

## Supplementary Information

### Band Engineering and Hybridization of Competing Arsenene

#### Allotropes: A Computational Study

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#### COMPUTATIONAL DETAILS:

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The Vienna Ab initio Simulation Package (VASP)<sup>1</sup> within the framework of density functional theory (DFT) was adopted to perform structural relaxations and electronic structure calculations. The Perdew-Burke-Ernzerhof functional<sup>2</sup> in the generalized gradient approximation (GGA)<sup>3</sup> was used. The electron-ion interactions were treated using the projector-augmented-wave (PAW) method<sup>4</sup> with  $4s^24p^3$  as the valence electrons of As. A plane-wave basis set cutoff of 500 eV and the Monkhorst-Pack (MP) scheme<sup>5</sup> with a dense  $k$ -point grid of  $2\pi \times 0.03 \text{ \AA}^{-1}$  spacing in the Brillouin zone were adopted to ensure the energy converges to 1 meV/atom. The separation along the  $c$  direction is larger than 15  $\text{\AA}$  for all systems. During the structural relaxation, the energy convergent criterion was set to  $10^{-5}$  eV per unit cell, and the atomic forces were smaller than  $0.01 \text{ eV \AA}^{-1}$ . For multiple layers, van der Waals interaction was considered in the vdW-DF level using the optB88 exchange functional<sup>6</sup>. Phonon dispersions were calculated using Phonopy<sup>7</sup>. Ab-initio molecular dynamics simulations adopting the canonical (NVT) ensemble were performed with a time step of 1 fs for a total simulation time of 2 ps at 300 K, 600 K and 1000 K using a  $3 \times 5 \times 1$  supercell (60 atoms), a  $3 \times 3 \times 1$  supercell (72 atoms) and a  $3 \times 3 \times 1$  supercell (72 atoms) for  $\gamma$ -As,  $\delta'$ -As and s/o-As, respectively. Band structures were calculated in the PBE and hybrid functional (HSE06) levels<sup>8</sup>. The simulated STM image was constructed on the basis of Tersoff–Hamann theory<sup>9</sup> and visualized using the p4VASP program<sup>10</sup>. Spin-orbit coupling (SOC) was neglected due to its minor effects on As<sup>11</sup>. The minimum energy pathway (MEP) between different allotropes was determined utilizing transition state theory as formulated in the generalized solid-state nudged elastic band (G-SSNEB) method<sup>12</sup> implemented in the VTST extension of VASP.

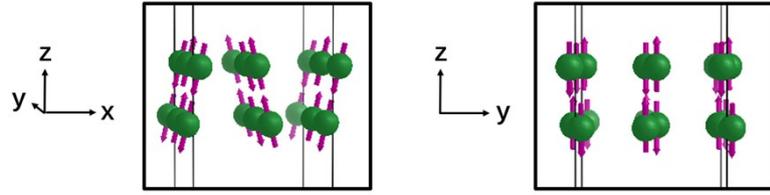
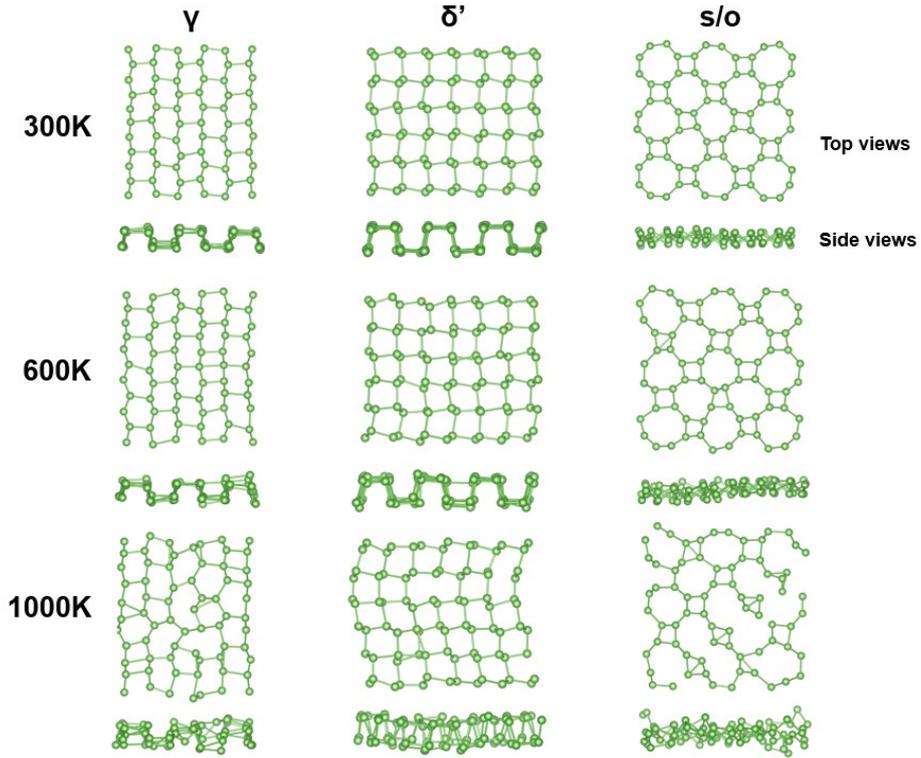
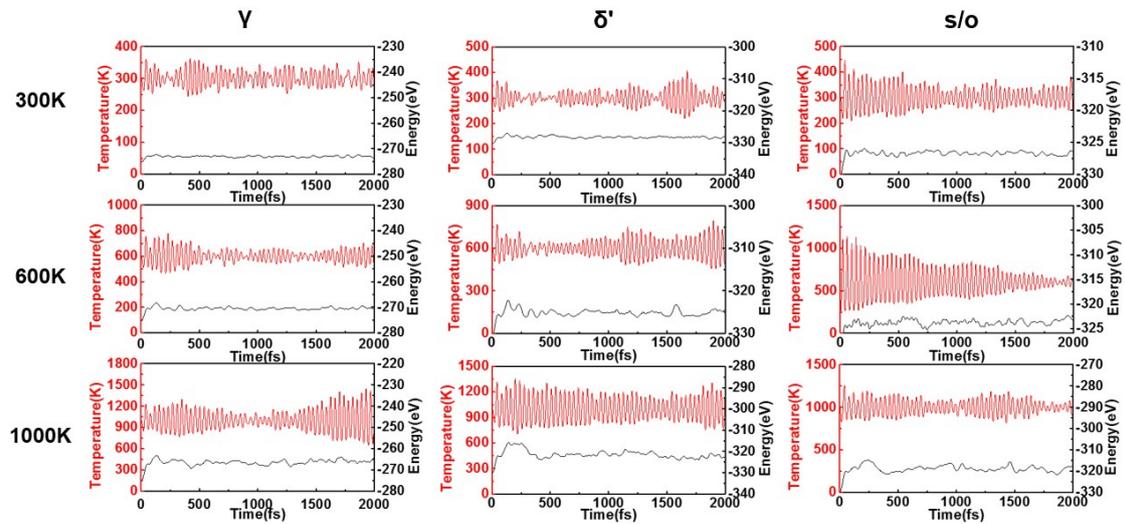


Fig. S1. Phonon vibrational mode of  $\delta$ -As with imaginary frequency at  $\Gamma$  point.

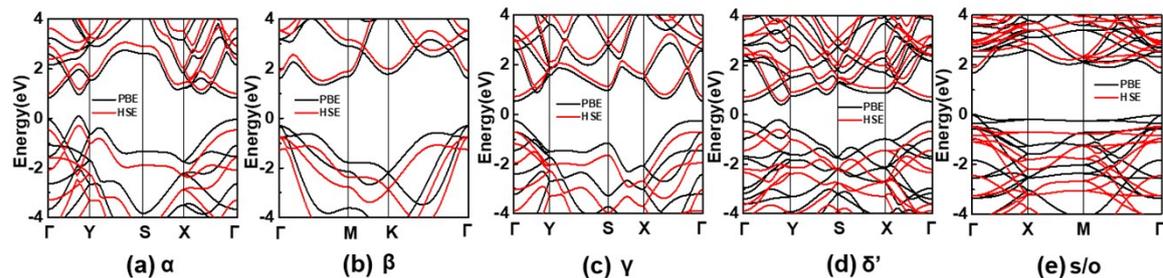


(a)

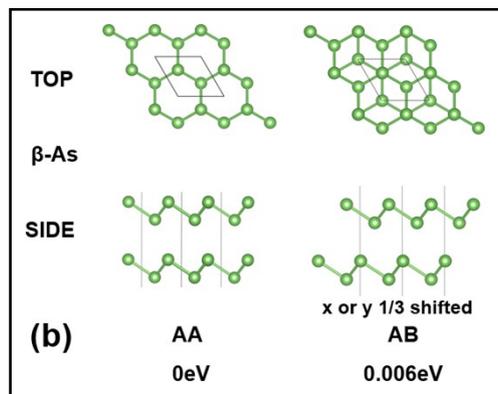
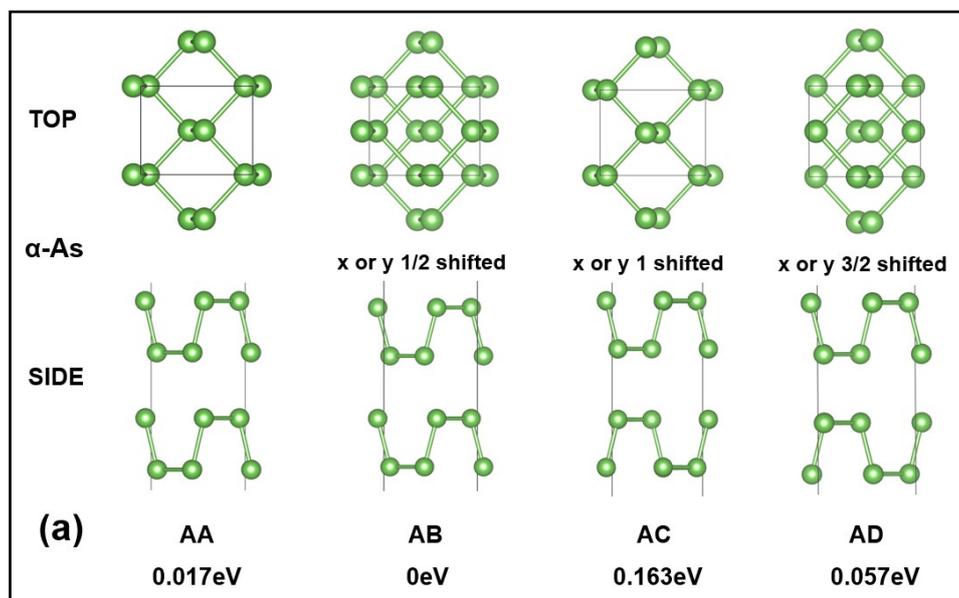


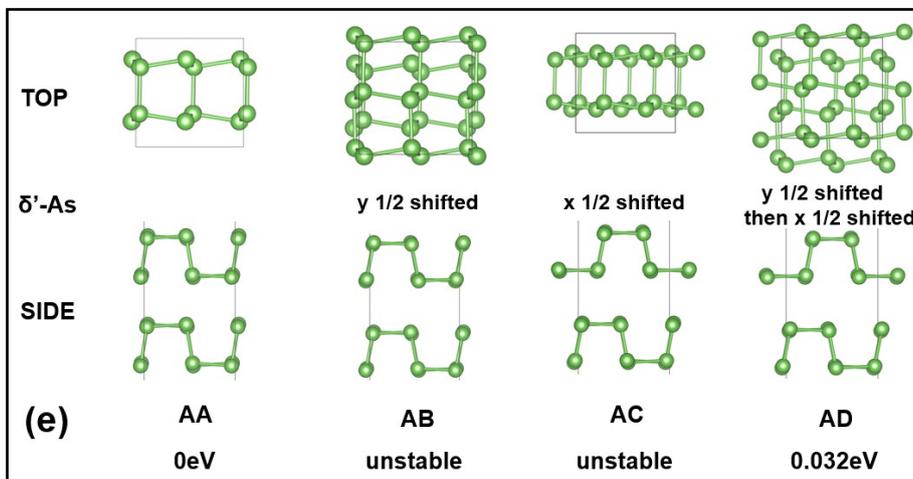
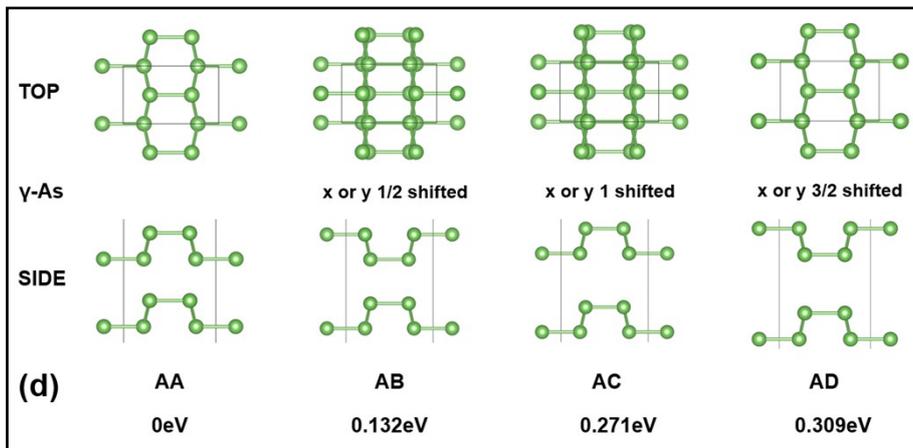
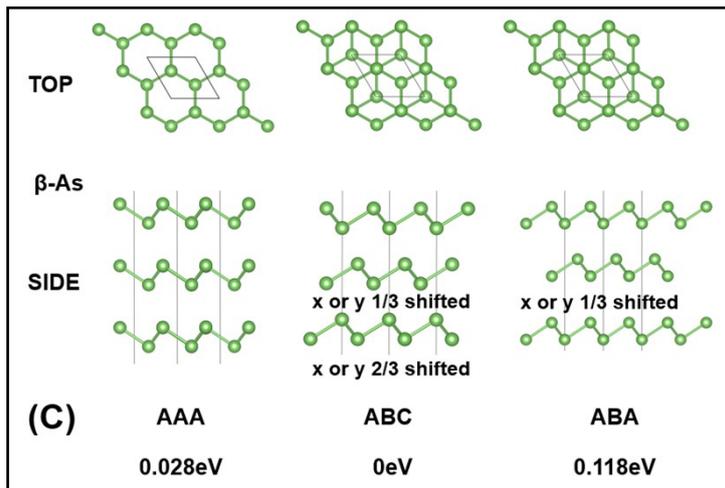
(b)

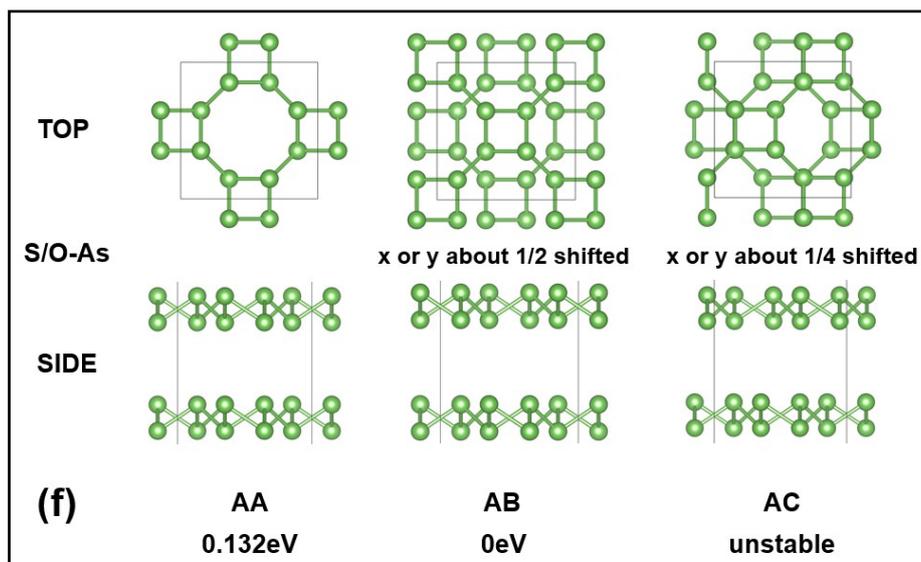
**Fig. S2.** (a) Snapshots of canonical molecular dynamics simulations of the  $\gamma$ ,  $\delta'$  and s/o phases at 300 K, 600 K, and 1000 K. (b) Temperature and total energy fluctuations of the  $\gamma$ ,  $\delta'$ , and s/o phases during AIMD simulations.



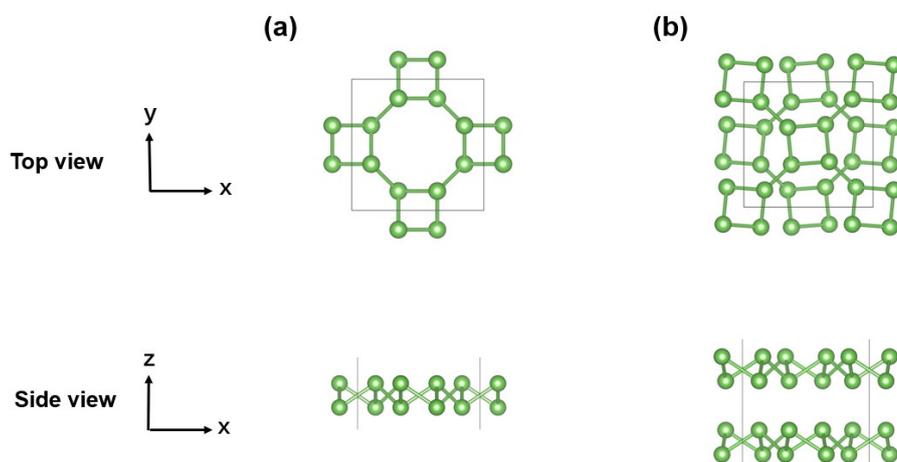
**Fig. S3.** Band structures of monolayer arsenic allotropes (a)  $\alpha$ -As, (b)  $\beta$ -As, (c)  $\gamma$ -As, (d)  $\delta'$ -As, and (e) s/o-As calculated in the PBE and HSE levels. Fermi levels are shifted to 0 eV.



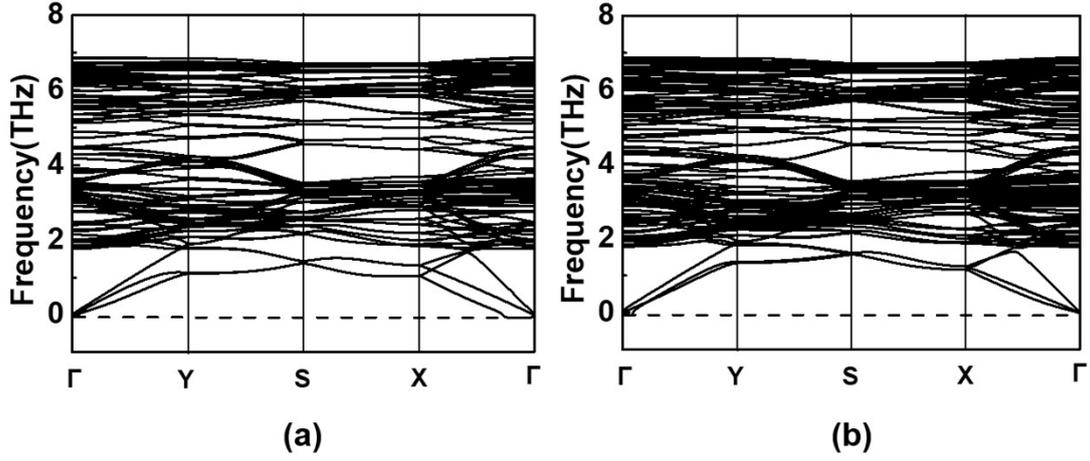




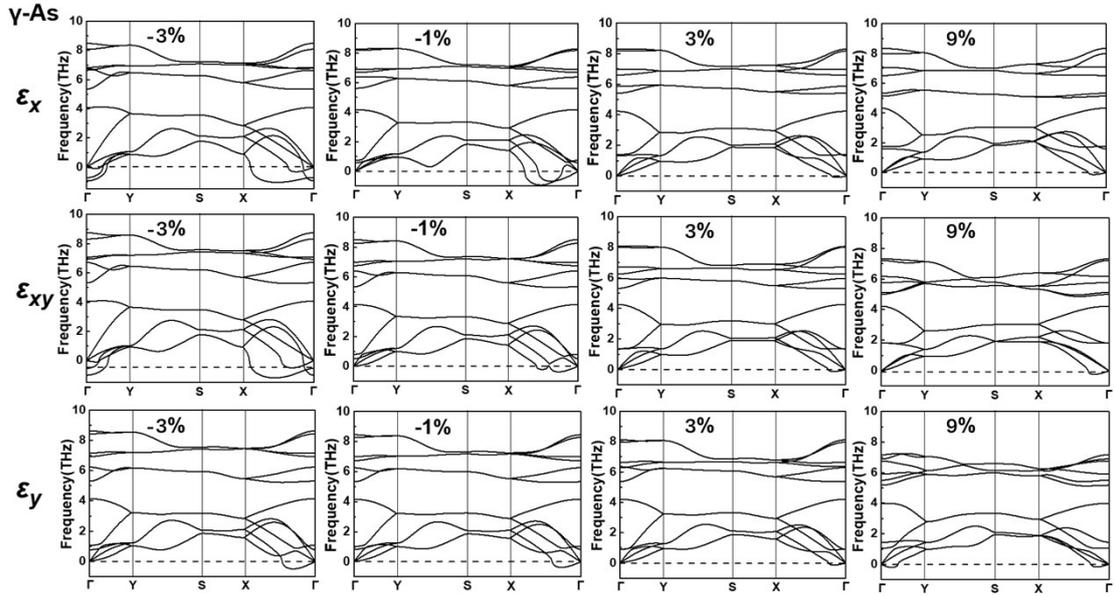
**Fig. S4.** Top and side views of various stacking orders of bilayer/tri-layer arsenene allotropes; relative energies with respect to the most favorable stacking orders are also given. The unstable stackings transform to other stacking orders after structural optimization.



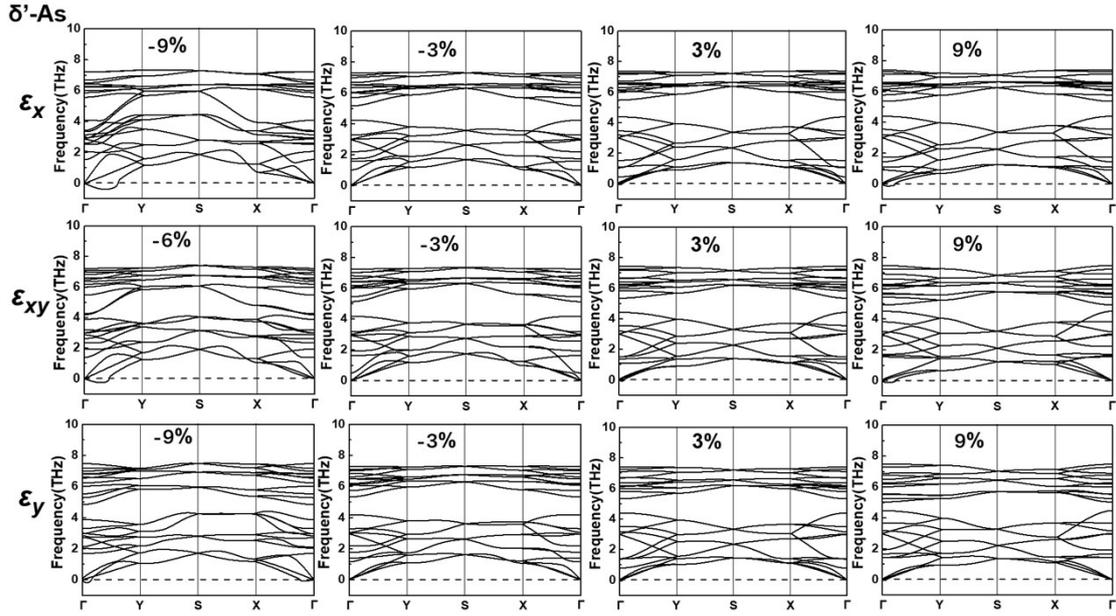
**Fig. S5.** Top and side views of (a) monolayer s/o-As and (b) bilayer AB stacking s/o-As after structural optimizations.



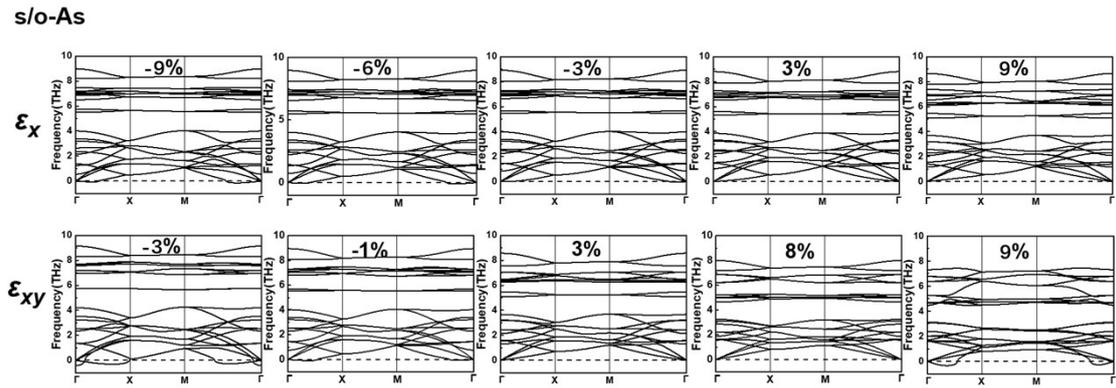
**Fig. S6.** Phonon dispersions of (a) 4-layer AA stacking  $\delta$ -As and (b) 5-layer AA stacking  $\delta$ -As.



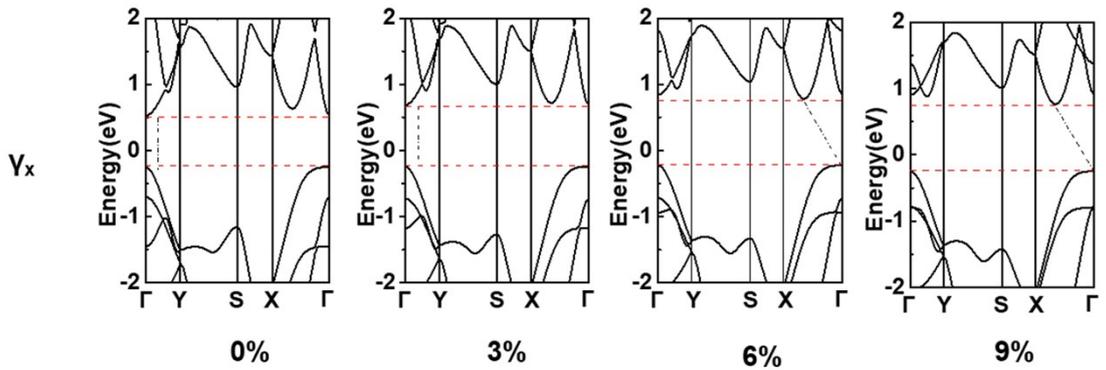
**Fig. S7.** Phonon dispersions of  $\gamma$ -As under strains. Negative and positive strains represent compressive and tensile strains, respectively.



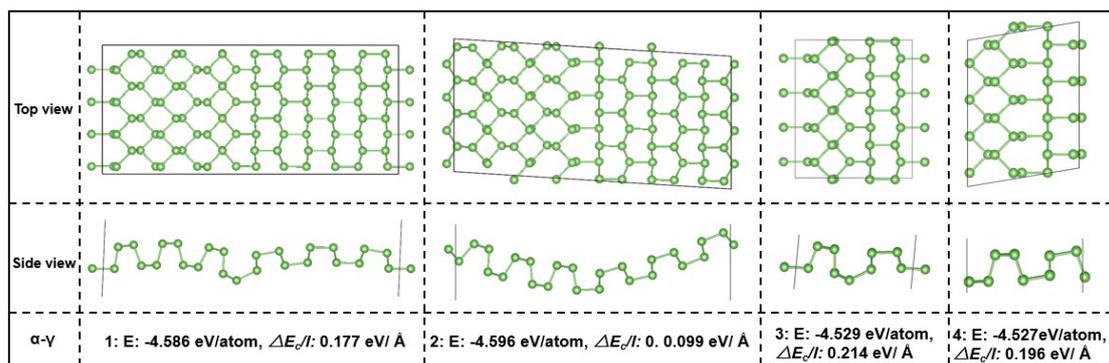
**Fig. S8.** Phonon dispersions of  $\delta'$ -As under strains. Negative and positive strains represent compressive and tensile strains, respectively.



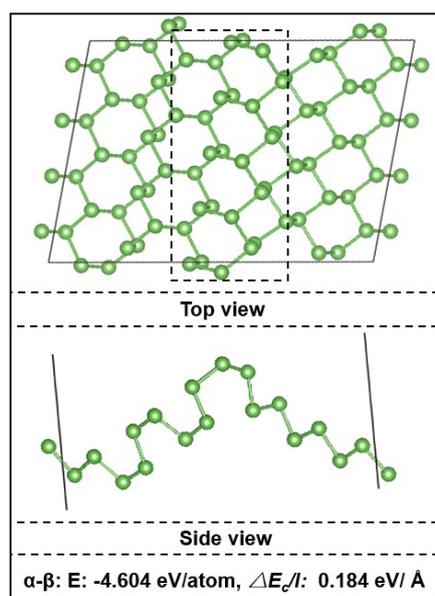
**Fig. S9.** Phonon dispersions of s/o-As under strains. Negative and positive strains represent compressive and tensile strains, respectively.



**Fig. S10.** Band structures of  $\gamma$ -As under different uniaxial  $x$  tensile strains. Fermi levels are shifted to 0 eV.

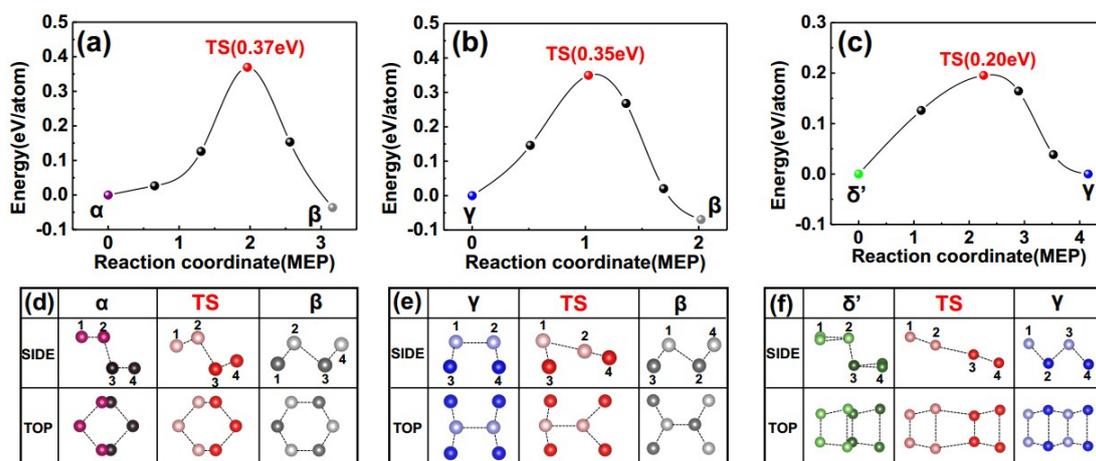


(a)



(b)

**Fig.S11.** Other potential hybridizations of different arsenene allotropes with relatively higher energies.



**Fig.S12** The calculated transition minimum energy paths (MEP) between (a)  $\alpha$ -As and  $\beta$ -As, (b)  $\gamma$ -As and  $\beta$ -As, and (c)  $\delta'$ -As and  $\gamma$ -As, as determined using VTST<sup>12</sup>.

## References

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