

SUPPLEMENTARY INFORMATION:

**Electron Transport Investigation of Redox-Switching
Azulenequinones/Hydroquinones via First-Principles Studies**

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Fig. S1. The frontier orbitals (FO) for the 4 molecules and their corresponding HOMO-LUMO energy gap calculated using SIESTA LDA:

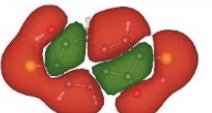
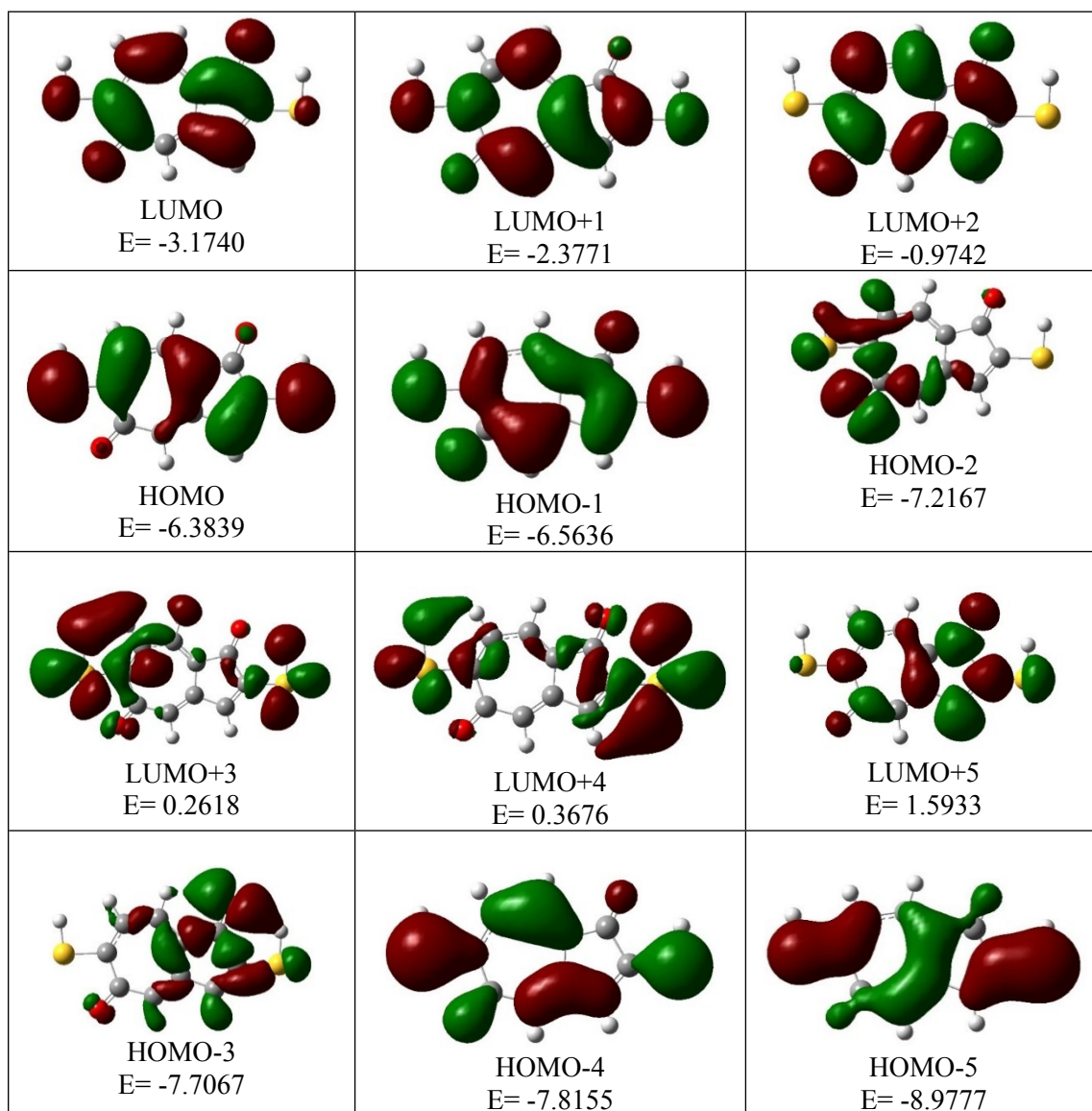
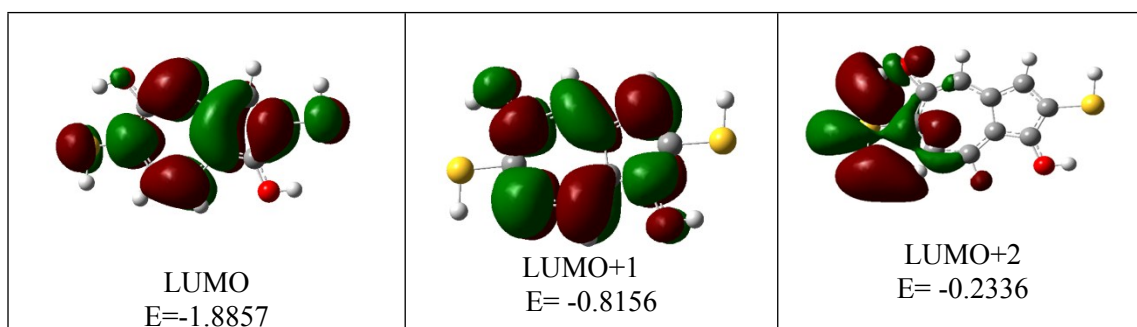
FO	HOMO(H)	LUMO (L)	$E_{\text{gap}} = E_L - E_H$
15Q			1.06 eV
15OH			1.16 eV
17Q			0.72 eV
17OH			1.14 eV

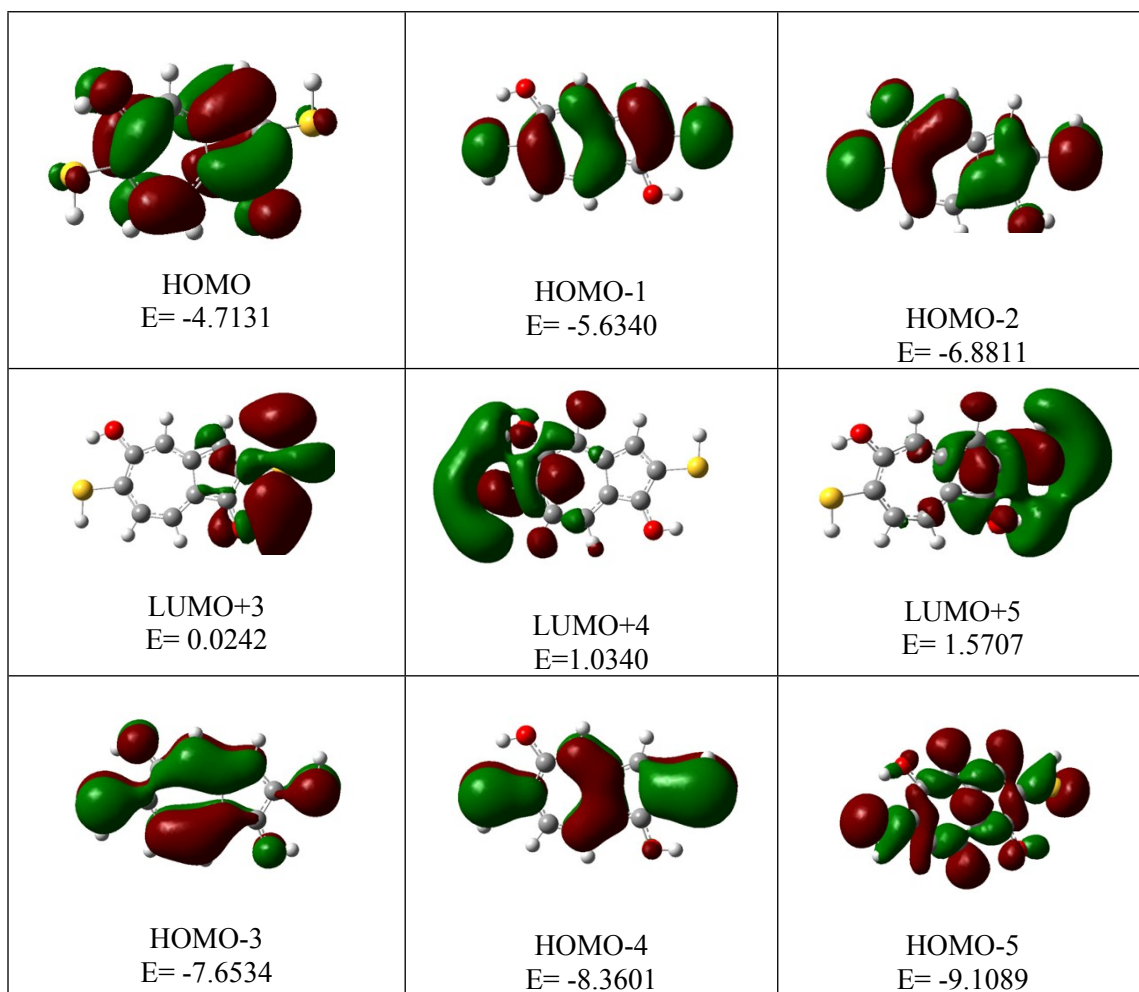
Fig. S2. The Frontier (as well as other) orbitals for the four free molecules, their associated energy levels (in eV) and calculated HOMO-LUMO energy gap at B3LYP/6-31G(d,p) level:

(a) 1,5-azulenequinone 2,6- dithiolate (15Q), $\Delta E=3.2099$ eV:

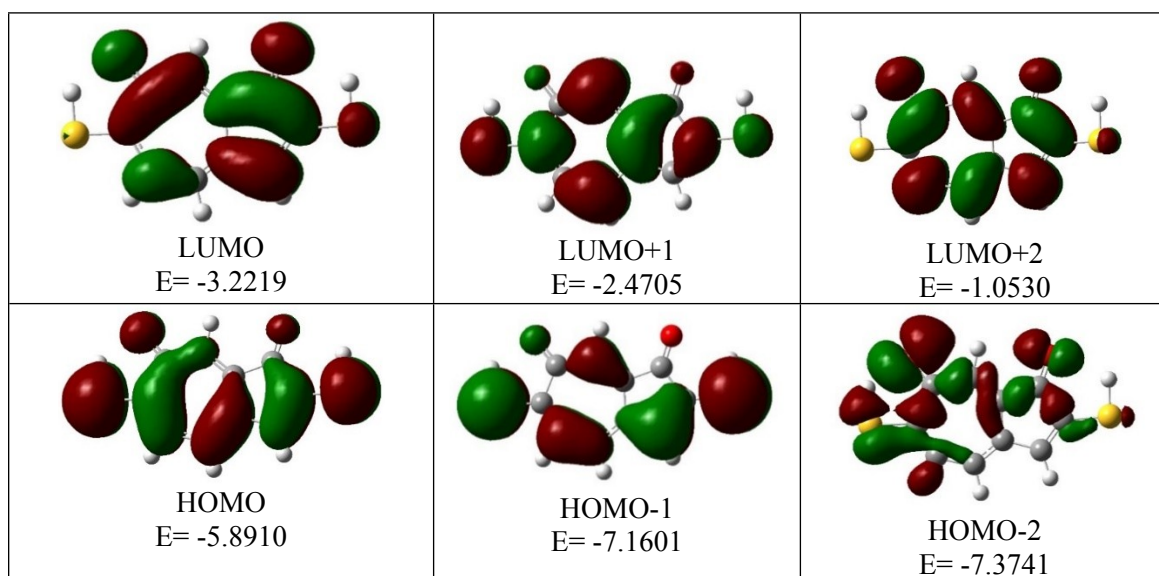


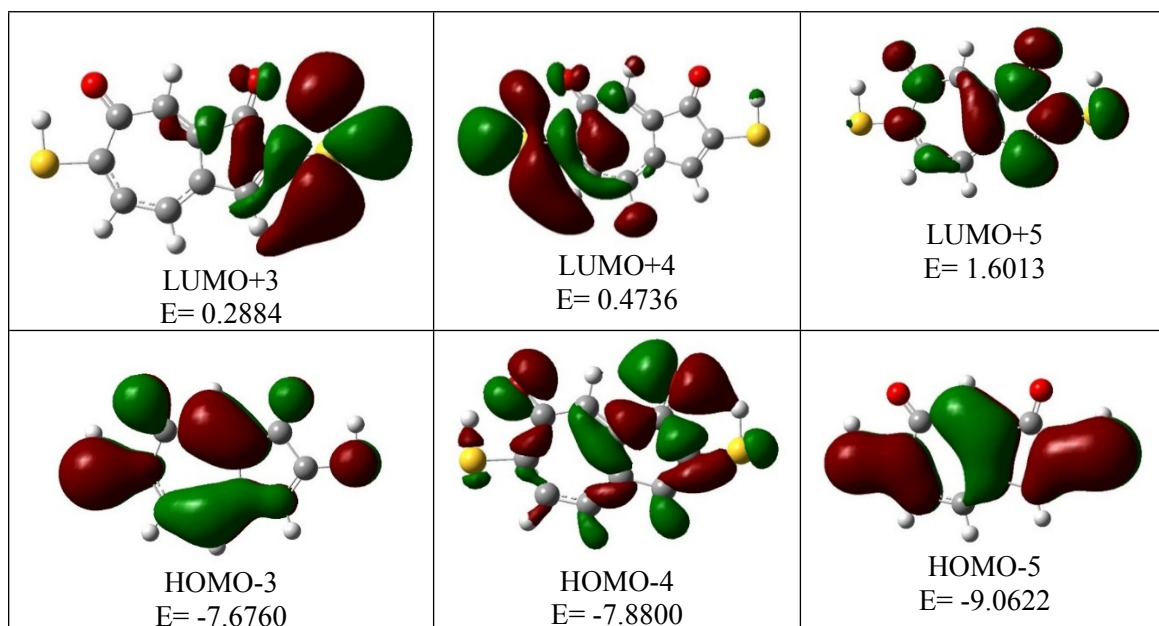
(b) 1,5-azulene hydroquinone 2,6- dithiolate (15OH), $\Delta E=2.83$ eV:



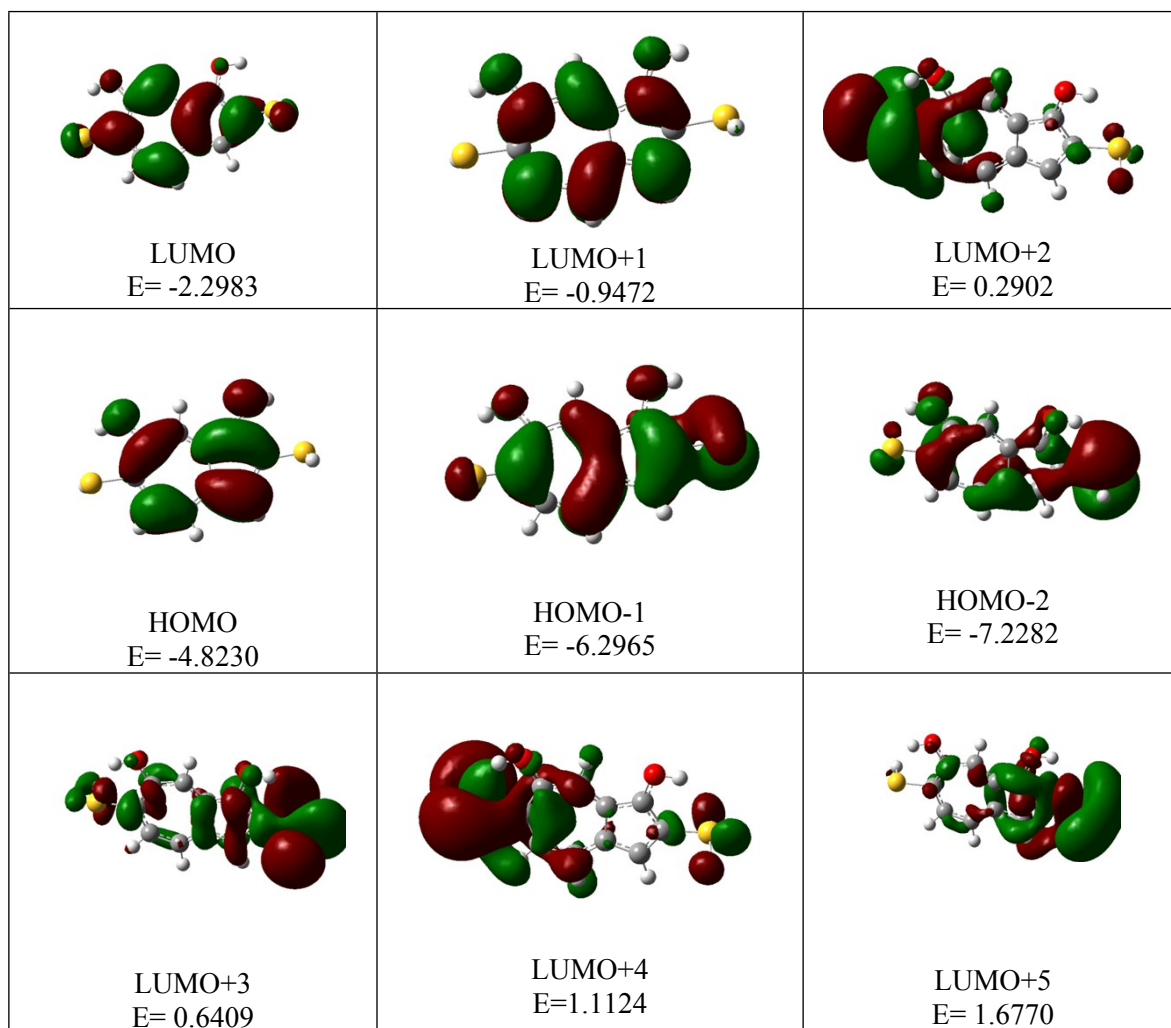


(c) 1,7-azulenequinone 2,6- dithiolate (17Q), $\Delta E=2.6691$ eV:





d) 1,7-azulene hydroquinone 2,6- dithiolate (17OH), $\Delta E=2.53$ eV:



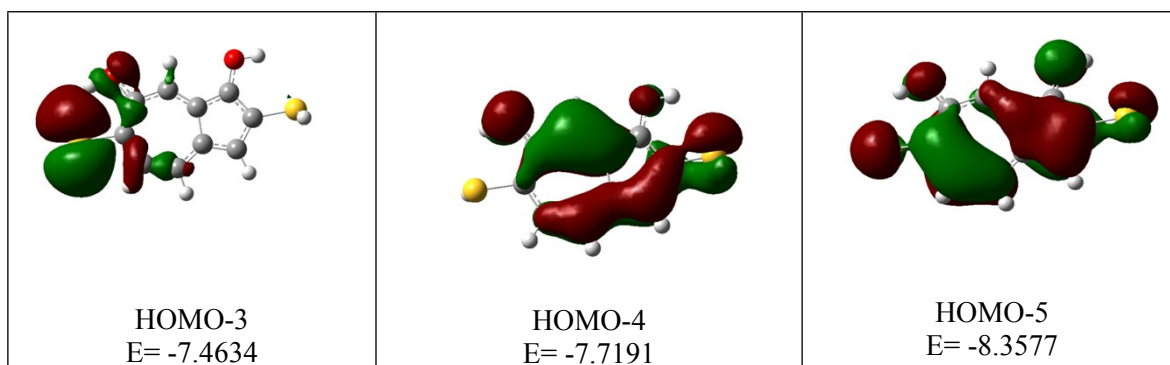
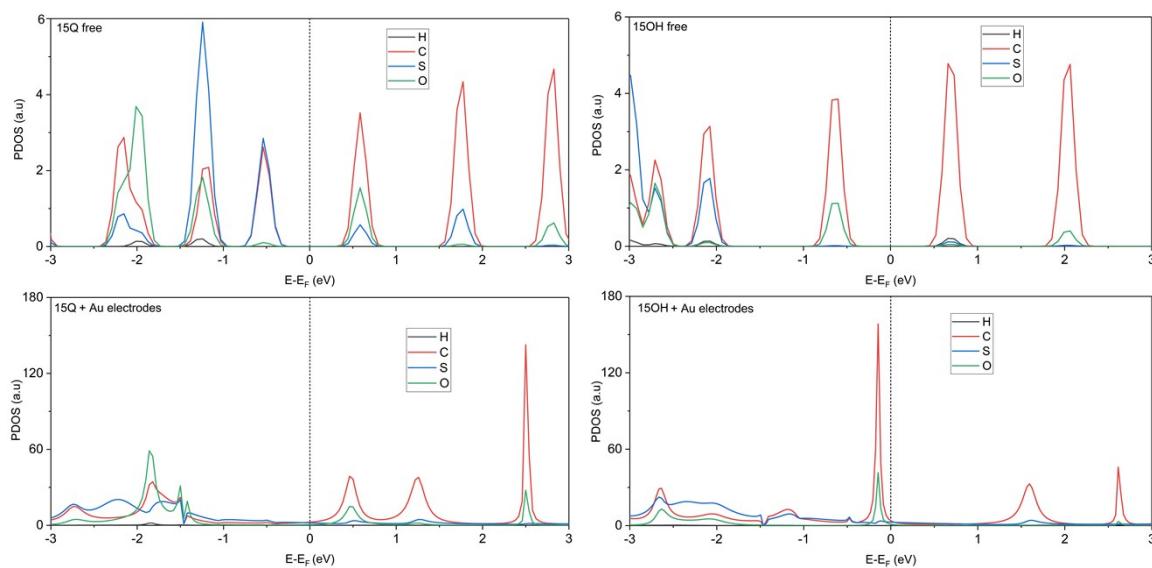


Fig S3. Projected Density of States (PDOS) of the free molecules and when connected to gold electrodes:

(a) 1,5-azulenequinone 2,6- dithiolate (15Q) (b) 1,5-azulene hydroquinone 2,6- dithiolate (15OH)



(c) 1,7-azulenequinone 2,6-dithiolate (17Q) (d) 1,7-azulene hydroquinone 2,6- dithiolate (17OH)

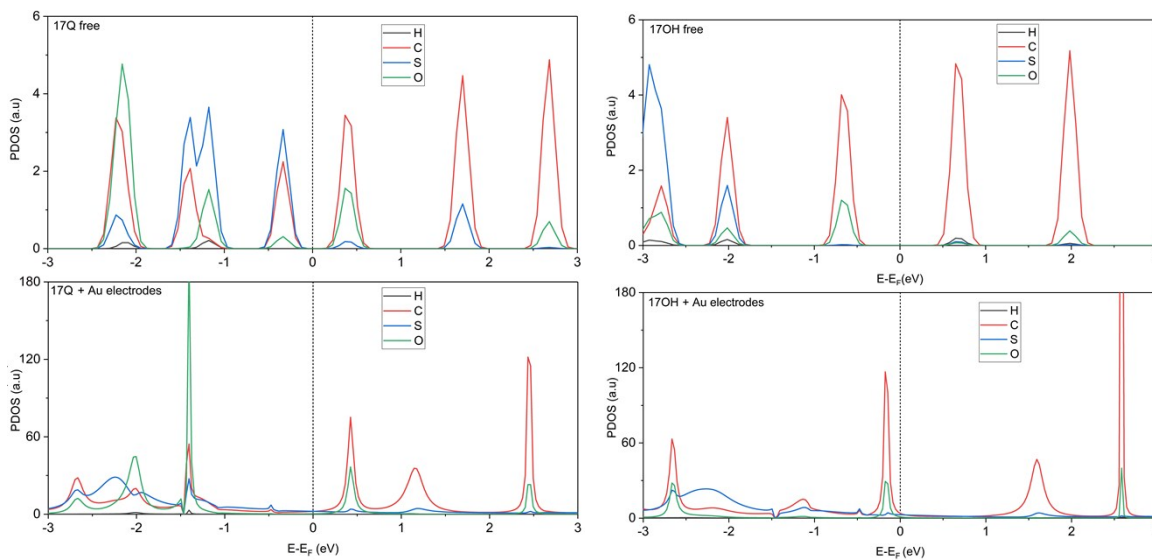
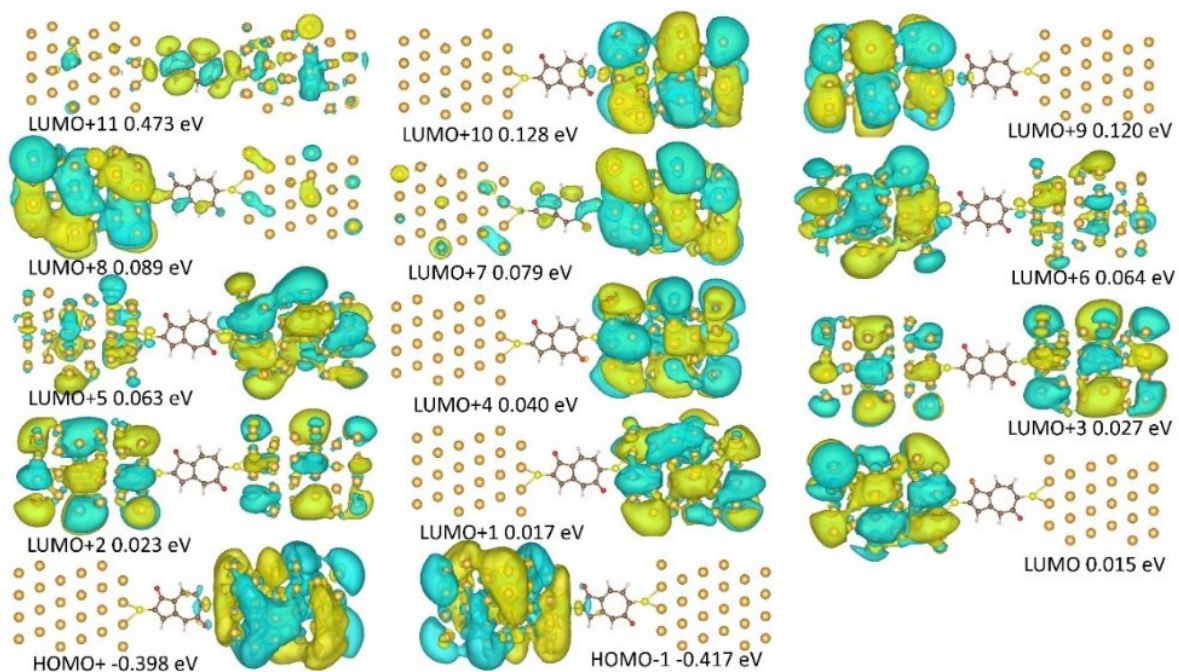
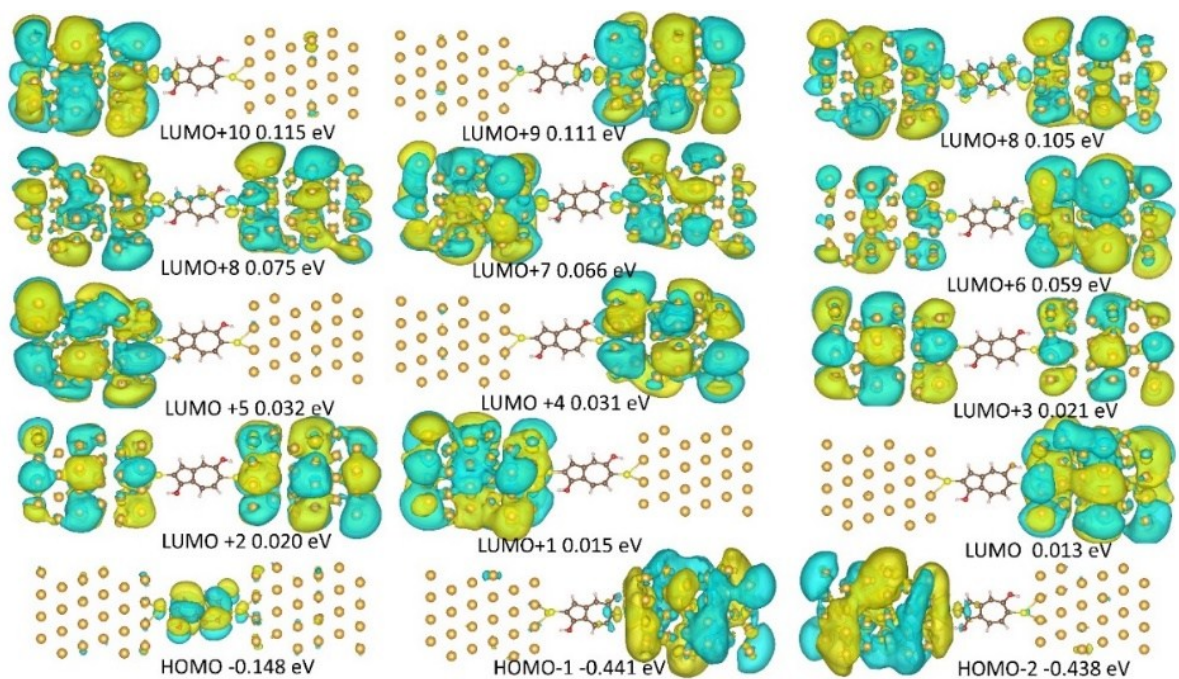


Fig. S4. Molecular Projected Self consistent Hamiltonian (MPSH) states at zero bias voltage for the four molecules.

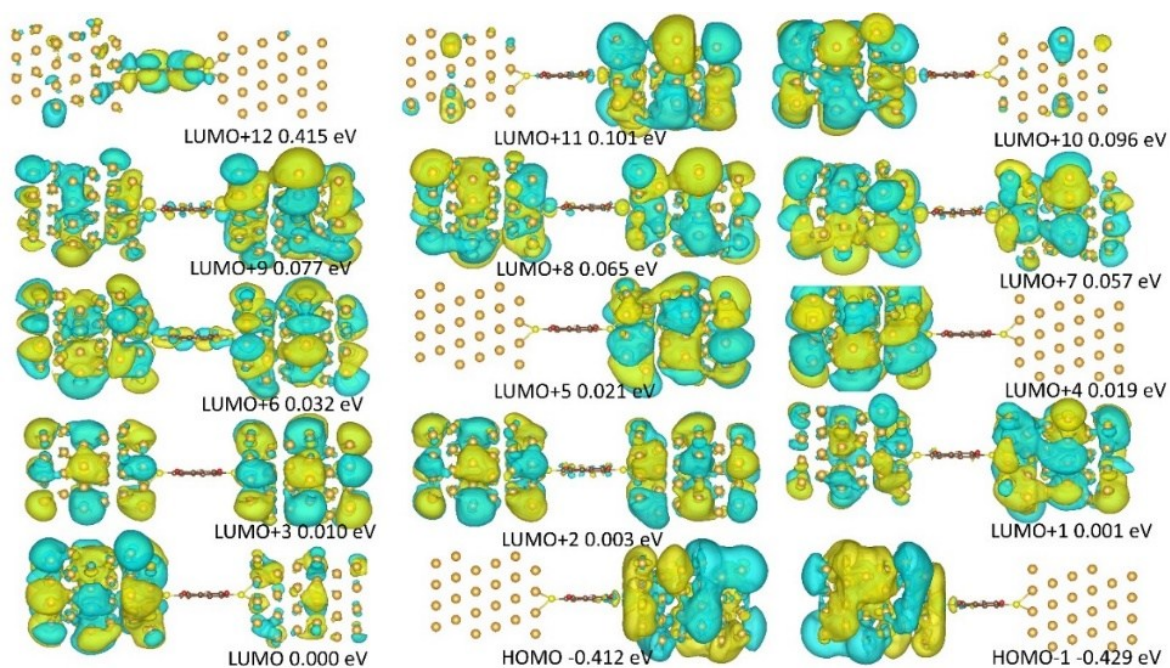
(a) 15Q



(b) 15OH



(c) 17Q



(d) 17OH

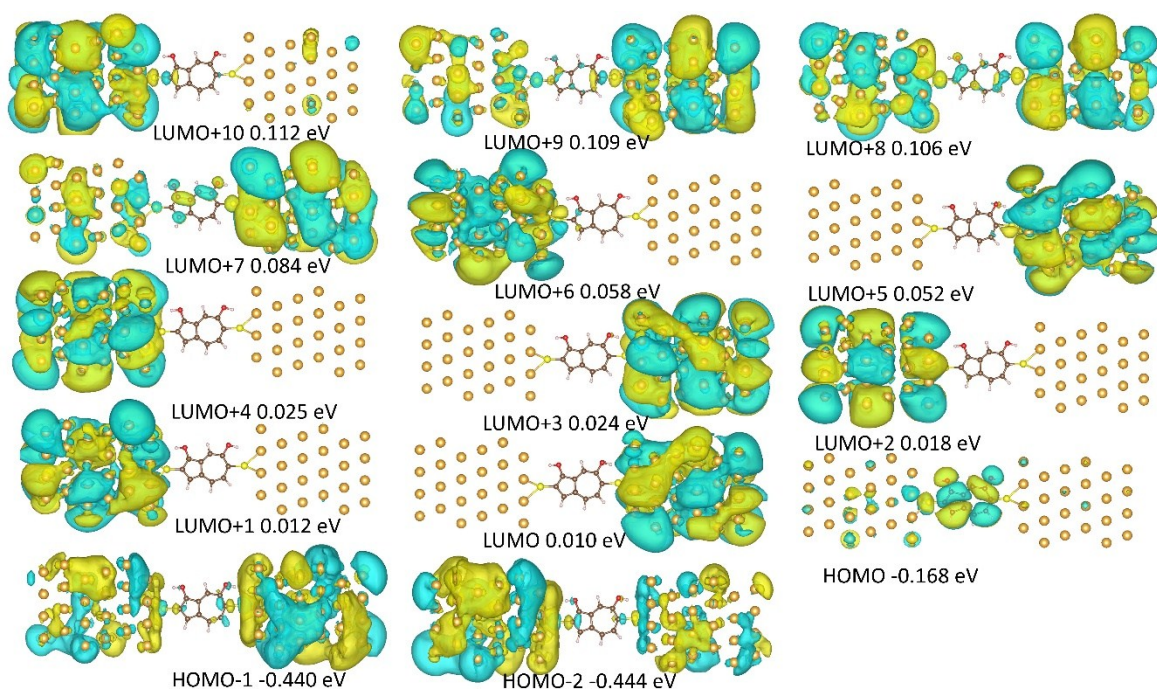
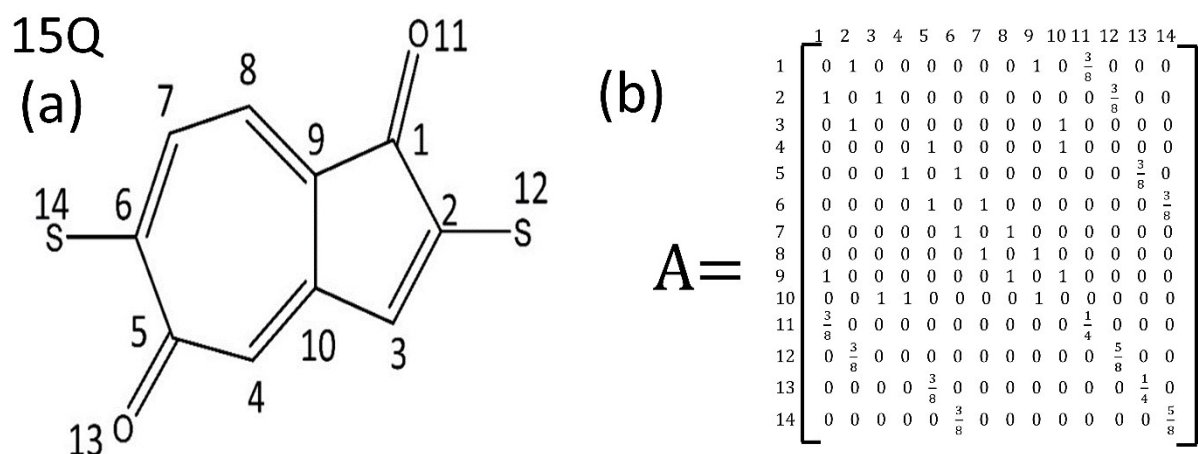
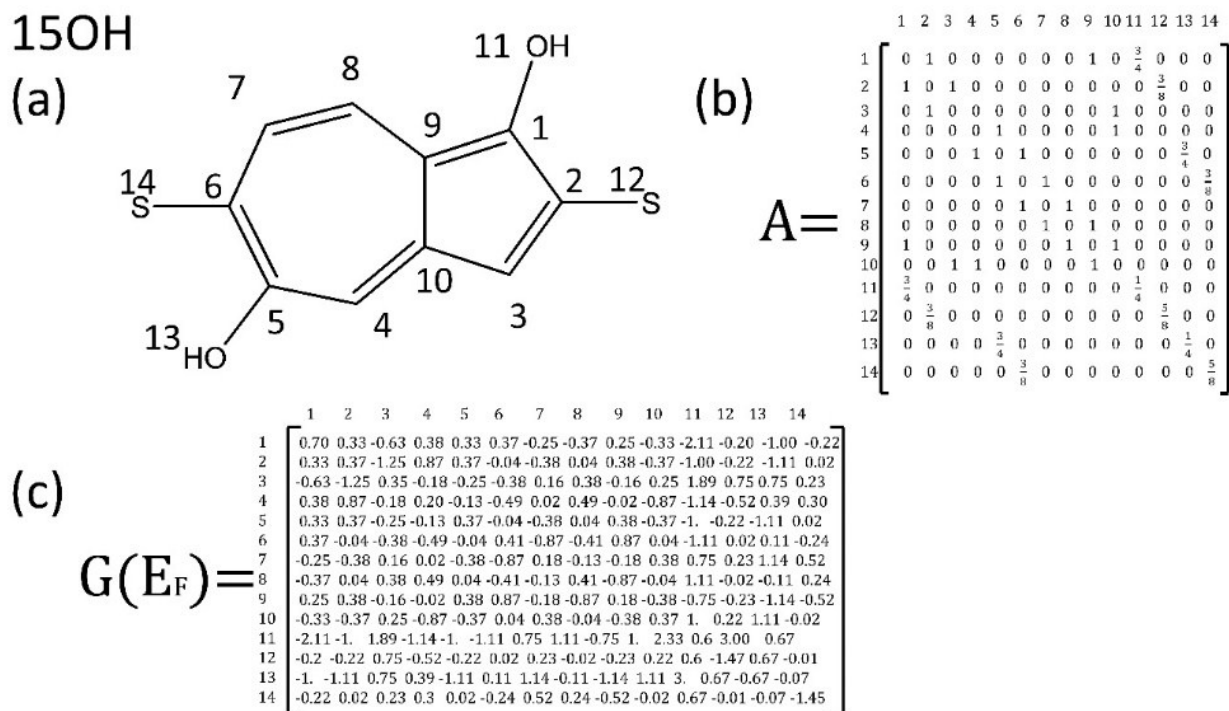


Fig. S5. Schematic diagrams of the other three molecules (with IUPAC numbering) (a), the corresponding matrix A from graph theory (from Eqs (3), (4) and (5)) (b), and the Green function $G(E_F)$. Note that $G(E_F) = -A^{-1}$ with A^{-1} the inverse of A.



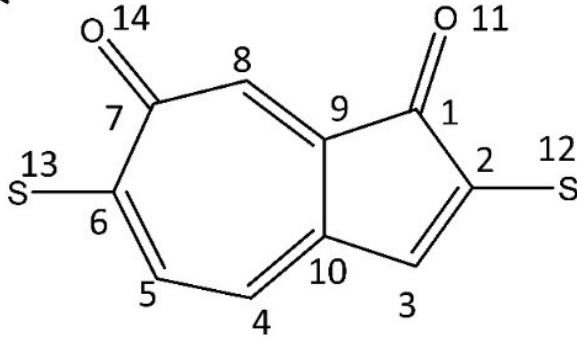
(c) $G(E_F) =$

	1	2	3	4	5	6	7	8	9	10	11	12	13	14
1	-1.17	-0.86	0.97	-0.18	-0.86	-0.31	0.79	0.31	-0.79	0.86	1.75	0.520	1.29	0.18
2	-0.86	-0.31	-0.21	0.39	-0.31	-0.56	0.18	0.56	-0.18	0.31	1.29	0.18	0.46	0.33
3	0.97	-0.21	-1.02	0.27	0.79	0.18	-0.75	-0.18	0.75	-0.79	-1.46	0.12	-1.19	-0.11
4	-0.18	0.39	0.27	0.22	-0.61	-0.57	0.49	0.57	-0.49	-0.39	0.27	-0.23	0.92	0.34
5	-0.86	-0.31	0.79	-0.61	-0.31	-0.56	0.18	0.56	-0.18	0.31	1.29	0.18	0.46	0.33
6	-0.31	-0.56	0.18	-0.57	-0.56	0.25	-0.39	-0.25	0.39	0.56	0.46	0.33	0.84	-0.15
7	0.79	0.18	-0.75	0.49	0.18	-0.39	-0.27	-0.61	0.27	-0.18	-1.19	-0.11	-0.27	0.23
8	0.31	0.56	-0.18	0.57	0.56	-0.25	-0.61	0.25	-0.39	-0.56	-0.46	-0.33	-0.84	0.15
9	-0.79	-0.18	0.75	-0.49	-0.18	0.39	0.27	-0.39	-0.27	0.18	1.19	0.11	0.27	-0.23
10	0.86	0.31	-0.79	-0.39	0.31	0.56	-0.18	-0.56	0.18	-0.31	-1.29	-0.18	-0.46	-0.33
11	1.75	1.29	-1.46	0.27	1.29	0.46	-1.19	-0.46	1.19	-1.29	-6.63	-0.78	-1.94	-0.27
12	0.52	0.18	0.12	-0.23	0.18	0.33	-0.11	-0.33	0.11	-0.18	-0.78	-1.71	-0.27	-0.2
13	1.29	0.46	-1.19	0.92	0.46	0.84	-0.27	-0.84	0.27	-0.46	-1.94	-0.27	-4.69	-0.5
14	0.18	0.33	-0.11	0.34	0.33	-0.15	0.23	0.15	-0.23	-0.33	-0.27	-0.2	-0.5	-1.51



17Q

(a)



(b)

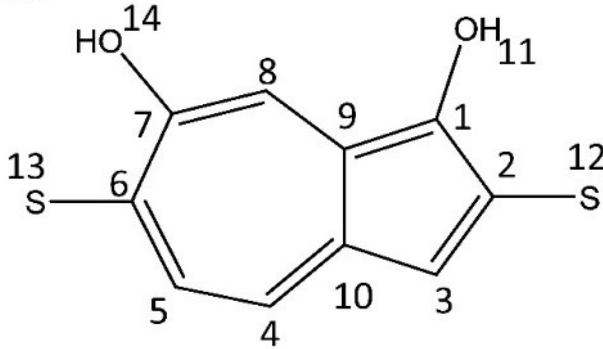
$$A = \begin{bmatrix} 1 & 2 & 3 & 4 & 5 & 6 & 7 & 8 & 9 & 10 & 11 & 12 & 13 & 14 \\ 1 & 0 & 1 & 0 & 0 & 0 & 0 & 0 & 0 & 1 & 0 & \frac{3}{8} & 0 & 0 & 0 \\ 2 & 1 & 0 & 1 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & \frac{3}{8} & 0 & 0 \\ 3 & 0 & 1 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 1 & 0 & 0 & 0 & 0 \\ 4 & 0 & 0 & 0 & 0 & 1 & 0 & 0 & 0 & 0 & 1 & 0 & 0 & 0 & 0 \\ 5 & 0 & 0 & 0 & 1 & 0 & 1 & 0 & 0 & 0 & 0 & 0 & \frac{3}{8} & 0 & 0 \\ 6 & 0 & 0 & 0 & 0 & 1 & 0 & 1 & 0 & 0 & 0 & 0 & 0 & \frac{3}{8} & 0 \\ 7 & 0 & 0 & 0 & 0 & 0 & 1 & 0 & 1 & 0 & 0 & 0 & 0 & 0 & 0 \\ 8 & 0 & 0 & 0 & 0 & 0 & 0 & 1 & 0 & 1 & 0 & 0 & 0 & 0 & 0 \\ 9 & 1 & 0 & 0 & 0 & 0 & 0 & 0 & 1 & 0 & 1 & 0 & 0 & 0 & 0 \\ 10 & 0 & 0 & 1 & 1 & 0 & 0 & 0 & 0 & 1 & 0 & 0 & 0 & 0 & 0 \\ 11 & \frac{3}{8} & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & \frac{1}{4} & 0 & 0 & 0 \\ 12 & 0 & \frac{3}{8} & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & \frac{5}{8} & 0 & 0 \\ 13 & 0 & 0 & 0 & 0 & 0 & \frac{3}{8} & 0 & 0 & 0 & 0 & 0 & 0 & \frac{5}{8} & 0 \\ 14 & 0 & 0 & 0 & 0 & 0 & 0 & \frac{3}{8} & 0 & 0 & 0 & 0 & 0 & 0 & \frac{1}{4} \end{bmatrix}$$

(c)

$$G(E_F) = \begin{bmatrix} 1 & 2 & 3 & 4 & 5 & 6 & 7 & 8 & 9 & 10 & 11 & 12 & 13 & 14 \\ 1 & -1.15 & -0.81 & 0.97 & -0.13 & -0.81 & 0.13 & 0.84 & 0.34 & -0.84 & 0.81 & 1.73 & 0.49 & -0.08 & -1.26 \\ 2 & -0.81 & -0.28 & -0.25 & 0.43 & -0.28 & -0.43 & 0.18 & 0.53 & -0.18 & 0.28 & 1.21 & 0.17 & 0.26 & -0.27 \\ 3 & 0.97 & -0.25 & -1.03 & 0.23 & 0.75 & -0.23 & -0.8 & -0.22 & 0.8 & -0.75 & -1.45 & 0.15 & 0.14 & 1.2 \\ 4 & -0.13 & 0.43 & 0.23 & 0.28 & -0.57 & -0.28 & 0.51 & 0.56 & -0.51 & -0.43 & 0.2 & -0.26 & 0.17 & -0.76 \\ 5 & -0.81 & -0.28 & 0.75 & -0.57 & -0.28 & -0.43 & 0.18 & 0.53 & -0.18 & 0.28 & 1.21 & 0.17 & 0.26 & -0.27 \\ 6 & 0.13 & -0.43 & -0.23 & -0.28 & -0.43 & 0.28 & -0.51 & -0.56 & 0.51 & 0.43 & -0.2 & 0.26 & -0.17 & 0.76 \\ 7 & 0.84 & 0.18 & -0.8 & 0.51 & 0.18 & -0.51 & -0.29 & -0.66 & 0.29 & -0.18 & -1.26 & -0.11 & 0.3 & 0.44 \\ 8 & 0.34 & 0.53 & -0.22 & 0.56 & 0.53 & -0.56 & -0.66 & 0.19 & -0.34 & -0.53 & -0.51 & -0.32 & 0.34 & 0.99 \\ 9 & -0.84 & -0.18 & 0.8 & -0.51 & -0.18 & 0.51 & 0.29 & -0.34 & -0.29 & 0.18 & 1.26 & 0.11 & -0.3 & -0.44 \\ 10 & 0.81 & 0.28 & -0.75 & -0.43 & 0.28 & 0.43 & -0.18 & -0.53 & 0.18 & -0.28 & -1.21 & -0.17 & -0.26 & 0.27 \\ 11 & 1.73 & 1.21 & -1.45 & 0.2 & 1.21 & -0.2 & -1.26 & -0.51 & 1.26 & -1.21 & -6.59 & -0.73 & 0.12 & 1.89 \\ 12 & 0.49 & 0.17 & 0.15 & -0.26 & 0.17 & 0.26 & -0.11 & -0.32 & 0.11 & -0.17 & -0.73 & -1.7 & -0.16 & 0.16 \\ 13 & -0.08 & 0.26 & 0.14 & 0.17 & 0.26 & -0.17 & 0.3 & 0.34 & -0.3 & -0.26 & 0.12 & -0.16 & -1.5 & -0.45 \\ 14 & -1.26 & -0.27 & 1.2 & -0.76 & -0.27 & 0.76 & 0.44 & 0.99 & -0.44 & 0.27 & 1.89 & 0.16 & -0.45 & -4.66 \end{bmatrix}$$

17OH

(a)



(b)

$$A = \begin{bmatrix} 1 & 2 & 3 & 4 & 5 & 6 & 7 & 8 & 9 & 10 & 11 & 12 & 13 & 14 \\ 1 & 0 & 1 & 0 & 0 & 0 & 0 & 0 & 0 & 1 & 0 & \frac{3}{4} & 0 & 0 & 0 \\ 2 & 1 & 0 & 1 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & \frac{3}{8} & 0 & 0 \\ 3 & 0 & 1 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 1 & 0 & 0 & 0 & 0 \\ 4 & 0 & 0 & 0 & 0 & 1 & 0 & 0 & 0 & 0 & 1 & 0 & 0 & 0 & 0 \\ 5 & 0 & 0 & 0 & 1 & 0 & 1 & 0 & 0 & 0 & 0 & 0 & \frac{3}{8} & 0 & 0 \\ 6 & 0 & 0 & 0 & 0 & 1 & 0 & 1 & 0 & 0 & 0 & 0 & 0 & \frac{3}{4} & 0 \\ 7 & 0 & 0 & 0 & 0 & 0 & 1 & 0 & 1 & 0 & 0 & 0 & 0 & 0 & 0 \\ 8 & 0 & 0 & 0 & 0 & 0 & 0 & 1 & 0 & 1 & 0 & 0 & 0 & 0 & 0 \\ 9 & 1 & 0 & 0 & 0 & 0 & 0 & 0 & 1 & 0 & 1 & 0 & 0 & 0 & 0 \\ 10 & 0 & 0 & 1 & 1 & 0 & 0 & 0 & 0 & 1 & 0 & 0 & 0 & 0 & 0 \\ 11 & \frac{3}{4} & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & \frac{1}{4} & 0 & 0 & 0 \\ 12 & 0 & \frac{3}{8} & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & \frac{5}{8} & 0 & 0 \\ 13 & 0 & 0 & 0 & 0 & 0 & \frac{3}{8} & 0 & 0 & 0 & 0 & 0 & 0 & \frac{5}{8} & 0 \\ 14 & 0 & 0 & 0 & 0 & 0 & 0 & \frac{3}{4} & 0 & 0 & 0 & 0 & 0 & 0 & \frac{1}{4} \end{bmatrix}$$

(c)

$$G(E_F) = \begin{bmatrix} 1 & 2 & 3 & 4 & 5 & 6 & 7 & 8 & 9 & 10 & 11 & 12 & 13 & 14 \\ 1 & 0.71 & 0.27 & -0.65 & 0.32 & 0.27 & -0.32 & -0.34 & -0.45 & 0.34 & -0.27 & -2.14 & -0.16 & 0.19 & 1.02 \\ 2 & 0.27 & 0.21 & -1.22 & 0.83 & 0.21 & -0.83 & -0.39 & -0.06 & 0.39 & -0.21 & -0.8 & -0.12 & 0.5 & 1.18 \\ 3 & 0.65 & -1.22 & 0.38 & -0.13 & -0.22 & 0.13 & 0.25 & 0.43 & -0.25 & 0.22 & 1.96 & 0.73 & -0.08 & -0.75 \\ 4 & 0.32 & 0.83 & -0.13 & 0.25 & -0.17 & -0.25 & 0.12 & 0.51 & -0.12 & -0.83 & -0.95 & -0.5 & 0.15 & -0.35 \\ 5 & 0.27 & 0.21 & -0.22 & -0.17 & 0.21 & -0.83 & -0.39 & -0.06 & 0.39 & -0.21 & -0.8 & -0.12 & 0.5 & 1.18 \\ 6 & 0.32 & -0.83 & 0.13 & -0.25 & -0.83 & 0.25 & -0.12 & -0.51 & 0.12 & 0.83 & 0.95 & 0.5 & -0.15 & 0.35 \\ 7 & 0.34 & -0.39 & 0.25 & 0.12 & -0.39 & -0.12 & 0.37 & -0.06 & -0.37 & 0.39 & 1.02 & 0.24 & 0.07 & -1.1 \\ 8 & 0.45 & -0.06 & 0.43 & 0.51 & -0.06 & -0.51 & -0.06 & 0.39 & -0.94 & 0.06 & 1.34 & 0.04 & 0.31 & 0.17 \\ 9 & 0.34 & 0.39 & -0.25 & -0.12 & 0.39 & 0.12 & -0.37 & -0.94 & 0.37 & -0.39 & -1.02 & -0.24 & -0.07 & 1.1 \\ 10 & 0.27 & -0.21 & 0.22 & -0.83 & -0.21 & 0.83 & 0.39 & 0.06 & -0.39 & 0.21 & 0.8 & 0.12 & -0.5 & -1.18 \\ 11 & 2.14 & -0.8 & 1.96 & -0.95 & -0.8 & 0.95 & 1.02 & 1.34 & -1.02 & 0.8 & 2.42 & 0.48 & -0.57 & -3.05 \\ 12 & 0.16 & -0.12 & 0.73 & -0.5 & -0.12 & 0.5 & 0.24 & 0.04 & -0.24 & 0.12 & 0.48 & -1.53 & -0.3 & -0.71 \\ 13 & 0.19 & 0.5 & -0.08 & 0.15 & 0.5 & -0.15 & 0.07 & 0.31 & -0.07 & -0.5 & -0.57 & -0.3 & -1.51 & -0.21 \\ 14 & 1.02 & 1.18 & -0.75 & -0.35 & 1.18 & 0.35 & -1.1 & 0.17 & 1.1 & -1.18 & -3.05 & -0.71 & -0.21 & -0.69 \end{bmatrix}$$