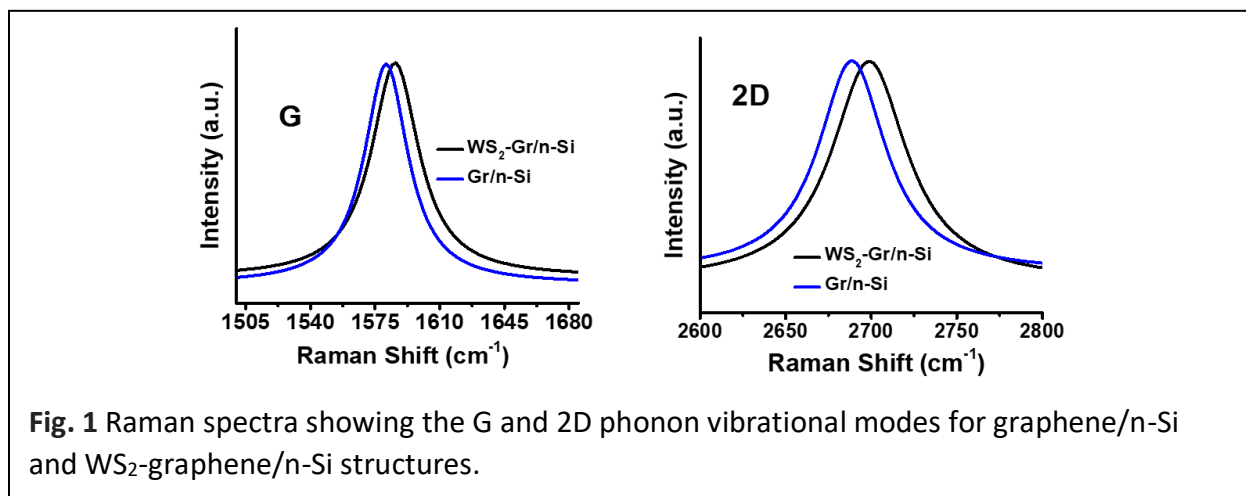
WS₂-Induced Enhanced Optical Absorption and Efficiency in Graphene/Silicon Heterojunction Photovoltaic Cells

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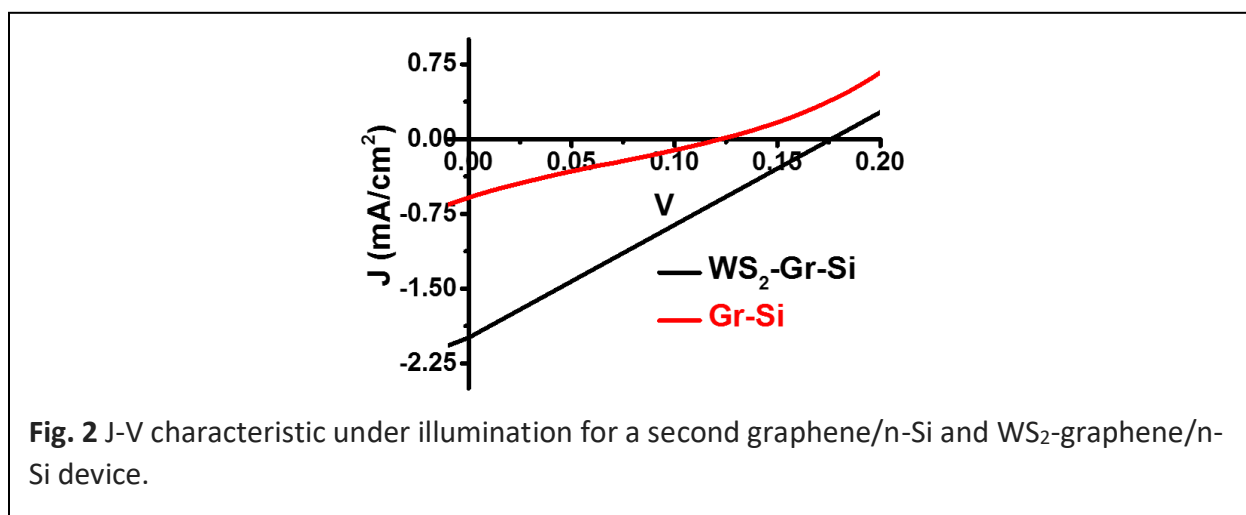
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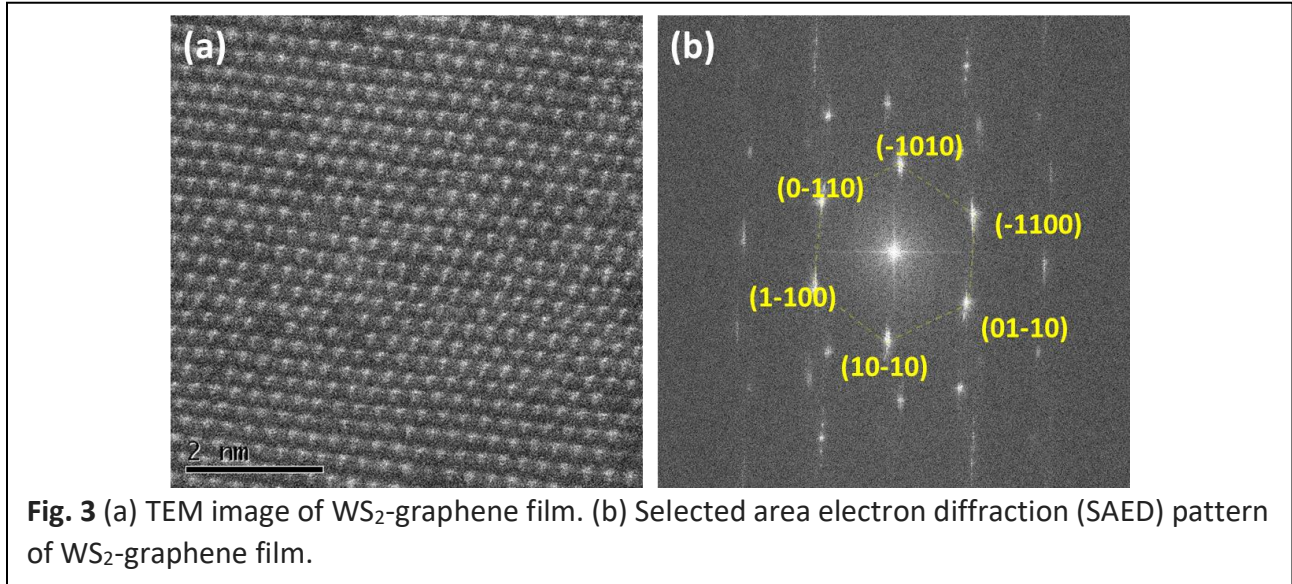
1. Raman spectra showing the G and 2D bands for graphene on n-Si with and without WS₂.



2. Current density vs. voltage (J-V) characteristic under illumination for a second graphene/n-Si and WS₂-graphene/n-Si device.



3. Transmission Electron Microscopy Characterization for WS₂-Graphene Film.



4. Doping Levels of Graphene in WS₂-Graphene/n-Si Heterostructure.

The doping level for the graphene sheet has been calculated from the shift in the graphene G peak position. The upshifts in the peak positions of both the G and 2D peak positions point to the electron (n) doping of the underlying graphene after the deposition of WS₂ layers *via* chemical vapor deposition.¹ The table below shows the peak positions (also shown in the Raman spectra in the above Figure 1).

	Graphene/n-Si	WS ₂ -Graphene/n-Si
G peak position (cm ⁻¹)	1581	1586
2D peak position (cm ⁻¹)	2688	2699

At room temperature (298 K) the G peak position for undoped graphene is 1579 cm⁻¹.² The total shift in the G peak position can be modelled as:

$$\Delta\omega = \Delta\omega_A + \Delta\omega_{NA}$$

where $\Delta\omega_A$ and $\Delta\omega_{NA}$ represent shifts due to adiabatic and non-adiabatic contributions.³ The adiabatic contribution⁴ is given by the formula:

$$\Delta\omega_A = -2.13n - 0.036n^2 - 0.00329n^3 - 0.226|n|^{3/2}$$

where $\Delta\omega_A$ is the shift in cm⁻¹ and n is the charge carrier concentration in graphene (10¹³ cm⁻²). The non-adiabatic contribution is given by:

$$\Delta\omega_{NA} = \frac{2\pi\alpha P}{h} \int_{-\infty}^{\infty} \frac{[f(E - E_F) - f(E)]E^2 \text{sgn}(E)}{E^2 - \left(\frac{h\omega_0}{4\pi}\right)^2} dE$$

where $\Delta\omega_{NA}$ is the shift in cm^{-1} , $\alpha=4.39 \times 10^{-3}$ is a constant, P is the principal part, h is the Planck constant, f is the Fermi-Dirac distribution, E_F is the Fermi energy, and ω_0 is the G mode frequency of the undoped graphene.⁵ For $|E_F| < 1 \text{ eV}$ the adiabatic contribution to the total peak shift can be ignored:

$$\Delta\omega \approx \Delta\omega_{NA}$$

The non-adiabatic shift exhibits asymptotic behavior when $|E_F| \gg h\omega_0/4\pi$ and the total shift exhibits a linear relationship with the Fermi energy. For $E_F \geq 100 \text{ meV}$ (electron doping), the linear relationship between the G peak shift and the Fermi energy is given by:

$$E_F = 21\Delta\omega + 75$$

where E_F is in meV and $\Delta\omega$ is in cm^{-1} . The Fermi energy can be further related to the carrier concentration by the formula:

$$E_F = \frac{\text{sgn}(n)\sqrt{n\pi}h v_F}{2\pi}$$

where n is the carrier concentration and v_F is the Fermi velocity ($v_F = 1.1 \times 10^6 \text{ m/s}$). The calculated Fermi energy and doping levels are shown in the table below.

	Graphene/n-Si	WS ₂ -Graphene/n-Si
$\Delta\omega (\text{cm}^{-1})$	2	7
$E_F (\text{meV})$	117	222
$n (\text{cm}^{-2})$	8.28×10^{11}	2.98×10^{12}

The doping levels of the graphene exhibited an increase of 260% on the deposition of WS₂ layers.

References

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