#### SUPPLEMENTARY INFORMATION

# Sandwich-type Na<sub>6</sub>B<sub>7</sub><sup>-</sup> and Na<sub>8</sub>B<sub>7</sub><sup>+</sup> clusters: Charge-transfer complexes, four-fold $\pi/\sigma$ aromaticity, and dynamic fluxionality<sup>+</sup>

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#### Supplementary Information – Part I

- **Table S1.**Cartesian coordinates for the global-minimum (GM) structures of  $Na_6B_7^-$  (1,  $D_{3d}$ , $^1A_{1g}$ ) and  $Na_8B_7^+$  (5,  $D_{3d}$ ,  $^1A_{1g}$ ) clusters at the PBE0/6-311+G\* level.
- Figure S1. Alternative low-lying structures of  $Na_6B_7^-$  cluster. Relative energies at the PBE0/6-311+G\* level are shown in square brackets, with corrections for zero-point energies (ZPEs). Also shown are energies for top low-lying isomers at the single-point CCSD(T)/6-311G\*//PBE0/6-311+G\* level. All energies are in eV.
- Figure S2. Alternative low-lying structures of Na<sub>8</sub>B<sub>7</sub><sup>+</sup> cluster. Relative energies at the PBE0/6-311+G\* level are shown in square brackets, with corrections for ZPEs. Also shown are energies for top low-lying isomers at the single-point CCSD(T)/6-311G\*//PBE0/6-311+G\* level. All energies are in eV.
- **Figure S3.** Structural evolution of  $Na_8B_7^+$  cluster during the dynamic rotations. Two pathways are available via transition states **6** and **7**, which are denoted as TS<sub>1</sub> and

 $TS_2$ , respectively. Each pathway is associated to a soft vibrational mode of  $Na_8B_7^+$  cluster. The lower pathway is related to free rotation of  $B_7$  wheel against two  $Na_4$  subunits, while the upper one is due to twisting between two  $Na_4$  subunits.

- Figure S4. Calculated bond distances (in Å; black color), Wiberg bond indices (WBIs; blue color), and natural atomic charges (in |e|; red color) for (a) Na<sub>6</sub>B<sub>7</sub><sup>-</sup> (2, TS<sub>1</sub>), (b) Na<sub>6</sub>B<sub>7</sub><sup>-</sup> (3, TS<sub>2</sub>), and (c) Na<sub>6</sub>B<sub>7</sub><sup>-</sup> (4, LM). Here TS and LM represent transition state and local minimum, respectively. WBIs and natural atomic charges are obtained from natural bond orbital (NBO) analyses at the PBE0/6-311G\* level.
- Figure S5. Calculated bond distances (in Å; black color), WBIs (blue color), and natural atomic charges (in |e|; red color) for (a) Na<sub>8</sub>B<sub>7</sub><sup>+</sup> (6, TS<sub>1</sub>), (b) Na<sub>8</sub>B<sub>7</sub><sup>+</sup> (7, TS<sub>2</sub>), and (c) Na<sub>8</sub>B<sub>7</sub><sup>+</sup> (8, LM). WBIs and natural atomic charges are obtained from the NBO analyses at the PBE0/6-311G\* level.
- **Figure S6.** Canonical molecular orbitals (CMOs) of  $D_{3d}$  (**5**,  ${}^{1}A_{1g}$ ) GM structure of Na<sub>8</sub>B<sub>7</sub><sup>+</sup> cluster. (a) Six  $\sigma$  CMOs for peripheral two-center two-electron (2c-2e) B–B  $\sigma$  bonds in the B<sub>7</sub> wheel. (b) Three delocalized  $\sigma$  CMOs. (c) Three delocalized  $\pi$  CMOs. (d) Two delocalized  $\sigma$  CMOs over two Na<sub>4</sub> tetrahedra. Subsystems (b) through (d) collectively render four-fold ( $2\sigma/6\pi/6\sigma/2\sigma$ ) aromaticity for Na<sub>8</sub>B<sub>7</sub><sup>+</sup> cluster.
- **Figure S7.** Occupied CMOs of the  $D_{3d}$  (2,  ${}^{1}A_{1g}$ ) TS<sub>1</sub> structure for Na<sub>6</sub>B<sub>7</sub><sup>-</sup> cluster. The CMOs are similar to those in Figs. 4 and S6, except for a slight spatial shift of the electron clouds, which does not alter the essence of chemical bonding.
- **Figure S8.** Bonding pattern of the  $D_{3d}$  (2,  ${}^{1}A_{1g}$ ) TS<sub>1</sub> structure for Na<sub>6</sub>B<sub>7</sub><sup>-</sup> cluster on the basis of adaptive natural density partitioning (AdNDP) analysis. Occupation numbers (ONs) are indicated.
- **Figure S9.** Occupied CMOs of the  $D_{3h}$  (4,  ${}^{1}A_{1}$ ) LM structure for Na<sub>6</sub>B<sub>7</sub><sup>-</sup> cluster. The CMOs are similar to those in Figs. 4, S6, and S7, except for a slight spatial shift of the electron clouds, which does not alter the essence of chemical bonding.

- **Figure S10.** AdNDP bonding pattern of the  $D_{3h}$  (**4**,  ${}^{1}A_{1}$ ) LM structure for Na<sub>6</sub>B<sub>7</sub><sup>-</sup> cluster. ONs are indicated.
- **Figure S11.** Simulated photoelectron spectrum of  $Na_6B_7^-$  cluster at the time-dependent PBE0/6-311+G\* (TD-PBE0) level. The simulation was conducted using the  $D_{3d}$ (1,  ${}^{1}A_{1g}$ ) GM structure by fitting the calculated vertical detachment energies (VDEs) with unit-area Gaussian functions of 0.02 eV half-width.

#### Supplementary Information – Part II

A short movie extracted from the BOMD simulation for Na<sub>6</sub>B<sub>7</sub><sup>-</sup> cluster. The simulation was performed at 300 K for 50 ps. The movie roughly covers a time span of 8 ps. Similar BOMD properties have been probed for Na<sub>8</sub>B<sub>7</sub><sup>+</sup> cluster at 300 K (not shown).

**Figure S1.** Alternative low-lying structures of Na<sub>6</sub>B<sub>7</sub><sup>-</sup> cluster. Relative energies at the PBE0/6-311+G\* level are shown in square brackets, with corrections for zero-point energies (ZPEs). Also shown are energies for top low-lying isomers at the single-point CCSD(T)/6-311G\*//PBE0/6-311+G\* level. All energies are in eV.



#### (... continued)



**Figure S2.** Alternative low-lying structures of Na<sub>8</sub>B<sub>7</sub><sup>+</sup> cluster. Relative energies at the PBE0/6-311+G\* level are shown in square brackets, with corrections for ZPEs. Also shown are energies for top low-lying isomers at the single-point CCSD(T)/6-311G\*//PBE0/6-311+G\* level. All energies are in eV.



## (... continued)



Figure S3. Structural evolution of Na<sub>8</sub>B<sub>7</sub><sup>+</sup> cluster during the dynamic rotations. Two pathways are available via transition states 6 and 7, which are denoted as TS<sub>1</sub> and TS<sub>2</sub>, respectively. Each pathway is associated to a soft vibrational mode of Na<sub>8</sub>B<sub>7</sub><sup>+</sup> cluster. The lower pathway is related to free rotation of B<sub>7</sub> wheel against two Na<sub>4</sub> subunits, while the upper one is due to twisting between two Na<sub>4</sub> subunits.



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Figure S5. Calculated bond distances (in Å; black color), WBIs (blue color), and natural atomic charges (in |e|; red color) for (a) Na<sub>8</sub>B<sub>7</sub><sup>+</sup> (6, TS<sub>1</sub>), (b) Na<sub>8</sub>B<sub>7</sub><sup>+</sup> (7, TS<sub>2</sub>), and (c) Na<sub>8</sub>B<sub>7</sub><sup>+</sup> (8, LM). WBIs and natural atomic charges are obtained from the NBO analyses at the PBE0/6-311G\* level.



**Figure S6.** Canonical molecular orbitals (CMOs) of  $D_{3d}$  (**5**,  ${}^{1}A_{1g}$ ) GM structure of Na<sub>8</sub>B<sub>7</sub><sup>+</sup> cluster. (a) Six  $\sigma$  CMOs for peripheral two-center two-electron (2c-2e) B–B  $\sigma$  bonds in the B<sub>7</sub> wheel. (b) Three delocalized  $\sigma$  CMOs. (c) Three delocalized  $\pi$  CMOs. (d) Two delocalized  $\sigma$  CMOs over two Na<sub>4</sub> tetrahedra. Subsystems (b) through (d) collectively render four-fold ( $2\sigma/6\pi/6\sigma/2\sigma$ ) aromaticity for Na<sub>8</sub>B<sub>7</sub><sup>+</sup> cluster.



**Figure S7.** Occupied CMOs of the  $D_{3d}$  (2,  ${}^{1}A_{1g}$ ) TS<sub>1</sub> structure for Na<sub>6</sub>B<sub>7</sub><sup>-</sup> cluster. The CMOs are similar to those in Figs. 4 and S6, except for a slight spatial shift of the electron clouds, which does not alter the essence of chemical bonding.



**Figure S8.** Bonding pattern of the  $D_{3d}$  (2,  ${}^{1}A_{1g}$ ) TS<sub>1</sub> structure for Na<sub>6</sub>B<sub>7</sub><sup>-</sup> cluster on the basis of adaptive natural density partitioning (AdNDP) analysis. Occupation numbers (ONs) are indicated.



3×7c-2e π bonds ON = 2.00-1.86 |e| **Figure S9.** Occupied CMOs of the  $D_{3h}$  (4,  ${}^{1}A_{1}$ ) LM structure for Na<sub>6</sub>B<sub>7</sub><sup>-</sup> cluster. The CMOs are similar to those in Figs. 4, S6, and S7, except for a slight spatial shift of the electron clouds, which does not alter the essence of chemical bonding.



**Figure S10.** AdNDP bonding pattern of the  $D_{3h}$  (4,  ${}^{1}A_{1}$ ) LM structure for Na<sub>6</sub>B<sub>7</sub><sup>-</sup> cluster. ONs are indicated.



**Figure S11.** Simulated photoelectron spectrum of  $Na_6B_7^-$  cluster at the time-dependent PBE0/6-311+G\* (TD-PBE0) level. The simulation was conducted using the  $D_{3d}$ (1,  ${}^{1}A_{1g}$ ) GM structure by fitting the calculated vertical detachment energies (VDEs) with unit-area Gaussian functions of 0.02 eV half-width.



**Table S1.** Cartesian coordinates for the global-minimum (GM) structures of  $Na_6B_7^-$  (1,  $D_{3d}$ , $^1A_{1g}$ ) and  $Na_8B_7^+$  (5,  $D_{3d}$ ,  $^1A_{1g}$ ) clusters at the PBE0/6-311+G\* level.

(a) GM, Na<sub>6</sub>B<sub>7</sub><sup>-</sup> (**1**,  $D_{3d}$ , <sup>1</sup>A<sub>1g</sub>)

В	0.81156285	1.40566809	0.00000000
В	-0.81156285	1.40566809	0.00000000
В	0.81156285	-1.40566809	0.00000000
В	-0.81156285	-1.40566809	0.00000000
В	-1.62312570	-0.00000000	0.00000000
В	1.62312570	0.00000000	0.00000000
В	0.00000000	0.00000000	0.00000000
Na	1.64088312	0.94736431	2.59772681
Na	-0.00000000	1.89472862	-2.59772681
Na	-1.64088312	0.94736431	2.59772681
Na	-1.64088312	-0.94736431	-2.59772681
Na	0.00000000	-1.89472862	2.59772681
Na	1.64088312	-0.94736431	-2.59772681

### (b) GM, Na<sub>8</sub>B<sub>7</sub><sup>+</sup> ( $\mathbf{5}$ , $D_{3d}$ , <sup>1</sup>A<sub>1g</sub>)

В	0.81035200	1.40357100	0.00000000
В	-0.81035200	1.40357100	0.00000000
В	0.81035200	-1.40357100	0.00000000
В	-0.81035200	-1.40357100	0.00000000
В	-1.62070400	0.00000000	0.00000000
В	1.62070400	0.00000000	0.00000000
В	0.00000000	0.00000000	0.00000000
Na	1.76725100	1.02032300	2.48933400

Na	0.00000000	2.04064600	-2.48933400
Na	-1.76725100	1.02032300	2.48933400
Na	-1.76725100	-1.02032300	-2.48933400
Na	0.00000000	-2.04064600	2.48933400
Na	1.76725100	-1.02032300	-2.48933400
Na	0.00000000	0.00000000	5.46523900
Na	0.00000000	0.00000000	-5.46523900