

## Supporting Information

### Association and Relaxation of Supra-Macromolecular Polymers

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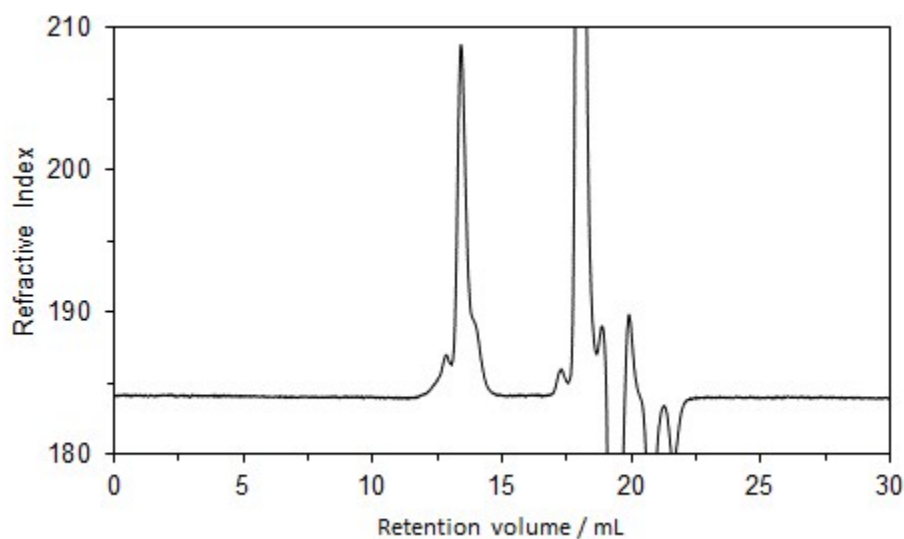
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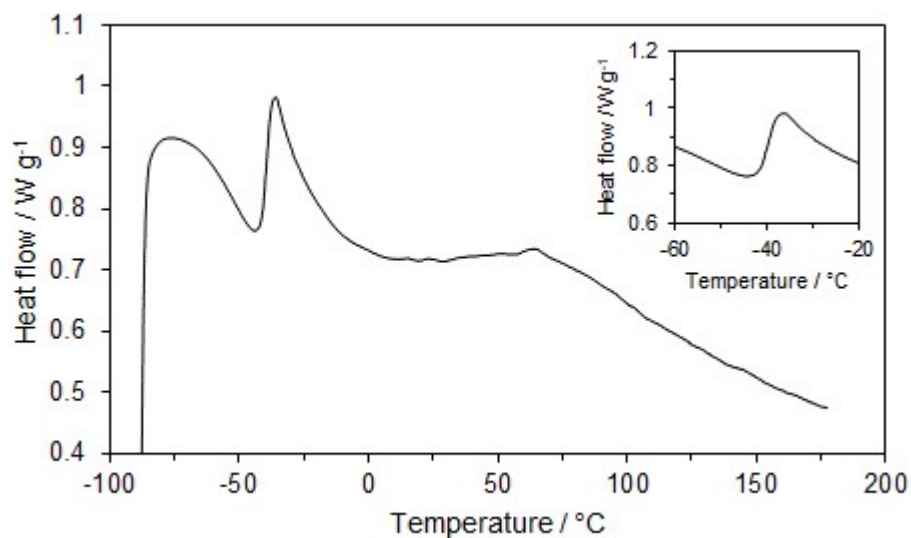
#### Size Exclusion Chromatography (SEC)



**Figure S1:** SEC of UPy1

Fig. S1 shows a representative SEC sample, for UPy1. The sample was measured using a Viscotek TDA 302 instrument. Tetrahydrofuran was used as the eluent at a flow rate of 1 mL min<sup>-1</sup>, and the  $M_w$  calibrated with PBD standards.  $M_w$  was determined to be 27,800 Da, and  $M_n$  was 21,000 Da. SEC data for all samples is reported in Table 1 in the main text.

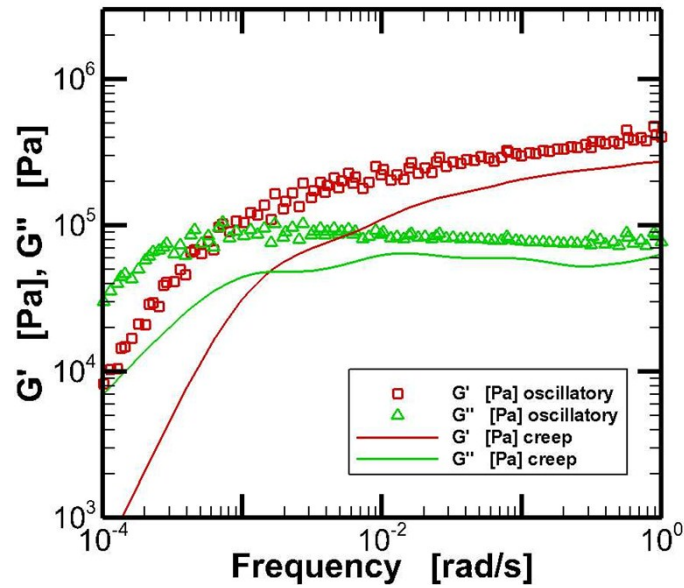
## Differential scanning calorimetry (DSC)



**Figure S2:** DSC heating curve of UPy1. Inset highlights the glass transition.

Fig. S2 shows a representative DSC curve, of UPy1, determined using a TA instruments Q1000. Samples were subjected to a heating and cooling cycle at a rate of  $10^{\circ}\text{C min}^{-1}$  from  $-90 - 180^{\circ}\text{C}$ . The glass transition ( $T_g$ ) was taken as the inflection point of the heat flow curve, analysed using the TA Universal Analysis software. The  $T_g$  was determined to be  $-39.6^{\circ}\text{C}$ .

## Creep Recovery Spectra



**Figure S3:** Creep recovery spectra (lines) of UPy1 at 25 °C, and comparison with TTS shifted oscillatory data (see main text)

Fig. S3 shows a comparison between the creep recovery spectra of UPy1 at 25 °C and the corresponding oscillatory data, TTS shifted as described in the main text. The creep recovery data was collected by first applying a constant stress of 2000 Pa for 10 minutes to the sample using an 8 mm parallel plate, equipped with a peltier plate. The stress was then removed and the strain recovery monitored for  $\sim 10,000$  s. A discrete retardation spectra<sup>1</sup> was then fitted to the recovery data, using the TA Rheology Advantage Data Analysis software:

$$J_r(t) = \sum_{k=1}^N J_k \left( 1 - \exp\left(\frac{-t}{\lambda_k}\right) \right)$$

where  $\lambda_k$  is the retardation time and  $J_k$  the retardation strength. The fitted parameters are shown in Table S1:

**Table S1:** Retardation spectrum parameters fitted to creep relaxation data

$\lambda_k$	$J_k$	$\eta_0$	$J_0$
s	Pa <sup>-1</sup>	Pa s	Pa <sup>-1</sup>
721.9	$2.86 \times 10^{-6}$	$1.19 \times 10^8$	$4.45 \times 10^{-11}$
97.2	$2.68 \times 10^{-6}$		
8.2	$1.46 \times 10^{-6}$		
1.75	$1.08 \times 10^{-7}$		
0.23	$2.18 \times 10^{-6}$		
$8.04 \times 10^{-3}$	$1.32 \times 10^{-6}$		

The corresponding viscoelastic data can then be determined from the creep recovery.<sup>1</sup> Firstly the storage and loss compliance ( $J'$  and  $J''$  respectively) are calculated from the retardation spectrum as a function of frequency ( $\omega$ ):

$$J'(\omega) = J_0 + \sum_{k=1}^N J_k \frac{1}{1 + \omega^2 \lambda_k^2}$$

$$J''(\omega) = \frac{1}{\omega \eta_0} \sum_{k=1}^N J_k \frac{\omega \lambda_k}{1 + \omega^2 \lambda_k^2}$$

From this the storage and loss moduli ( $G'$  and  $G''$  respectively) are calculated:

$$G'(\omega) = \frac{J'(\omega)}{\{J'(\omega)\}^2 + \{J''(\omega)\}^2}$$

$$G''(\omega) = \frac{J''(\omega)}{\{J'(\omega)\}^2 + \{J''(\omega)\}^2}$$

The corresponding data is shown in Fig. S3, and is compared with the time temperature superposition (TTS) oscillatory data. A good match between the TTS and creep recovery data is seen, given the differences in technique. This shows that despite the fanning in the TTS data it remains a good representation of the viscoelastic properties of UPy1.

## Multimode Modelling

**Table S2:** Multi-mode modelling fit parameters for extensional data of UPy1 at 25 °C

Mode	Type	Maxwell fit		Pom-Pom	Stretch Rolie-Poly	$q$ arms
		$\tau_{di}$ (s)	$G_i$ (Pa)	$\tau_d/\tau_s$	$\tau_s$ (s)	
1	Pom-pom	10000	6294	12	-	15
2	Pom-pom	3511	33763	15	-	10
3	Stretch Rolie-Poly	1233	111611	-	0.6	-
4	Stretch Rolie-Poly	433	60893	-	0.5	-
5	Stretch Rolie-Poly	152	47484	-	0.4	-
6	Non-stretch Rolie-Poly	53.4	50531		-	-
7	Non-stretch Rolie-Poly	18.7	47484		-	-
8	Non-stretch Rolie-Poly	6.6	46031		-	-
9	Non-stretch Rolie-Poly	2.3	44622		-	-
10	Non-stretch Rolie-Poly	0.81	48810		-	-
11	Non-stretch Rolie-Poly	0.28	55470		-	-
12	Non-stretch Rolie-Poly	0.10	103302		-	-

## References

- 1 J. D. Ferry, *Viscoelastic properties of polymers*, Wiley, 1980.