

Electronic Supplementary Information (ESI)

Sr[B(OH)₄](IO₃) and Li₄Sr₅[B₁₂O₂₂(OH)₄](IO₃)₂: Two Unprecedented Metal Borate-Iodates Showing Subtle Balance of Enlarged Band Gap and Birefringence[†]

Guang Peng,^a Chensheng Lin,^a Dan Zhao,^b Liling Cao,^{ac} Huixin Fan,^{ac} Kaichuang Chen,^a and Ning Ye^{*a}

^a Key Laboratory of Optoelectronic Materials Chemistry and Physics, Fujian Institute of Research on the Structure of Matter, Chinese Academy of Sciences, Fuzhou, Fujian 350002, P. R. China.

^b Department of Physics and Chemistry, Henan Polytechnic University, Jiaozuo, Henan 454000, China

^c University of the Chinese Academy of Sciences, Beijing 100049, P. R. China

E-mail: nye@fjirsm.ac.cn

Table of Contents

	Methods (Crystals Growth, Physical Measurements, Computational methods)	S3
Table S1	Crystal data and structural refinement for SBIO and LSBIO	S4
Table S2	Atomic coordinates ($\times 10^4$) and equivalent isotropic displacement parameters ($\text{\AA}^2 \times 10^3$) for SBIO	S4
Table S3	Selected bond lengths (\AA) and angles (degrees) for SBIO	S4
Table S4	Anisotropic displacement parameters ($\text{\AA}^2 \times 10^3$) for SBIO	S5
Table S5	Hydrogen coordinates ($\times 10^4$) and isotropic displacement parameters ($\text{\AA}^2 \times 10^3$) for SBIO	S5
Table S6	Atomic coordinates ($\times 10^4$) and equivalent isotropic displacement parameters ($\text{\AA}^2 \times 10^3$) for LSBIO	S5
Table S7	Selected bond lengths (\AA) and angles (degrees) for LSBIO	S6
Table S8	Anisotropic displacement parameters ($\text{\AA}^2 \times 10^3$) for LSBIO	S6
Figure S1	Crystal picture of SBIO	S7
Figure S2	Crystal picture of LSBIO	S7
Figure S3	Calculated and experimental powder X-ray diffraction patterns of SBIO	S7
Figure S4	Calculated and experimental powder X-ray diffraction patterns of LSBIO	S8
Figure S5	Coordination mode of a Sr^{2+} in SBIO	S8
Figure S6	TGA and DTA curves of SBIO	S9
Figure S7	TGA and DTA curves of LSBIO	S9
Figure S8	IR absorption spectra of SBIO and LSBIO	S10
Figure S9	Calculated electronic band structure for SBIO	S10
Figure S10	Calculated electronic band structure for LSBIO	S11
Figure S11	Calculated refractive index dispersion curves for SBIO	S11
Figure S12	Calculated refractive index dispersion curves for LSBIO	S12
Figure S13	Photograph of LSBIO and SBIO for the measurement of birefringence	S12
Figure S14	Calculated refractive index dispersion curves for $\text{Li}_3\text{KB}_4\text{O}_8$	S13
References		S13

Methods

Crystals Growth

LiBO_2 (99%), I_2O_5 (99%), HIO_3 (99%), and $\text{Sr}(\text{OH})_2 \cdot 8\text{H}_2\text{O}$ (>99%) were all purchased from Taitan and used as received. Both the crystals were synthesized under traditional subcritical hydrothermal condition. A mixture of LiBO_2 (0.015 mol, 0.746 g), I_2O_5 (0.005 mol, 1.669 g), $\text{Sr}(\text{OH})_2 \cdot 8\text{H}_2\text{O}$ (0.01 mol, 2.656 g) and H_2O (10 mL) were sealed in an autoclave equipped with a Teflon liner (23 mL) and heated at 220 °C for 5 days, followed by slow cooling to room temperature at a rate of 3 °C·h⁻¹. The reaction product was washed with deionized water and ethanol, and then dried in air. Large amount of octahedral colorless crystal were obtained and determined to be $\text{Li}_4\text{Sr}_5[\text{B}_{12}\text{O}_{22}(\text{OH})_4](\text{IO}_3)_2$ (LSBIO). Under the same experimental conditions and operating procedures, when I_2O_5 was changed to be HIO_3 (0.01 mol, 1.759 g) or NaIO_3 (0.005 mol, 0.99g), the $\text{Sr}[\text{B}(\text{OH})_4](\text{IO}_3)$ (SBIO) crystal was synthesized. The largest yields of LSBIO and SBIO were about 70% according to Sr.

Physical Measurements

Powder XRD analysis was carried out on a Miniflex-600 diffractometer with Cu K α radiation ($\lambda = 1.54059$ Å) at room temperature in the angular range of 20=5–75° with a scan step width of 0.02° and a fixed time of 0.2 s. Single crystal X-ray diffraction data for SBIO and LSBIO were collected at room temperature on a Rigaku Mercury CCD diffractometer equipped with graphite-monochromatic Mo K α radiation ($\lambda = 0.71073$ Å). The hemisphere of data was corrected using a narrow-frame method with ω -scan mode. By using the CrystalClear program, all data were integrated, and the intensities were corrected for Lorentz polarization, air absorption, and absorption attributable to the variation in the path length through the detector faceplate. Absorption corrections were also applied based on the Multiscan technique. The crystal structures were determined by the direct methods and refined by full-matrix least-squares fitting on F^2 using SHELXL.^[1,2] All the atoms were refined with anisotropic displacement parameters. All the thermal parameters were satisfying. The PLATON program^[3] was used to check the correctness of the structures and no higher symmetry was found. The thermogravimetric analysis (TGA) and differential thermal analysis (DTA) for SBIO and LSBIO were conducted on a Netzsch STA449F3 simultaneous analyzer. Reference (Al_2O_3) and crystal samples (5–10 mg) were enclosed in Al_2O_3 crucibles and heated from 30 to 1100 °C at a rate of 10 °C·min⁻¹ under a constant flow of nitrogen gas. The UV-vis-NIR diffuse reflections were measured at room temperature in the range of 190–2500 nm with BaSO_4 as the standard of 100% reflectance. All the data were collected on a PerkinElmer Lamda-950 ultraviolet/visible/near-infrared spectrophotometer. The reflectance values were converted to absorbance using the Kubelka-Munk function $F(R) = (1-R)^2/(2R) = K/S$ (R is the reflectance, K is the absorption, and S is the scattering).^[4,5] The birefringence were measured on a Nikon ECLIPSE LV100 POL polarizing microscope with the wavelength of the light source in 589.6 nm. The formula for the calculation of birefringence can be expressed as follows: $\Delta R(\text{retardation}) = \Delta n \times T$, where ΔR represents the optical path difference, Δn denotes the birefringence, and T denotes the thickness of the crystal. The positive and negative rotation of compensatory can determine the retardation. The crystals were ground into micron fragment for the measurement of the maximum birefringence. The retardation of LSBIO and SBIO were 850 and 579 nm, respectively. The thickness of LSBIO and SBIO were 20.72 and 10.8 μm .

Computational methods

The electronic structure for all compounds were accomplished by using CASTEP, a plane-wave pseudopotential total energy package based on density functional theory (DFT).^[6,7] The functional developed by Perdew-Burke-Ernzerhoff (PBE) functional within the generalized gradient approximation (GGA)^[8] form were adopted to describe the exchange-correlation energy. Interaction of the electrons with ion cores was represented by the norm-conserving pseudopotentials, and the valence electrons were treated as H: 1s¹, Li: 2s¹, B: 2s²2p¹, O: 2s²2p⁴, Sr: 4s²4p⁶5s², I: 5s²5p⁵. The k-point of first Brillouin zone for SBIO and LSBIO were sampled as 2 × 2 × 2 and 1 × 1 × 2 Monkhorst-Pack scheme, respectively.^[9] The energy cut-off and convergence criteria were set to 340 and 750 eV for SBIO and LSBIO. The self-consistent convergence of the total energy was 1.0×10^{-6} eV per atom for the two compounds. Because of the commonly underestimate of band gap by DFT, the scissor operator was adopted to make the calculated band gaps consistent with the experimental values.^[10] Based on the scissor-corrected electron band structure, the imaginary part of the dielectric function was calculated according to the electron transition from the valence bands (VB) to conduction band (CB). Consequently, the real part of the dielectric function is obtained by the Kramers-Kronig^[11] transform and the calculated refractive index is determined.

Table S1. Crystal data and structural refinement for SBIO and LSBIO

formula	Sr[B(OH) ₄](IO ₃)	Li ₄ Sr ₅ [B ₁₂ O ₂₂ (OH) ₄](IO ₃) ₂
formula mass (amu)	341.36	1365.41
temperature (K)	293(2)	293(2)
$\lambda(\text{\AA})$	0.71073	0.71073
crystal system	Triclinic	Monoclinic
space group	P	C2/m
a (Å)	6.595(17)	14.245(8)
b(Å)	6.868(16)	11.239(5)
c (Å)	7.120(19)	9.215(5)
α (deg)	96.73(3)	90
β (deg)	108.18(2)	123.625(7)
γ (deg)	92.37(4)	90
V (Å ³)	303.3(13)	1228.5(11)
Z	2	2
ρ (calcd) (g/cm ³)	3.738	3.691
μ (mm ⁻¹)	13.959	13.446
F(000)	312	1256
ϑ (deg)	2.997-27.514	2.869-27.480
index range	-8 ≤ h ≤ 7, -8 ≤ k ≤ 8, -9 ≤ l ≤ 9	-18 ≤ h ≤ 18, -14 ≤ k ≤ 14, -11 ≤ l ≤ 11
Reflections collected / unique	3550/1384	4900/1472
R _{int}	0.0594	0.0316
Completeness to $\theta = 27.42^\circ$ (%)	99.6	99.6
GOF on F^2	1.102	1.098
R_1/wR_2 [$F_o^2 > 2\sigma(F_o^2)$] ^a	0.0395/0.0715	0.0220/0.0504
R_1/wR_2 (all data)	0.0462/0.0757	0.0248/0.0513
Extinction coefficient	0.0052(10)	n/a

^a $R_1(F) = \sum |F_o| - |F_c| | / \sum |F_o|$, $wR_2(F_o^2) = [\sum w(F_o^2 - F_c^2)^2 / \sum w(F_o^2)^2]^{1/2}$.

Table S2. Atomic coordinates ($\times 10^4$) and equivalent isotropic displacement parameters (Å² $\times 10^3$) for SBIO

Atom	x	y	z	U(eq)
I(1)	11963(1)	8998(1)	8954(1)	10(1)
Sr(1)	8883(1)	3538(1)	6932(1)	11(1)
O(1)	3099(7)	2824(7)	8634(7)	16(1)
O(2)	5413(7)	5103(7)	7626(7)	13(1)
O(3)	2036(7)	3563(7)	5283(7)	14(1)
O(4)	12783(7)	8289(7)	6785(7)	15(1)
O(5)	9383(7)	9898(7)	7776(7)	15(1)
O(6)	10979(7)	6646(7)	9320(7)	14(1)
O(7)	5258(7)	1774(7)	6527(8)	16(1)
B(1)	3931(13)	3320(12)	6948(12)	15(2)

U(eq) is defined as one third of the trace of the orthogonalized U_{ij} tensor.

Table S3. Selected bond lengths (Å) and angles (degrees) for SBIO

I(1)-O(6)	1.794(6)	O(2)-B(1)	1.469(10)
I(1)-O(4)	1.811(6)	O(3)-B(1)	1.460(9)
I(1)-O(5)	1.816(5)	O(7)-B(1)	1.466(9)
Sr(1)-O(7)	2.552(7)	O(6)-I(1)-O(4)	100.2(2)
Sr(1)-O(6)	2.607(6)	O(6)-I(1)-O(5)	97.4(2)
Sr(1)-O(5)#3	2.649(7)	O(4)-I(1)-O(5)	100.3(3)
Sr(1)-O(3)#4	2.657(7)	O(3)-B(1)-O(7)	115.2(7)
Sr(1)-O(6)#1	2.660(9)	O(3)-B(1)-O(2)	112.5(6)
Sr(1)-O(4)#5	2.661(8)	O(7)-B(1)-O(2)	104.2(6)
Sr(1)-O(3)#6	2.689(7)	O(3)-B(1)-O(1)	105.9(6)
Sr(1)-O(2)	2.724(7)	O(7)-B(1)-O(1)	109.0(6)
Sr(1)-O(1)#6	2.755(8)	O(2)-B(1)-O(1)	110.0(6)
O(1)-B(1)	1.532(10)		

Symmetry transformations used to generate equivalent atoms:

#1 -x+2,-y+1,-z+2	#2 x,y+1,z	#3 x,y-1,z	#4 -x+1,-y+1,-z+1
#5 -x+2,-y+1,-z+1	#6 x+1,y,z	#7 x-1,y,z	

Table S4. Anisotropic displacement parameters ($\text{\AA}^2 \times 10^3$) for SBIO

The anisotropic displacement factor exponent takes the form: $-2\pi^2 [h^2 a^{*2} U_{11} + \dots + 2hka^* b^* U_{12}]$

	U11	U22	U33	U23	U13	U12
I(1)	11(1)	11(1)	9(1)	4(1)	2(1)	2(1)
Sr(1)	12(1)	13(1)	9(1)	5(1)	3(1)	2(1)
O(1)	13(3)	21(3)	14(3)	4(2)	4(2)	-5(2)
O(2)	13(3)	11(3)	14(3)	8(2)	2(2)	3(2)
O(3)	14(3)	7(3)	17(3)	0(2)	-2(2)	3(2)
O(4)	16(1)	15(1)	14(1)	1(1)	6(1)	1(1)
O(5)	12(3)	19(3)	13(3)	9(2)	-1(2)	7(2)
O(6)	20(3)	10(3)	11(3)	4(2)	3(2)	0(2)
O(7)	15(3)	14(3)	22(3)	7(2)	9(2)	4(2)
B(1)	14(4)	16(5)	15(5)	4(4)	3(4)	3(4)

Table S5. Hydrogen coordinates ($\times 10^4$) and isotropic displacement parameters ($\text{\AA}^2 \times 10^3$) for SBIO

	x	y	z	U(eq)
H(1)	4510(20)	2770(110)	9300(40)	24
H(2)	4650(40)	6090(30)	7550(80)	19
H(3)	1890(110)	2460(60)	4560(100)	22
H(7)	4550(50)	660(20)	6350(110)	24

Table S6. Atomic coordinates ($\times 10^4$) and equivalent isotropic displacement parameters ($\text{\AA}^2 \times 10^3$) for LSBIO

Atom	x	y	z	U(eq)
Sr(1)	2136(1)	2024(1)	7374(1)	8(1)
Sr(2)	5000	0	5000	12(1)
I(1)	2208(1)	0	4209(1)	5(1)
Bi(1)	3957(3)	1121(4)	11219(5)	7(1)
Bi(2)	2095(4)	0	9974(7)	5(1)
Bi(3)	5000	2148(5)	10000	7(1)
Bi(4)	-288(3)	-2146(4)	7139(5)	7(1)
O(1)	523(2)	2962(2)	7372(3)	7(1)
O(2)	2694(3)	0	6503(4)	7(1)
O(3)	2746(2)	1090(2)	10529(3)	8(1)
O(4)	1360(3)	0	7958(4)	7(1)
O(5)	-1292(3)	0	9485(4)	8(1)
O(6)	4531(3)	0	12024(4)	7(1)
O(7)	4097(2)	1409(2)	9802(3)	9(1)
O(8)	3143(2)	1186(2)	4405(3)	12(1)
O(9)	-518(2)	-2089(2)	8425(3)	8(1)
O(10)	-772(2)	-1383(2)	5787(3)	9(1)
Li(1)	4196(7)	0	8402(11)	9(2)
Li(2)	0	0	5000	37(4)
Li(3)	0	787(17)	10000	16(4)

U(eq) is defined as one third of the trace of the orthogonalized U_{ij} tensor.

Table S7. Selected bond lengths (Å) and angles (degrees) for LSBIO

Sr(1)-O(8)#1	2.484(3)	B(4)-O(1)#7	1.395(4)
Sr(1)-O(7)	2.523(3)	B(4)-O(9)	1.397(5)
Sr(1)-O(1)	2.527(3)	O(2)-Li(1)	1.869(9)
Sr(1)-O(10)#2	2.552(3)	O(4)-Li(2)	2.309(3)
Sr(1)-O(2)	2.676(2)	O(5)-Li(3)	1.852(9)
Sr(1)-O(4)	2.710(2)	O(5)-Li(3)#15	1.852(9)
Sr(1)-O(3)	2.741(3)	O(6)-Li(1)#5	2.058(9)
Sr(1)-O(3)#3	2.810(3)	O(7)-Li(1)	2.095(6)
Sr(1)-O(9)#4	3.084(3)	O(7)-Li(1)#5	2.589(7)
Sr(2)-O(6)#5	2.437(4)	O(9)-Li(3)#15	1.899(15)
Sr(2)-O(6)#6	2.437(4)	O(10)-Li(2)	2.244(2)
Sr(2)-O(8)	2.733(3)	O(8)-I(1)-O(8)#7	94.08(17)
Sr(2)-O(8)#7	2.733(3)	O(8)-I(1)-O(2)	95.59(10)
Sr(2)-O(8)#8	2.733(3)	O(8)#7-I(1)-O(2)	95.59(10)
Sr(2)-O(8)#9	2.733(3)	O(6)-B(1)-O(7)	109.2(3)
Sr(2)-O(1)#10	2.962(3)	O(6)-B(1)-O(3)	113.0(3)
Sr(2)-O(1)#11	2.962(3)	O(7)-B(1)-O(3)	109.1(3)
Sr(2)-O(1)#1	2.962(3)	O(6)-B(1)-O(1)#3	106.5(3)
Sr(2)-O(1)#12	2.962(3)	O(7)-B(1)-O(1)#3	112.1(3)
I(1)-O(8)	1.822(2)	O(3)-B(1)-O(1)#3	106.9(3)
I(1)-O(8)#7	1.822(2)	O(3)#7-B(2)-O(3)	115.5(4)
I(1)-O(2)	1.823(3)	O(3)#7-B(2)-O(5)#15	110.2(3)
B(1)-O(6)	1.461(4)	O(3)-B(2)-O(5)#15	110.2(3)
B(1)-O(7)	1.463(5)	O(3)#7-B(2)-O(4)	107.4(3)
B(1)-O(3)	1.471(4)	O(3)-B(2)-O(4)	107.4(3)
B(1)-O(1)#3	1.493(5)	O(5)#15-B(2)-O(4)	105.6(4)
B(2)-O(3)#7	1.449(4)	O(7)-B(3)-O(7)#14	110.4(4)
B(2)-O(3)	1.449(4)	O(7)-B(3)-O(9)#16	112.31(13)
B(2)-O(5)#15	1.479(6)	O(7)#14-B(3)-O(9)#16	106.29(13)
B(2)-O(4)	1.547(6)	O(7)-B(3)-O(9)#4	106.29(13)
B(3)-O(7)	1.454(4)	O(7)#14-B(3)-O(9)#4	112.31(13)
B(3)-O(7)#14	1.454(4)	O(9)#16-B(3)-O(9)#4	109.3(4)
B(3)-O(9)#16	1.483(4)	O(10)-B(4)-O(1)#7	121.2(3)
B(3)-O(9)#4	1.483(4)	O(10)-B(4)-O(9)	121.0(3)
B(4)-O(10)	1.346(5)	O(1)#7-B(4)-O(9)	117.6(3)

Symmetry transformations used to generate equivalent atoms:

```
#1 -x+1/2,-y+1/2,-z+1 #2 -x,-y,-z+1 #3 -x+1/2,-y+1/2,-z+2 #4 x+1/2,y+1/2,z #5 -x+1,-y,-z+2 #6 x,y,z-1 #7 x,-y,z
#8 -x+1,y,z+1 #9 -x+1,-y,z+1 #10 x+1/2,-y+1/2,z #11 -x+1/2,y-1/2,-z+1 #12 x+1/2,y-1/2,z #13 x,-y,z-1 #14 -x+1,y,-z+2 #15 -x,-y,z+2
#16 -x+1/2,y+1/2,-z+2 #17 x,y,z+1 #18 x-1/2,y+1/2,z #19 x-1/2,y-1/2,z #20 -x,y,-z+1
```

Table S8. Anisotropic displacement parameters (Å²×10³) for LSBIOThe anisotropic displacement factor exponent takes the form: $-2\pi^2 [h^2 a^{*2} U_{11} + \dots + 2hka^* b^* U_{12}]$

	U11	U22	U33	U23	U13	U12
Sr(1)	10(1)	6(1)	7(1)	1(1)	5(1)	2(1)
Sr(2)	9(1)	20(1)	7(1)	0	5(1)	0
I(1)	5(1)	5(1)	5(1)	0	3(1)	0
B(1)	6(2)	9(2)	9(2)	-1(2)	5(2)	0(2)
B(2)	2(2)	8(3)	3(3)	0	1(2)	0
B(3)	12(3)	5(3)	6(3)	0	6(2)	0
B(4)	5(2)	6(2)	10(2)	-3(2)	3(2)	-4(1)
O(1)	9(1)	9(1)	5(1)	-2(1)	4(1)	-3(1)
O(2)	8(2)	10(2)	2(2)	0	3(1)	0
O(3)	6(1)	5(1)	12(1)	0(1)	5(1)	0(1)
O(4)	6(2)	9(2)	6(2)	0	3(1)	0
O(5)	10(2)	10(2)	9(2)	0	7(2)	0
O(6)	6(2)	6(2)	6(2)	0	1(1)	0
O(7)	9(1)	12(1)	4(1)	-3(1)	4(1)	-6(1)
O(8)	9(1)	12(1)	14(1)	1(1)	7(1)	-7(1)
O(9)	12(1)	7(1)	9(1)	4(1)	8(1)	4(1)
O(10)	12(1)	7(1)	9(1)	2(1)	6(1)	2(1)
Li(1)	12(4)	6(4)	11(4)	0	8(4)	0
Li(2)	22(8)	66(13)	19(8)	0	8(7)	0
Li(3)	23(10)	14(10)	18(10)	0	16(9)	0

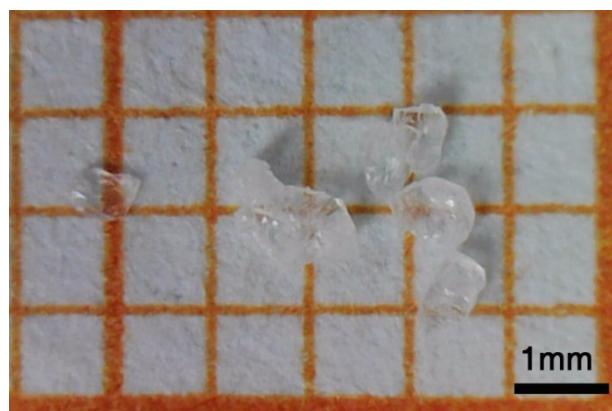


Figure S1. Crystal picture of SBIO.

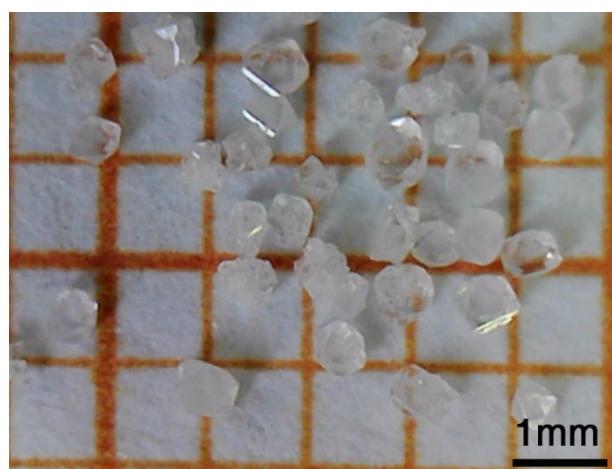


Figure S2. Crystal picture of LSBIO.

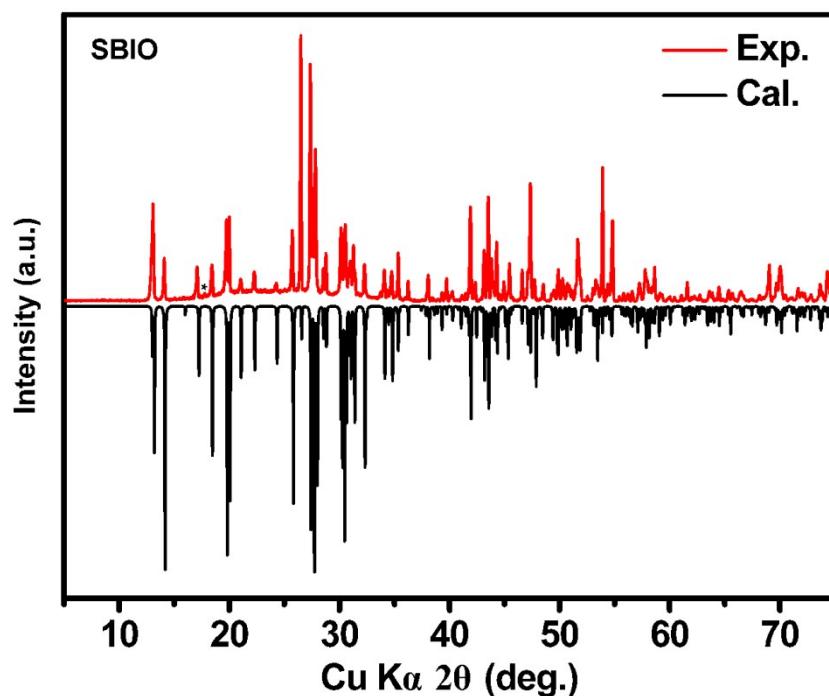


Figure S3. Calculated and experimental powder X-ray diffraction patterns of SBIO. The reflections marked with an asterisk may result from Sr(OH)₂ (PDF-27-0847).

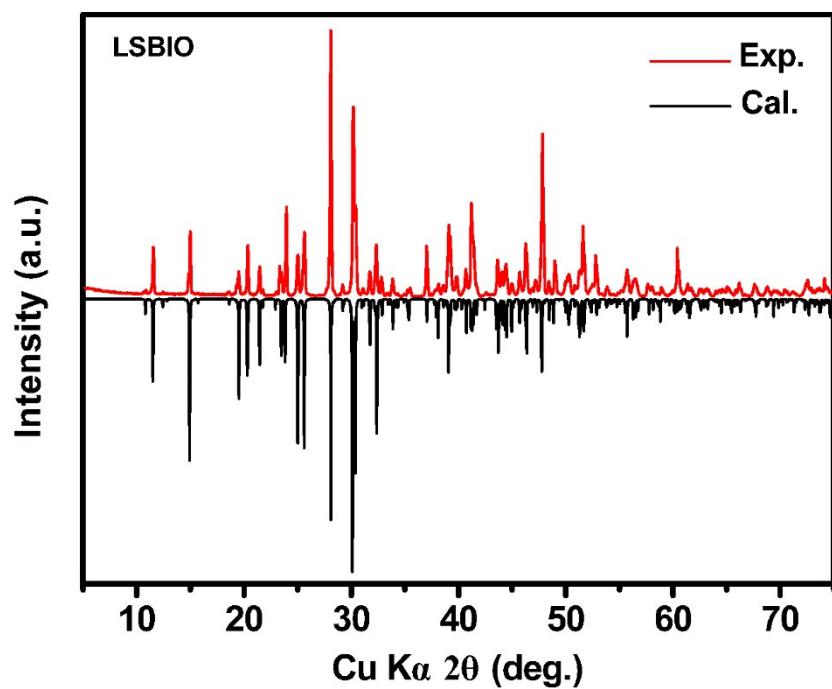


Figure S4. Calculated and experimental powder X-ray diffraction patterns of LSBIO

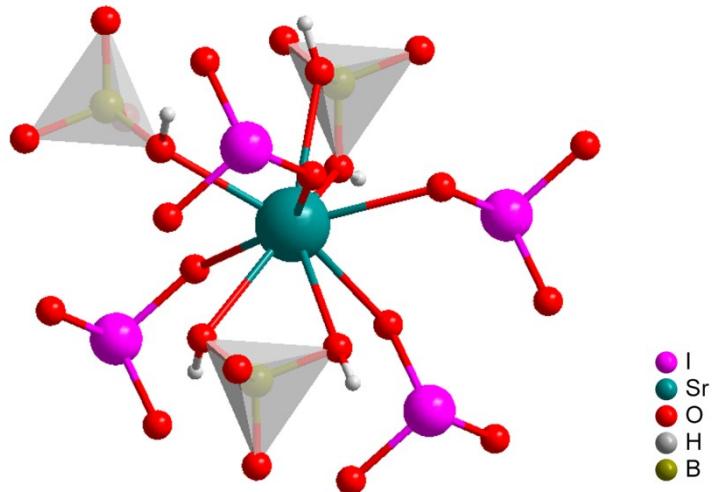


Figure S5. Coordination mode of a Sr^{2+} in SBIO

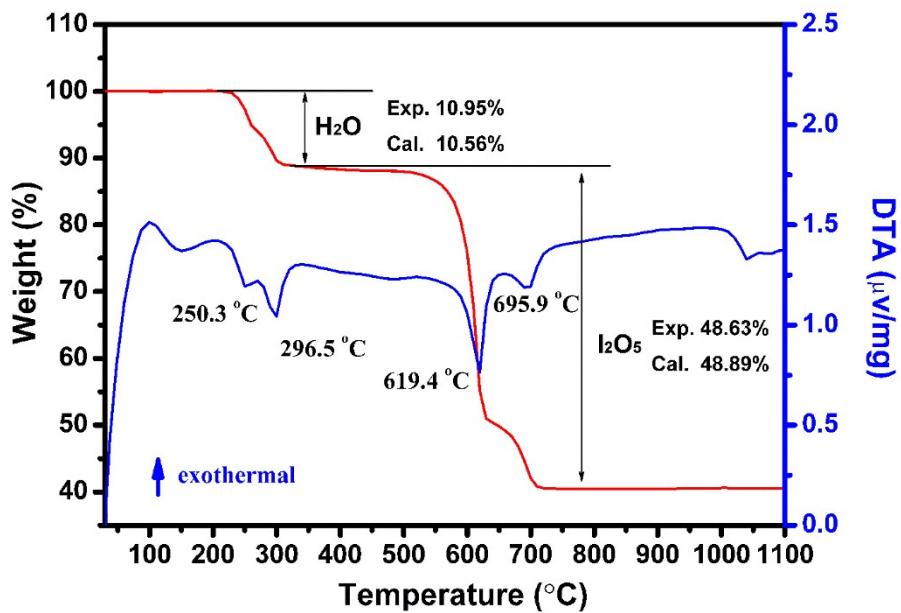


Figure S6. TGA and DTA curves of SBIO

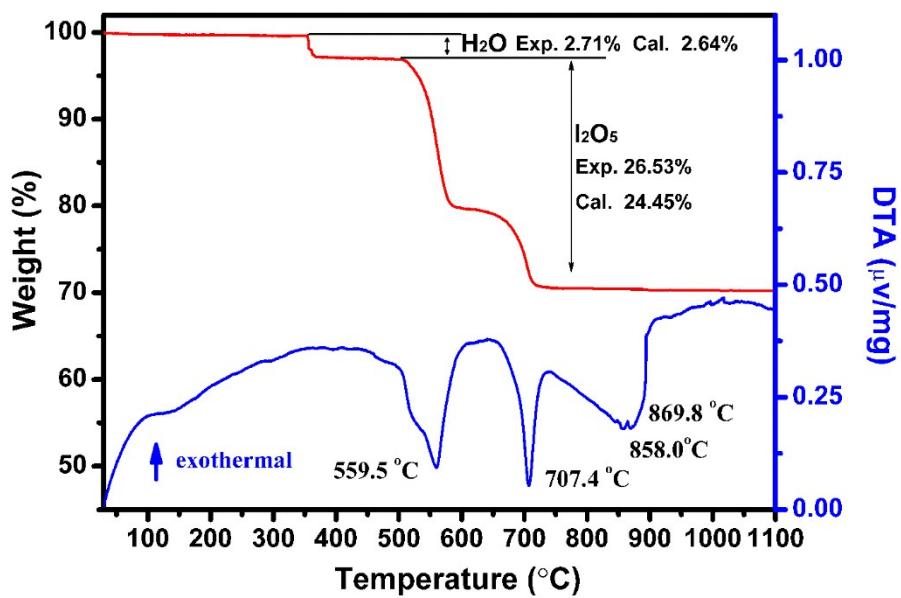


Figure S7. TGA and DTA curves of LSBIO

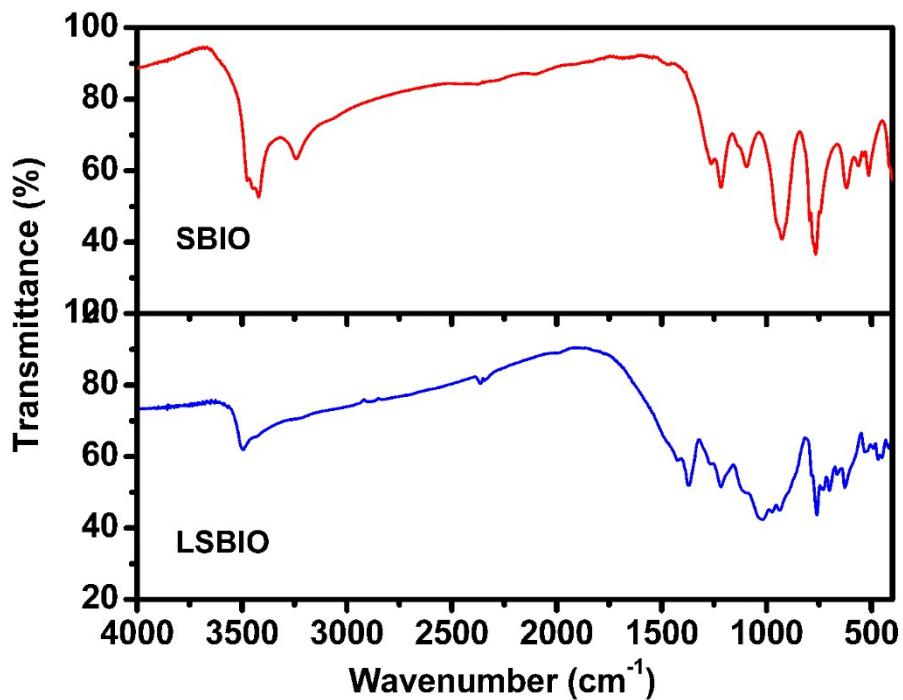


Figure S8. IR absorption spectra of SBIO and LSBIO

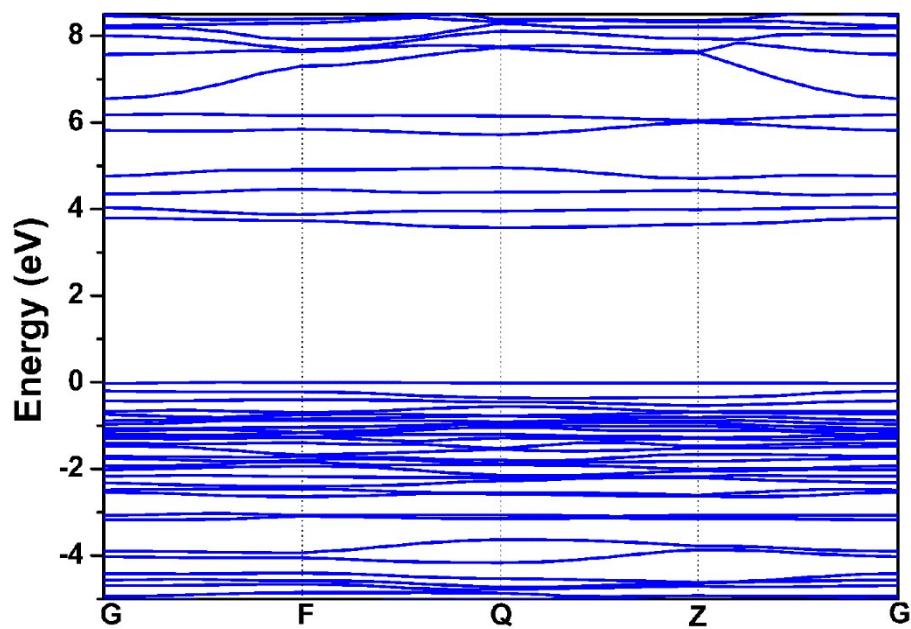


Figure S9. Calculated electronic band structure for SBIO

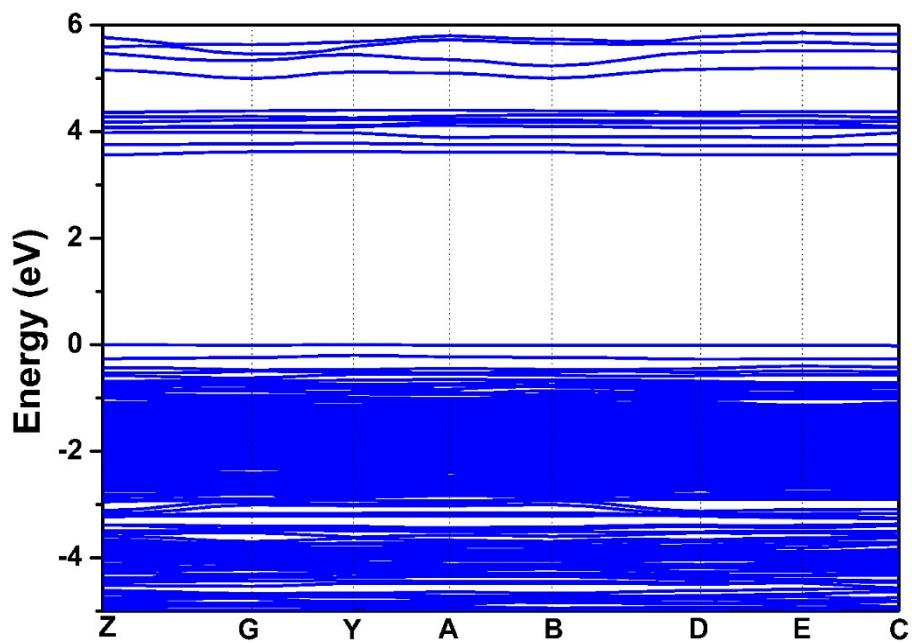


Figure S10. Calculated electronic band structure for LSBIO

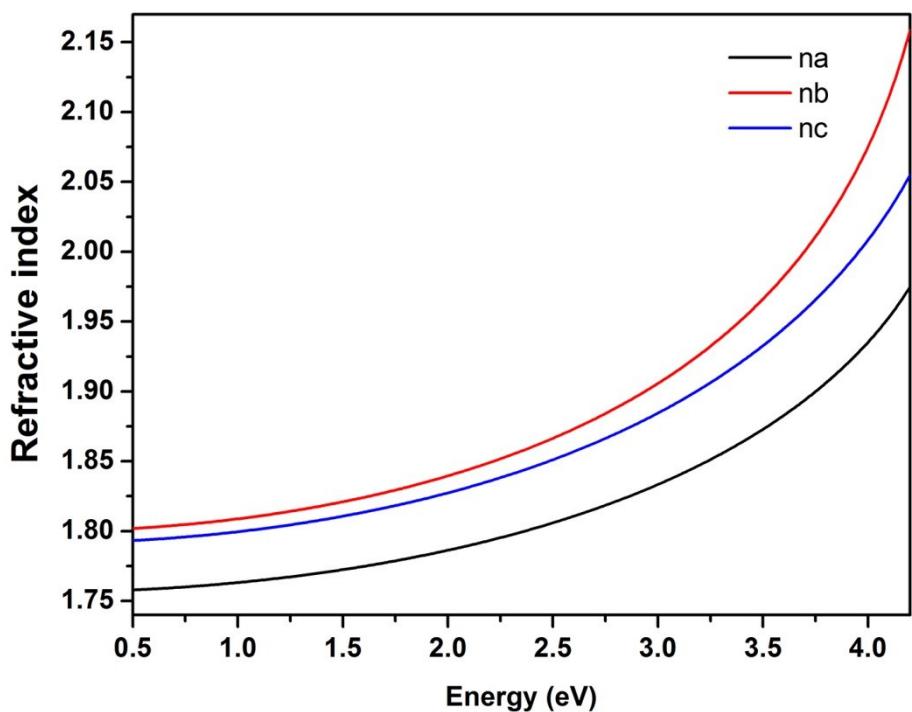


Figure S11. Calculated refractive index dispersion curves for SBIO

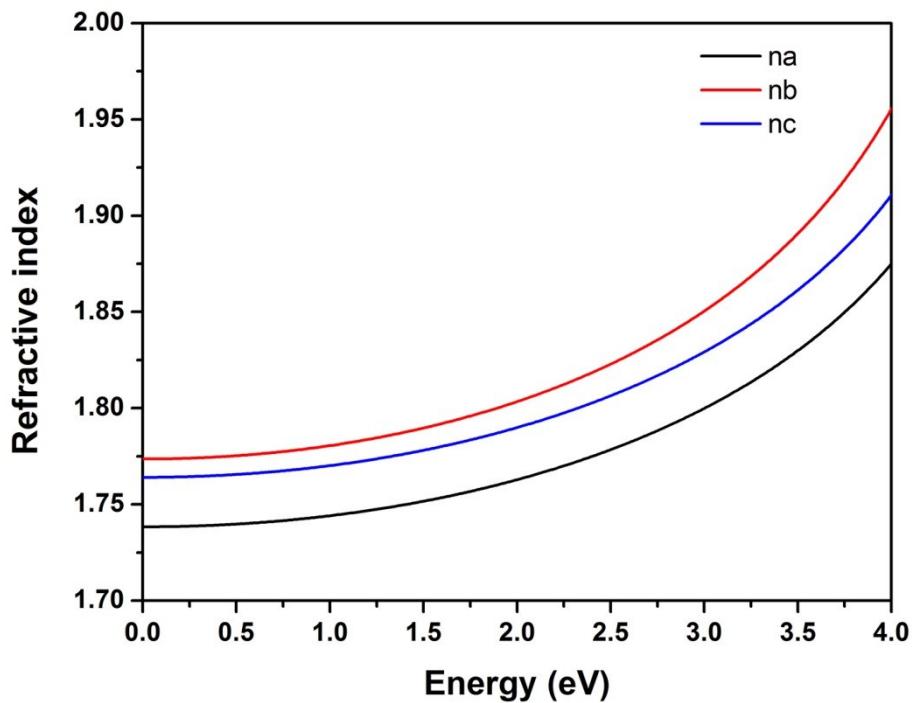


Figure S12. Calculated refractive index dispersion curves for LSBIO

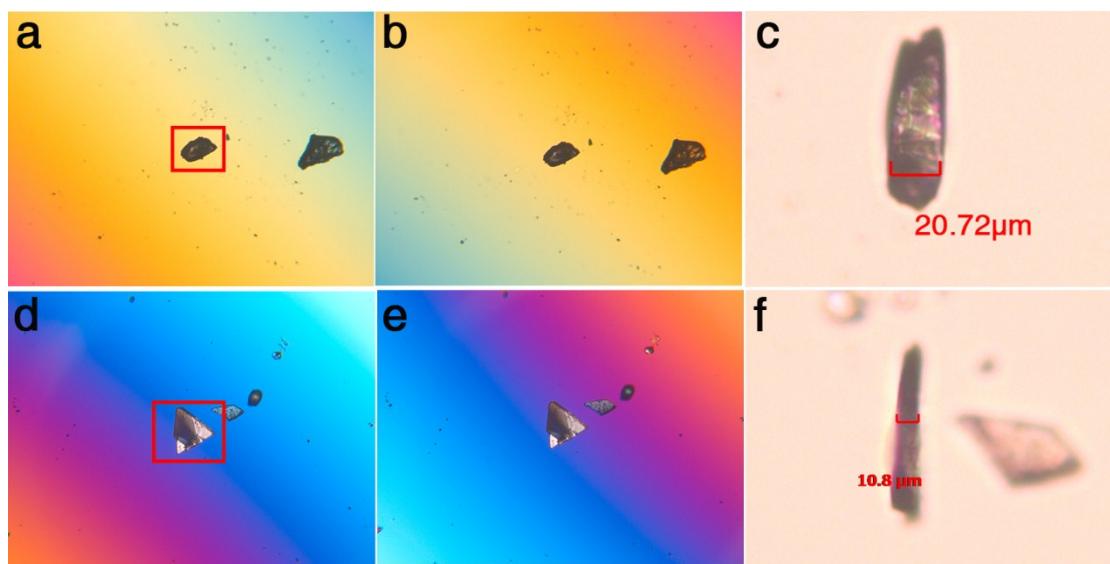


Figure S13. Photograph of LSBIO (a-c) and SBIO (d-f) for the measurement of birefringence

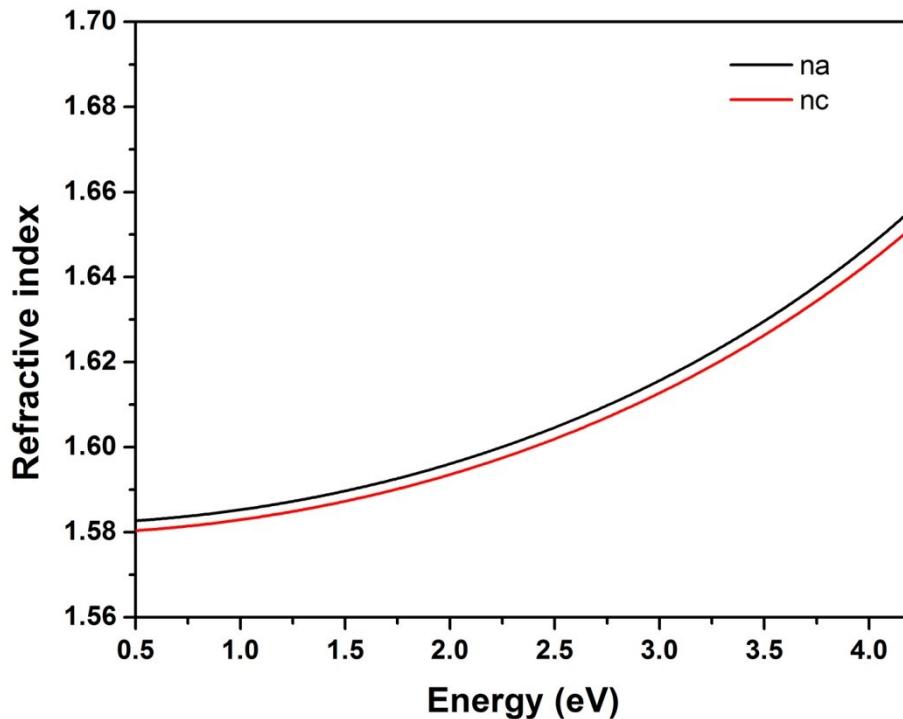


Figure S14. Calculated refractive index dispersion curves for $\text{Li}_3\text{KB}_4\text{O}_8$

References

- [1] G. M. Sheldrick, *Acta Crystallogr., Sect. A: Found. Crystallogr.* 2008, **64**, 112-122.
- [2] G. M. Sheldrick, *Acta Cryst.* 2015, **C71**, 3-8.
- [3] A. L. Spek, *J. Appl. Crystallogr.* 2003, **36**, 7-13.
- [4] P. Kubelka, F. Z. Munk, *Tech. Phys.* 1931, **12**, 593-601.
- [5] J. Tauc, *Mater. Res. Bull.* 1970, **5**, 721-729.
- [6] S. J. Clark, M. D. Segall, C. J. Pickard, P. J. Hasnip, M. J. Probert, K. Refson, M. C. Payne, *Z. Kristallogr. - Cryst. Mater.* 2005, **220**, 567-570.
- [7] M. C. Payne, M. P. Teter, D. C. Allan, T. A. Arias, J. D. Joannopoulos, *Rev. Mod. Phys.* 1992, **64**, 1045-1097.
- [8] J. P. Perdew, K. Burke, M. Ernzerhof, *Phys. Rev. Lett.*, 1996, **77**, 3865 - 3868.
- [9] H. J. Monkhorst, J. D. Pack, *Phys. Rev. B* 1976, **13**, 5188-5192.
- [10] R. W. Godby, M. Schluter, L. Sham, *J. Phys. Rev. B* 1988, **37**, 10159-10175.
- [11] E. D. Palik, *Handbook of Optical Constants of Solids*, Academic Press, New York, 1985.