

Table S1. Band gaps of metal oxide nanoparticles from literature and experiments

Metal oxide	α (°)	β (°)	γ (°)	a (Å)	b (Å)	c (Å)	Size (nm)	E_g (eV) (Exp.)	Reference
Al ₂ O ₃	90	90	120	4.81	4.81	13.12	66.0	5.97	19
Al ₂ O ₃	90	90	120	4.81	4.81	13.12	86.0	5.97	20
CeO ₂	90	90	90	5.46	5.46	5.46	12.0	3.39	21
CeO ₂	90	90	90	5.46	5.46	5.46	3.6	3.68	21
CeO ₂	90	90	90	5.46	5.46	5.46	2.6	3.44	21
Cr ₂ O ₃	90	90	120	4.58	4.58	14.72	35.1	3.78	22
Cr ₂ O ₃	90	90	120	4.58	4.58	14.72	38.1	3.72	22
Cr ₂ O ₃	90	90	120	4.58	4.58	14.72	40.3	3.67	22
Cr ₂ O ₃	90	90	120	4.58	4.58	14.72	25.0	4.33	23
Cr ₂ O ₃	90	90	120	4.58	4.58	14.72	28.0	4.11	23
Cr ₂ O ₃	90	90	120	4.58	4.58	14.72	34.0	3.81	23
Cr ₂ O ₃	90	90	120	4.58	4.58	14.72	35.0	3.78	23
Cr ₂ O ₃	90	90	120	4.58	4.58	14.72	40.0	3.62	23
Cr ₂ O ₃	90	90	120	4.58	4.58	14.72	45.0	3.54	23
Cu ₂ O	90	90	90	4.31	4.31	4.31	4.0	2.90	24
Cu ₂ O	90	90	90	4.31	4.31	4.31	9.0	2.50	24
Cu ₂ O	90	90	90	4.31	4.31	4.31	6.0	2.83	25
Cu ₂ O	90	90	90	4.31	4.31	4.31	20.0	2.04	24
Fe ₂ O ₃	90	90	120	4.74	4.74	13.49	100.0	2.05	26
Fe ₂ O ₃	90	90	120	4.74	4.74	13.49	100.0	2.12	26
Fe ₂ O ₃	90	90	120	4.74	4.74	13.49	100.0	2.46	26
Fe ₂ O ₃	90	90	120	4.74	4.74	13.49	100.0	2.88	26
Fe ₃ O ₄	90	90	90	8.04	8.04	8.04	12.0	1.85	3
Ga ₂ O ₃	90	103.7	90	12.50	3.10	5.92	2.5	5.10	27
Ga ₂ O ₃	90	103.7	90	12.50	3.10	5.92	70.0	4.90	28
Ga ₂ O ₃	90	103.7	90	12.50	3.10	5.92	60.0	4.80	29
HfO ₂	90	99.216	90	5.14	5.19	5.31	17.0	6.07	30
In ₂ O ₃	90	90	90	10.35	10.35	10.35	17.4	3.84	31
In ₂ O ₃	90	90	90	10.35	10.35	10.35	16.6	3.86	31
La ₂ O ₃	90	90	120	3.94	3.94	6.18	20.0	5.77	3
La ₂ O ₃	90	90	120	3.94	3.94	6.18	40.0	4.20	32
MgO	90	90	90	4.25	4.25	4.25	7.0	4.27	33
Mn ₂ O ₃	90	90	90	9.03	9.03	9.03	30.2	3.27	34
NiO	90	90	90	4.16	4.16	4.16	3.5	3.67	35
NiO	90	90	90	4.16	4.16	4.16	4.6	3.63	35
NiO	90	90	90	4.16	4.16	4.16	5.5	3.62	35
NiO	90	90	90	4.16	4.16	4.16	10.1	3.62	35
NiO	90	90	90	4.16	4.16	4.16	12.4	3.61	35
NiO	90	90	90	4.16	4.16	4.16	8.3	3.22	36
NiO	90	90	90	4.16	4.16	4.16	11.6	3.24	36

NiO	90	90	90	4.16	4.16	4.16	18.3	3.34	36
NiO	90	90	90	4.16	4.16	4.16	20.7	3.19	36
NiO	90	90	90	4.16	4.16	4.16	31.0	3.41	36
NiO	90	90	90	4.16	4.16	4.16	43.4	3.21	36
Sb ₂ O ₃	90	90	90	5.18	16.61	5.51	11.8	4.49	3
SnO ₂	90	90	90	4.83	4.83	3.24	4.5	4.20	37
SnO ₂	90	90	90	4.83	4.83	3.24	4.0	4.10	38
SnO ₂	90	90	90	4.83	4.83	3.24	5.0	4.21	39
SnO ₂	90	90	90	4.83	4.83	3.24	5.2	4.20	40
SnO ₂	90	90	90	4.83	4.83	3.24	3.7	4.33	40
SnO ₂	90	90	90	4.83	4.83	3.24	62.4	4.00	3
SnO ₂	90	90	90	4.83	4.83	3.24	12.8	3.40	41
SnO ₂	90	90	90	4.83	4.83	3.24	29.1	3.16	41
SnO ₂	90	90	90	4.83	4.83	3.24	37.0	3.35	40
SnO ₂	90	90	90	4.83	4.83	3.24	8.0	4.26	42
SnO ₂	90	90	90	4.83	4.83	3.24	15.0	4.00	42
SnO ₂	90	90	90	4.83	4.83	3.24	17.0	3.90	42
TiO ₂ -a	90	90	90	3.82	3.82	9.70	5.0	3.18	exp.
TiO ₂ -a	90	90	90	3.82	3.82	9.70	25.0	3.23	exp.
TiO ₂ -a	90	90	90	3.82	3.82	9.70	40.0	3.21	exp.
TiO ₂ -a	90	90	90	3.82	3.82	9.70	12.6	3.33	3
TiO ₂ -a	90	90	90	3.82	3.82	9.70	9.8	3.21	43
TiO ₂ -a	90	90	90	3.82	3.82	9.70	16.0	3.25	43
TiO ₂ -a	90	90	90	3.82	3.82	9.70	3.9	3.26	43
TiO ₂ -a	90	90	90	3.82	3.82	9.70	10.6	3.26	43
TiO ₂ -a	90	90	90	3.82	3.82	9.70	16.9	3.25	43
TiO ₂ -a	90	90	90	3.82	3.82	9.70	9.3	3.25	43
TiO ₂ -a	90	90	90	3.82	3.82	9.70	5.0	3.22	43
TiO ₂ -a	90	90	90	3.82	3.82	9.70	7.9	3.25	43
TiO ₂ -a	90	90	90	3.82	3.82	9.70	9.2	3.28	43
TiO ₂ -a	90	90	90	3.82	3.82	9.70	18.0	3.24	43
TiO ₂ -a	90	90	90	3.82	3.82	9.70	12.3	3.25	43
TiO ₂ -a	90	90	90	3.82	3.82	9.70	7.8	3.24	43
TiO ₂ -a	90	90	90	3.82	3.82	9.70	7.4	3.24	43
TiO ₂ -a	90	90	90	3.82	3.82	9.70	17.0	3.23	43
TiO ₂ -a	90	90	90	3.82	3.82	9.70	12.4	3.25	43
TiO ₂ -a	90	90	90	3.82	3.82	9.70	16.7	3.27	43
TiO ₂ -b	90	90	90	9.28	5.52	5.19	7.9	3.48	44
TiO ₂ -b	90	90	90	9.28	5.52	5.19	18.9	3.11	45
TiO ₂ -r	90	90	90	4.66	4.66	2.97	40.0	3.00	exp.
TiO ₂ -r	90	90	90	4.66	4.66	2.97	100.0	3.00	exp.
WO ₃	90	91.75	90	5.39	5.36	7.84	42.0	2.77	46
Y ₂ O ₃	90	90	90	10.65	10.65	10.65	14.6	5.30	47
ZnO	90	90	120	3.29	3.29	5.31	22.6	3.31	3

ZnO	90	90	120	3.29	3.29	5.31	14.0	3.30	48
ZnO	90	90	120	3.29	3.29	5.31	20.0	3.25	48
ZnO	90	90	120	3.29	3.29	5.31	26.0	3.22	48
ZnO	90	90	120	3.29	3.29	5.31	50.0	3.11	exp.
ZnO	90	90	120	3.29	3.29	5.31	53.4	3.35	49
ZnO	90	90	120	3.29	3.29	5.31	43.4	3.19	50
ZrO ₂	90	99.2	90	5.19	5.24	5.38	40.0	5.04	3

*exp.: Band gaps measured by UV-vis spectroscopic analysis in this study

Number of reference is corresponding to that in text

Table S2. Applicability domain characterization for developed nano-QSPR model

Training Set													
Metal oxide	BETA-standardized	D ² -standardized	H _F -standardized	V ₂ -standardized	E _{Fermi} ⁻ standardized	TFW-standardized	R-standardized	E _T -standardized	DENC-standardized	XCENC-standardized	AVERAGE	STDEV	AVERAGE +1.28STDEV
Al ₂ O ₃	0.3995	0.6402	2.8965	0.2238	0.7241	0.0561	0.0148	0.3893	0.1578	0.0139	0.5516	0.8167	1.5970
CeO ₂ -1	0.3995	0.4826	0.0280	0.0280	0.4048	0.1804	0.8010	0.5736	0.3484	0.4753	0.3722	0.2288	0.6650
CeO ₂ -2	0.3995	1.1771	0.0280	0.0280	0.4048	0.1804	0.8010	0.5736	0.3484	0.4753	0.4416	0.3333	0.8682
CeO ₂ -3	0.3995	2.8498	0.0280	0.0280	0.4048	0.1804	0.8010	0.5736	0.3484	0.4753	0.6089	0.7804	1.6077
Cr ₂ O ₃ -1	0.3995	0.6131	0.8364	0.3126	0.8111	0.6370	0.0148	1.3924	0.2193	0.1786	0.5415	0.3852	1.0345
Cu ₂ O-1	0.3995	0.8305	1.0666	0.4156	0.0039	0.7675	0.8010	1.9253	3.4123	1.4792	1.1101	0.9276	2.2975
Fe ₃ O ₄ -1	0.3995	0.4826	0.2296	1.0201	0.4074	0.9465	0.4203	3.7281	2.1972	1.6076	1.1439	1.0464	2.4834
Ga ₂ O ₃ -1	3.0522	0.6412	0.4689	0.8796	1.2124	0.8372	0.0148	0.3459	0.1090	0.2095	0.7771	0.8384	1.8502
Ga ₂ O ₃ -2	3.0522	3.1351	0.4689	0.8796	1.2124	0.8372	0.0148	0.3459	0.1090	0.2095	1.0265	1.0931	2.4256
HfO ₂ -1	1.9225	0.6462	1.8193	0.0755	0.3906	0.6409	0.8010	0.4266	0.7110	0.5899	0.8024	0.5685	1.5300
In ₂ O ₃ -1	0.3995	0.5650	0.4947	1.9048	0.5893	1.5153	0.0148	0.3224	0.4003	1.1509	0.7357	0.5632	1.4566
La ₂ O ₃ -1	0.3995	0.6205	0.9077	0.5582	0.7149	0.4778	0.0148	0.2401	0.8432	2.0528	0.6830	0.5233	1.3527
MgO-1	0.3995	0.1644	0.0202	0.4393	0.5084	0.9339	1.6417	1.3465	1.4933	1.0546	0.8002	0.5439	1.4963
Mn ₂ O ₃ -1	0.3995	0.6209	0.0129	1.3995	0.5045	0.7409	0.0148	1.1922	0.3090	0.4396	0.5634	0.4294	1.1130
NiO-1	0.3995	1.2828	1.0837	0.4727	1.5137	1.6062	1.6417	0.4772	0.4885	0.3975	0.9363	0.5125	1.5923
NiO-2	0.3995	0.4703	1.0837	0.4727	1.5137	1.6062	1.6417	0.4772	0.4885	0.3975	0.8551	0.5155	1.5149
NiO-4	0.3995	0.4151	1.0837	0.4727	1.5137	1.6062	1.6417	0.4772	0.4885	0.3975	0.8496	0.5199	1.5150
NiO-5	0.3995	0.4930	1.0837	0.4727	1.5137	1.6062	1.6417	0.4772	0.4885	0.3975	0.8574	0.5138	1.5151
NiO-6	0.3995	0.5979	1.0837	0.4727	1.5137	1.6062	1.6417	0.4772	0.4885	0.3975	0.8678	0.5073	1.5172

Sb ₂ O ₃ -1	0.3995	0.4770	0.9059	4.3114	0.0178	1.8456	0.0148	0.6620	1.3169	0.8049	1.0756	1.2023	2.6145
SnO ₂ -1	0.3995	0.5205	0.7629	0.2157	0.2892	0.8889	0.8010	0.4689	0.6904	1.8074	0.6844	0.4305	1.2354
SnO ₂ -3	0.3995	0.2987	0.7629	0.2157	0.2892	0.8889	0.8010	0.4689	0.6904	1.8074	0.6623	0.4439	1.2304
SnO ₂ -5	0.3995	1.0798	0.7629	0.2157	0.2892	0.8889	0.8010	0.4689	0.6904	1.8074	0.7404	0.4417	1.3058
SnO ₂ -6	0.3995	0.6205	0.7629	0.2157	0.2892	0.8889	0.8010	0.4689	0.6904	1.8074	0.6944	0.4277	1.2419
TiO ₂ -a-1	0.3995	0.5678	0.2672	0.6028	1.6847	0.6854	0.8010	0.4793	0.6452	0.3098	0.6443	0.3818	1.1329
TiO ₂ -b-1	0.3995	0.2680	0.8859	0.0483	1.4179	0.4829	0.8010	0.4753	0.7877	0.3097	0.5876	0.3733	1.0654
TiO ₂ -r-1	0.3995	0.6419	0.6315	0.2799	1.1793	0.3855	0.8010	0.4882	0.8533	0.3087	0.5969	0.2700	0.9425
WO ₃ -1	0.0414	0.6334	0.2382	0.0103	1.7081	0.8903	1.6169	0.5189	0.6150	0.0057	0.6278	0.5908	1.3840
ZnO-1	0.3995	0.6275	1.1849	0.8082	1.5343	0.8892	1.6417	1.3457	1.5188	0.8894	1.0839	0.4013	1.5976
ZrO ₂ -1	1.9185	0.6320	1.7784	0.0560	0.6278	0.5906	0.8010	0.5188	0.2860	1.2868	0.8496	0.5847	1.5981

Validation Set

NAME	BETA- standardized	D ² - standardized	H _F - standardized	V ₂ - standardized	E _{Fermi} - standardized	TFW- standardized	R- standardized	E _T - standardized	DENC- standardized	XCENC- standardized	AVER- AGE	STDE V	AVERAGE +1.28STDEV
Cr ₂ O ₃ -2	0.3995	0.6306	0.8364	0.3126	0.8111	0.6370	0.0148	1.3924	0.2193	0.1786	0.5432	0.3855	1.0367
Cu ₂ O-2	0.3995	0.3550	1.0666	0.4156	0.0039	0.7675	0.8010	1.9253	3.4123	1.4792	1.0626	0.9526	2.2819
Cu ₂ O-3	0.3995	0.0098	1.0666	0.4156	0.0039	0.7675	0.8010	1.9253	3.4123	1.4792	1.0281	0.9834	2.2868
Cu ₂ O-4	0.3995	0.5877	1.0666	0.4156	0.0039	0.7675	0.8010	1.9253	3.4123	1.4792	1.0859	0.9377	2.2862
Fe ₂ O ₃ -1	0.3995	0.6444	0.0916	0.2514	0.3448	1.1364	0.0148	2.0181	0.6478	1.0160	0.6565	0.5720	1.3887
NiO-3	0.3995	0.1346	1.0837	0.4727	1.5137	1.6062	1.6417	0.4772	0.4885	0.3975	0.8215	0.5493	1.5246
SnO ₂ -2	0.3995	0.8305	0.7629	0.2157	0.2892	0.8889	0.8010	0.4689	0.6904	1.8074	0.7154	0.4287	1.2642
SnO ₂ -4	0.3995	0.2274	0.7629	0.2157	0.2892	0.8889	0.8010	0.4689	0.6904	1.8074	0.6551	0.4502	1.2313
TiO ₂ -b-2	0.3995	0.5806	0.8859	0.0483	1.4179	0.4829	0.8010	0.4753	0.7877	0.3097	0.6189	0.3580	1.0771
Y ₂ O ₃ -1	0.3995	0.5359	4.3427	2.0225	1.2205	0.1735	0.0148	0.2606	2.1465	2.4678	1.3584	1.3126	3.0385

Table S3. Band gaps calculated by empirical equation

Metal oxide	α (°)	β (°)	γ (°)	a (Å)	b (Å)	c (Å)	Size (nm)	E_{g1} (eV)	E_{g2} (eV)
Al ₂ O ₃	90	90	120	4.81	4.81	13.12	76.0	4.99	9.61
CeO ₂	90	90	90	5.46	5.46	5.46	12.0	1.87	4.46
CeO ₂	90	90	90	5.46	5.46	5.46	3.6	1.87	4.46
CeO ₂	90	90	90	5.46	5.46	5.46	2.6	1.87	4.46
Cr ₂ O ₃	90	90	120	4.58	4.58	14.72	26.5	2.75	3.77
Cu ₂ O	90	90	90	4.31	4.31	4.31	4.0	0.67	1.8
Fe ₃ O ₄	90	90	90	8.04	8.04	8.04	12.0	1.59	2.68
Ga ₂ O ₃	90	103.7	90	12.50	3.10	5.92	65.0	2.35	4.86
Ga ₂ O ₃	90	103.7	90	12.50	3.10	5.92	2.5	2.35	4.86
HfO ₂	90	99.216	90	5.14	5.19	5.31	200.0	3.82	7.16
In ₂ O ₃	90	90	90	10.35	10.35	10.35	17.0	2.37	4.03
La ₂ O ₃	90	90	120	3.94	3.94	6.18	30.0	2.82	9.5
MgO	90	90	90	4.25	4.25	4.25	7.0	1.86	6.68
Mn ₂ O ₃	90	90	90	9.03	9.03	9.03	30.2	1.82	3.08
NiO	90	90	90	4.16	4.16	4.16	3.5	0.66	2.37
NiO	90	90	90	4.16	4.16	4.16	4.6	0.66	2.37
NiO	90	90	90	4.16	4.16	4.16	10.1	0.66	2.37
NiO	90	90	90	4.16	4.16	4.16	12.4	0.66	2.37
NiO	90	90	90	4.16	4.16	4.16	22.0	0.66	2.37
Sb ₂ O ₃	90	90	90	5.18	16.61	5.51	11.8	2.82	2.6
SnO ₂	90	90	90	4.83	4.83	3.24	4.5	1.00	3.76
SnO ₂	90	90	90	4.83	4.83	3.24	5.0	1.00	3.76
SnO ₂	90	90	90	4.83	4.83	3.24	3.7	1.00	3.76
SnO ₂	90	90	90	4.83	4.83	3.24	30.0	1.00	3.76
TiO ₂ -a	90	90	90	3.82	3.82	9.70	17.3	2.13	—
TiO ₂ -b	90	90	90	9.28	5.52	5.19	7.9	2.80	4.99
TiO ₂ -r	90	90	90	4.66	4.66	2.97	70.0	1.15	—
WO ₃	90	91.75	90	5.39	5.36	7.84	42.0	1.58	2.68
ZnO	90	90	120	3.29	3.29	5.31	35.0	0.55	3.41
ZrO ₂	90	99.2	90	5.19	5.24	5.38	40.0	3.77	8.38

* E_{g1} values were computed according to empirical equation using computed heat of formation.

* E_{g2} values were computed according to empirical equation using experimental heat of formation.

Table S4. Comparison of computed and experimental values for heat of formation

Name	$\square \Delta H_{\text{exp.}}$ (cal/mol)	$\square \Delta H_{\text{cal}}$ (cal/mol)
Al ₂ O ₃	399090	265782
CeO ₂	233000	114800
Cr ₂ O ₃	269700	63573
Cu ₂ O	39840	-26726
Fe ₂ O ₃	196500	112108
Fe ₃ O ₄	267125	124930
Ga ₂ O ₃	260550	112344
HfO ₂	266910	181544
In ₂ O ₃	222500	114771
La ₂ O ₃	458000	211066
MgO	143840	57091
Mn ₂ O ₃	229053	121907
NiO	58400	28623
Sb ₂ O ₃	133400	149498
SnO ₂	138800	-40043
TiO ₂ -a	363260	102261
TiO ₂ -b	218000	139569
WO ₃	200840	92490
Y ₂ O ₃	455001	382593
ZnO	83170	-41090
ZrO ₂	288200	179955

* ΔH_{exp} : Experimental heat of formation of unit cell.

* ΔH_{cal} : Computed heat of formation of unit cell.

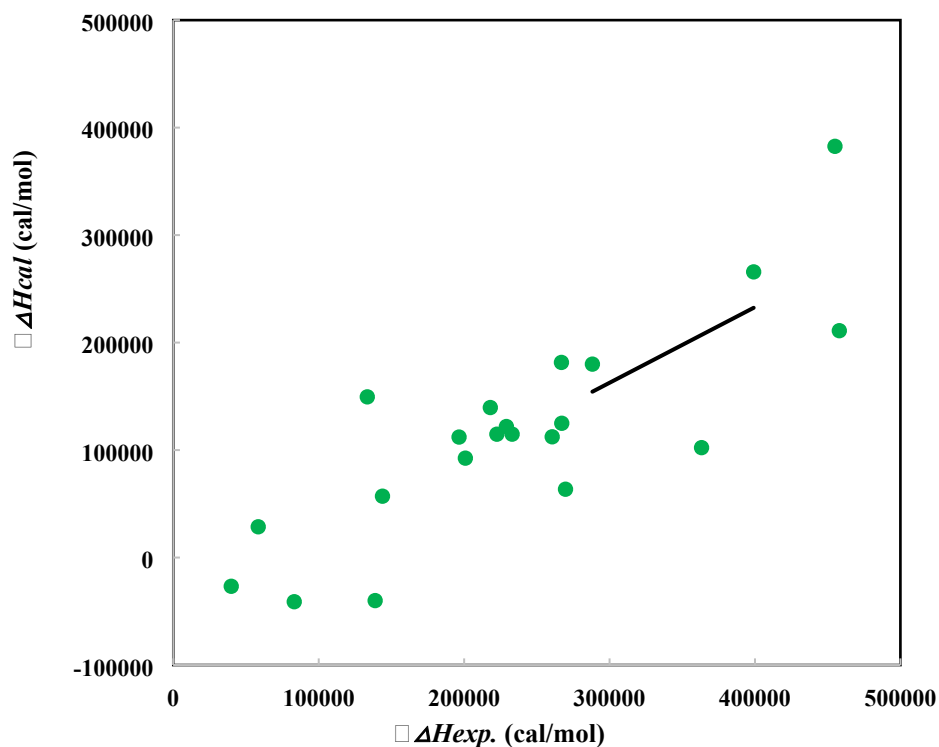


Figure S1. Relationship between computed and experimental values for heat of formation

References:

- [1] Portier, J., Campet, G., Kwon, C. W., Etourneau, J., Subramanian, M. A. Relationships between optical band gap and thermodynamic properties of binary oxides. *International Journal of Inorganic Materials*, 2001, 3(7), 1091-1094.
- [2] Appendix-Standard Thermodynamic Properties of Chemical Substance. 2000, CRC Handbook of Chemistry and Physics, CRC PRESS LLC.

Table S5. Standard error of regression coefficients of the QSPR model

Descriptors	Coefficient	Standard error
H_F	0.553	0.211
$BETA$	0.0806	0.050
D^{-2}	1.09	6.51
$V2$	-0.0159	0.0917
E_{Fermi}	0.180	0.096
TFW	-2.23	1.43
R	0.803	0.611
E_T	0.00469	0.0009
$DENC$	-0.000305	0.00147
$XCENC$	-0.00403	0.00498