Electronic Supplementary Information (ESI) on

The influence of plasma treatment on the elasticity of the in-situ oxidized gradient layer in PDMS: Towards crack-free wrinkling

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Figure S1: Evaluation process for topographical AFM images (a) via 2D-FT and PSD, exemplarily shown for one of the three samples used in the power screening at 4 W (5 % Plasma Cleaner power). For 2D-FT the AFM image is first transformed over a 2-Dimensional Fast Fourier Transformation (2D-FFT) to a FT-spectrum (b). In here, the area marked with the white box (including the FT-origin peak and the 1st order peak) is extracted as a profile. The data is fitted in Origin Pro with an FFT-filter (c) and the peak positions are subtracted from each other, resulting in the wavenumber k of the according corrugation length observed within the topographical AFM image. For PSD, the horizontal axis of the AFM image gets transformed in NanoScope Analysis software (d) and eventually the extracted profile is analyzed similar to 2D-FT (c), with the addition that the origin peak is automatically set to x = 0.



Figure S2: Topographical AFM images of the power screening, with (\mathbf{a}) = 4 W, (\mathbf{b}) = 8 W, (\mathbf{c}) = 16 W, (\mathbf{d}) = 32 W, (\mathbf{e}) = 48 W, (\mathbf{f}) = 64 W and (\mathbf{g}) = 80 W. 10 x 10 µm cutouts are added to the power screening in Fig. 2 b. Scale bar is 20 µm.



Figure S3: Topographical AFM images of the pressure screening, determined analogous to Figure S2. With (a) = 0.05 mbar, (b) = 0.1 mbar, (c) = 0.2 mbar, (d) = 0.3 mbar, (e) = 0.6 mbar, (f) = 0.9 mbar and (g) = 1.2 mbar. 10 x 10 μ m cutouts are added to the pressure screening in Fig. 2 c. Scale bar is 20 μ m.

Pressure	PSD				2 D -FT				Crack Density		
	Individual		Ø		Individual		Ø		Individual	Ď	
mbar	λ	$\sigma\pm$	λ	$\sigma\pm$	λ	$\sigma\pm$	λ	$\sigma\pm$	marviduai	Area	- +
	nm	nm	nm	nm	nm	nm	nm	nm	Area %	%	$0 \pm$
	1730,8	121,0			1710,9	24,2			7,3		
0,05	1698,1	116,5	1698,5	123,8	1697,7	30,7	1703,3	28,0	11,5	8,6	2,5
	1666,7	121,4	 		1701,3	26,6	 		7,1		
	1216,2	87,3			1217,6	22,4			7,7		
0,10	1046,5	63,2	1070,0	153,1	1040,5	16,3	1063,4	145,6	7,7	7,9	0,5
	947,4	60,9			932,0	23,1	 		8,5		
	514,3	29,3	 		511,6	15,8	 		7,8		
0,20	494,5	29,7	499,3	32,1	494,9	14,1	499,8	18,6	6,8	6,7	1,2
	489,1	28,9			492,8	16,5	 		5,3		
	454,6	22,9	 		454,1	14,8	 		4,6		
0,30	422,5	23,4	434,5	30,3	426,7	12,2	436,1	20,8	4,0	4,6	0,6
	426,5	28,0			427,6	14,3	 		5,3		
	350,2	16,0			359,9	10,0	 		4,4		
0,60	312,5	17,1	325,8	26,6	317,8	9,9	334,8	24,1	1,7	2,5	1,6
	314,7	15,4			326,8	8,4	 		1,6		
	305,1	21,1			304,4	11,1	 		0,0		
0,90	314,7	16,5	311,5	19,9	316,6	8,1	311,1	11,6	0,0	0,0	0,0
	314,7	19,8			312,3	10,4	 		0,0		
	258,6	19,6	 		259,0	5,7	 		0,0		
1,20	255,7	16,7	258,6	18,9	262,8	9,5	262,6	9,8	0,0	0,0	0,0
	261,6	19,7	 		266,0	12,2			0,0		

Table S1: Results of the pressure screening, displaying PSD (left columns), 2D-FT (middle) and the according crack density values at a time (right). For each data point, three samples were measured via AFM and analyzed with both PSD and 2D-FT. The results were averaged and the deviations summed up

via Gaussian error propagation.

Power	PSD				2 D -FT				Crack Density		
	Individual		Ø		Individual		Ø		Individual	ø	
W	λ	$\sigma\pm$	λ	$\sigma\pm$	λ	$\sigma\pm$	λ	$\sigma\pm$	marviauai	Area	- +
	nm	nm	nm	nm	nm	nm	nm	nm	Area %	%	$0 \pm$
	206,9	15,8			205,0	8,2			0,0		
5	197,4	15,9	197,4	18,6	202,6	9,8	198,5	12,9	0,0	0,0	0,0
	187,9	16,2	1		187,8	8,8	 		0,0		
	204,1	20,1			209,4	7,6	 		0,0		
10	211,3	16,8	205,3	18,1	209,5	8,5	207,1	9,0	0,0	0,0	0,0
	200,5	15,0	 		202,3	8,1	 		0,0		
	217,4	13,7	1		224,3	8,0	 		1,0		
20	239,0	16,2	225,4	19,2	235,2	8,0	225,8	12,2	0,0	0,9	0,8
	219,8	15,3	 		217,8	9,5	 		1,7		
	238,1	14,5	 		237,6	8,7	 		4,9		
40	250,7	14,6	244,4	17,1	251,1	7,7	244,3	12,6	4,1	4,5	0,6
	244,3	14,5			244,3	8,2	 		4,5		
	340,9	16,6	 		341,9	2,0	 		6,1		
60	326,1	18,4	344,3	27,7	331,6	12,2	346,2	19,0	4,4	4,7	1,2
	365,9	22,4			365,2	10,3	 		3,8		
	436,9	27,3	 		434,2	15,4	 		6,7		
80	471,2	28,4	455,0	32,2	476,1	15,7	455,9	27,2	4,6	5,4	1,2
	456,9	26,0	 		457,4	20,6	 		4,9		
	514,3	29,3	 		511,6	15,8	 		7,8		
100	494,5	29,7	499,3	32,1	494,9	14,1	499,8	18,6	6,8	6,7	1,2
	489,1	28,9			492,8	16,5			5,3		

Table S2: Results of the power screening. The results were obtained analogous to Table S1.



Figure S4: Wrinkle wavelengths for power (a) and pressure (b) screenings, determined via PSD (black curves) as well as 2D-FT (blue curves). PSD and 2D-FT are separated in both diagrams by an y-axis offset, since they superpose almost entirely when charting them on the same axis scale.



Figure S5: screening of the flat, unstrained samples, analyzed via QNM AFM method. The power range stretches from The highest accessible power at $P_{max} = 80$ W (a) to the lowest accessible power at $P_{min} = 4$ W (g). For every sample the maximum elasticity E_{max} as well as the average layer thickness t_l is denoted.



Figure S6: Pressure screening of the flat, unstrained samples, analyzed analogous to Fig. S5. The pressure range stretches from the lowest accessible pressure being $p_{min} = 0.05$ mbar (**a**) to the highest accessible at $p_{max} = 1,2$ mbar (**g**). For every sample the maximum elasticity E_{max} as well as the average layer thickness t_1

is denoted.



Figure S7: (a) Scheme of the calculated recreation of the gradient: The continuous gradient from I. is transferred into a corresponding multilayered stepwise gradient II. as well as a single step layer III. Below the corresponding stress diagrams for each layer-to-layer interface are shown schematically: For continuous (I.) and stepwise (II.) gradients a lower maximal von-Mises-stress σ_{max} than for the single step

(III.) is simulated, due to the broader distribution of overall stress between layer and substrate when compared with the single layer. The critical stress σ_{crit} for cracking these layers indicates that for particular conditions $\sigma_{max,single-step} > \sigma_{crit} > \sigma_{max,gradient}$, so crack-free wrinkles can be achieved. In (**b**) the real gradient from Fig. 4 a is compared to two theoretical models; on the one hand the exponential model of Sui et al., ⁴³ on the other hand the cubic model of Chan et al. ⁴² Both are in very good agreement with the experimental

data, however the exponential model is even closer ($R_2 = 0.996$) than the cubic one ($R_2 = 0.990$).