## Supporting Information

## **Electronic Structure and High-Temperature Thermochemistry**

## of BaZrO<sub>3-δ</sub> Perovskite from First-Principles Calculations

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**Figure S1.** Variation with temperature (0 - 2,000 K) of the calculated BZO properties from quasi-harmonic approximation: (a) thermal expansion  $(\alpha/K^{-1})$ , (b) bulk modulus (B/GPa), and (c) volume (V/Å).



**Figure S2.** PBE-PAW  $\Delta G_{RR}$  (equation (11)) at standard state pressure  $p^{\circ} = 1$  atm for BZO<sub>3- $\delta$ </sub> as a function of oxygen non-stoichiometry  $\delta$  between 0 – 2,000 K, with oxygen partial pressure: (a)  $P_{O_2} = 10^{-5}$  atm, (b)  $P_{O_2} = 10^{-10}$  atm, (c)  $P_{O_2} = 10^{-15}$  atm, and (d)  $P_{O_2} = 10^{-20}$  atm. The reduction temperature of BZO<sub>3- $\delta$ </sub> decreases with lower oxygen partial pressure.



**Figure S3.** (a) Vibrational entropy difference ( $\Delta S$ ), and (b) constant-pressure heat capacity difference ( $\Delta C_p$ ) in defect BZO<sub>3- $\delta$ </sub> between 0 – 2,000 K. The entropy and heat capacity differences become smaller with increased oxygen vacancy concentration, and hence give higher contributions to the highly-defected-BZO<sub>3- $\delta$ </sub>.



**Figure S4.** PBE phonon dispersion curves (left), and corresponding atomic vibrational densities of states (right) for representative structures of (a) BZO, (b) BZO<sub>2.875</sub>, (c) BZO<sub>2.75</sub>, (d) BZO<sub>2.625</sub>, and (e) BZO<sub>2.5</sub>.