## Supplementary Materials for "Prediction of new ZnS-CaS alloys with anomalous electronic properties"

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TABLE S1. Bulk modulus B (GPa), shear modulus G (GPa), Young's modulus E (GPa), Poisson's ratio v and Vickers hardness  $H_v$  (GPa) for possible ZnS, CaS and ZnS-CaS alloys at ambient pressure.

Phase	В	G	Е	v	Hv	
ZB-ZnS	70	34	87	0.293	3.62	
RS-ZnS	86	46	117	0.274	5.95	
Cmcm-ZnS	87	46	118	0.274	5.98	
RS-CaS	56	40	96	0.216	8.33	
$Pm\bar{3}m$ -CaS	62	18	50	0.365	-0.35	
$I4/mcm-CaZnS_2$	60	32	82	0.273	4.30	
$R\bar{3}$ -Ca <sub>2</sub> ZnS <sub>3</sub>	51	20	52	0.329	0.75	
$R\bar{3}$ -Ca <sub>7</sub> Zn <sub>2</sub> S <sub>9</sub>	40	18	48	0.303	1.34	



Fig. S1. Formation enthalpy of ZnS-CaS alloys with respect to decomposition into (a) ZnS and CaS, (b)  $CaZnS_2$  and CaS, and (c)  $Ca_2ZnS_3$  and CaS, where the stable phases with the lowest energy are chosen for special pressures.



Fig. S2. The phonon spectrums of predicted (a) I4/mcm-CaZnS<sub>2</sub>, (b)  $R\bar{3}$ -Ca<sub>2</sub>ZnS<sub>3</sub> and (c)  $R\bar{3}$ -Ca<sub>7</sub>Zn<sub>2</sub>S<sub>9</sub> at 0 GPa.



Fig. S3. The upper panels show the crystal structures of the predicted thermodynamically metastable ZnS-CaS alloys at special pressures, whose phonon spectrums are listed correspondingly in the bottom panels.

x = 1 and $x = 1$ and $x = 1$ and $x = 1$	P(GPa)
CaZn <sub>3</sub> S <sub>4</sub> $P\bar{4}21c$ a=b=5.62         Ca(2b)         0.00         0.00         0.50	70
c=6.02 $Zn(4d) = 0.00 = 0.50 = 0.04$	
$\alpha = \beta = \gamma = 90$ Zn(2a) 0.00 0.00 0.00	
S(8e) = 0.25 = 0.20 = 0.19	
CaZn <sub>2</sub> S <sub>3</sub> C2       a=8.45       Ca(4c)       1.00       0.26       0.67	50
b=5.85 $Ca(2b) = 0.00 = 0.28 = 0.50$	
c=17.38 $Ca(2a) = 0.00 = 0.82 = 0.00$	
$\alpha = \gamma = 90$ Zn(4c) 0.00 0.76 0.67	
$\beta = 133.49$ Zn(4c) 0.52 0.29 0.85	
Zn(4c) = 0.04 = 0.29 = 0.19	
Zn(2a) = 0.00 = 0.31 = 0.00	
Zn(2b) = 0.50 = 0.26 = 0.50	
S(4c) = 0.19 = 0.97 = 0.64	
S(4c) = 0.32 = 0.04 = 0.85	
S(4c) = 0.69 = 0.04 = 0.82	
S(4c) = 0.81 = 0.97 = 0.69	
S(4c) = 0.68 = 0.60 = 0.97	
S(4c) = 0.70 = 0.07 = 0.48	
$Ca_3Zn_2S_5$ $P\overline{1}$ $a=11.47$ $Ca(2i)$ $0.29$ $0.52$ $0.41$	30
b= $5.32$ Ca(2i) $0.52$ $0.77$ $0.25$	
c=5.34 $Ca(2i)$ 0.09 0.85 0.14	
$\alpha = 107.80$ Zn(2i) 0.90 0.66 0.36	
$\beta = 99.34$ Zn(2i) 0.30 0.01 0.92	
$\gamma = 78.00$ S(2i) 0.31 0.00 0.34	
S(2i) = 0.07 = 0.38 = 0.22	
S(2i) = 0.88 = 0.08 = 0.33	
S(2i) = 0.53 = 0.26 = 0.25	
S(2i)  0.27  0.45  0.90	
$Ca_5Zn_3S_8$ Amm2 $a=8.95$ $Ca(8f)$ $0.26$ $0.75$ $0.57$	30
b=8.82 $Ca(2a) = 0.00 = 0.50 = 0.55$	
c=6.11 $Zn(2a) = 0.00 = 0.00 = 0.55$	
$\alpha = \beta = \gamma = 90$ Zn(2b) 0.50 0.00 0.08	
m Zn(2b) = 0.50 = 0.00 = 0.57	
S(4c) = 0.69 = 0.00 = 0.83	
S(4c) = 0.21 = 0.00 = 0.33	
S(4d) = 0.00 = 0.21 = 0.76	
S(4e) = 0.50 = 0.81 = 0.32	
Ca <sub>3</sub> ZnS <sub>4</sub> $I\bar{4}3m$ a=b=c=6.27Ca(6b)0.500.000.00	30
$\alpha = \beta = \gamma = 90$ Zn(8c) 0.00 0.00 0.00	
S(2a) = 0.71 = 0.29 = 0.29	

TABLE S2. Structural parameters and atomic coordinates for metastable ZnS-CaS alloys at different pressures.

Phase	Elastic constant tensor $C_{ij}$ (GPa)
$I4/mcm-CaZnS_2$	$ \begin{pmatrix} 99 & 56 & 17 & 0 & 0 & 0 \\ 99 & 17 & 0 & 0 & 0 \\ & 162 & 0 & 0 & 0 \\ & & 26 & 0 & 0 \\ & & & 26 & 0 \\ & & & & 31 \end{pmatrix} $
$Rar{3} ext{-} ext{Ca}_2 ext{ZnS}_3$	$ \begin{pmatrix} 72 & 42 & 32 & -3 & -6 & 0 \\ & 72 & 32 & 3 & 6 & 0 \\ & 97 & 0 & 0 & 0 \\ & & 23 & 0 & 6 \\ & & & & 23 & -3 \\ & & & & & 15 \end{pmatrix} $
$Rar{3} ext{-} ext{Ca}_7 ext{Zn}_2 ext{S}_9$	$ \begin{pmatrix} 68 & 39 & 21 & -5 & 2 & 0 \\ & 68 & 21 & 5 & -2 & 0 \\ & & 66 & 0 & 0 & 0 \\ & & & 21 & 0 & -2 \\ & & & & & 21 & -5 \\ & & & & & & 14 \end{pmatrix} $
$C2 ext{-} ext{CaZn}_2 ext{S}_3$	$ \begin{pmatrix} 43 & 24 & 28 & 0 & -15 & 0 \\ 91 & 36 & 0 & -4 & 0 \\ 88 & 0 & -22 & 0 \\ 9 & 0 & 4 \\ & & 33 & 0 \\ & & & & 8 \end{pmatrix} $
Amm2-Ca <sub>5</sub> Zn <sub>3</sub> S <sub>8</sub>	$ \begin{pmatrix} 92 & 45 & 7 & 0 & 0 & 0 \\ 82 & 23 & 0 & 0 & 0 \\ & 141 & 0 & 0 & 0 \\ & & 16 & 0 & 0 \\ & & & -15 & 0 \\ & & & & & 10 \end{pmatrix} $
$P\bar{1}$ -Ca $_3$ Zn $_2$ S $_5$	$ \begin{pmatrix} 83 & 31 & 31 & 3 & 9 & 1 \\ 86 & 44 & -5 & 9 & -2 \\ & 78 & 5 & -2 & -8 \\ & 30 & -20 & 17 \\ & & 17 & -7 \\ & & & 35 \end{pmatrix} $
$Par{4}21c ext{-CaZn}_3S_4$	$ \begin{pmatrix} 114 & 30 & 33 & 0 & 0 & 0 \\ & 114 & 33 & 0 & 0 & 0 \\ & 98 & 0 & 0 & 0 \\ & & -13 & 0 & 0 \\ & & & -13 & 0 \\ & & & & -2 \end{pmatrix} $
$Iar{4}3m ext{-} ext{Ca}_3 ext{ZnS}_4$	$ \left(\begin{array}{cccccccccccccccccccccccccccccccccccc$

TABLE S3. Elastic constants tensors of predicted ZnS-CaS alloys.



Fig. S4. Full DOS of ZnS, CaS and their alloys at different pressures based on TB-mBJ functional. ZnS-CaS alloys: (a) I4/mcm-CaZnS<sub>2</sub> at 20 GPa, (b)  $R\bar{3}$ -Ca<sub>2</sub>ZnS<sub>3</sub> at 30 GPa, (c)  $R\bar{3}$ -Ca<sub>7</sub>Zn<sub>2</sub>S<sub>9</sub> at 40 GPa; ZnS: (d) ZB at 0 GPa, (e) RS at 20 GPa, (f) Cmcm at 70 GPa; and CaS: (g) RS at 0 GPa, (h)  $Pm\bar{3}m$  at 40 GPa, (i)  $Pm\bar{3}m$  at 90 GPa. The VBM is set to zero in each panel.



Fig. S5. Band structures and DOS of ZnS-CaS alloys based on TB-mBJ functional.



Fig. S6. Projected DOS above the Fermi level of stable ZnS-CaS alloys based on TB-mBJ functional.