

Water flow in carbon nanotubes: The role of tube chirality

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1 Simulation details

In classical molecular dynamics (MD) motion of the atoms are described by Newtonian equations of motion. The equation of motion of a particle i with mass m and position r acted upon by a net force F is given by:

$$m_i \frac{d^2 \mathbf{r}_i}{dt^2} = F_i(t) \quad (1)$$

where F_i can be expressed as the gradient of the potential energy (U):

$$F_i(r_1, r_2, \dots, r_N) = -\nabla U(r_1, r_2, \dots, r_N) \quad (2)$$

The potential energy consists of bonded $U(\vec{r})$ and non-bonded $U(r_{ij})$ interactions. In our study, we used the harmonic potentials for the bond stretching and angle bending interactions.

$$U(\vec{r}) = \sum_{\text{bond}} \frac{k_{\text{bond}}}{2} (r - r_0)^2 + \sum_{\text{angle}} \frac{k_{\text{angle}}}{2} (\theta - \theta_0)^2 \quad (3)$$

where k_{bond} and k_{angle} are the coefficients of the harmonic potentials of the bond stretching and angle bending, respectively. r_0 and θ_0 represents the reference bond length and angle. Non-bonded terms include van der Waals (vdW) and electrostatic interactions, which were modeled using 12-6 Lennard-Jones (LJ) and coulombic potentials, respectively.

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Table S1: Interaction parameters used for the study.

Parameter	Value
l_{OH} (nm)	0.1
θ_{OH}	109.47
$q_H(e)$	0.4238
$q_O(e)$	-0.8476
σ_{OO} (nm)	0.3166
ϵ_{OO} (kcal/mol)	0.15535
σ_{CO} (nm)	0.3190
ϵ_{CO} (kcal/mol)	0.09369

$$U(r_{ij}) = \sum_{i=1}^N \sum_{j=i+1}^N \left(4\epsilon_{ij} \left[\left(\frac{\sigma}{r} \right)^{12} - \left(\frac{\sigma}{r} \right)^6 \right] + \frac{q_i q_j}{4\pi\epsilon_0 r_{ij}} \right) \quad (4)$$

We performed MD simulations using the LAMMPS software package. [1] Carbon-carbon interactions are modeled with the reactive empirical bond order (REBO) potential [2], which has been widely used to study graphene and CNTs. SPC/E model was used for water molecules, whose bulk property predictions agree well with experiments [3]. Fluid-wall Lennard-Jones interaction parameters were taken from Werder *et al.* [4], and the interactions were truncated at a distance of 1 nm. Long range electrostatic interactions were handled by the Wolf method, [5, 6] using a 1 nm cutoff and a damping parameter of 2.25 nm^{-1} . The parameters for the interaction potentials are given in TABLE I.

Simulations were performed in the NVT ensemble at 300 K temperature. We coupled the Nosé-Hoover thermostat to the CNT walls to maintain the average system temperature. The Nosé-Hoover thermostat modulates the kinetic temperature by coupling the system to a “fictitious” heat bath (η) of mass Q . The average system temperature approaches the target value by scaling the velocities of each particle by a factor P_η . The equation of motion of a particle can be written as:

$$\frac{d^2 \mathbf{r}_i}{dt^2} = \frac{\mathbf{F}_i(\mathbf{r}_i)}{m_i} - \frac{P_\eta}{Q} \frac{d\mathbf{r}_i}{dt} \quad (5)$$

The net momentum of the CNT was set to zero at each time step to avoid drifting of the CNT due to the force imparted by the water.

References

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