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Supplementary Information

Vibrational Spectroscopy of the Hexahydrated Sulfate Dianion Revisited: Role of Isomers and Anharmonicities

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Figure S1: Mass spectrum of a 10 mmol H_2SO_4 in Water/Acetonitrile (ratio 2:1) solution. The ion optics are optimized for the mass of $SO_4^{2-}(H_2O)_6$.

Table S1: Relative electronic energies (all in kJ/mol) with zero-point-correction of SO_4^{2-} (H₂O)₆ and SO_4^{2-} (D₂O)₆ for different isomers taken form Lambrecht *et al.*¹ The values are calculated at CCSD(T)/CBS* and ZPE is estimated at B3LYP/6-311++G** level of theory.

Isomer ^a	$E_{\rm el}$	$E_{\rm el} + E_{\rm ZPE}({\rm H})$	$E_{\rm el} + E_{\rm ZPE}({\rm D})$
6.6.6-1	0.0	6.7	4.3
6.6.6-2	0.8	7.8	5.4
6.7.5-1	2.1	8.3	6.3
6.7.5-2	2.1	8.3	6.3
6.7.5-3	4.1	9.7	7.8
6.7.5-4	4.1	9.7	7.8
6.7.5-5	4.4	8.6	6.9
6.7.5-6	4.3	8.7	6.9
6.8.4-1	3.5	5.9	4.6
6.8.4-2	3.4	5.9	4.6
6.8.4-3	4.8	6.8	5.6
6.8.4-4	4.8	6.8	5.6
6.8.4-5	2.7	4.1	3.0
6.8.4-6	3.3	5.1	3.9
6.8.4-7	2.8	4.2	3.1
6.8.4-8	3.3	5.1	3.9
6.9.3-1	3.2	0.0	0.0
6.12.0-1	17.5	5.8	7.8

^a The following structures given by Lambrecht et al.¹ are enantiomers: 6.7.5-

^{6.8.4-3} and 6.8.4-4



Figure S2: Comparison between the experimental IRPD spectrum and Gaussian convolution (FWHM = 12 cm^{-1}) of the harmonic B3LYP/aug-cc-pVTZ stick spectra for different isomers. Structures and their relative energies¹ (in kJ/mol) are also reported.



Figure S3: Comparison of Gaussian line function convoluted (FWHM = 12 cm^{-1}) harmonic stick spectra for different combinations of theory and basis set of the isomer **6.9.3-1**. For better comparison, the spectra are not scaled.



Figure S4: Magnification of the IRPD spectrum and the AIMD simulation in the spectral range from 600 to 1800 cm⁻¹.



Figure S5: Calculated VPT2 spectra of 6.9.3-1 with D_2 tagging for different binding positions using B3LYP/6-31+G(d,p) with GD3BJ empirical dispersion correction. As a comparison, the IRPD spectrum is shown below.

The VPT2 implementation in Gaussian16 can cause problems.² For example, the calculation for isomer **VI-9-3a** failed regardless of the options used. This was solved by breaking the C_3 symmetry by attaching a D₂ molecule to the cluster. But, adding D₂ to **VI-12-0a** reduces the T_d symmetry to $C_{2\nu}$ is resulting in a failed calculation. As already mentioned there are three positions for the addition of D₂ to **VI-9-3a**. The spectra of these "sub"-isomers differ clearly between themselves (Figure S5), so that the spectrum shown here must be regarded as problematic.



Figure S6: IRPD spectrum of $SO_4^{2-}(H_2O)_6 (D_2)_n$ in the D_2 stretching region. Experimental values are represented as dots, while the line show a fit of two Lorentzian functions.

Table S2a-d: Parameters of the Lorentzian fit shown in figure S3. Given errors are estimated for a confidence level of 68%.

SO_4^2 -(H ₂ O) ₆ (D ₂) ₁		SO ₄ ²⁻ ($SO_4^{2-}(H_2O)_6 (D_2)_2$	
parameter	value	param	neter	value
A_1	$1957~\pm~44$		1	$3133~\pm~68$
μ_1	2943.41 ± 0.05	μ	1	2944.76 ± 0.05
σ_1	$2.31~\pm~0.07$	σ_{1}	1	$2.32~\pm~0.07$
A_2	$248~\pm~42$		2	$1228~\pm~76$
μ_2	2928.20 ± 0.30	μ	2	2929.15 ± 0.16
σ_2	$2.23~\pm~0.61$	σ	2	$2.87~\pm~0.23$

$504 (1120)_{6} (D2)_{3}$	SO_4^{2-1}	(H_2O)) ₆ (1	$D_{2})_{3}$
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parameter	value
A_1	$4420~\pm~220$
μ_1	2945.96 ± 0.11
σ_1	$2.05~\pm~0.12$
A_2	$2760~\pm~250$
μ_2	2929.47 ± 0.22
σ_2	$2.59~\pm~0.30$

$SO_4^{2-}(H_2O)_6(D_2)$

parameter	value
A_1	$6326~\pm~219$
μ_1	2946.46 ± 0.08
σ_1	2.57 ± 0.12
A_2	$5470~\pm~230$
μ_2	2930.74 ± 0.11
σ_2	2.83 ± 0.16

Isomor		E	temperature (K)						
15	omer	<i>L</i> electronic	0	50	100	150	200	250	300
- 11 U	VI-12-0a	14.4	5.5	5.8	5.3	4.5	3.3	1.7	0.0
VI-9-3a	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	
ط اله	VI-12-0a	14.4	7.7	7.9	7.3	6.1	4.5	2.7	0.6
all-D VI-9-3	VI-9-3a	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0

Table S3: Relative energies with thermal correction to Gibbs free energy (kJ/mol) for the two relevant isomers. Electronic energy is taken form the reference

Table S4: B3LYP+GD3BJ/aug-cc-pVTZ optimized geometries (charge = -2, multiplicity = 1) for $SO_4^{2-}(H_2O)_6$ isomers

Isomer	Coordinates			
6.12.0	S	-0.000000	0.00000	0.000000
	0	0.870971	-0.870971	0.870971
	0	-0.870971	0.870971	0.870971
	0	0.870971	0.870971	-0.870971
	0	-0.870971	-0.870971	-0.870971
	0	0.00000	3.476199	0.00000
	Н	0.516679	2.834442	-0.516679
	Н	-0.516679	2.834442	0.516679
	Н	-2.834442	0.516679	0.516679
	0	-3.476199	0.00000	0.00000
	Н	-2.834442	-0.516679	-0.516679
	Н	0.516679	-2.834442	0.516679
	0	-0.000000	-3.476199	0.00000
	Н	-0.516679	-2.834442	-0.516679
	Н	2.834442	0.516679	-0.516679
	0	3.476199	-0.000000	0.00000
	Н	2.834442	-0.516679	0.516679
	Н	0.516679	-0.516679	2.834442
	0	-0.000000	0.00000	3.476199
	Н	-0.516679	0.516679	2.834442
	Н	-0.516679	-0.516679	-2.834442
	0	-0.000000	-0.000000	-3.476199
	Н	0.516679	0.516679	-2.834442

Isomer	Coordinates				
6.9.3	S	0.00000	0.00000	0.341956	
	0	0.00000	0.00000	1.837929	
	0	0.00000	1.407190	-0.155587	
	0	1.218663	-0.703595	-0.155587	
	0	-1.218663	-0.703595	-0.155587	
	0	0.017264	2.857799	2.312821	
	Н	0.014091	1.917460	2.556056	
	Н	0.011524	2.733193	1.348018	
	0	2.466294	-1.443851	2.312821	
	Н	1.653523	-0.970933	2.556056	
	Н	2.361252	-1.376576	1.348018	
	0	-2.483558	-1.413948	2.312821	
	Н	-1.667615	-0.946526	2.556056	
	Н	-2.372776	-1.356616	1.348018	
	0	-0.402830	1.670433	-2.873014	
	Н	-0.273404	1.672414	-1.895275	
	Н	-0.923192	0.862510	-3.007465	
	0	1.648053	-0.486355	-2.873014	
	Н	1.585055	-0.599432	-1.895275	
	Н	1.208551	0.368253	-3.007465	
	0	-1.245223	-1.184078	-2.873014	
	Н	-1.311651	-1.072982	-1.895275	
	Н	-0.285359	-1.230763	-3.007465	

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