

**The Interplay among Molecular Structures,  
Crystal Symmetries and Lattice Energy  
Landscapes Revealed by Unsupervised Machine  
Learning: A Closer Look at Pyrrole  
Azaphenacenes  
Supporting Information**

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# Sketch-Maps

Table 1

Molecule	$\Delta E_{latt}$ (kJ/mol)	Number of Structures
<b>1</b>	10	774
<b>2</b>	20	202
<b>3</b>	10	475
<b>4</b>	25	887
<b>5</b>	20	627
<b>6</b>	15	1144
<b>7</b>	40	310
<b>8</b>	25	923
<b>9</b>	15	364
<b>10</b>	15	703
<b>11</b>	15	1349
<b>12</b>	15	635
<b>13</b>	15	1174
<b>14</b>	15	844
<b>15</b>	15	1395
<b>16</b>	15	1574
<b>17</b>	15	513
<b>18</b>	15	686
<b>19</b>	15	855
<b>20</b>	15	451
<b>21</b>	15	1266
<b>22</b>	15	782
<b>23</b>	15	306
<b>24</b>	15	1195

# Molecule 1

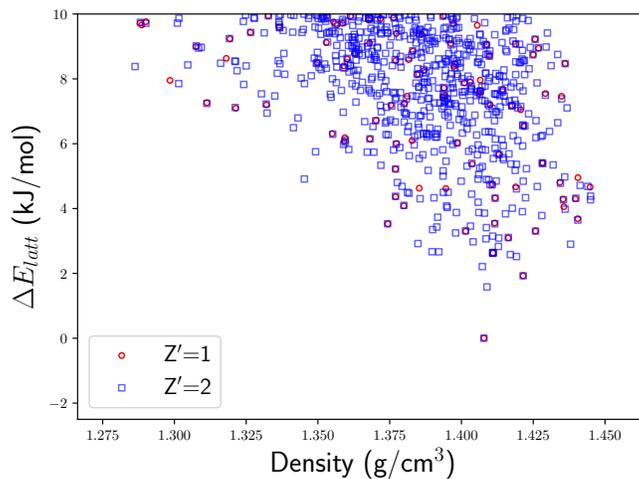


Figure 1: Energy–density plot for the predicted crystal structures for molecule **1** in both  $Z' = 1$  and  $Z' = 2$  settings.

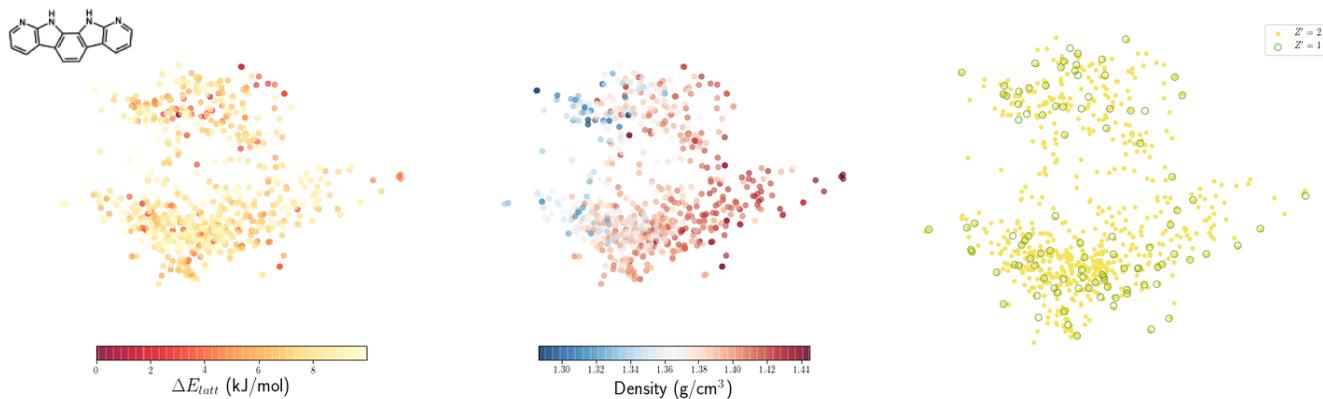


Figure 2: Sketch–map representation of the lattice for molecule **1**, with each point colour–coded according to (left) lattice energy difference to the global minimum, (middle) density and (right)  $Z'$  number. SOAP–REMatch kernel were calculated with  $r_c = 3 \text{ \AA}$ .

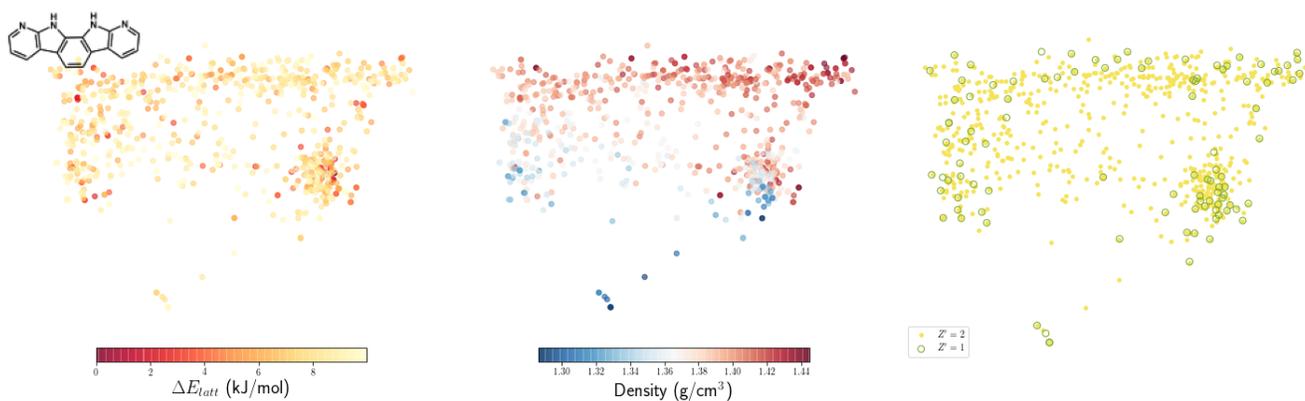


Figure 3: Sketch-map representation of the lattice for molecule **1**. SOAP-REMatch kernel were calculated with  $r_c = 5 \text{ \AA}$ .

## Molecule 2

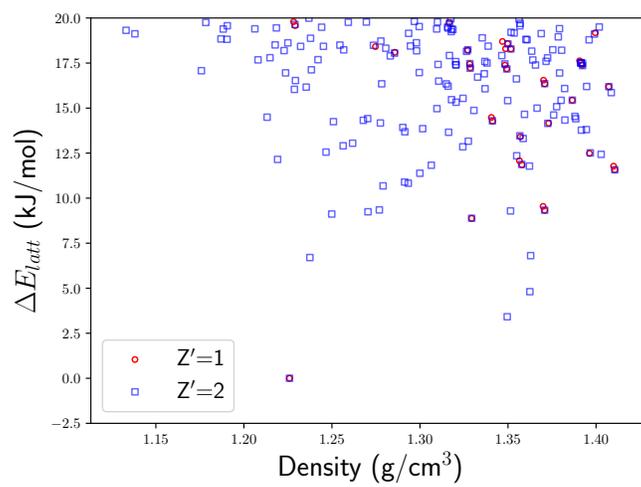


Figure 4: Energy–density plot for the predicted crystal structures for molecule **2** in both  $Z' = 1$  and  $Z' = 2$  settings.

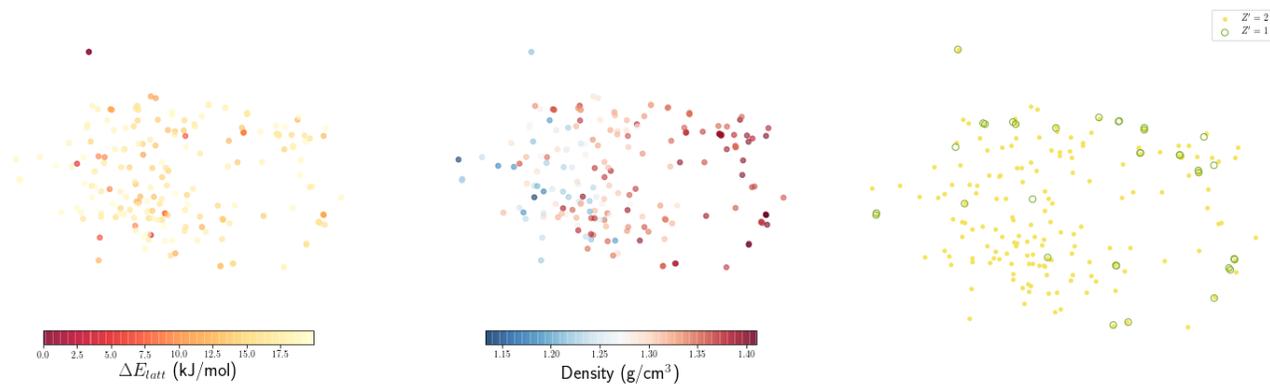


Figure 5: Sketch-map representation of the crystal packing landscapes for molecule **2**, with  $r_c = 3$  Å.

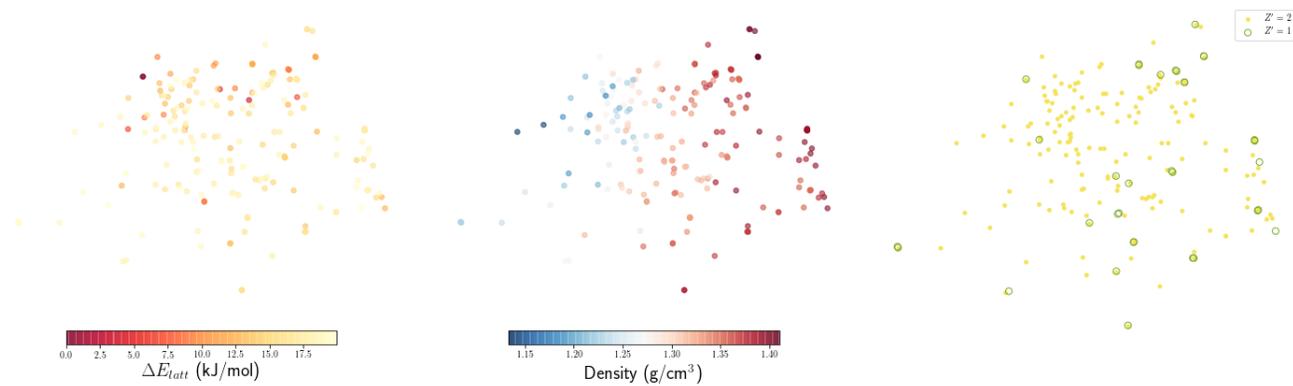


Figure 6: Sketch-map representation of the crystal packing landscapes for molecule **2**, with  $r_c = 5$  Å.

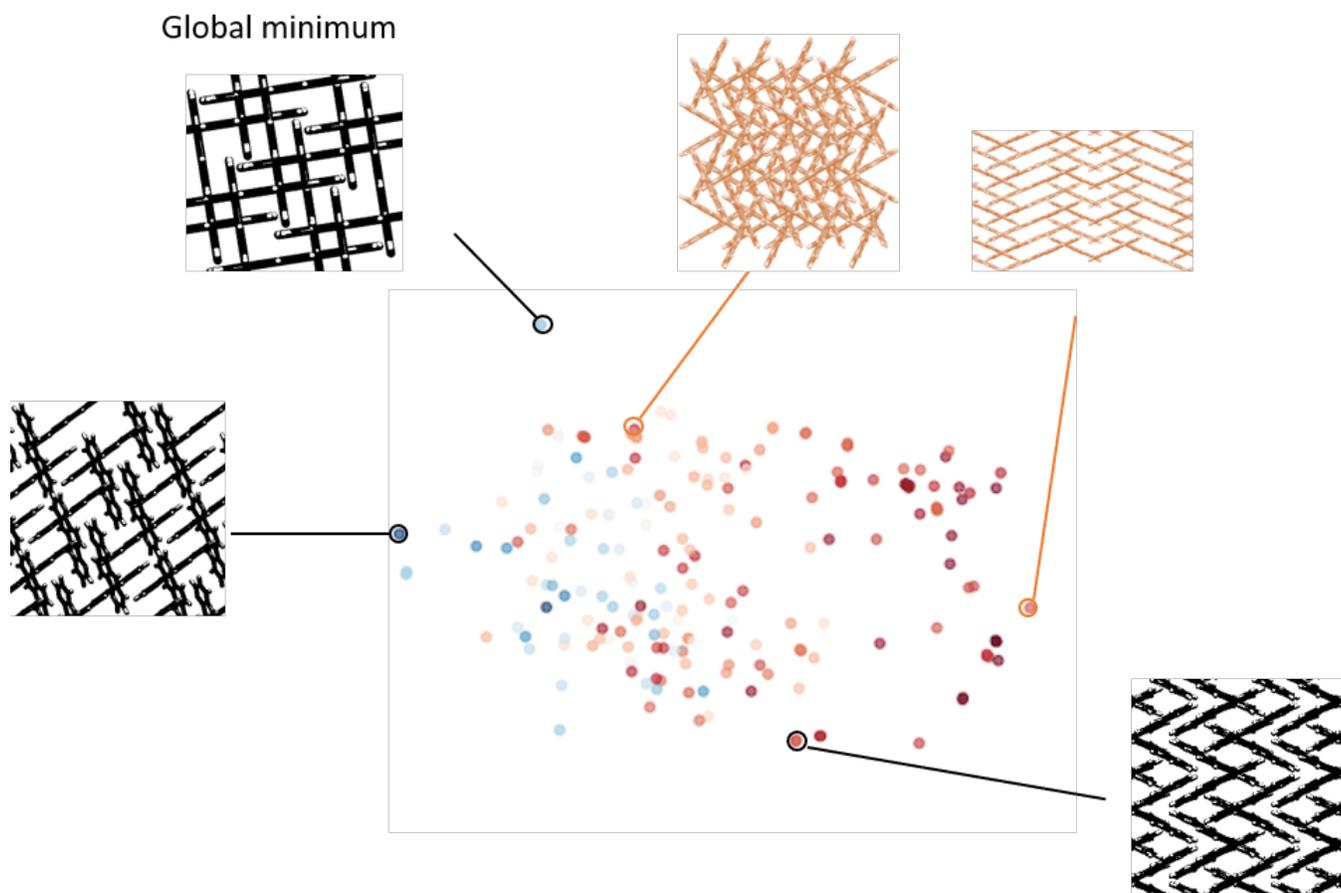


Figure 7: Sketch-map representation of the crystal packing landscapes for molecule 4 with SOAP-REMatch kernel calculated using  $r_c = 3 \text{ \AA}$ . Each point is colour-coded according to the density of the crystal [identical to Fig. 5 (middle)].

## Molecule 3

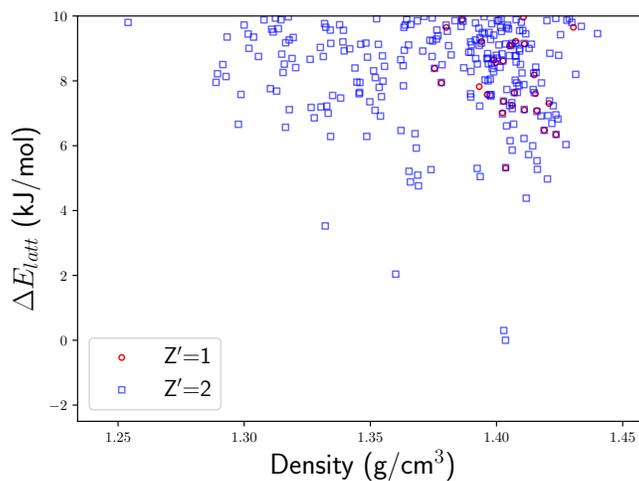


Figure 8: Energy–density plot for the predicted crystal structures for molecule **3** in both  $Z' = 1$  and  $Z' = 2$  settings.

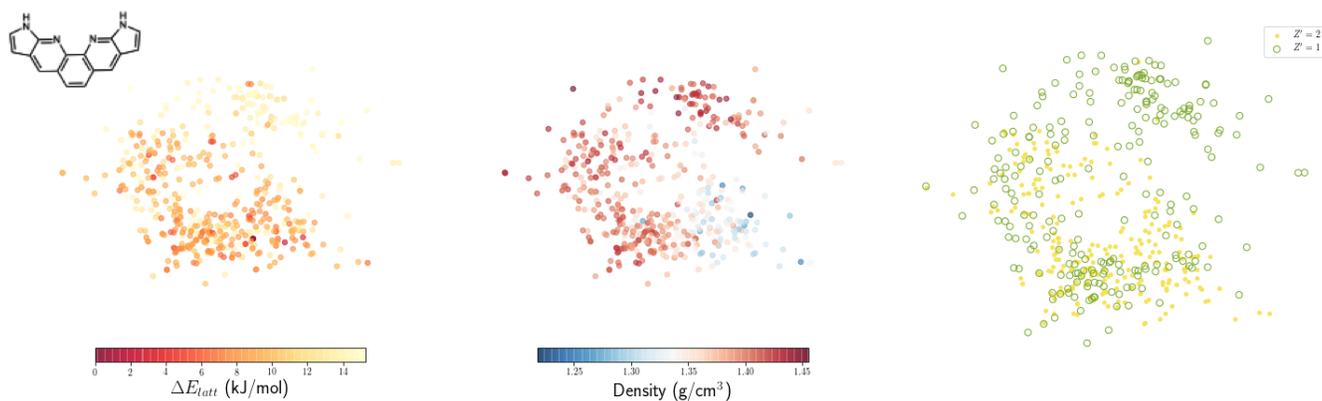


Figure 9: Sketch–map representation of the crystal packing landscapes for molecule **3** with  $r_c = 3$  Å

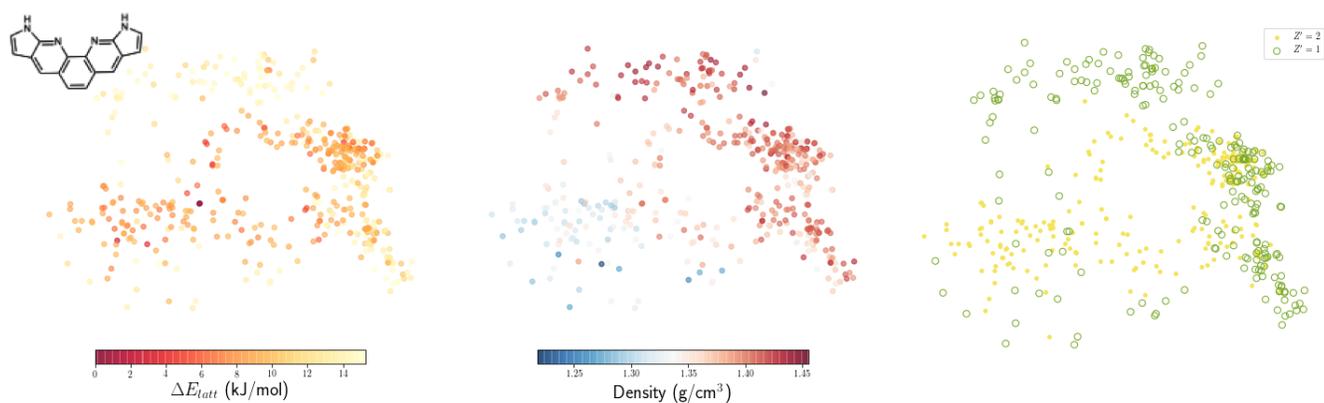


Figure 10: Sketch-map representation of the crystal packing landscapes for molecule **3** with  $r_c = 5 \text{ \AA}$

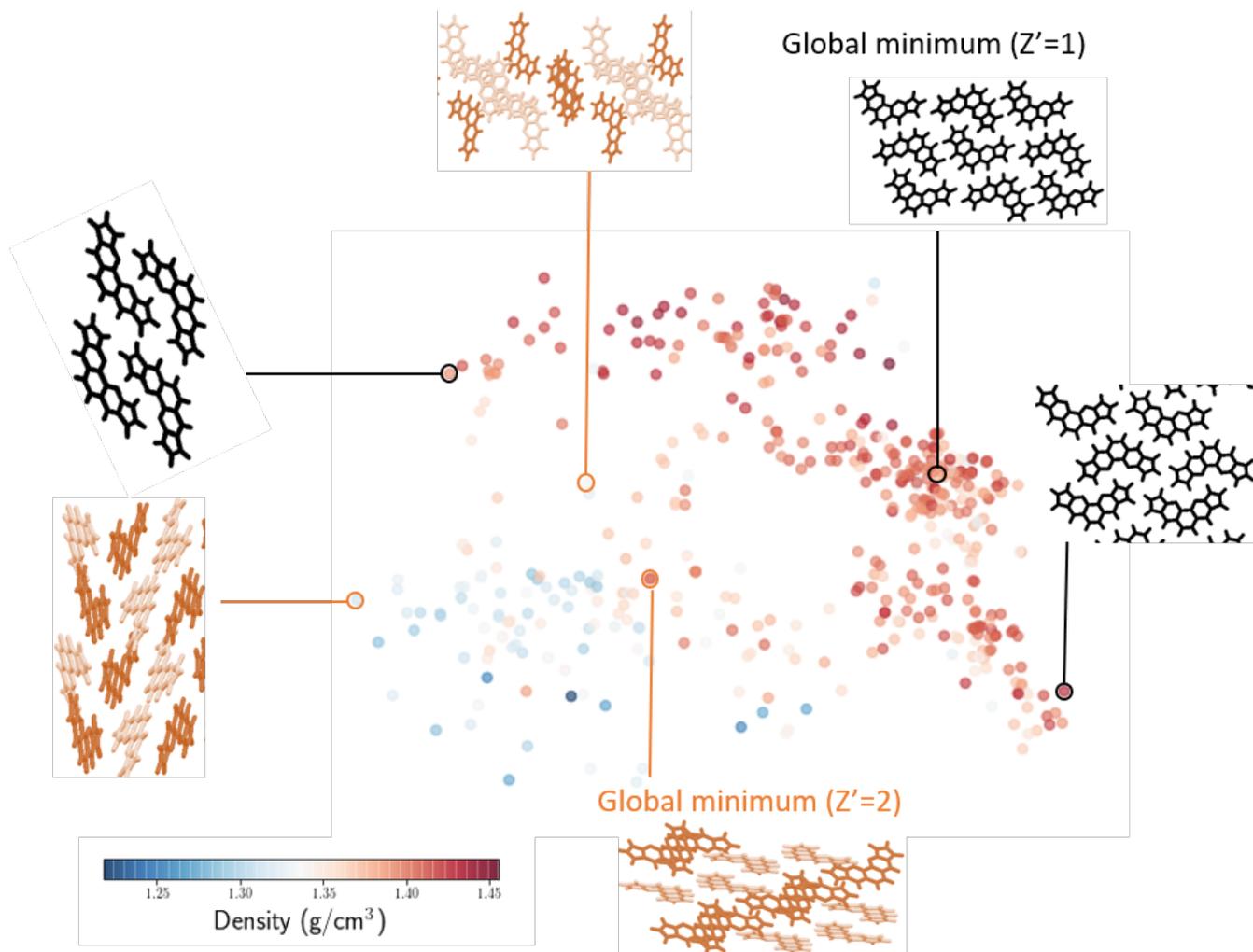


Figure 11: Sketch-map representation of the crystal packing landscapes for molecule **9** with SOAP-REMatch kernel calculated using  $r_c = 5 \text{ \AA}$ . Each point is colour-coded according to the density of the crystal [identical to Fig. 10 (middle)]. Structure(s) that are only found in the  $Z' = 1$  (2) searches are coloured in black (orange), whereas structures coloured in blue are found from both  $Z' = 1$  and 2 searches. For structures coloured in orange, the dark and light colouring corresponds to two symmetry unrelated molecules in the unit cell.

## Molecule 4

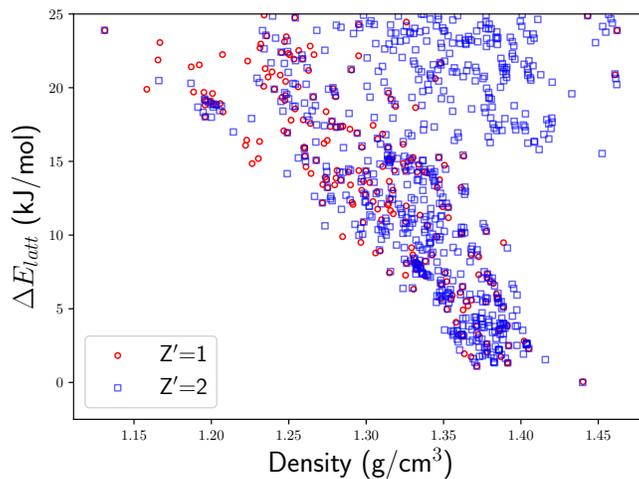


Figure 12: Energy–density plot for the predicted crystal structures for molecule 4 in both  $Z' = 1$  and  $Z' = 2$  settings.

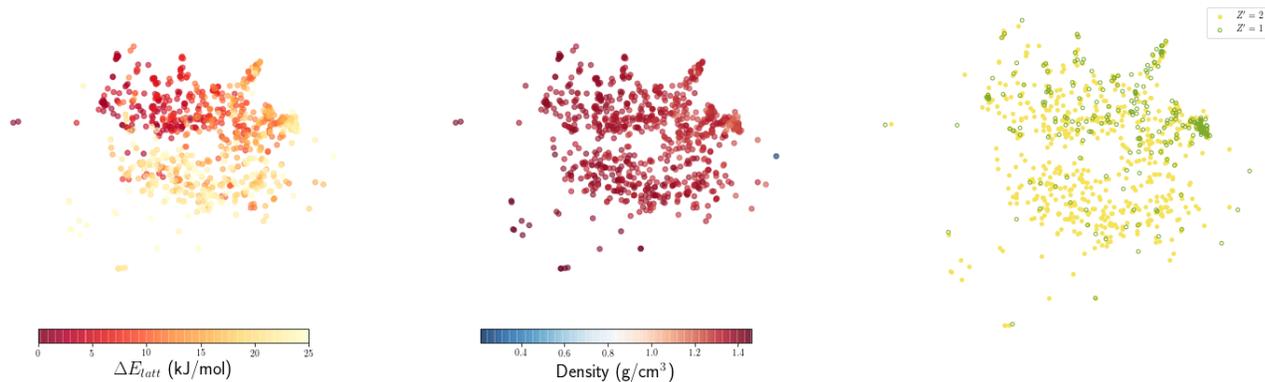


Figure 13: Sketch–map representation of the crystal packing landscapes for molecule 4 with  $r_c = 3$  Å.

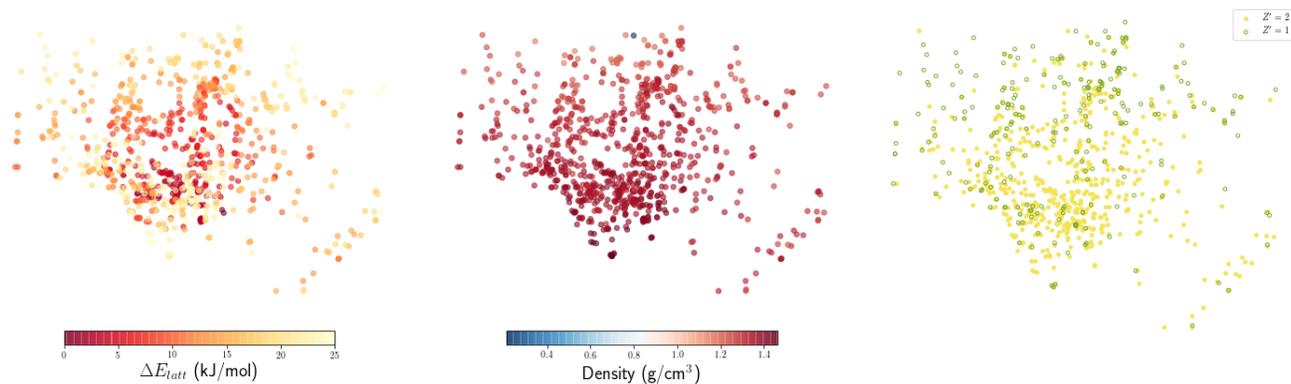


Figure 14: Sketch-map representation of the crystal packing landscapes for molecule **4** with  $r_c = 5$  Å.

## Molecule 5

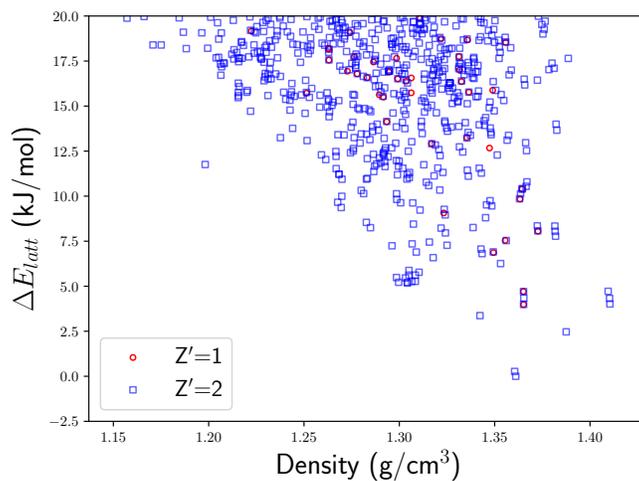


Figure 15: Energy–density plot for the predicted crystal structures for molecule **5** in both  $Z' = 1$  and  $Z' = 2$  settings.

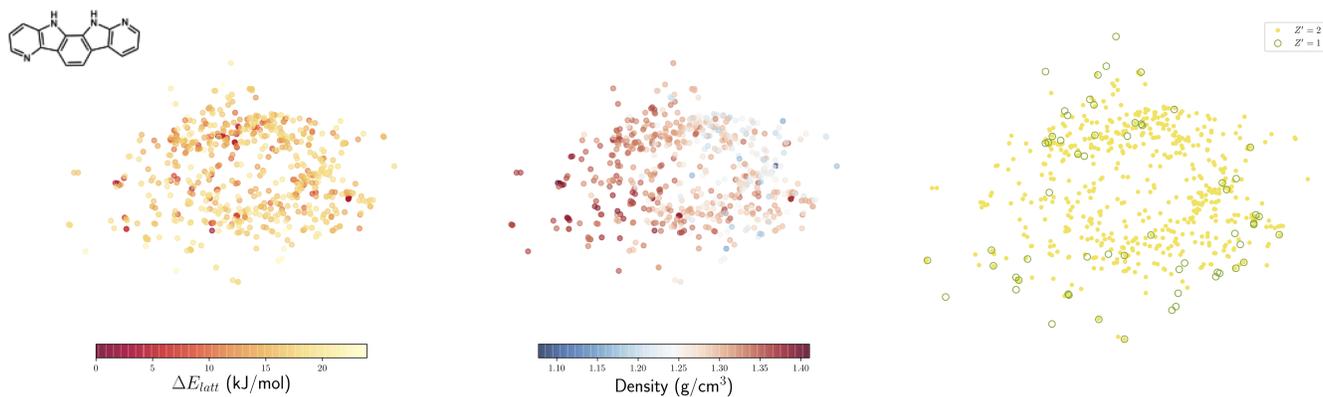


Figure 16: Sketch–map representation of the crystal packing landscapes for molecule **5** with  $r_c = 3$  Å.

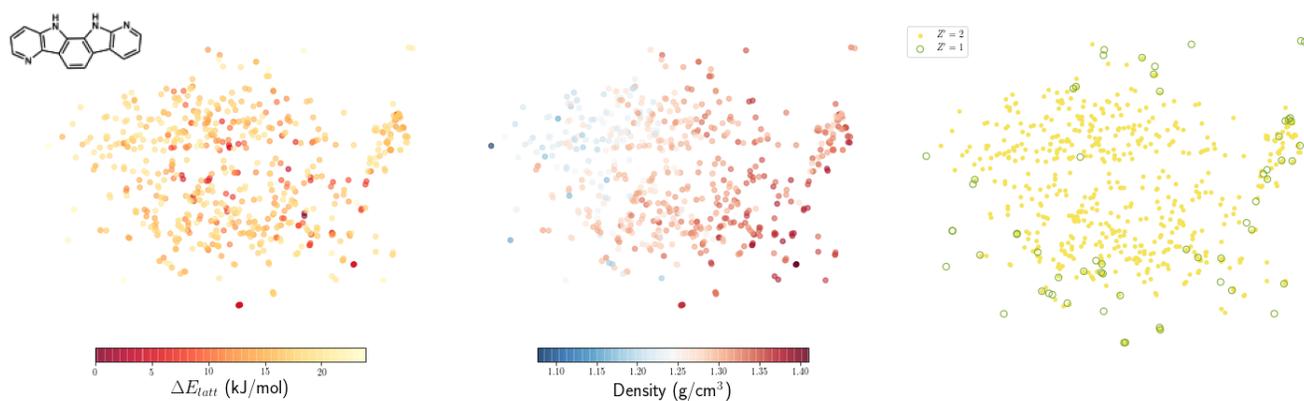


Figure 17: Sketch-map representation of the crystal packing landscapes for molecule **5** with  $r_c = 5$  Å.

## Molecule 6

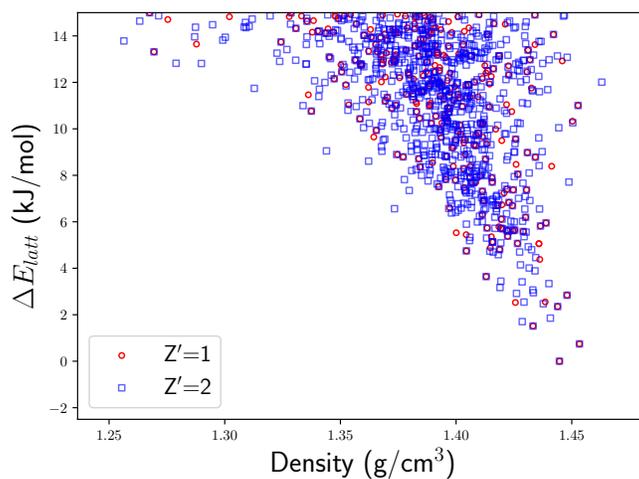


Figure 18: Energy–density plot for the predicted crystal structures for molecule **6** in both  $Z' = 1$  and  $Z' = 2$  settings.

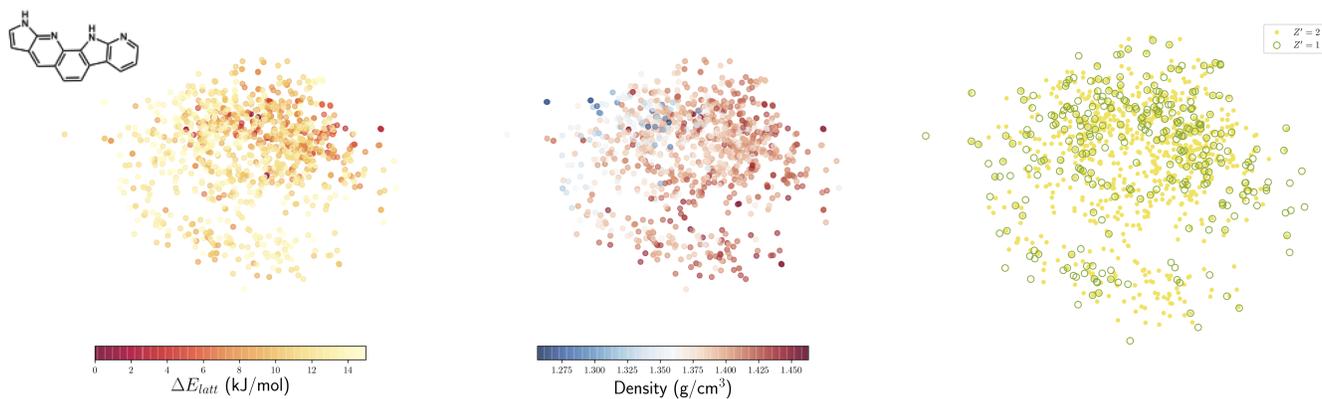


Figure 19: Sketch–map representation of the crystal packing landscapes for molecule **6** with  $r_c = 3$  Å.

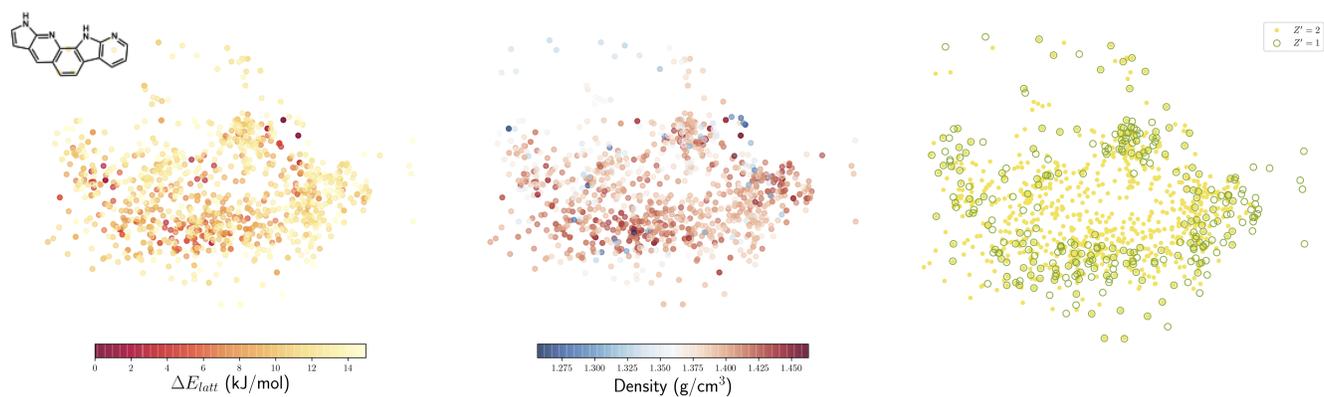


Figure 20: Sketch-map representation of the crystal packing landscapes for molecule **6** with  $r_c = 5$  Å.

## Molecule 7

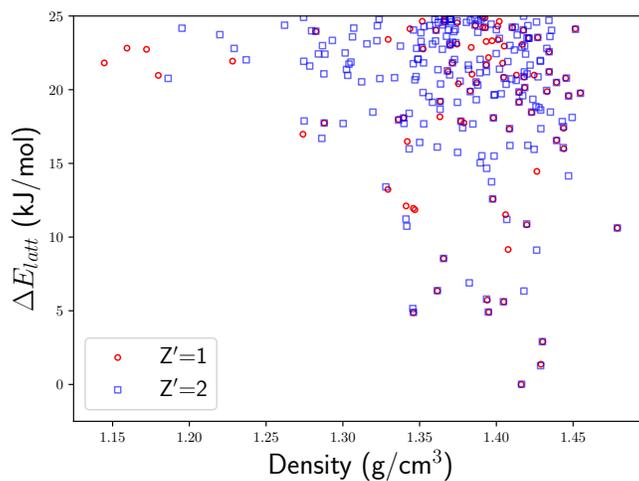


Figure 21: Energy–density plot for the predicted crystal structures for molecule **7** in both  $Z' = 1$  and  $Z' = 2$  settings.

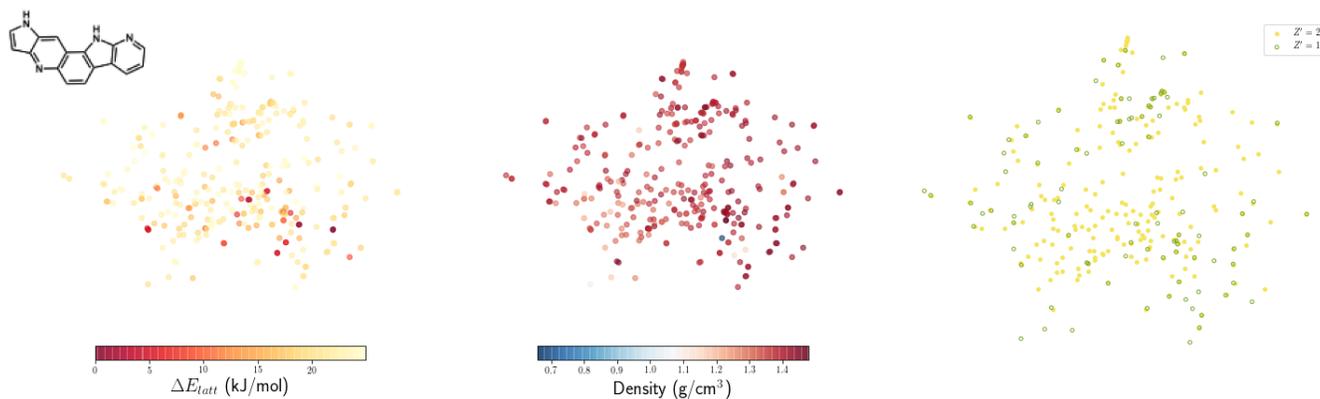


Figure 22: Sketch–map representation of the crystal packing landscapes for molecule **7** with  $r_c = 3$  Å.

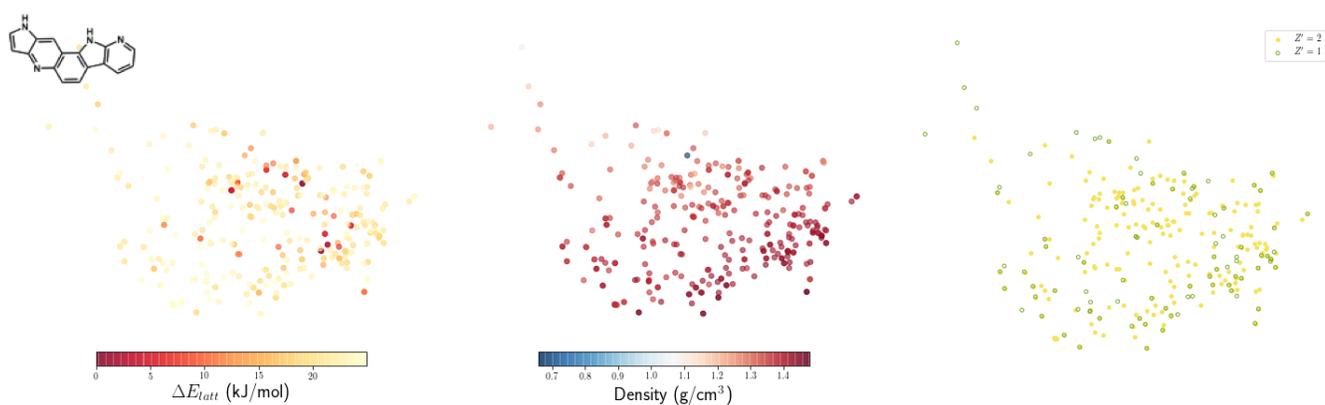


Figure 23: Sketch-map representation of the crystal packing landscapes for molecule **7** with  $r_c = 5$  Å.

## Molecule 8

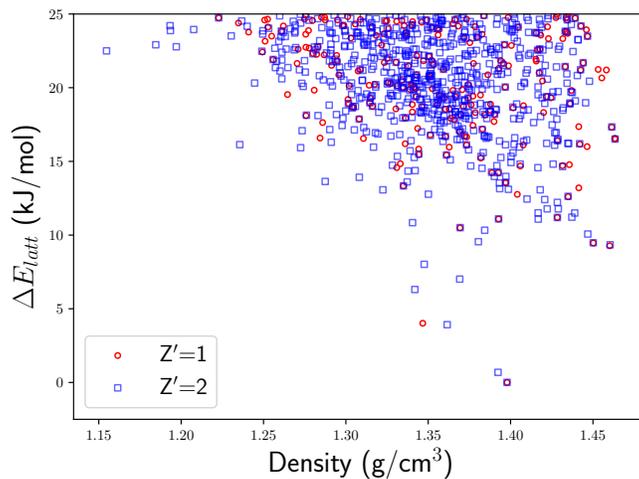


Figure 24: Energy–density plot for the predicted crystal structures for molecule **8** in both  $Z' = 1$  and  $Z' = 2$  settings.

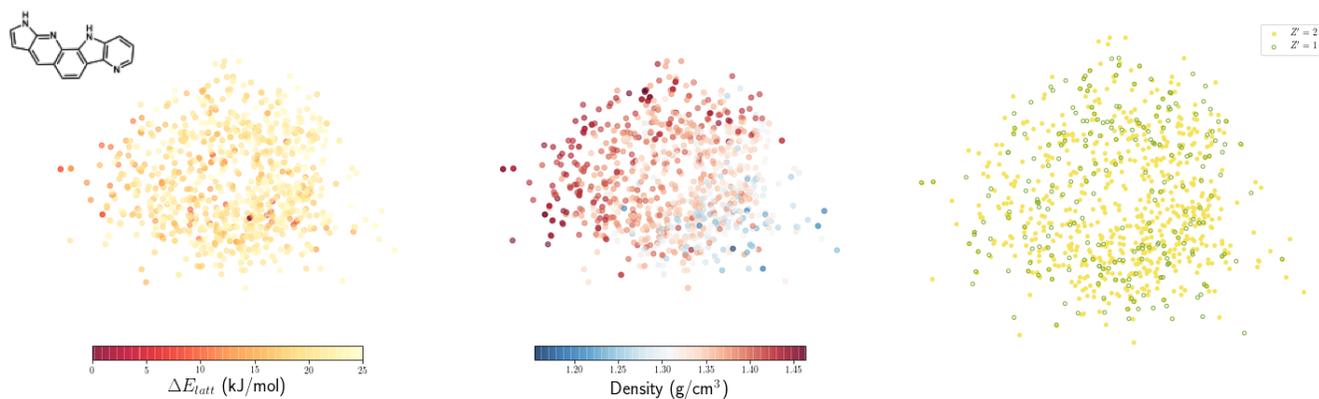


Figure 25: Sketch–map representation of the crystal packing landscapes for molecule **8** with  $r_c = 3$  Å.

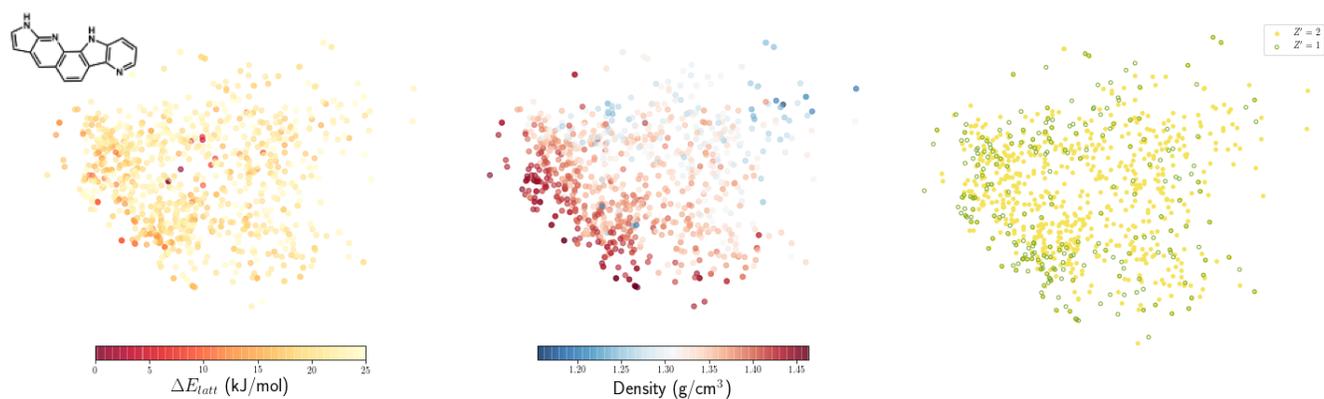


Figure 26: Sketch-map representation of the crystal packing landscapes for molecule **8** with  $r_c = 5$  Å.

# Halogen Substituted Pyrrole Azaphenacenes

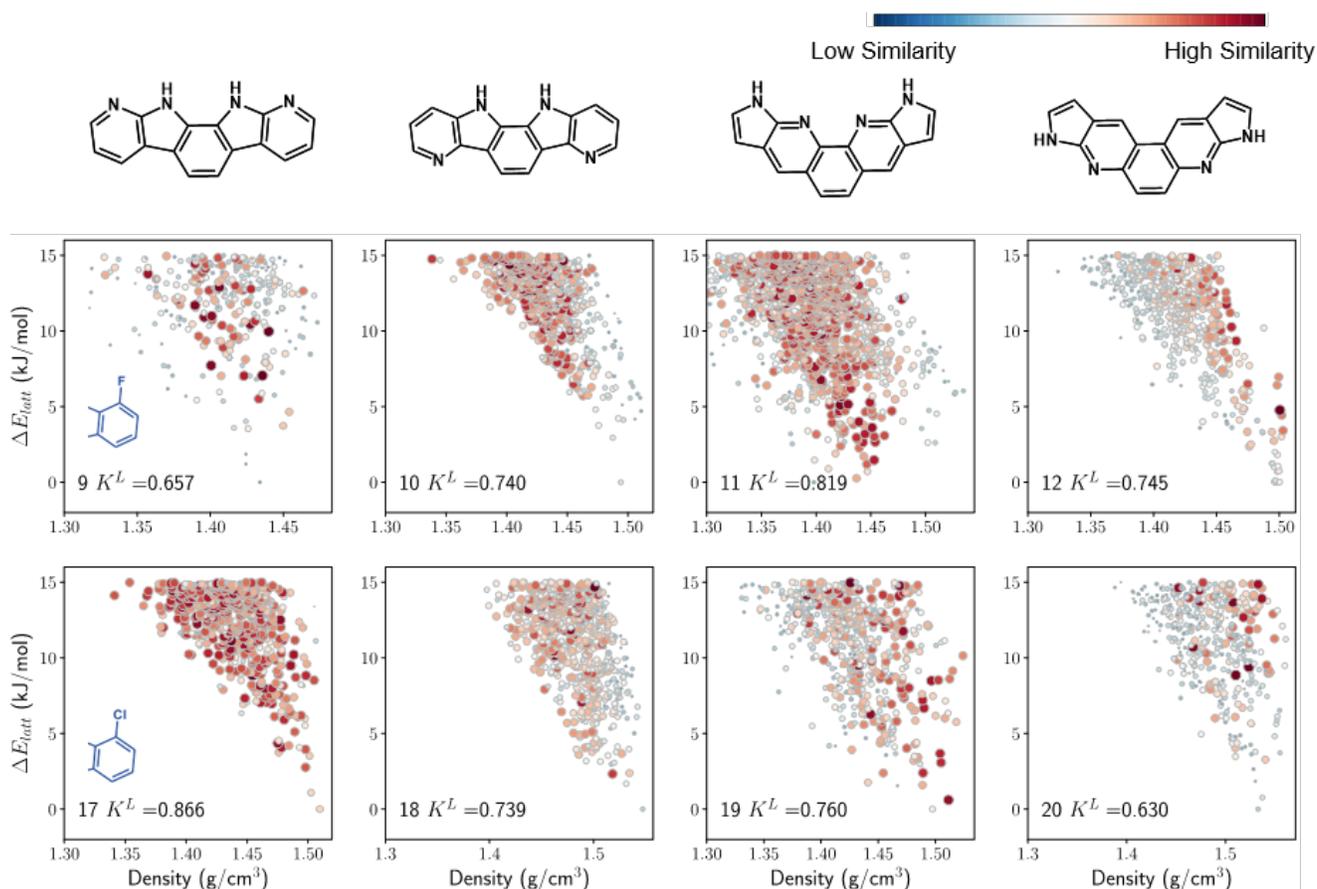


Figure 27: Energy–density plots of halogen–substituted symmetric pyrrole azaphenacenes, with each point sized and color–coded according to the normalized similarity scores with respect to the reference crystal structures [the global minimum of unsubstituted pyrrole azaphenacenes (top row) in  $Z' = 1$  settings]. The SOAP–REMatch kernels are calculated with  $r_c = 3 \text{ \AA}$  and  $\gamma = 1$  to highlight the similarities in short–range atomic environments.

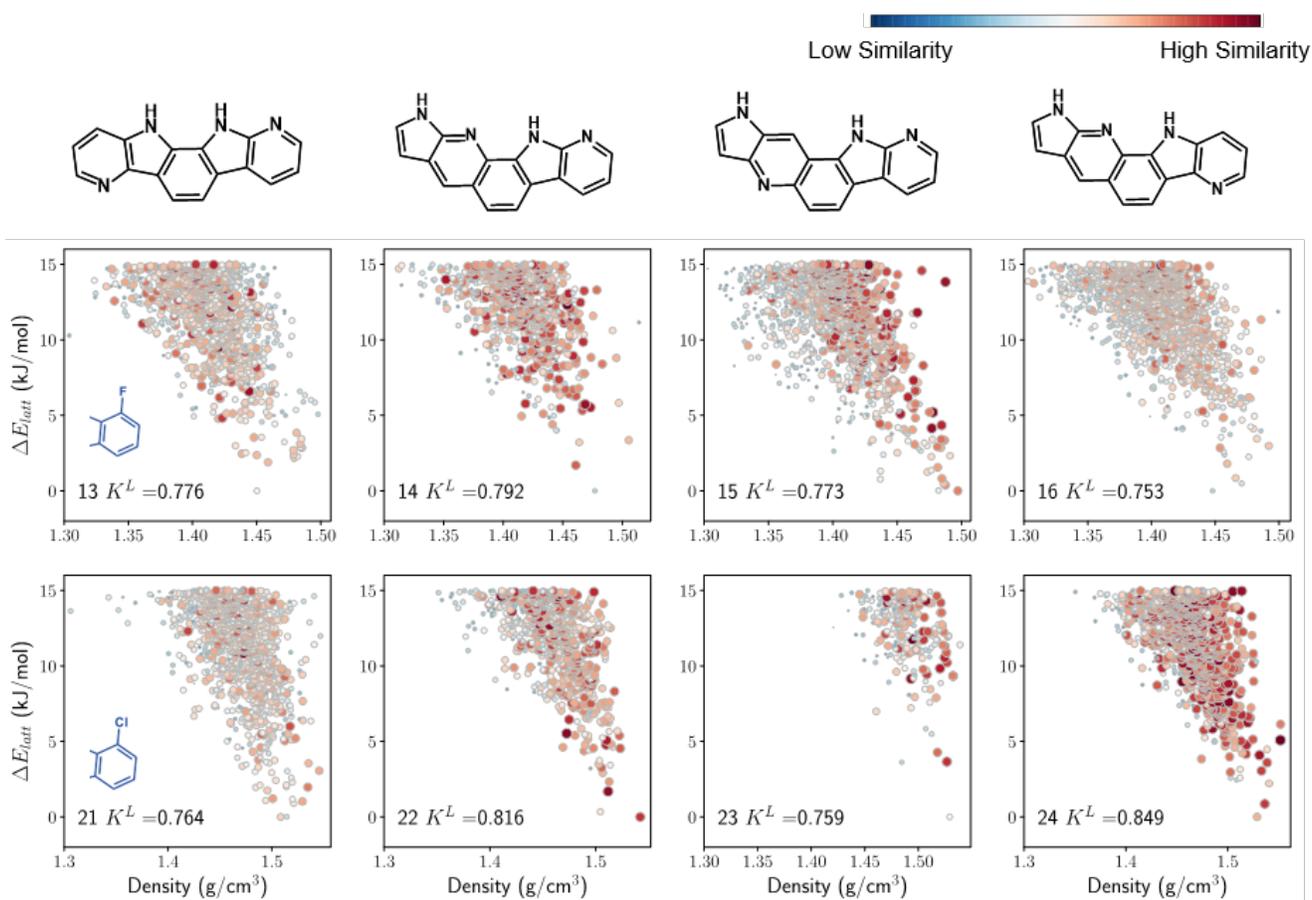


Figure 28: Energy–density plots of halogen–substituted asymmetric pyrrole azaphenacenes, with each point sized and color–coded according to the normalized similarity scores with respect to the reference crystal structures [the global minimum of unsubstituted pyrrole azaphenacenes (top row) in  $Z' = 1$  settings]. The SOAP–REMatch kernels are calculated with  $r_c = 3 \text{ \AA}$  and  $\gamma = 1$  to highlight the similarities in short–range atomic environments.