## **Supporting Information**

## Structure Evolution of Chromium-Doped Boron Clusters: Toward the Formation of Endohedral Boron Cages

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Fig. S1. Structures of low-lying isomers of  $CrB_8$ . Bottom labels are point-group symmetries, spin multiplicities and relative energies to the ground state at PBE0/Cr/Stuttgart/B/6-311G\* level of theory. Zero-point energy corrections were included for all isomers at the same level of theory.



**Fig. S2.** Structures of low-lying isomers of  $CrB_{10}$ . Bottom labels are point-group symmetries, spin multiplicities and relative energies to the ground state at PBE0/Cr/Stuttgart/B/6-311G\* level of theory. Zero-point energy corrections were included for all isomers at the same level of theory.



**Fig. S3.** Structures of low-lying isomers of  $CrB_{12}$ . Bottom labels are point-group symmetries, spin multiplicities and relative energies to the ground state at PBE0/Cr/Stuttgart/B/6-311G\* level of theory. Zero-point energy corrections were included for all isomers at the same level of theory.



**Fig. S4.** Structures of low-lying isomers of  $CrB_{14}$ . Bottom labels are point-group symmetries, spin multiplicities and relative energies to the ground state at PBE0/Cr/Stuttgart/B/6-311G\* level of theory. Zero-point energy corrections were included for all isomers at the same level of theory.



**Fig. S5.** Structures of low-lying isomers of  $CrB_{16}$ . Bottom labels are point-group symmetries, spin multiplicities and relative energies to the ground state at PBE0/Cr/Stuttgart/B/6-311G\* level of theory. Zero-point energy corrections were included for all isomers at the same level of theory.



**Fig. S6.** Structures of low-lying isomers of  $CrB_{18}$ . Bottom labels are point-group symmetries, spin multiplicities and relative energies to the ground state at PBE0/Cr/Stuttgart/B/6-311G\* level of theory. Zero-point energy corrections were included for all isomers at the same level of theory.



**Fig. S7.** Structures of low-lying isomers of  $CrB_{20}$ . Bottom labels are point-group symmetries, spin multiplicities and relative energies to the ground state at PBE0/Cr/Stuttgart/B/6-311G\* level of theory. Zero-point energy corrections were included for all isomers at the same level of theory.



**Fig. S8.** Structures of low-lying isomers of  $CrB_{22}$ . Bottom labels are point-group symmetries, spin multiplicities and relative energies to the ground state at PBE0/Cr/Stuttgart/B/6-311G\* level of theory. Zero-point energy corrections were included for all isomers at the same level of theory.



**Fig. S9.** Electron spin density of  $CrB_{12}$ ,  $CrB_{14}$  and  $CrB_{16}$  shows that with the addition of boron atoms, the magnetism of Chromium is vanished. The mul represent the charge spin multiplicity.



**Fig. S10.** The chemical bonding picture of  $CrB_{16}$  obtained from AdNDP analyses. ON stands for occupation number. Residual valence electrons of all atoms in the search list: 5.17.



Fig. S11. Total and projected density of states for the double-ring tubular  $CrB_{16}$  cluster. The dashed line highlights the position of HOMO.



**Fig. S12.** Total and projected density of states for the endohedral cage-like  $CrB_{20}$  cluster. The dashed line highlights the position of HOMO.

Table S1. Cartesian coordinates of the lowest-energy structure of  $CrB_8$ 

Cr	7.455200	7.685000	8.303500
В	6.400700	6.288800	6.501800
В	9.099400	8.465000	6.572800
В	9.107500	6.921800	6.573000
В	6.386100	9.069500	6.501500
В	7.512100	7.685000	6.136500
В	7.888300	9.420800	6.541000
В	7.906500	5.953300	6.541400
В	5.724000	7.675600	6.484000

Table S2. Cartesian coordinates of the lowest-energy structure of  $CrB_{10}$ 

Cr	8.645702	7.211105	9.087777
В	6.864284	5.502427	8.372888
В	9.020988	6.792001	6.580219
В	6.223682	8.009082	9.405405
В	7.034672	8.899758	8.364290
В	6.140807	6.438990	9.408009
В	8.380391	9.298630	7.612701
В	6.573325	7.140929	7.972259
В	9.297176	8.326311	6.784362
В	7.732423	7.833989	7.008769
В	7.780659	5.980770	7.161953

Table S3. Cartesian coordinates of the lowest-energy structure of  $CrB_{12}$ 

Cr	7.408980	12.00170	8.925550
В	9.988865	11.74960	8.455016
В	6.096917	13.38786	7.367074
В	6.357480	10.60534	6.954414
В	5.577452	11.92594	7.033333
В	8.845510	11.98716	7.179896
В	7.263334	12.05038	6.669873
В	9.479504	13.25263	8.456912
В	8.000589	13.41764	7.265269
В	7.903353	10.32969	7.184238
В	8.413115	14.41734	8.614398
В	6.952396	14.47569	8.143725
В	9.308192	10.48736	7.905393

Table S4. Cartesian coordinates of the lowest-energy structure of  $CrB_{14}$ 

Cr	8.128003	9.281546	9.685618
В	7.890778	10.49034	7.634534
В	7.618474	11.34589	8.887793
В	9.237603	7.786292	8.152818
В	10.11191	9.055685	8.813913
В	9.305986	10.67073	8.418975
В	7.896232	10.49345	11.73542
В	7.620565	11.34703	10.48153
В	9.241713	7.788647	11.21756
В	10.11438	9.056974	10.55232
В	9.309338	10.67265	10.94699
В	8.751063	9.127525	7.529478
В	8.756863	9.130798	11.84024
В	9.560383	7.535482	9.684950
В	10.28896	10.43102	9.681860

Table S5. Cartesian coordinates of the lowest-energy structure of  $CrB_{16}$ 

Cr	9.624430	9.754655	9.617720
В	8.821323	8.619560	11.23690
В	10.45231	8.033580	10.94501
В	10.00375	9.545160	11.77099
В	8.919185	9.365770	7.598717
В	10.41296	11.815044	10.07717
В	7.805689	8.478948	9.995451
В	11.42911	9.306202	10.74312
В	9.307754	11.74265	8.908493
В	9.316485	7.518392	9.953526
В	10.80018	10.86572	11.30281
В	9.742898	10.75500	7.521438
В	7.520514	9.350567	8.686934
В	11.60741	10.54971	9.771393
В	8.164130	10.78749	8.342902
В	8.759641	8.108065	8.555354
В	10.934278	11.22797	8.467739

Table S6. Cartesian coordinates of the lowest-energy structure of  $CrB_{18}$ 

Cr	9.484292	9.598221	9.596623
В	8.976945	10.45209	7.577232
В	8.521071	9.643048	11.75060
В	9.730086	11.54307	8.491449
В	7.573799	10.27316	8.942234
В	8.074629	9.163772	7.808622
В	8.921591	7.755554	8.350101
В	9.767626	8.876038	7.511701
В	10.74662	10.07216	7.990947
В	9.447378	8.251537	11.23415
В	10.24903	9.594576	11.67276
В	10.99756	10.76240	10.86963
В	9.232151	11.02627	11.29130
В	8.329586	11.36782	9.859221
В	7.770250	8.555643	10.83934
В	11.20853	10.96310	9.260464
В	9.916308	11.83123	10.04379
В	7.537472	8.571655	9.234528
В	8.814145	7.516334	9.931367

Table S7. Cartesian coordinates of the lowest-energy structure of  $CrB_{20}$ 

Cr	9.584947	9.635535	9.630617
В	9.753406	9.785738	11.81456
В	8.983707	9.789686	7.524600
В	7.520008	9.070878	10.15126
В	8.580328	7.691453	9.809075
В	9.959386	7.519548	8.889377
В	11.82478	9.913027	9.901116
В	11.02234	11.27526	9.374230
В	9.342607	11.82279	9.525436
В	10.36000	8.703804	7.790768
В	11.32468	9.941580	8.313984
В	10.03502	11.13862	8.094803
В	8.391316	11.10006	8.366722
В	7.637407	9.634861	8.600584
В	8.708270	8.306085	8.119140
В	10.89440	10.66063	11.06416
В	9.225208	11.25880	11.07611
В	8.164302	10.00949	11.36525
В	8.702090	8.436803	11.24436
В	10.15248	7.706890	10.53178
В	11.11716	8.944666	11.05500

Table S8. Cartesian coordinates of the lowest-energy structure of  $CrB_{22}$ 

Cr	9.633957	9.811267	9.887219
В	11.00359	10.00034	7.899784
В	8.709324	10.84326	11.91010
В	8.834966	7.548270	9.876499
В	10.54646	7.571715	9.570152
В	9.913372	11.95653	9.268650
В	8.414387	11.40262	8.865994
В	11.54533	8.549652	10.60443
В	9.504776	9.446677	7.497333
В	7.961305	11.31284	10.53267
В	10.01762	7.896601	11.09237
В	11.75764	9.477294	9.263734
В	7.393579	10.16376	9.518860
В	10.60263	8.418262	8.196409
В	9.524230	11.89029	10.95246
В	10.79828	9.224353	11.84426
В	11.04902	11.51433	10.50062
В	8.360643	8.323800	11.18953
В	11.37080	11.16110	8.982868
В	8.073254	9.942856	8.097206
В	8.724533	8.356861	8.449228
В	10.36217	10.76718	11.93347
В	7.663247	9.770044	11.20857