

Supplementary Information

New Insight into the Structure of PuGaO₃ from *ab initio* Particle-swarm Optimization Methodology

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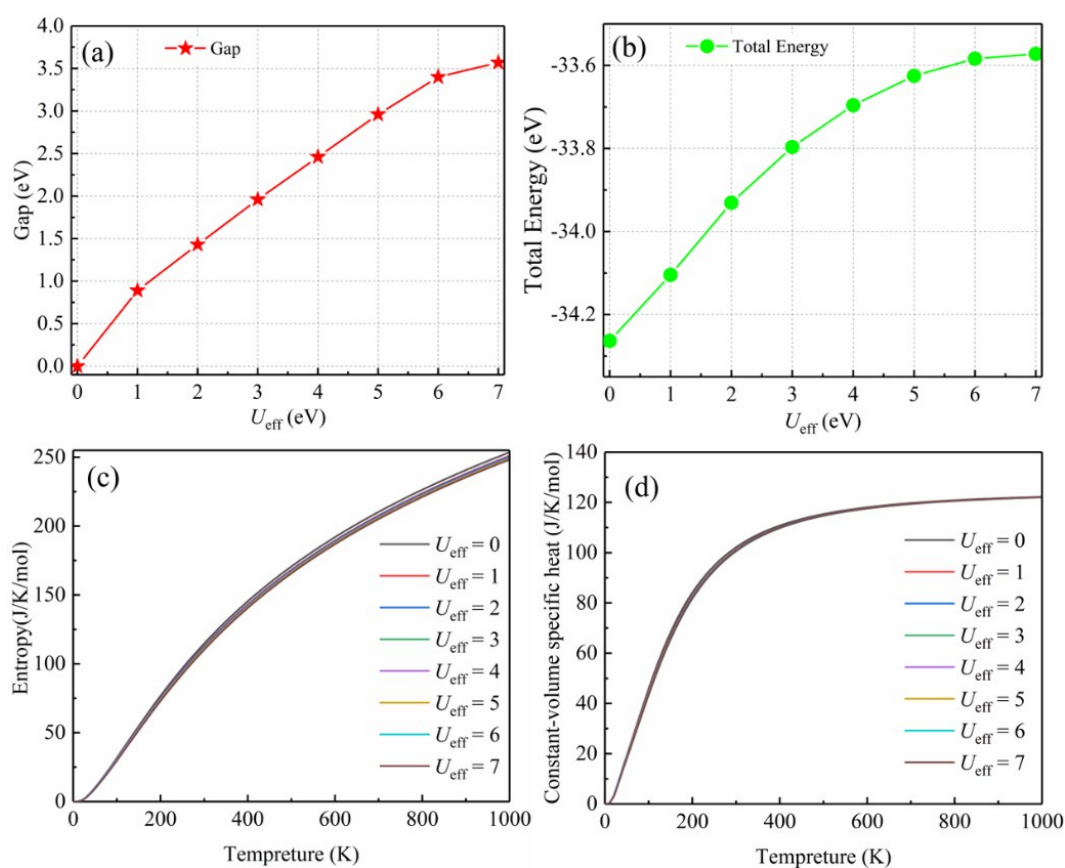


Fig. S1 Dependences of the (a) band gap, (b) total energy, (c) enthalpy and (d) constant-volume specific heat on different U_{eff} for $Pnma$ PuGaO₃.

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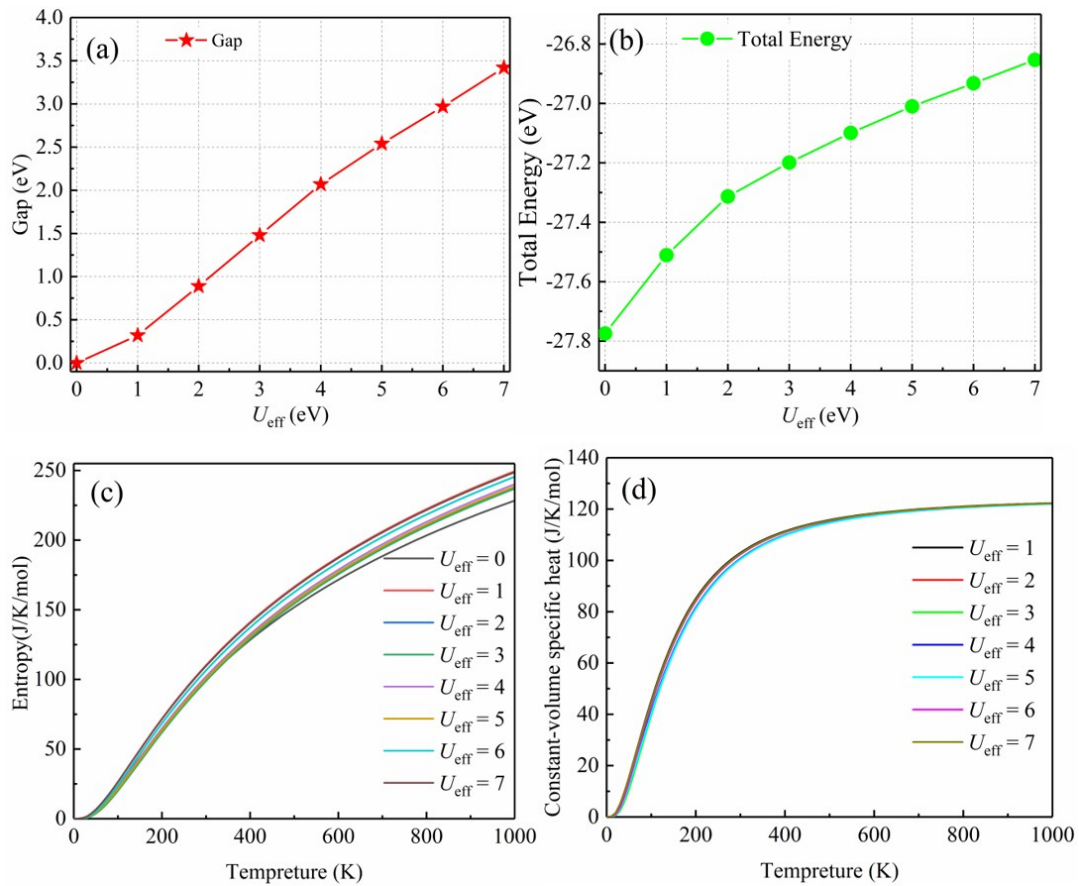


Fig. S2 Dependences of the (a) band gap, (b) total energy, (c) enthalpy and (d) constant-volume specific heat on different U_{eff} for *Pnma* CeGaO₃.

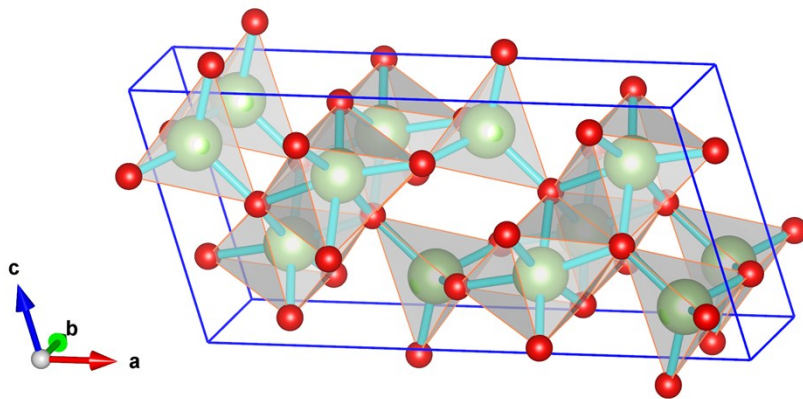


Fig. S3 The monoclinic structure of Ga₂O₃. The lines indicate Ga–O separations shorter than 2.2 Å. Green balls are Ga, red O.

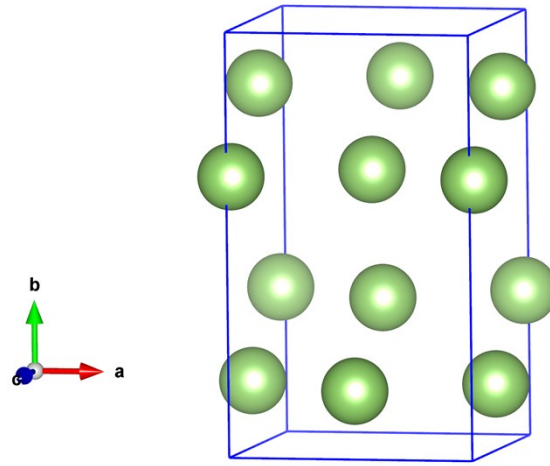


Fig. S4 The orthorhombic structures of Ga.

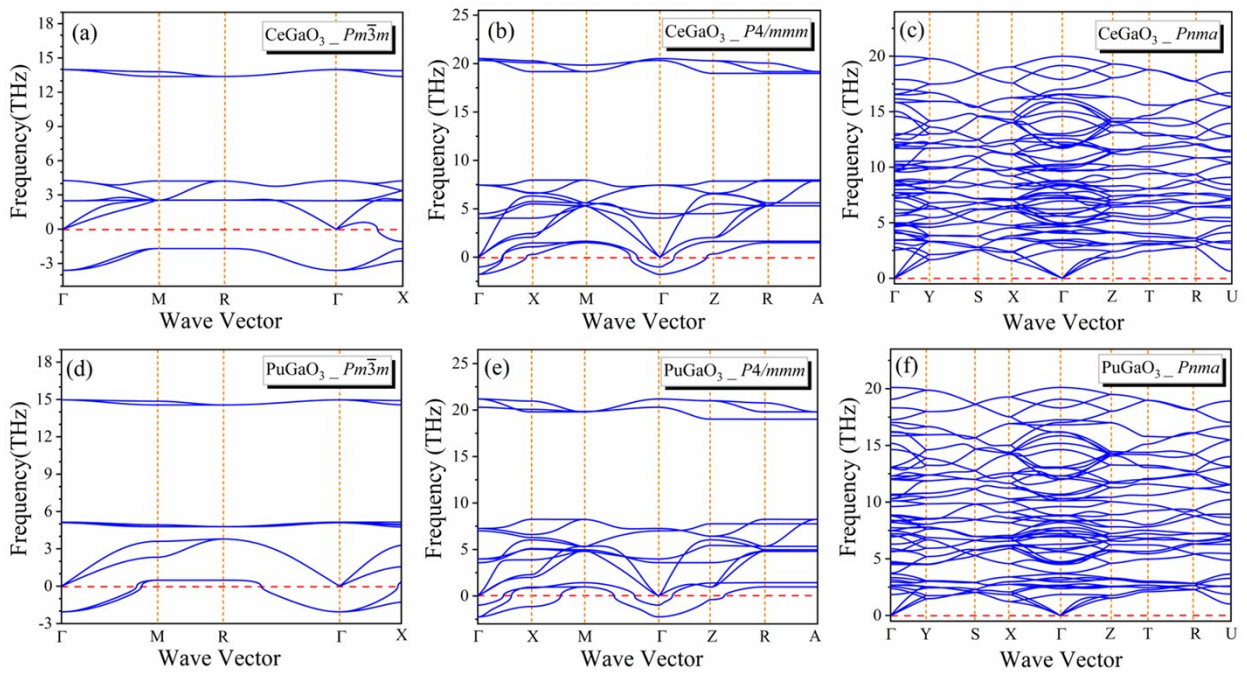


Fig. S5 The calculated phonon dispersion curves of $AGaO_3$ ($A = Ce, Pu$) in the states of AFM magnetism from PBEsol + U . (a) CeGaO3_ $Pm\bar{3}m$, (b) CeGaO3_ $P4/mmm$, (c) CeGaO3_ $Pnma$, (d) PuGaO3_ $Pm\bar{3}m$, (e) PuGaO3_ $P4/mmm$, (f) PuGaO3_ $Pnma$.

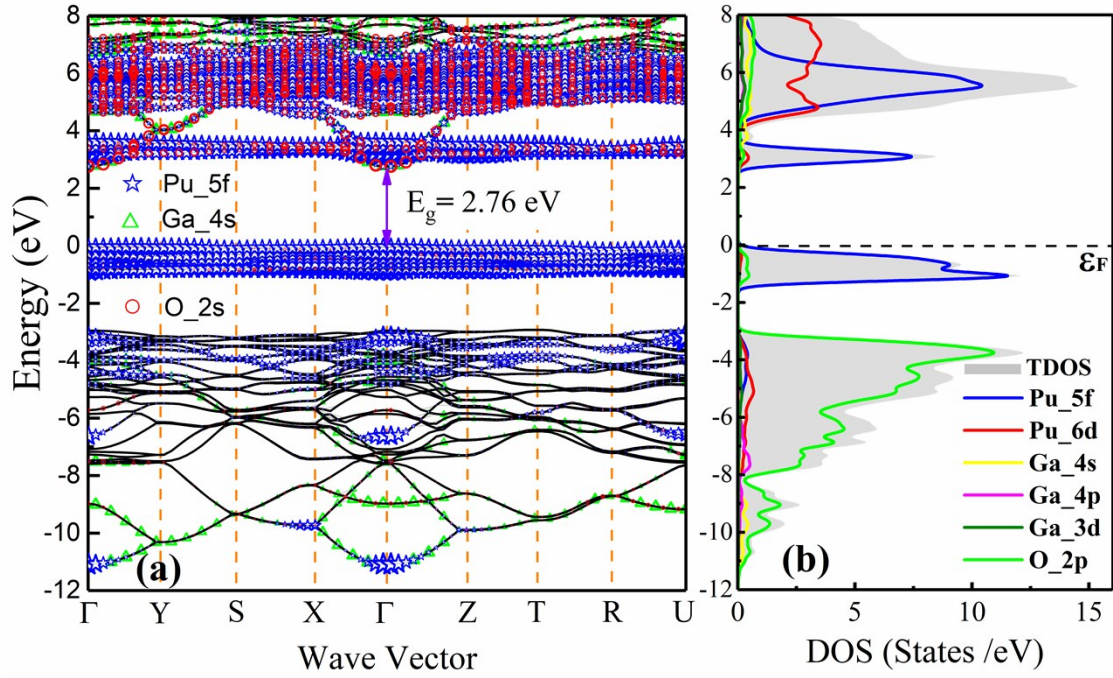


Fig. S6 The calculated (a) fat-band dispersions and (b) PDOS of PuGaO₃ for *Pnma* phase in the states of AFM magnetism using HSE06 method. The DOS projected onto Pu-5f, Pu-6d, Ga-4s, Ga-4p, Ga-3d, and O-2p orbitals. Energy is shifted so that the Fermi level ϵ_F equals to zero.

Supporting Tables

Table S1. Detailed structure information of predicted structures of PuGaO₃ and CeGaO₃ from PEBsol + *U* calculations.

Phase	Lattice parameter (Å, deg)	Atom	Wyckoff position	Atomic coordinates (fractional)			Energy (eV/f.u.)
				x	y	z	
PuGaO ₃ (<i>No</i> :62, <i>Z</i> = 4)	<i>a</i> = 5.513	Pu	4c	0.0398	0.2500	0.9931	-33.7028
	<i>b</i> = 7.694	Ga	4b	0.5000	0.0000	0.0000	
	<i>c</i> = 5.467	O ₁	8d	0.2926	0.0402	0.7085	
	$\alpha = \beta = \gamma = 90$	O ₂	4c	0.4831	0.2500	0.0782	
CeGaO ₃ (<i>No</i> :62, <i>Z</i> = 4)	<i>a</i> = 5.508	Ce	4c	0.0349	0.2500	0.9927	-27.1508
	<i>b</i> = 7.794	Ga	4b	0.5000	0.0000	0.0000	
	<i>c</i> = 5.589	O ₁	8d	0.2875	0.0379	0.7136	
	= = =	O ₂	4c	0.4869	0.2500	0.0715	
	90						

Table S2. Calculated lattice constants (a_0 , b_0 , c_0), the band gap (E_g), and total energy (E) for the $Pnma$ PuGaO₃ and CeGaO₃ through PBEsol + U and HSE06 methods ^a

System	V_{xc}	Method	a_0 (Å)	b_0 (Å)	c_0 (Å)	EMS	E_g (eV)	E (eV/f.u.)
PuGaO ₃	PBEsol+ U	FM	5.533	7.691	5.477		2.32	-33.696
		AFM	5.513	7.694	5.467		2.46	-33.703
	HSE06	FM	5.465	7.635	5.419		2.51	-49.949
		AFM	5.458	7.637	5.422		2.76	-49.951
CeGaO ₃	PBEsol+ U	FM	5.509	7.795	5.588		2.40	-27.145
		AFM	5.508	7.794	5.589	0.065	2.36	-27.150
	HSE06	FM	5.494	7.716	5.416		2.81	-39.633
		AFM	5.494	7.710	5.418	0.047	2.88	-39.634
	exp.[3]		5.484	7.747	5.490			

$$^a EMS^2 = \frac{1}{3} \left[(a - a_{exp.})^2 + (b - b_{exp.})^2 + (c - c_{exp.})^2 \right]$$

Table S3. The optical phonon frequencies (unit:cm⁻¹) and LO-TO splitting for infrared active modes at Γ point of PuGaO₃. R represents Raman active, IR represents infrared active. The first column (e = 0) is for no electric field, the

e//x, e//y and e//z are for the field parallel to x, y and z principal axis, respectively. $\Delta\omega^2 = \Delta\omega_{LO}^2 - \Delta\omega_{TO}^2$

	Modes	TO (e=0)	LO (e//x)	LO (e//y)	LO (e//z)	$\sqrt{\Delta\omega^2}$
Infrared (IR)	B _{1u} (1)	85.893	85.893	85.893	86.393	9.285
	B _{1u} (2)	150.504	150.504	150.504	160.178	54.821
	B _{1u} (3)	227.524	227.524	227.524	235.663	61.399
	B _{1u} (4)	241.834	241.834	241.834	275.758	132.509
	B _{1u} (5)	280.761	280.761	280.761	292.936	83.575
	B _{1u} (6)	311.749	311.749	311.749	312.483	21.403
	B _{1u} (7)	343.705	343.705	343.705	433.000	263.355
	B _{1u} (8)	433.000	432.100	432.100	517.492	283.388
	B _{1u} (9)	542.376	542.376	542.376	584.672	218.334
	B _{2u} (1)	128.522	128.522	152.172	128.522	81.476
	B _{2u} (2)	153.773	153.773	161.011	153.773	47.734
	B _{2u} (3)	237.264	237.264	258.746	237.264	103.223
	B _{2u} (4)	260.781	260.781	279.527	260.781	100.642
	B _{2u} (5)	323.524	323.524	473.595	323.524	345.867

	B _{2u} (6)	495.810	495.810	507.685	495.810	109.162
	B _{2u} (7)	544.544	544.544	596.313	544.544	243.025
	B _{3u} (1)	86.260	86.727	86.260	86.260	8.988
	B _{3u} (2)	153.940	161.278	153.940	153.940	48.096
	B _{3u} (3)	221.620	227.157	221.620	221.620	49.849
	B _{3u} (4)	249.439	256.911	249.439	249.439	61.509
	B _{3u} (5)	263.016	287.899	263.016	263.016	117.085
	B _{3u} (6)	290.368	389.436	290.368	290.368	259.514
	B _{3u} (7)	399.043	454.048	399.043	399.043	216.620
	B _{3u} (8)	492.308	515.590	492.308	492.308	153.188
	B _{3u} (9)	516.891	574.998	516.891	516.891	251.886
Raman(R)	A _g (1)	77.787				
	A _g (2)	105.673				
	A _g (3)	197.103				
	A _g (4)	273.923				
	A _g (5)	331.063				
	A _g (6)	353.445				
	A _g (7)	434.001				
	B _{1g} (1)	122.285				
	B _{1g} (2)	188.464				
	B _{1g} (3)	327.961				
	B _{1g} (4)	352.377				
	B _{1g} (5)	578.334				
	B _{2g} (1)	84.425				
	B _{2g} (2)	111.677				
	B _{2g} (3)	205.743				
	B _{2g} (4)	337.167				
	B _{2g} (5)	409.384				
	B _{2g} (6)	488.305				
	B _{2g} (7)	604.319				
	B _{3g} (1)	100.470				
	B _{3g} (2)	293.103				
	B _{3g} (3)	359.349				
	B _{3g} (4)	430.131				
	B _{3g} (5)	635.974				
Silent	A _u (1)	62.443				
	A _u (2)	150.171				
	A _u (3)	176.622				
	A _u (4)	225.189				
	A _u (5)	266.785				

$A_u(6)$	340.302
$A_u(7)$	504.483
$A_u(8)$	527.565
