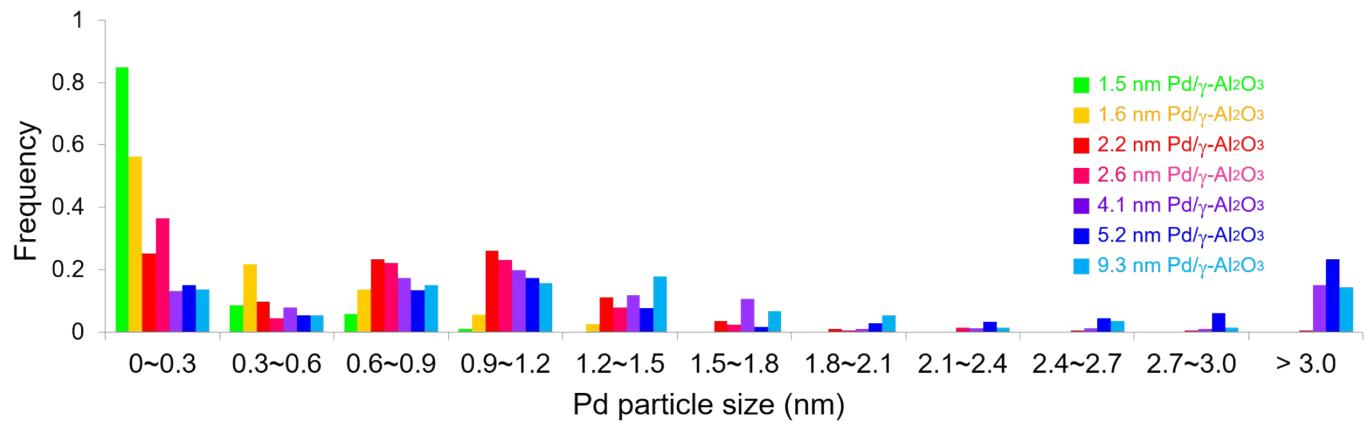


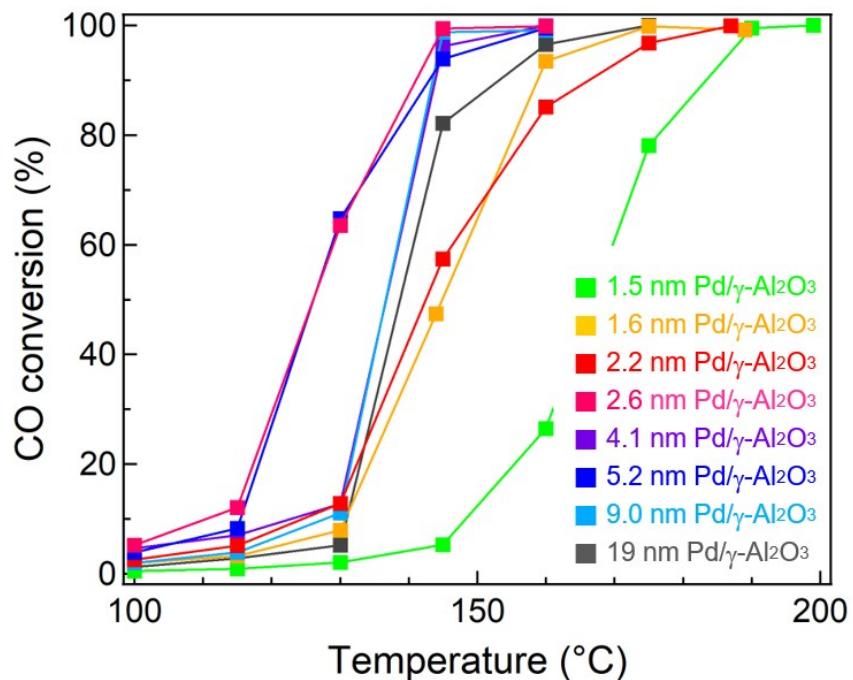
**Figure S1.** Typical Cs-STEM images of (a) 1.6 nm Pd/ $\gamma$ -Al<sub>2</sub>O<sub>3</sub>, (b) 2.6 nm Pd/ $\gamma$ -Al<sub>2</sub>O<sub>3</sub>, (c) 4.1 nm Pd/ $\gamma$ -Al<sub>2</sub>O<sub>3</sub>, and (d) 5.2 nm Pd/ $\gamma$ -Al<sub>2</sub>O<sub>3</sub>.

**Table S1.** Counted particle numbers of Pd/ $\gamma$ -Al<sub>2</sub>O<sub>3</sub> in Figure S2.

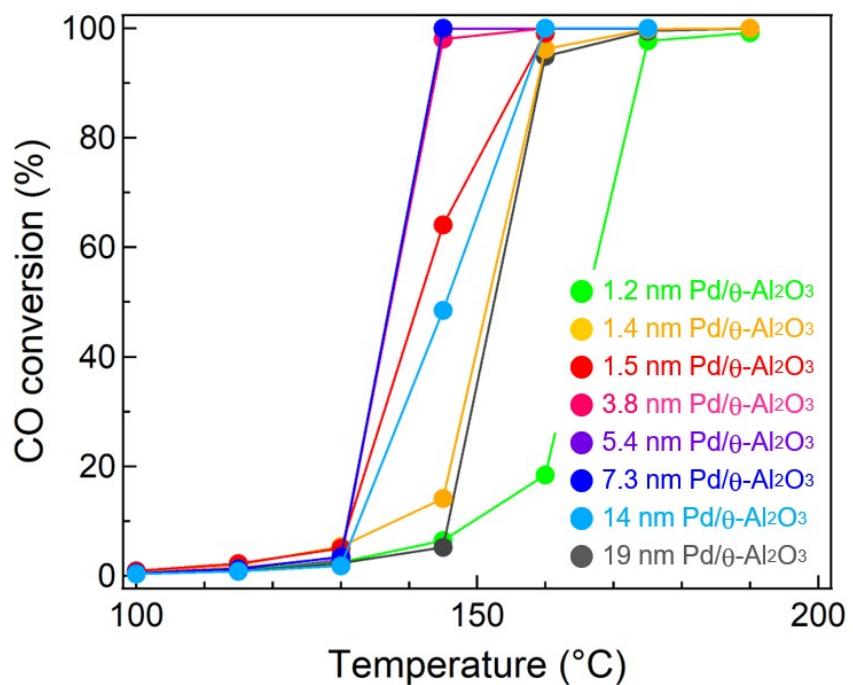
Catalyst	Counted particle number
1.5 nm Pd/ $\gamma$ -Al <sub>2</sub> O <sub>3</sub>	245
1.6 nm Pd/ $\gamma$ -Al <sub>2</sub> O <sub>3</sub>	197
2.2 nm Pd/ $\gamma$ -Al <sub>2</sub> O <sub>3</sub>	370
2.6 nm Pd/ $\gamma$ -Al <sub>2</sub> O <sub>3</sub>	203
4.1 nm Pd/ $\gamma$ -Al <sub>2</sub> O <sub>3</sub>	418
5.2 nm Pd/ $\gamma$ -Al <sub>2</sub> O <sub>3</sub>	185
9.0 nm Pd/ $\gamma$ -Al <sub>2</sub> O <sub>3</sub>	147



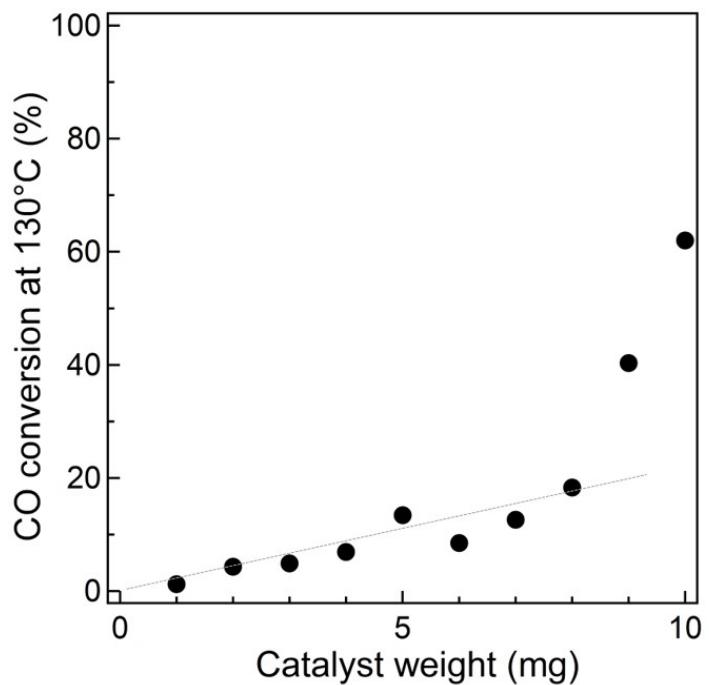
**Figure S2.** Size distributions for the number of Pd particles of various Pd/ $\gamma$ -Al<sub>2</sub>O<sub>3</sub> catalysts.



**Figure S3.** CO conversion over 10 mg of various Pd/γ-Al<sub>2</sub>O<sub>3</sub> catalysts.



**Figure S4.** CO conversion over 10 mg of various Pd/θ-Al<sub>2</sub>O<sub>3</sub> catalysts.

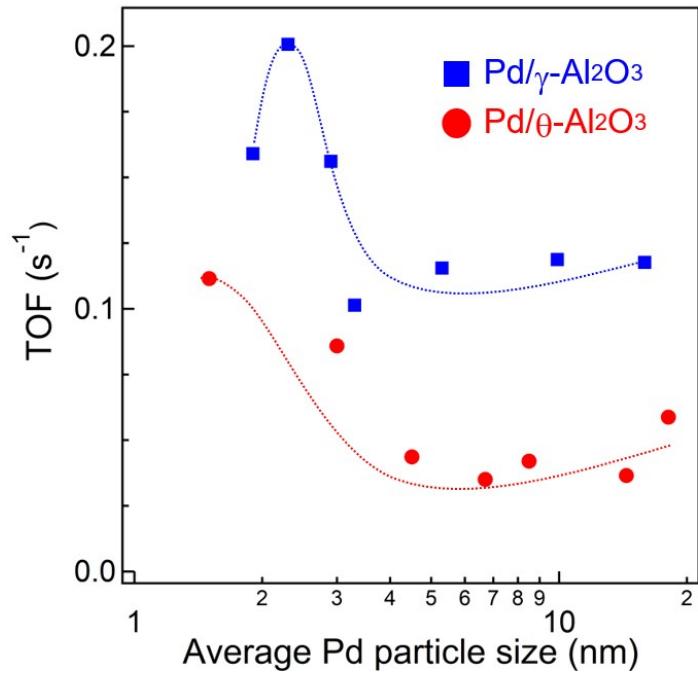


**Figure S5.** CO conversion at 130°C on various amounts of 2.2 nm Pd/ $\gamma$ -Al<sub>2</sub>O<sub>3</sub>. When the CO conversion on < 10 mg of the catalyst was evaluated, the catalyst powder was diluted with inert quartz powder to be 10 mg of powder in the tube reactor. A linear relationship between catalyst amount and CO conversion is seen on the figure in the range of < 20 % CO conversion. The data confirms that our kinetic analysis based on < 20 % CO conversion does not contain the problems due to thermal and gas diffusion effects.

**Table S2.** The list of data for TOF calculation

Catalyst	Catalyst weight <sup>a</sup> (mg)	Molar amount of surface Pd <sup>b</sup> ( $\times 10^{-7}$ mol)	CO conversion (%)	CO oxidation rate <sup>c</sup> ( $\times 10^{-8}$ mol $\cdot$ s $^{-1}$ )	TOF (s $^{-1}$ )
1.5 nm Pd/ $\gamma$ -Al <sub>2</sub> O <sub>3</sub>	10	0.66	1.7 $\pm$ 0.2	0.51 $\pm$ 0.06	0.076 $\pm$ 0.010
1.6 nm Pd/ $\gamma$ -Al <sub>2</sub> O <sub>3</sub>	10	1.34	6.0 $\pm$ 1.3	1.79 $\pm$ 0.38	0.134 $\pm$ 0.028
2.2 nm Pd/ $\gamma$ -Al <sub>2</sub> O <sub>3</sub>	10	2.53	15.1 $\pm$ 2.7	4.49 $\pm$ 0.80	0.177 $\pm$ 0.032
2.6 nm Pd/ $\gamma$ -Al <sub>2</sub> O <sub>3</sub>	2	0.85	3.8 $\pm$ 0.4	1.12 $\pm$ 0.11	0.133 $\pm$ 0.013
4.1 nm Pd/ $\gamma$ -Al <sub>2</sub> O <sub>3</sub>	2	1.03	4.4 $\pm$ 2.6	1.30 $\pm$ 0.79	0.079 $\pm$ 0.010
5.2 nm Pd/ $\gamma$ -Al <sub>2</sub> O <sub>3</sub>	2	0.90	3.0 $\pm$ 0.9	0.90 $\pm$ 0.26	0.100 $\pm$ 0.028
9.0 nm Pd/ $\gamma$ -Al <sub>2</sub> O <sub>3</sub>	10	2.35	8.5 $\pm$ 1.7	2.52 $\pm$ 0.52	0.107 $\pm$ 0.022
19 nm Pd/ $\gamma$ -Al <sub>2</sub> O <sub>3</sub>	10	1.11	5.2	1.55	0.140
1.2 nm Pd/ $\theta$ -Al <sub>2</sub> O <sub>3</sub>	10	0.91	2.5	0.74	0.081
1.4 nm Pd/ $\theta$ -Al <sub>2</sub> O <sub>3</sub>	10	1.56	5.4	1.61	0.103
1.5 nm Pd/ $\theta$ -Al <sub>2</sub> O <sub>3</sub>	10	3.42	5.0	1.49	0.044
3.8 nm Pd/ $\theta$ -Al <sub>2</sub> O <sub>3</sub>	10	2.74	3.4	1.01	0.037
5.4 nm Pd/ $\theta$ -Al <sub>2</sub> O <sub>3</sub>	2.5	0.99	0.9	0.28	0.028
7.3 nm Pd/ $\theta$ -Al <sub>2</sub> O <sub>3</sub>	10	2.89	3.5	1.04	0.036
14 nm Pd/ $\theta$ -Al <sub>2</sub> O <sub>3</sub>	10	1.47	1.8	0.54	0.037
19 nm Pd/ $\theta$ -Al <sub>2</sub> O <sub>3</sub>	10	1.09	2.3	0.68	0.063

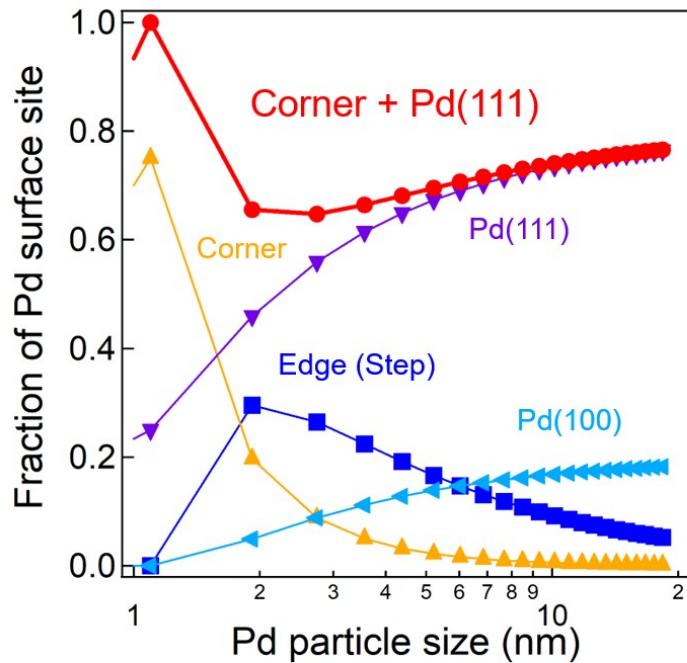
<sup>a</sup>Catalyst weight used to evaluate the TOF. <sup>b</sup>Molar amount of surface Pd (mol) was defined as (molar amount of Pd atom (mol)) / (Pd dispersion (%) / 100). <sup>c</sup>CO oxidation rate (mol $\cdot$ s $^{-1}$ ) was defined as (flow rate of CO molecule (mol $\cdot$ s $^{-1}$ )) $\times$ (CO conversion (%)) / 100



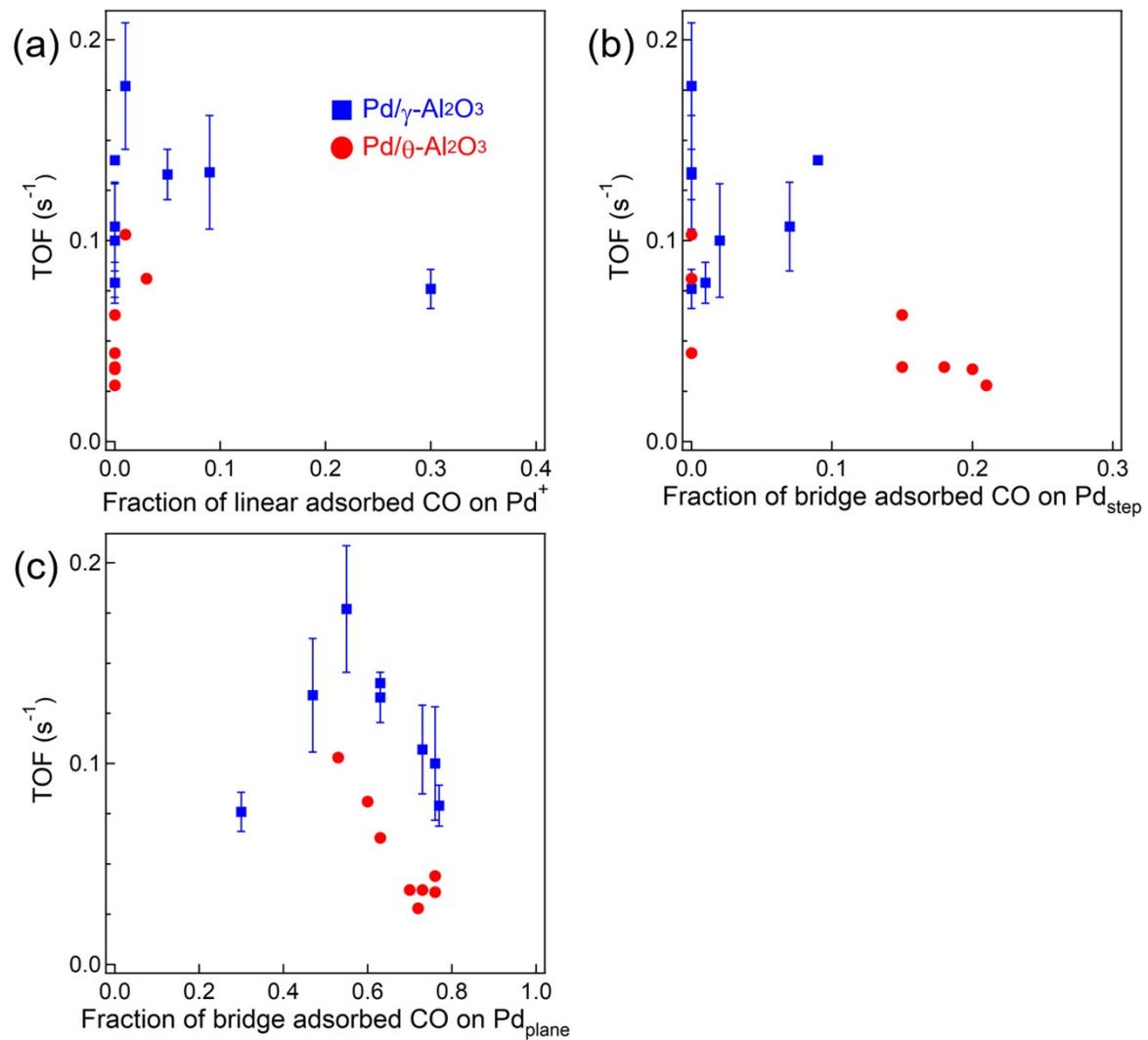
**Figure S6.** Dependence of TOF at 130°C on average Pd particle size estimated from H<sub>2</sub> pulse chemisorption. The 0.1wt% Pd/Al<sub>2</sub>O<sub>3</sub> with high fraction of the isolated were excluded.

**Table S3.** The ratios of the IR band area of various CO species on Pd/Al<sub>2</sub>O<sub>3</sub> catalysts.

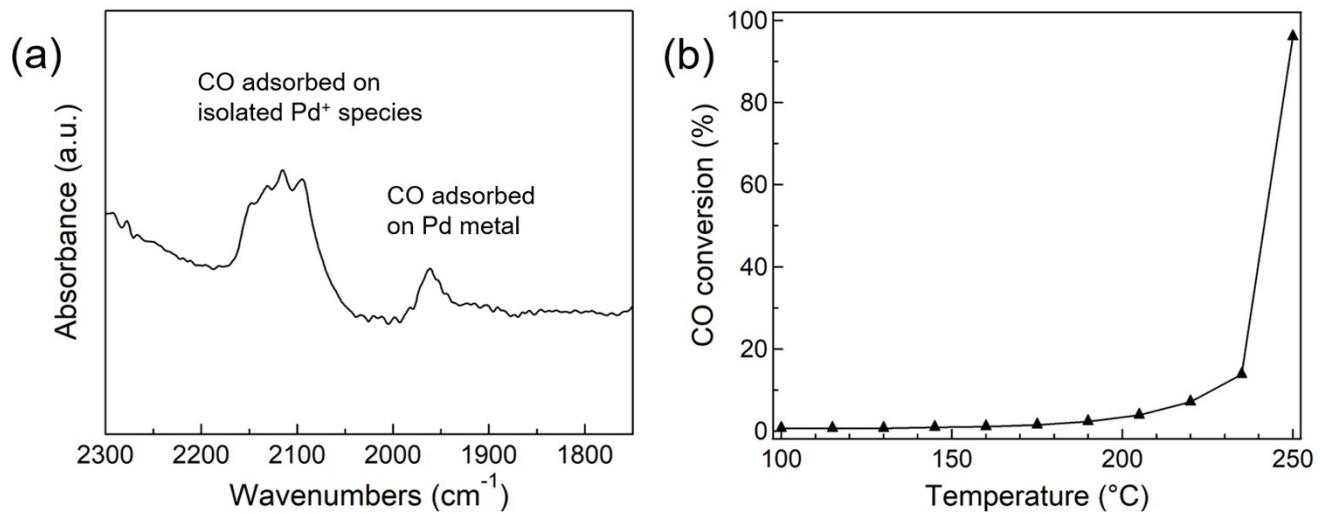
Catalyst	Linear adsorbed	Linear adsorbed	Bridge adsorbed	Bridge adsorbed
	CO on Pd <sup>+</sup> (2200-2100 cm <sup>-1</sup> )	CO on Pd <sup>0</sup> (2100-2000 cm <sup>-1</sup> )	CO on Pd step (2000-1960 cm <sup>-1</sup> )	CO on plane (1960-1700 cm <sup>-1</sup> )
1.5 nm Pd/γ-Al <sub>2</sub> O <sub>3</sub>	0.30	0.40	0.00	0.30
1.6 nm Pd/γ-Al <sub>2</sub> O <sub>3</sub>	0.09	0.44	0.00	0.47
2.2 nm Pd/γ-Al <sub>2</sub> O <sub>3</sub>	0.01	0.45	0.00	0.55
2.6 nm Pd/γ-Al <sub>2</sub> O <sub>3</sub>	0.05	0.33	0.00	0.63
4.1 nm Pd/γ-Al <sub>2</sub> O <sub>3</sub>	0.00	0.22	0.01	0.77
5.2 nm Pd/γ-Al <sub>2</sub> O <sub>3</sub>	0.00	0.23	0.02	0.76
9.0 nm Pd/γ-Al <sub>2</sub> O <sub>3</sub>	0.00	0.19	0.07	0.73
19 nm Pd/γ-Al <sub>2</sub> O <sub>3</sub>	0.00	0.28	0.09	0.63
1.2 nm Pd/θ-Al <sub>2</sub> O <sub>3</sub>	0.03	0.37	0.00	0.60
1.4 nm Pd/θ-Al <sub>2</sub> O <sub>3</sub>	0.01	0.45	0.00	0.53
1.5 nm Pd/θ-Al <sub>2</sub> O <sub>3</sub>	0.00	0.24	0.00	0.76
3.8 nm Pd/θ-Al <sub>2</sub> O <sub>3</sub>	0.00	0.09	0.18	0.73
5.4 nm Pd/θ-Al <sub>2</sub> O <sub>3</sub>	0.00	0.06	0.21	0.72
7.3 nm Pd/θ-Al <sub>2</sub> O <sub>3</sub>	0.00	0.05	0.20	0.76
14 nm Pd/θ-Al <sub>2</sub> O <sub>3</sub>	0.00	0.15	0.15	0.70
19 nm Pd/θ-Al <sub>2</sub> O <sub>3</sub>	0.00	0.22	0.15	0.63



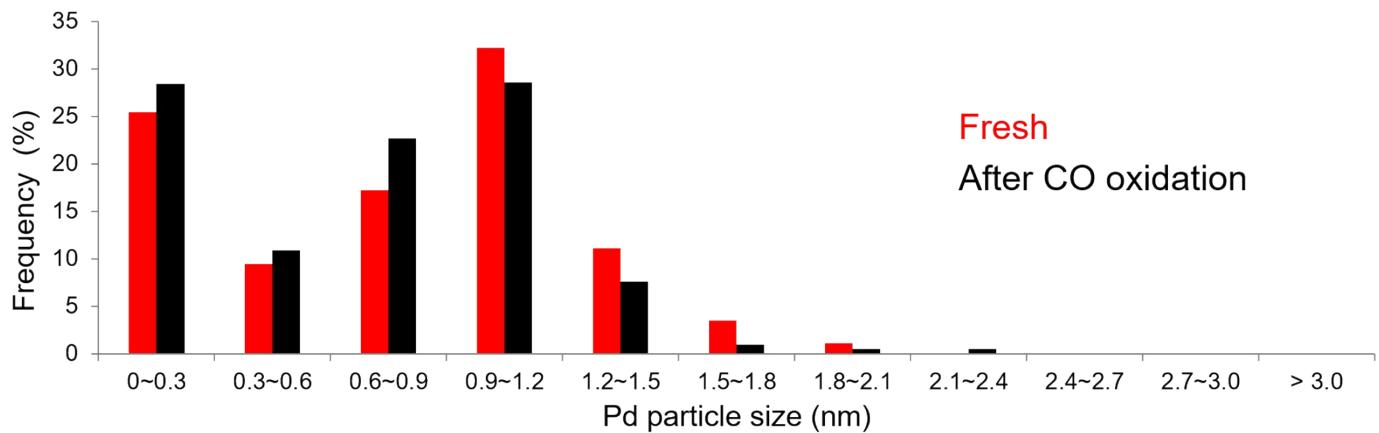
**Figure S7.** Particle size dependence of fraction of corner site and Pd(111) (●) and corner site (▲), Pd(111) (▼), Pd(100) (◀), edge site (or step) (■). We assumed a cubo-octahedron as a tentative model particle.



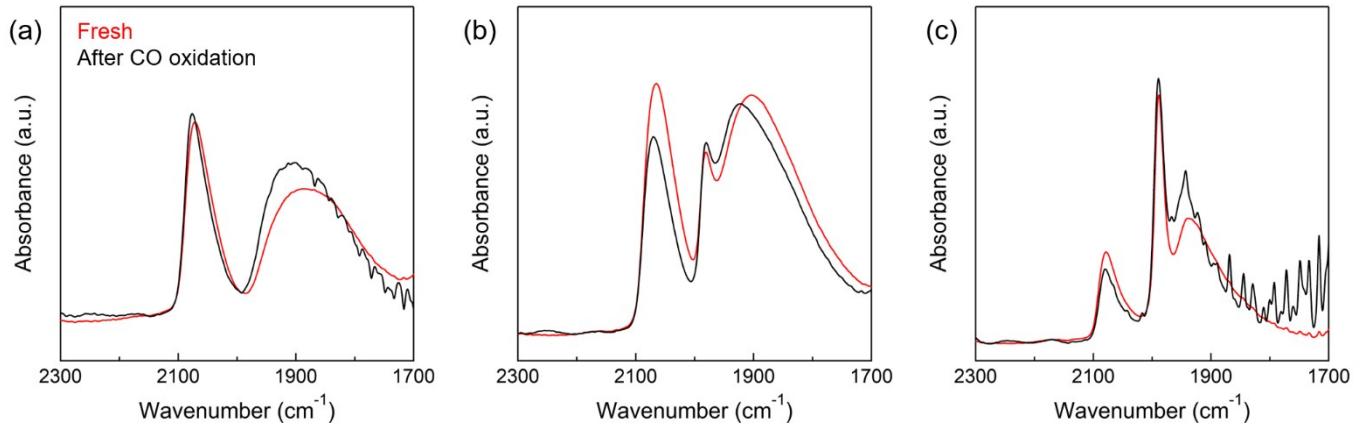
**Figure S8.** Plot of TOFs (at 130°C) against the fraction of (a) linear adsorbed CO on  $Pd^+$ , (b) bridge adsorbed CO on step site and (c) linear adsorbed CO on plane.



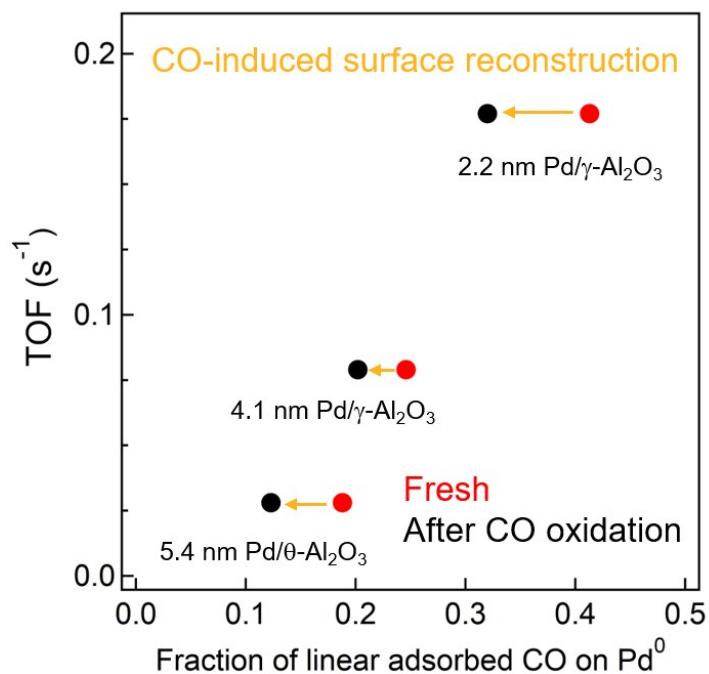
**Figure S9.** (a) IR spectra of adsorbed CO on Pd/ZSM-5. (b) The CO conversion of Pd/ZSM-5 as a function of temperature.



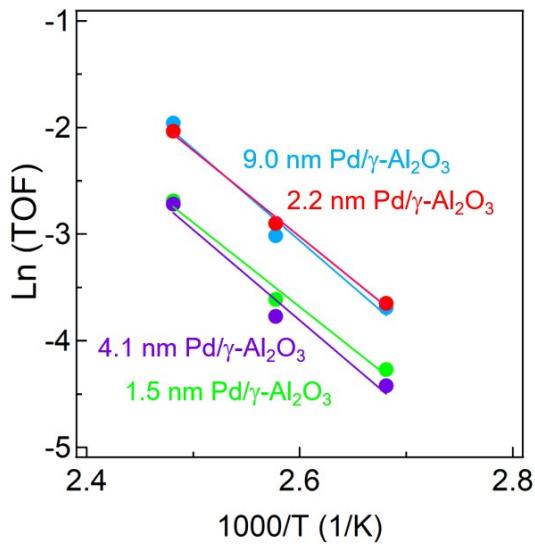
**Figure S10.** Size distributions for the number of Pd particles of 2.2 nm Pd/ $\gamma$ -Al<sub>2</sub>O<sub>3</sub> catalyst after prereduction by H<sub>2</sub> (red) and CO oxidation reaction at 130°C (black).



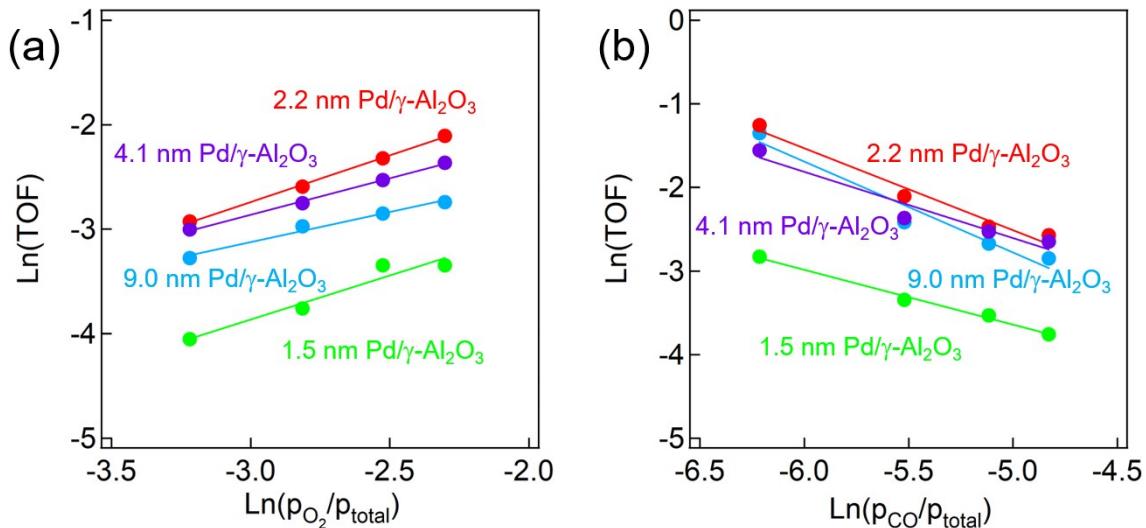
**Figure S11.** IR spectra of adsorbed CO on (a) 2.2 nm Pd/ $\gamma$ -Al<sub>2</sub>O<sub>3</sub> and (b) 4.1 nm Pd/ $\gamma$ -Al<sub>2</sub>O<sub>3</sub>, (c) 5.4 nm Pd/ $\theta$ -Al<sub>2</sub>O<sub>3</sub> after prereduction by H<sub>2</sub> (red) and CO oxidation at 130°C (black).



**Figure S12.** Plot of TOFs (at 130°C) against the fraction of linear adsorbed CO on Pd<sup>0</sup> for Pd/Al<sub>2</sub>O<sub>3</sub> after prereduction by H<sub>2</sub> (red) and CO oxidation (black).



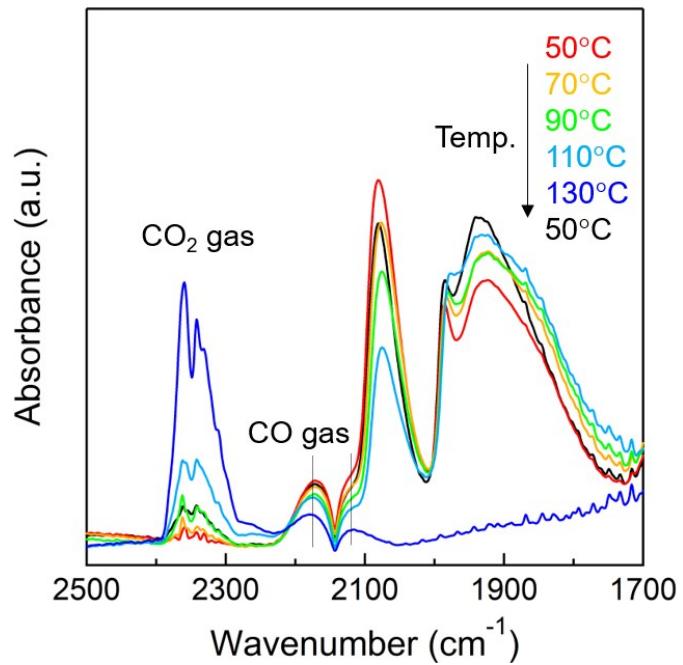
**Figure S13.** The dependence of TOFs on temperature for CO oxidation over Pd/γ-Al<sub>2</sub>O<sub>3</sub>.



**Figure S14.** The dependence of TOFs on partial pressure of (a) O<sub>2</sub> and (b) CO for CO oxidation over Pd/γ-Al<sub>2</sub>O<sub>3</sub>.

**Table S4.** The apparent activation energy (E<sub>a</sub>) and the reaction order for CO oxidation over Pd/γ-Al<sub>2</sub>O<sub>3</sub>.

Catalyst	E <sub>a</sub> (kJ mol <sup>-1</sup> )	Reaction order of O <sub>2</sub>	Reaction order of CO
1.5 nm Pd/γ-Al <sub>2</sub> O <sub>3</sub>	66±8	0.84±0.15	-0.66±0.04
2.2 nm Pd/γ-Al <sub>2</sub> O <sub>3</sub>	66±7	0.89±0.02	-0.98±0.12
4.1 nm Pd/γ-Al <sub>2</sub> O <sub>3</sub>	71±11	0.69±0.03	-0.79±0.15
9.0 nm Pd/γ-Al <sub>2</sub> O <sub>3</sub>	72±11	0.58±0.06	-1.08±0.18



**Figure S15.** IR spectra of adsorbed CO on 4.1 nm Pd/\gamma-Al<sub>2</sub>O<sub>3</sub> measured under a flow of gaseous mixtures (0.4% CO, 10% O<sub>2</sub>, Ar balance, 100 mL/min) at various temperatures.