

# Partition of electronic excitation energies: the IQA/EOM-CCSD method

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## 1 XYZ coordinates

### 1.1 Nitrogen

Table 1: xyz coordinates, in (Å), for the nitrogen molecule computed with the CCSD/Sadlej-plus approximation as implemented in the Psi4 program.

	<i>x</i>	<i>y</i>	<i>z</i>
N	0.000	0.000	-0.557
N	0.000	0.000	0.557

### 1.2 Carbon monoxide

Table 2: xyz coordinates, in Å, for the carbon monoxide molecule computed with the CCSD/Sadlej-pVTZ approximation as implemented in the Psi4 program.

	<i>x</i>	<i>y</i>	<i>z</i>
C	0.000	0.000	0.648
O	0.000	0.000	-0.486

### 1.3 Water

Table 3: xyz coordinates, in Å, for the water molecule as reported in reference [39] in the main body of the paper.

	$x$	$y$	$z$
O	0.000	0.000	0.118
H	0.000	0.758	-0.473
H	0.000	-0.758	-0.473

### 1.4 Ethylene

Table 4: xyz coordinates, in Å, for the ethylene as reported in reference [42] in the main body of the paper.

	$x$	$y$	$z$
C	0.000	0.000	0.670
C	0.000	0.000	-0.670
H	0.000	0.926	1.235
H	0.000	-0.926	1.235
H	0.000	0.926	-1.235
H	0.000	-0.926	-1.235

### 1.5 Methane

Table 5: xyz coordinates, in Å, for the methane molecule computed with the MP2/aug-cc-pVTZ approximation as implemented in the Psi4 program.

	$x$	$y$	$z$
C	0.000	0.000	0.000
H	0.885	0.000	0.626
H	0.000	-0.885	-0.626
H	0.000	0.885	-0.626
H	-0.885	0.000	0.626

## 2 QTAIM analysis and IQA partition for the ground and excited states

### 2.1 Nitrogen

Table 6: QTAIM charges and delocalisation indexes as well as the IQA energy partition of the ground state and the examined excited states of the N<sub>2</sub> molecule. Atomic units are used throughout.

	GS	1 <sup>1</sup> Π <sub>g</sub>	1 <sup>1</sup> Σ <sub>u</sub> <sup>-</sup>	1 <sup>1</sup> Δ <sub>u</sub>	1 <sup>1</sup> Π <sub>u</sub>	2 <sup>1</sup> Π <sub>u</sub>
DI(N, N)	2.073	1.948	1.927	1.974	2.352	2.304
$q^{\text{N}}$	0.000	0.000	0.000	0.000	0.002	0.001
$E_{\text{class}}^{\text{N,N}}$	0.243	0.275	0.270	0.271	0.439	0.341
$E_{\text{xc}}^{\text{N,N}}$	-0.719	-0.660	-0.656	-0.671	-0.793	-0.698
$E_{\text{net}}^{\text{N}}$	-54.407	-54.277	-54.263	-54.249	-54.234	-54.218

### 2.1 Carbon monoxide

Table 7: QTAIM charges and delocalisation indexes as well as the IQA energy partition of the ground state and the examined excited states of the CO molecule. Atomic units are used throughout.

	GS	1 <sup>1</sup> Π	1 <sup>1</sup> Σ <sup>-</sup>	2 <sup>1</sup> Σ <sup>+</sup>
DI(C, O)	1.426	1.622	1.181	1.171
$q^{\text{C}}$	1.187	0.898	0.745	0.769
$q^{\text{O}}$	1.188	-0.897	-0.745	-0.769
$E_{\text{class}}^{\text{C,O}}$	-1.244	-0.712	-0.686	-0.706
$E_{\text{xc}}^{\text{C,O}}$	-0.441	-0.495	-0.368	-0.366
$E_{\text{net}}^{\text{C}}$	-36.962	-37.010	-37.169	-37.151
$E_{\text{net}}^{\text{O}}$	-74.428	-74.539	-74.483	-74.479

Table 8: Continuation of Table 7.

	$3^1\Sigma^+$	$2^1\Sigma^-$	$4^1\Sigma^+$	$3^1\Sigma^-$
DI(C, O)	1.952	1.789	1.450	1.373
$q^C$	1.189	1.004	1.290	1.340
$q^O$	-1.181	-0.993	-1.290	-1.340
$E_{\text{class}}^{C,O}$	-1.064	-1.046	-1.031	-1.043
$E_{\text{xc}}^{C,O}$	-0.492	-0.503	-0.380	-0.371
$E_{\text{net}}^C$	-36.634	-36.569	-36.745	-36.747
$E_{\text{net}}^O$	-74.394	-74.453	-74.388	-74.381

## 2.3 Water

Table 9: QTAIM charges and delocalisation indexes as well as the IQA energy partition of the ground state and the examined excited states of the H<sub>2</sub>O molecule. Atomic units are used throughout.

	GS	$1^1B_2$	$1^1A_2$	$1^1A_1$	$1^1B_1$
DI(O, H)	0.603	0.634	0.477	0.619	0.458
DI(H, H)	0.021	0.148	0.391	0.096	0.374
$q^O$	-1.159	-0.878	-0.560	-1.052	-0.686
$q^H$	0.580	0.439	0.280	0.526	0.343
$E_{\text{class}}^{H,H}$	0.137	0.127	0.113	0.153	0.135
$E_{\text{xc}}^{H,H}$	-0.003	-0.011	-0.022	-0.007	-0.021
$E_{\text{class}}^{O,H}$	-0.315	-0.235	-0.188	-0.296	-0.236
$E_{\text{xc}}^{O,H}$	-0.193	-0.164	-0.145	-0.150	-0.130
$E_{\text{net}}^O$	-74.800	-74.754	-74.805	-74.672	-74.744
$E_{\text{net}}^H$	-0.297	-0.284	-0.280	-0.247	-0.245

Table 10: Continuation of Table 9.

	$2^1A_2$	$2^1B_2$	$2^1B_1$	$3^1B_1$	$2^1A_1$
DI(O, H)	0.642	0.418	0.505	0.552	0.577
DI(H, H)	0.072	0.010	0.013	0.144	0.048
$q^O$	-0.968	-1.487	-1.367	-1.091	-1.224
$q^H$	0.484	0.744	0.682	0.545	0.612
$E_{\text{class}}^{\text{H,H}}$	0.115	0.208	0.184	0.164	0.184
$E_{\text{xc}}^{\text{H,H}}$	-0.008	-0.001	-0.002	-0.012	-0.003
$E_{\text{class}}^{\text{O,H}}$	-0.181	-0.398	-0.362	-0.259	-0.360
$E_{\text{xc}}^{\text{O,H}}$	-0.172	-0.132	-0.152	-0.130	-0.141
$E_{\text{net}}^O$	-74.706	-74.519	-74.491	-74.712	-74.492
$E_{\text{net}}^H$	-0.269	-0.207	-0.220	-0.215	-0.196

## 2.4 Ethylene

Table 11: QTAIM charges and delocalisation indexes as well as the IQA energy partition of the ground state and the examined excited states of the  $C_2H_4$  molecule. The labelling of the atoms is shown in Figure 1 in the body of the manuscript. Atomic units are used throughout.

	GS	$1^1B_{1u}$	$1^1B_{3g}$	$1^1B_{3u}$	$1^1B_{2g}$	$2^1B_{1u}$
$DI(C_1, C_2)$	1.335	1.468	1.268	1.690	1.268	1.294
$DI(C_1, H_3)$	0.802	0.810	0.755	0.777	0.787	0.795
$DI(C_1, H_5)$	0.059	0.077	0.040	0.103	0.049	0.068
$DI(H_3, H_4)$	0.050	0.039	0.130	0.044	0.114	0.084
$DI(H_3, H_5)$	0.024	0.031	0.123	0.033	0.096	0.082
$DI(H_3, H_5)$	0.019	0.020	0.096	0.027	0.079	0.067
$q^H$	0.046	0.141	-0.007	0.096	0.021	0.042
$q^C$	-0.091	-0.280	0.020	-0.191	-0.033	-0.077
$E_{class}^{C_1, C_2}$	0.064	0.076	0.070	0.072	0.071	0.073
$E_{xc}^{C_1, C_2}$	-0.433	-0.422	-0.414	-0.456	-0.412	-0.415
$E_{class}^{C_1, H_3}$	0.038	0.029	0.034	0.033	0.034	0.032
$E_{xc}^{C_1, H_3}$	-0.258	-0.249	-0.242	-0.251	-0.246	-0.246
$E_{class}^{C_1, H_5}$	0.002	0.004	0.008	0.003	0.008	0.007
$E_{xc}^{C_1, H_5}$	-0.007	-0.007	-0.005	-0.010	-0.005	-0.007
$E_{class}^{H_3, H_4}$	0.004	0.014	0.010	0.009	0.012	0.011
$E_{xc}^{H_3, H_4}$	-0.006	-0.004	-0.008	-0.005	-0.010	-0.007
$E_{class}^{H_3, H_5}$	0.001	0.007	0.005	0.004	0.005	0.005
$E_{xc}^{H_3, H_5}$	-0.002	-0.004	-0.010	-0.003	-0.005	-0.007
$E_{class}^{H_3, H_6}$	0.001	0.006	0.003	0.003	0.004	0.003
$E_{xc}^{H_3, H_6}$	-0.001	-0.001	-0.004	-0.002	-0.003	-0.003
$E_{net}^C$	-37.612	-37.533	-37.560	-37.499	-37.561	-37.558
$E_{net}^H$	-0.466	-0.438	-0.443	-0.448	-0.443	-0.446

## 2.5 Methane

Table 12: Average of QTAIM charges and delocalisation indexes as well as the IQA energy partition of the investigated electronic systems of CH<sub>4</sub>. Atomic units are used throughout.

	GS		1 <sup>1</sup> T <sub>2</sub>		1 <sup>1</sup> A <sub>2</sub>
$\langle \text{DI}(\text{C}, \text{H}) \rangle$	0.798	0.760	0.760	0.760	0.772
$\langle \text{DI}(\text{H}, \text{H}) \rangle$	0.054	0.102	0.100	0.100	0.121
$\langle q^{\text{C}} \rangle$	-0.083	-0.420	-0.418	-0.418	-0.415
$\langle q^{\text{H}} \rangle$	0.021	0.105	0.104	0.104	0.103
$\langle E_{\text{class}}^{\text{C,H}} \rangle$	0.037	0.014	0.015	0.015	0.018
$\langle E_{\text{xc}}^{\text{C,H}} \rangle$	-0.256	-0.226	-0.226	-0.226	-0.226
$\langle E_{\text{class}}^{\text{H,H}} \rangle$	0.003	0.020	0.019	0.019	0.021
$\langle E_{\text{xc}}^{\text{H,H}} \rangle$	-0.007	-0.009	-0.008	-0.008	-0.010
$E_{\text{net}}^{\text{C}}$	-37.614	-37.570	-37.570	-37.570	-37.567
$\langle E_{\text{net}}^{\text{H}} \rangle$	-0.469	-0.413	-0.413	-0.413	-0.405

Table 13: Continuation of Table 12

	1 <sup>1</sup> E		2 <sup>1</sup> T <sub>2</sub>		
$\langle \text{DI}(\text{C}, \text{H}) \rangle$	0.791	0.788	0.793	0.771	0.771
$\langle \text{DI}(\text{H}, \text{H}) \rangle$	0.089	0.090	0.040	0.037	0.037
$\langle q^{\text{C}} \rangle$	-0.513	-0.499	-0.982	-1.053	-1.053
$\langle q^{\text{H}} \rangle$	0.128	0.125	0.245	0.262	0.262
$\langle E_{\text{class}}^{\text{C,H}} \rangle$	0.017	0.017	-0.010	-0.013	-0.013
$\langle E_{\text{xc}}^{\text{C,H}} \rangle$	-0.229	-0.228	-0.228	-0.227	-0.227
$\langle E_{\text{class}}^{\text{H,H}} \rangle$	0.019	0.019	0.029	0.029	0.029
$\langle E_{\text{xc}}^{\text{H,H}} \rangle$	-0.008	-0.008	-0.005	-0.005	-0.005
$E_{\text{net}}^{\text{C}}$	-37.532	-37.533	-37.484	-37.474	-37.474
$\langle E_{\text{net}}^{\text{H}} \rangle$	-0.402	-0.402	-0.401	-0.403	-0.403

## 2.6 Helium dimer

Table 14: IQA partition of the excitation energy ( $E_h$ ) of GS, in net as well as classical and exchange-correlation interatomic components, as a function of distance ( $\text{\AA}$ ) between the helium atoms in the excimer formation. We also present the changes in the delocalisation index (au) for each point.

Distance $\text{\AA}$	DI(He, He)	$E_{\text{class}}^{\text{He,He}}$	$E_{\text{xc}}^{\text{He,He}}$	$E_{\text{net}}$	$E$	$E_{\text{MRCC}}$
0.800	0.409	0.07	-0.14	-2.69	-5.45	-5.45
1.047	0.245	0.02	-0.08	-2.80	-5.65	-5.65
1.072	0.234	0.01	-0.07	-2.80	-5.67	-5.67
1.200	0.185	0.01	-0.05	-2.83	-5.71	-5.71
1.400	0.130	0.00	-0.03	-2.86	-5.75	-5.75
1.600	0.092	0.00	-0.02	-2.87	-5.77	-5.77
1.800	0.063	0.00	-0.01	-2.88	-5.77	-5.77
2.000	0.043	0.00	-0.01	-2.88	-5.78	-5.78
2.970	0.004	0.00	0.00	-2.89	-5.78	-5.78
3.000	0.004	0.00	0.00	-2.89	-5.78	-5.78
4.000	0.000	0.00	0.00	-2.89	-5.78	-5.78
5.000	0.000	0.00	0.00	-2.89	-5.78	-5.78