Supplementary Information

Two-dimensional infrared spectroscopy from the gas to liquid phase: Density dependent *J*-scrambling, vibrational relaxation, and the onset of liquid character

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2DIR spectra and CLS decays of N₂O in SF₆ at $\rho^* = 0.86$:



Figure S1. 2DIR spectra and corresponding CLS decays of N₂O ν_3 in SF₆ at $\rho^* = 0.86$. Red contours denote positive-going GSB-SE signals and blue contours denote negative-going ESA signals.

Hard sphere collision time determination:

The mean free time for a single N₂O molecule is calculated using a hard sphere model at the given state point density of SF₆ and the mean speed is based on a Maxwell-Boltzmann speed distribution for an ideal gas. The collision frequency, v_{coll} , is given by:

$$\nu_{\rm coll} = N_{\rm A} \rho_{\rm SF_6} \pi \left(r_{\rm SF_6} + r_{\rm N_2O} \right)^2 \sqrt{\frac{8RT}{\pi \mu_{\rm N_2O}}}$$
(Eq. S8)

where N_A is the Avogadro constant (6.022 × 10²³ mol⁻¹), ρ_{SF_6} is the respective density of SF₆¹, $r_{SF_6} = 2.326 \times 10^{-10} \text{ m}^2$ and $r_{N_2O} = 1.94 \times 10^{-10} \text{ m}^3$ are the radii of SF₆ and N₂O, respectively, *R* is the universal gas constant (8.3145 J mol⁻¹ K⁻¹), *T* is the temperature of the solution, and $\mu_{N_2O} =$ 0.03382 kg mol⁻¹ is the reduced mass of N₂O. The mean free time between collisions is then calculated as the inverse of the collision frequency:

$$\tau_{\rm coll} = \frac{1}{\nu_{\rm coll}} \tag{Eq. S9}$$

FTIR spectra of N₂O in liquid SF₆ ($\rho^* = 1.87$):



Figure S2. Observed (blue) FTIR spectrum of the v_3 asymmetric stretch mode of N₂O in $\rho^* =$ 1.87 (liquid) SF₆ (20°C, 22 atm, 0.92*T*_c, 0.60*P*_c). A sum of 2 Lorentzian fit (red) is overlaid with peaks centered at 2221 cm⁻¹, the observed v_3 peak maximum, and 2209 cm⁻¹, the frequency of the red-shifted N₂O bending (v_2) hot band absorption ($v_2 \rightarrow v_2 + v_3$) to demonstrate the dominant Lorentzian character of this absorption feature.

Magic angle, one-color, pump-probe responses of the v_3 v = 1 excited state of N₂O in SF₆:



Figure S3. Magic angle pump-probe spectrum of N₂O ν_3 in SF₆ at $\rho^* = 0.16$.



Figure S4. Magic angle pump-probe spectrum of N₂O ν_3 in SF₆ at $\rho^* = 0.30$.



Figure S5. Magic angle pump-probe spectrum of N₂O ν_3 in SF₆ at $\rho^* = 0.86$.



Figure S6. Magic angle pump-probe spectrum of N₂O ν_3 in SF₆ at $\rho^* = 0.99$.



Figure S7. Magic angle pump-probe spectrum of N₂O ν_3 in SF₆ at ρ^* 1.36.



Figure S8. Magic angle pump-probe spectrum of N₂O ν_3 in SF₆ at ρ^* 1.87.

Rate equations for this one-color N_2O ν_3 pump-probe response in SF₆ corresponding to mechanism:

The differential rate equations for the N₂O ν_3 pump-probe responses in SF₆ are given by:

$$\frac{dN_{001}}{dt} = -\frac{N_{001}(t)}{T_1}$$
(Eq. S1)

$$\frac{dN_{100}}{dt} = \frac{N_{001}(t)}{T_1} - \frac{N_{100}(t)}{T_2}$$
(Eq. S2)

$$\frac{dN_{000}}{dt} = \frac{N_{100}(t)}{T_2}$$
(Eq. S3)

The time-dependent populations within this model are given by:

$$N_{001}(t) \propto e^{-t/T_1}$$
 (Eq. S4)

$$N_{100}(t) \propto \frac{T_2}{T_2 - T_1} e^{-t/T_2} - \frac{T_2}{T_2 - T_1} e^{-t/T_1}$$
 (Eq. S5)

$$N_{000}(t) \propto 1 - \frac{T_2}{T_2 - T_1} e^{-t/T_2} + \frac{T_1}{T_2 - T_1} e^{-t/T_1}$$
 (Eq. S6)

The corresponding normalized pump-probe signal at delay time *t* is correspondingly given by:

$$\Delta OD(t) = C_1 e^{-k_1 t} - C_2 \left(\frac{k_1}{k_1 - k_2} e^{-k_1 t} - \frac{k_1}{k_1 - k_2} e^{-k_2 t} \right)$$
(Eq. S7)

where C_1 and C_2 are proportional to the $(00^00) \rightarrow (00^01)$ and $(10^00) \rightarrow (10^01)$ absorption cross sections respectively, and k_1 and k_2 are the inverse lifetimes of the v_3 and v_1 N₂O states, respectively. The fit parameters, i.e., the coefficients and lifetimes, are given for all densities in Table 2.



Figure S9. Representative best-fit to the v_3 resonant pump-probe response in $\rho^* = 0.86$ SF₆ and the component kinetics for the v_3 vibrational energy relaxation and the subsequent v_1 population build up

References:

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2. Jameson, C. J.; Jameson, A. K., Effective collision cross sections for SF6 from nuclear magnetic relaxation. *The Journal of Chemical Physics* **1988**, *88* (12), 7448-7452.

3. Yardley, J. T., *Introduction to Molecular Energy Transfer*. Academic Press: New York, 1980.