

Supplementary Information for:

Energetics of Exciton Binding and Dissociation in Conjugated Polymers: A Tight Binding Approach

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Coulomb integral between two smeared charge distributions

We evaluate the Coulomb integral between two smeared charge distributions, represented as three-dimensional Gaussians given by

$$\rho(r) = q_0 \frac{e^{-r^2/(2\sigma)^2}}{(2\pi\sigma)^{3/2}} \quad (1)$$

where σ is the characteristic size (radius), and q_0 the elementary charge. The integral for such charge distributions located at site i and j , $E_C(i, j)$, is given by

$$\begin{aligned} E_C(i, j) &= \int dr \int dr' \frac{\rho_i(r)\rho_j(r')}{|r - r'|} \\ &= \frac{1}{r} \operatorname{erf}\left(\frac{r}{2\sigma}\right) \end{aligned} \quad (2)$$

where the latter result is obtained by evaluating the integral in Fourier space. Evidently $E_C(i, j)$ only depends on the distance r between sites i and j , and the characteristic width σ of the smeared charge distribution ρ . Figure S1 displays this result as a dimensionless function of r/σ , in units of the energy scale $U_0 = q_0^2/(4\pi\epsilon_0\sigma)$. A deviation from the $1/r$ potential is seen for interactions involving smeared charges that are two sites or less apart.

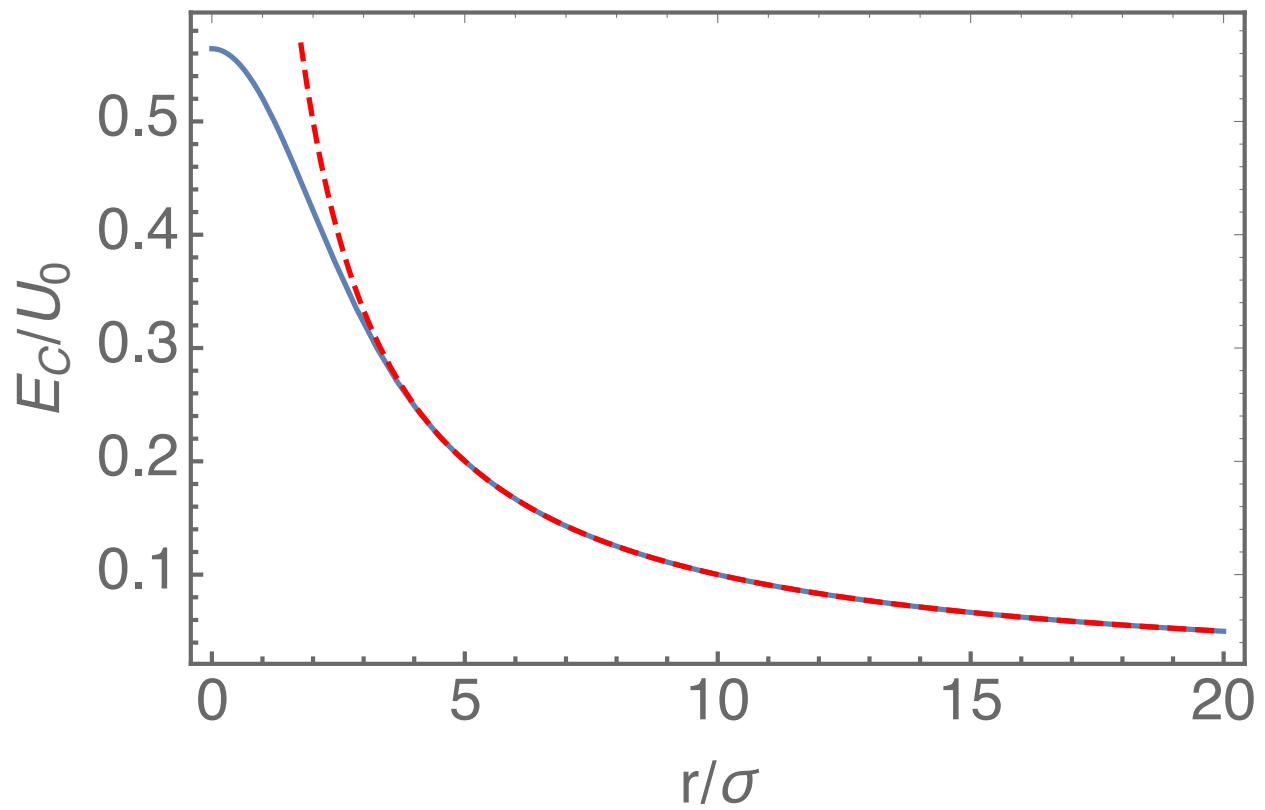


Figure S1: Interaction energy between two Gaussian charge distributions separated by r . Solid curve is Equation 2; dashed curve is $1/r$, valid at large separations.

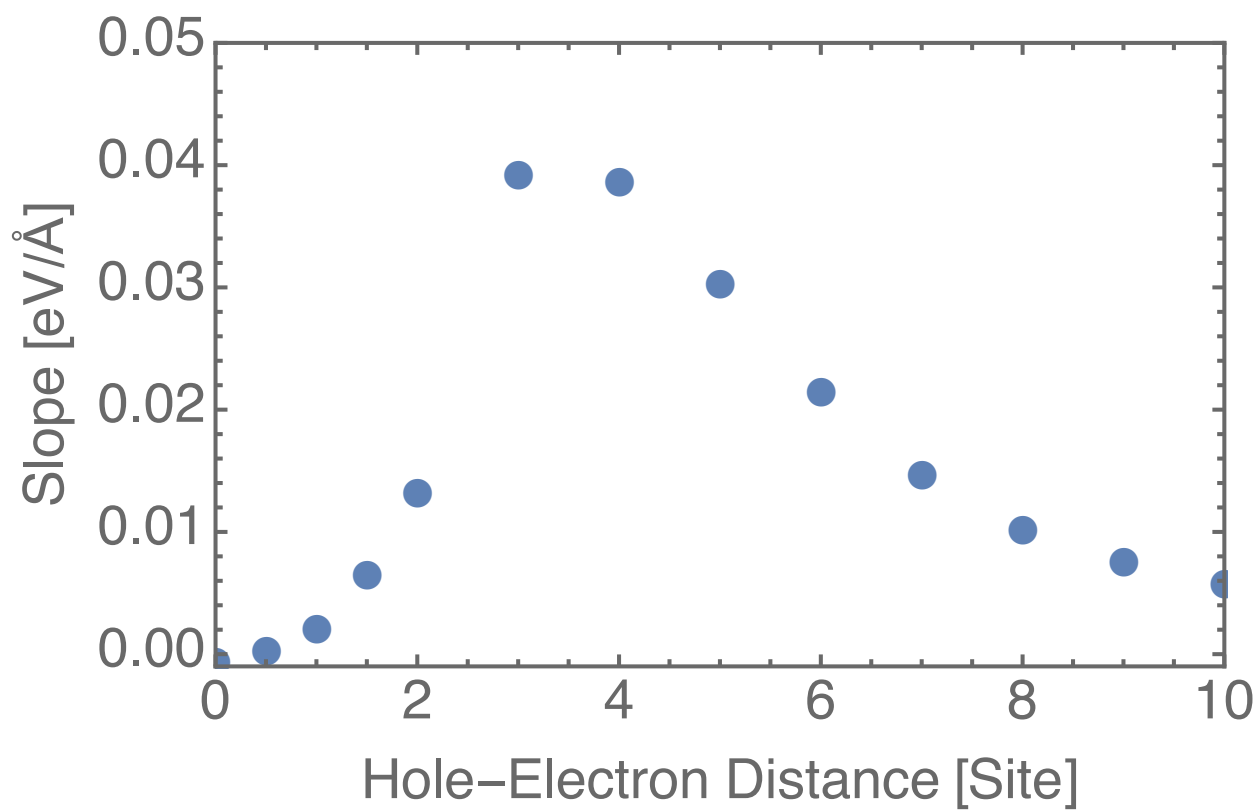


Figure S2: Attractive force (slope of bare Coulomb potential) between the two carriers as a function of hole-electron distance.