

Supporting Information

Pressure-Stabilized Polymerization of Nitrogen in Alkaline-Earth-Metal Strontium Nitrides

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Table S1. Structural parameters of all considered structures for Sr-N.

Str. And S.G.	Lattice parameters (\AA , $^\circ$)	Atomic coordinates (fractional)	Sites
R-3m-Sr₂N P = 0 GPa	a = 3.862 c = 20.858 γ = 120	N1 (0.0, 0.0, 0.5) Sr1 (0.0, 0.0, 0.0767)	3a 6c
Cc-Sr₂N P = 20 GPa	a = 7.601 b = 10.775 c = 6.592 β =54.94	N1 (0.281, 0.127, -0.725) N2 (0.723, 0.064, -0.356) Sr1 (0.473, -0.056, -0.984) Sr2 (0.032, 0.005, -0.863) Sr3 (0.718, -0.184, -0.485) Sr4 (0.401, -0.248, -0.593)	4a 4a 4a 4a 4a 4a
C2/m-SrN P = 0 GPa	a = 13.692 b = 3.797 c = 6.761 β =94.839	N1 (0.977, 0.0 0.906) N2 (0.754, 0.0, 0.251) Sr1 (0.646, 0.0 0.906) Sr2 (0.847, 0.0, 0.611)	4i 4i 4i 4i
P2₁/c-SrN P = 20 GPa	a = 4.605 b = 4.576 c = 6.806 β =66.53	N (0.868, 0.593, 0.568) Sr (0.246, 0.0.589, 0.751)	4e 4e
P-62m-Sr₂N₃ P = 20 GPa	a = 7.001 c = 3.111 γ = 120	N (0.657, 0.889, 0.50) Sr1 (0.558, 0.558, 0.0) Sr2 (0.0, 0.0, 0.0)	6k 3f 1a
C2/c-Sr₂N₃ P = 50 GPa	a = 12.851 b = 6.221 c = 5.642 β =104.679	N1 (0.384, 0.254, 0.470) N2 (0.388, 0.269, 0.901) N3 (0.651, -0.181, 0.333) Sr1 (0.767, -0.035, 0.121) Sr2 (0.50, -0.032, 0.75) Sr3 (0.50, -0.481, 0.75)	8f 8f 8f 8f 4e 4e
I4/mmm-SrN₂ P = 0 GPa	a = 3.848 c = 6.333	N1 (0.5, 0.5, 0.602) Sr1 (0.5, 0.5, 0.0)	4e 2b
P-1-SrN₂ P = 20 GPa	a = 3.833 α =76.07 b = 3.408 β =81.29 c = 5.879 γ = 90.12	N1 (0.701, 0.665, 0.199) N2 (0.337, 0.515, 0.565) Sr (0.803, 0.836, 0.776)	2i 2i 2i
P2/m-SrN₂ P = 100 GPa	a = 3.876 b = 2.691 c = 5.152 β =78.01	N1 (0.169, 0.0, 0.427) N2 (0.812, 0.0, 0.831) Sr (0.321, 0.5, 0.779)	2m 2m 2n
C2/m-SrN₃	a = 8.579	N1 (0.929, 0.219, 0.700)	8j

	b = 5.277 c = 3.342 $\beta=67.25$	N2 (0.579, 0.50, 0.054) Sr (0.175, 0.5, 0.688)	4 <i>i</i> 4 <i>i</i>
C2/c-SrN₄ P = 20 GPa	a = 5.306 b = 5.350 c = 10.136 $\beta=133.54$	N1 (0.643, 0.662, 0.934) N2 (0.323, 0.021, 0.435) Sr (0.0, 0.411, 0.25)	8 <i>f</i> 8 <i>f</i> 4 <i>e</i>
P2₁/c-SrN₄ P = 60 GPa	a = 4.660 b = 5.997 c = 7.246 $\beta=123.36$	N1 (0.542, 0.891, 0.509) N2 (0.331, 0.515, 0.421) N3 (0.296, 0.337, 0.777) N4 (0.784, 0.885, 0.258) Sr1 (0.137, 0.730, 0.621)	4 <i>e</i> 4 <i>e</i> 4 <i>e</i> 4 <i>e</i> 4 <i>e</i>
P-1-SrN₅ P = 60 GPa	a = 3.402 b = 5.455 c = 5.649 $\alpha=78.62$ $\beta=93.33$ $\gamma = 77.90$	N1 (0.738, 0.648, 0.885) N2 (0.073, 0.176, 0.066) N3 (0.142, 0.889, 0.745) N4 (0.906, 0.259, 0.412) N5 (0.151, 0.415, 0.318) Sr1 (0.492, 0.245, 0.737)	2 <i>i</i> 2 <i>i</i> 2 <i>i</i> 2 <i>i</i> 2 <i>i</i> 2 <i>i</i>
Fm-3m-Sr	a = 6.032	Sr (0.0, 0.0, 0.0)	4 <i>a</i>
P6₃/mmc-Sr	a = 4.251, c = 7.056 $\gamma = 120$	Sr (0.667, 0.333, 0.75)	2 <i>c</i>

Table S2. Calculated Bader charges for *C2/m*-SrN₃, *C2/c*-SrN₄, and *P-1*-SrN₅, respectively.

Str.	Atom	N	Charge value(e)	$\delta(e)$
<i>C2/m</i> -SrN ₃	N1	8	5.58	0.58
	N2	4	5.22	0.22
	Sr	4	8.62	-1.38
<i>C2/c</i> -SrN ₄	N1	8	5.37	0.37
	N2	8	5.39	0.39
	Sr	4	8.49	-1.51
<i>P-1</i> -SrN ₅	N1	2	5.19	0.19
	N2	2	5.33	0.33
	N3	2	5.28	0.28

	N4	2	5.33	0.33
	N5	2	5.35	0.35
	Sr	2	8.52	-1.48

Table S3. Calculated integrated crystal orbital Hamiltonian populations of N–N pairs without inclusion of spin polarization in $C2/m$ -SrN₃, $C2/c$ -SrN₄ and $P-1$ -SrN₅.

Str. And S.G.	Pressur e	Atom	Atom	Distance (Å)	ICOHP(E _f)
$C2/m$ -SrN ₃	60	N1	N1		-2.09
		N 2s	N 2s		0.06
		N 2s	N 2p		-0.78
		N 2p	N 2p		-1.37
		N1	N2		-3.22
		N 2s	N 2s		0.46
		N 2s	N 2p		-1.29
		N 2p	N 2p		-2.39
		N2	N2		-3.13
		N 2s	N 2s		0.11
		N 2s	N 2p		-0.66
		N 2p	N 2p		-2.58
$C2/c$ -SrN ₄	20	N1	N1		-2.33
		N 2s	N 2s		0.40
		N 2s	N 2p		0.45
		N 2p	N 2p		-3.18
		N1	N2		0.60
		N 2s	N 2s		1.49
		N 2s	N 2p		0.21
		N 2p	N 2p		-1.10
		N2	N2		-3.79
		N 2s	N 2s		0.07
		N 2s	N 2p		-0.07
		N 2p	N 2p		-3.79
$P-1$ -SrN ₅	60	N1	N2	1.33	-4.43

	N 2s	N 2s		1.36
	N 2s	N 2p		-2.48
	N 2p	N 2p		-3.31
	N2	N3		-3.57
	N 2s	N 2s	1.36	0.69
	N 2s	N 2p		-1.49
	N 2p	N 2p		-2.77
	N3	N4		-4.38
	N 2s	N 2s	1.34	0.98
	N 2s	N 2p		-2.72
	N 2p	N 2p		-2.64
	N4	N5		-4.55
	N 2s	N 2s	1.37	0.66
	N 2s	N 2p		-2.23
	N 2p	N 2p		-2.97
	N5	N1		-3.80
	N 2s	N 2s	1.31	1.12
	N 2s	N 2p		-2.06
	N 2p	N 2p		-2.86

Table S4. Vickers hardness(H_v) of $P2_1/c$ -SrN , $P-62m$ -Sr₂N₃ , $C2/c$ -Sr₂N₃ , $P-1$ -SrN₂ , $P2/m$ -SrN₂ , $C2/m$ -SrN₃ , $C2/c$ -SrN₄ , $P2_1/c$ -SrN₄ , $P-1$ - SrN₅.

Str.	$P2_1/c$ -SrN	$P-62m$ -Sr ₂ N ₃	$C2/c$ -Sr ₂ N ₃	$P-1$ -SrN ₂	$P2/m$ -SrN ₂	$C2/m$ -SrN ₃	$C2/c$ -SrN ₄	$P2_1/c$ -SrN ₄	$P-1$ - SrN ₅
H_v (GPa)	8.7	14.5	17.9	15.9	21.8	29.1	25.7	28.4	32.5

Table S5. The enthalpy of $C2/m$ -SrN₃, $C2/c$ -SrN₄ and $P-1$ - SrN₅ under different pressures, considering SOC or not.

Enthalpy(eV/f.u.)	P = 0 GPa	P = 10 GPa	P = 20 GPa	P = 30 GPa	P = 40 GPa	P = 50 GPa	P = 60 GPa	P = 70 GPa	P = 80 GPa	P = 90 GPa	P = 100 GPa
$C2/m$ -SrN ₃	-26.66806	-23.74975	-21.03437	-18.48055	-16.04878	-13.71575	-11.46595	-9.39854	-7.31601	-5.28422	-3.29775
$C2/m$ -SrN ₃ with SOC	-26.66807	-23.74975	-21.03437	-18.48054	-16.04878	-13.71575	-11.46595	-9.39857	-7.31599	-5.28422	-3.29775
$C2/c$ -SrN ₄	-35.47447	-31.88885	-28.55612	-25.41302	-22.41567	-19.53634	-16.75607	-14.06085	-11.44007	-8.88541	-6.3901
$C2/c$ -SrN ₄ with SOC	-35.49005	-31.88896	-28.55611	-25.41304	-22.41567	-19.53634	-16.75607	-14.06085	-11.44007	-8.88541	-6.3901
$P-1$ - SrN ₅	-43.29589	-38.87962	-34.98612	-31.36552	-27.93648	-24.65795	-21.50308	-18.45313	-15.49428	-12.61554	-9.80825
$P-1$ - SrN ₅ with SOC	-43.47356	-38.88499	-34.98768	-31.36648	-27.93703	-24.65828	-21.50341	-18.45357	-15.49479	-12.61613	-9.80873

**The enthalpy difference curves of the strontium nitrides
under high pressures.**

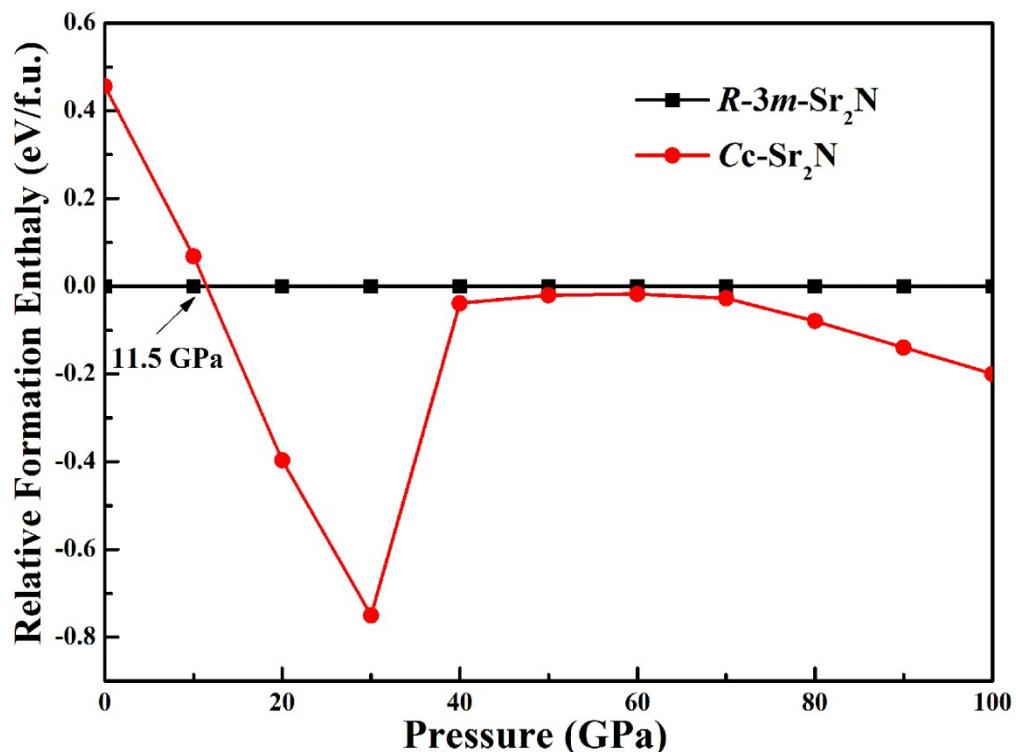


Fig. S1 Calculated enthalpies per formula unit (f.u.) of the high-pressure Sr₂N phases with respect to *R*-3*m*-Sr₂N structure.

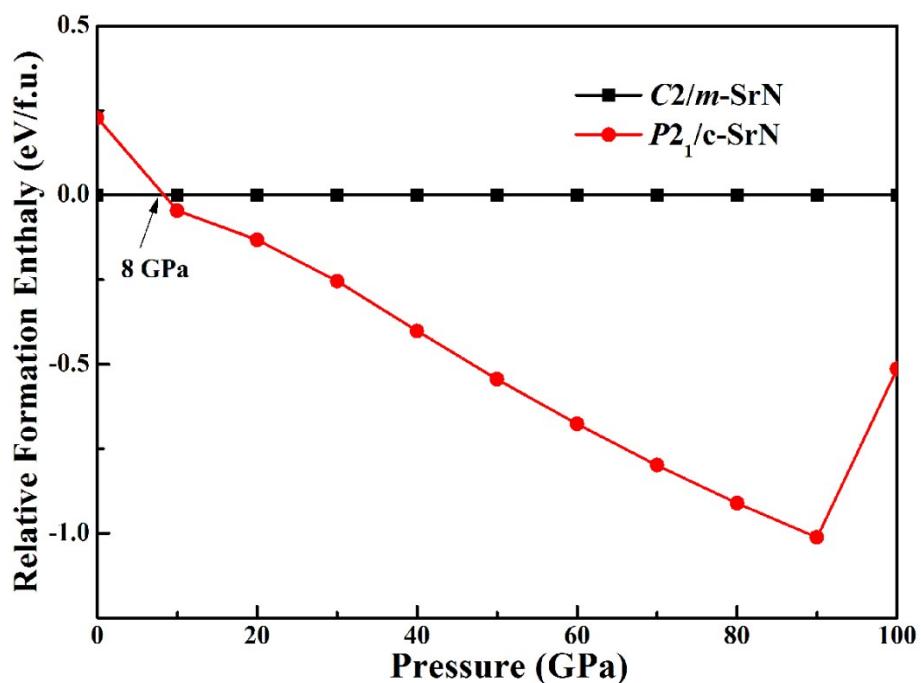


Fig. S2 Calculated enthalpies per formula unit (f.u.) of the high-pressure SrN phases with respect to *C2/m*-SrN structure.

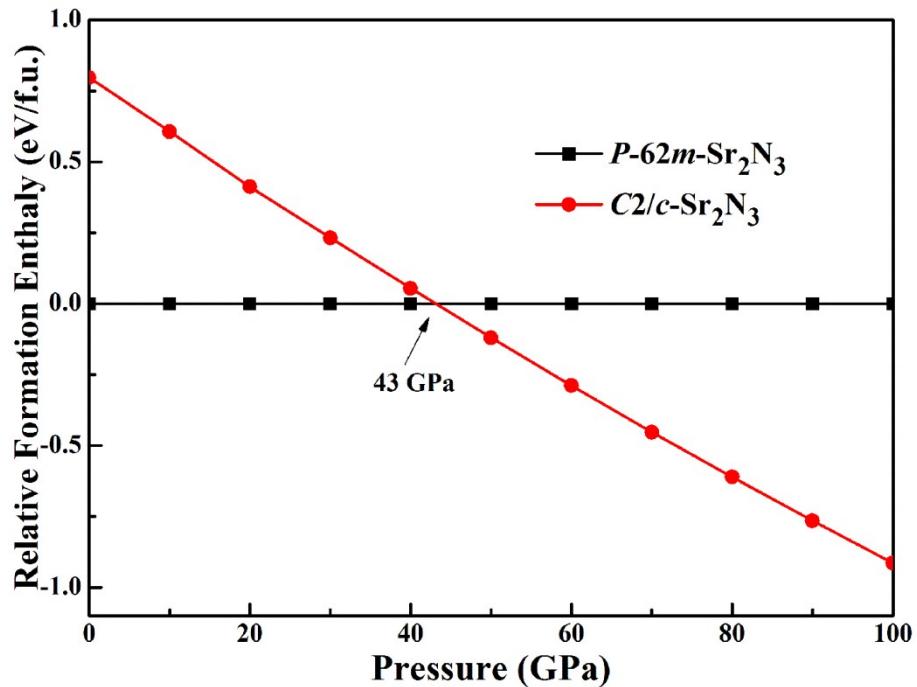


Fig. S3 Calculated enthalpies per formula unit (f.u.) of the high-pressure Sr₂N₃ phases with respect to *P-62m*-Sr₂N₃ structure.

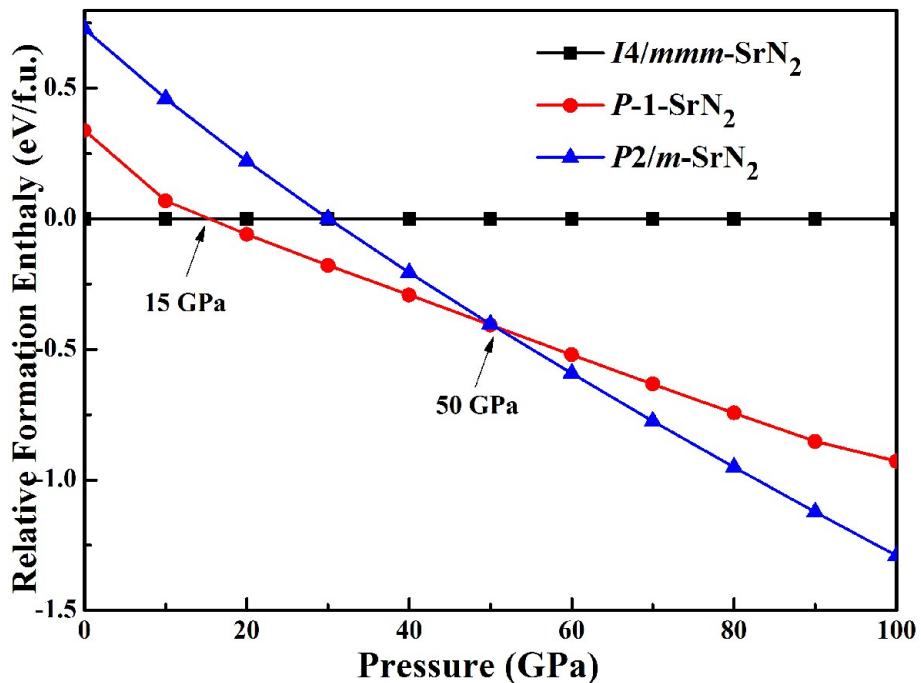


Fig. S4 Calculated enthalpies per formula unit (f.u.) of the high-pressure SrN₂ phases with respect to ambient-pressure *I4/mmm*-SrN₂ structure.

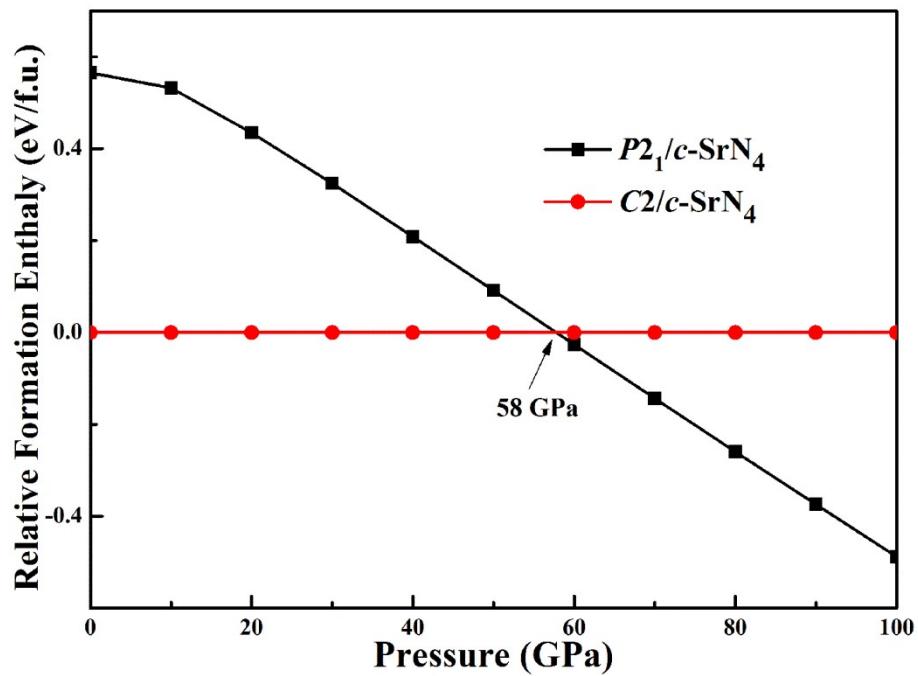


Fig. S5 Calculated enthalpies per formula unit (f.u.) of the high-pressure SrN_4 phases with respect to $C2/c\text{-SrN}_4$ structure.

Phonon dispersion curves for the strontium nitrides

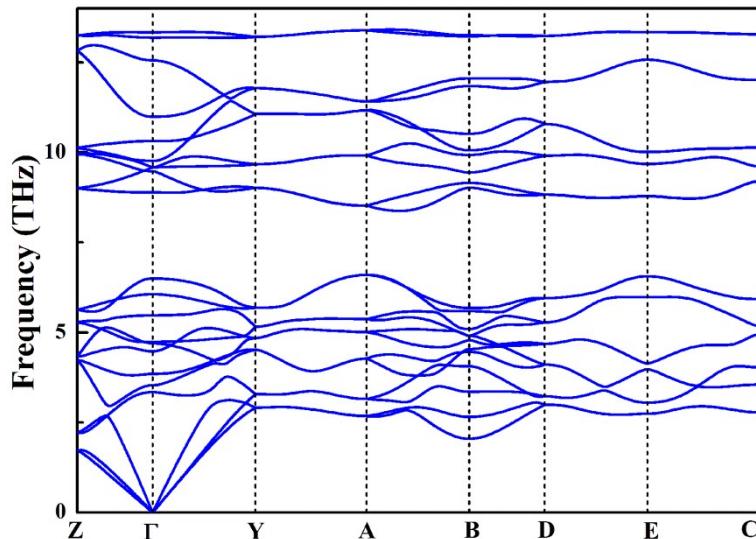


Fig. S6 Phonon dispersion curves for the $P2_1/c\text{-SrN}$ at $P = 20$ GPa

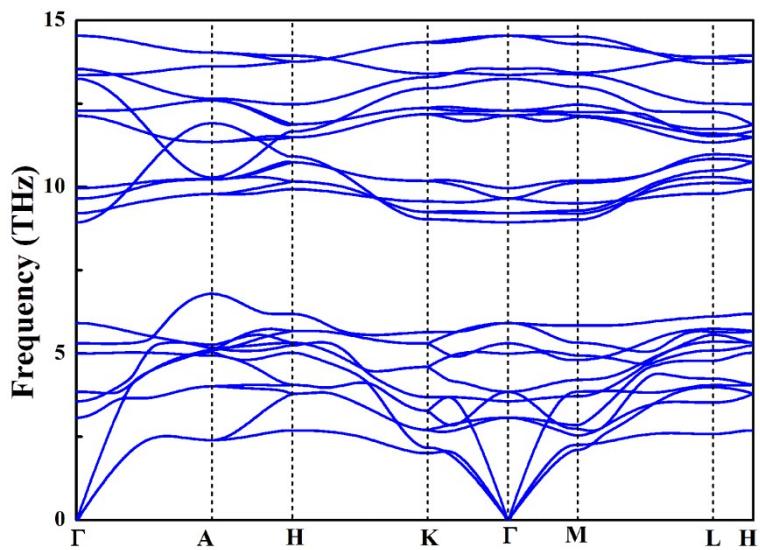


Fig. S7 Phonon dispersion curves for the $P\text{-}62m\text{-}\text{Sr}_2\text{N}_3$ at $P = 20$ GPa

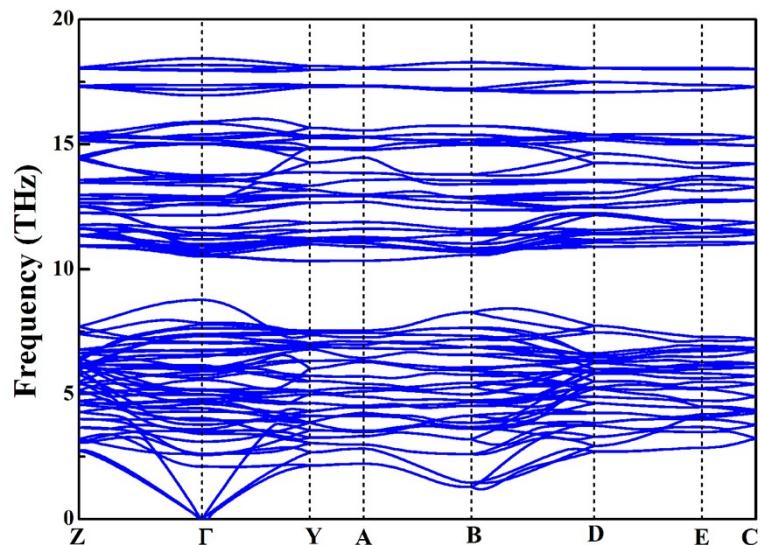


Fig. S8 Phonon dispersion curves for the $C2/c\text{-}\text{Sr}_2\text{N}_3$ at $P = 50$ GPa

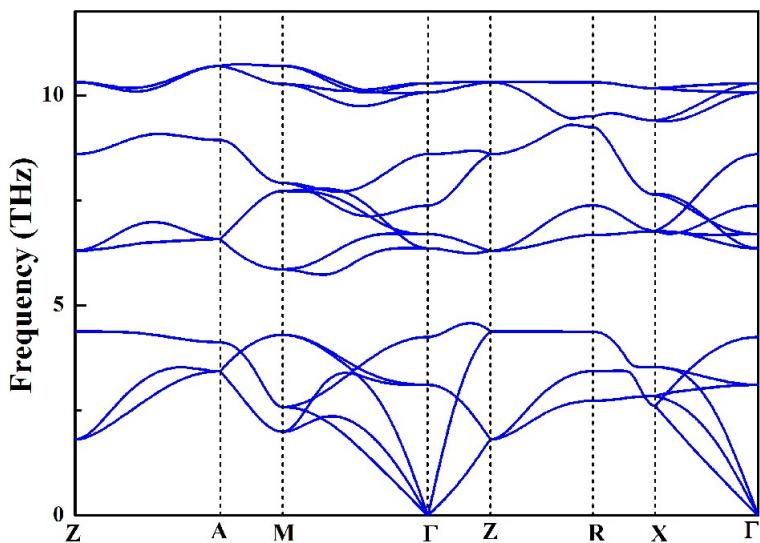


Fig. S9 Phonon dispersion curves for the $I4/mmm$ -SrN₂ at P = 0 GPa.

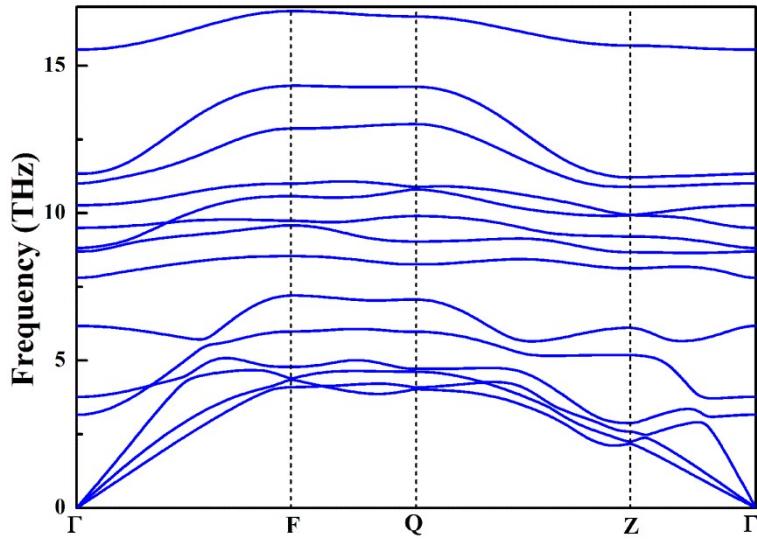


Fig. S10 Phonon dispersion curves for the $P-1$ -SrN₂ at P = 20 GPa.

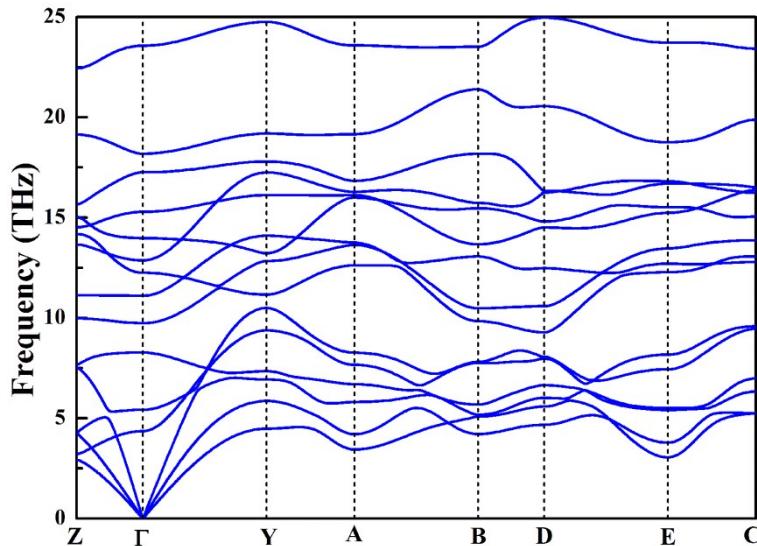


Fig. S11 Phonon dispersion curves for the $P2/m$ -SrN₂ at P = 100 GPa.

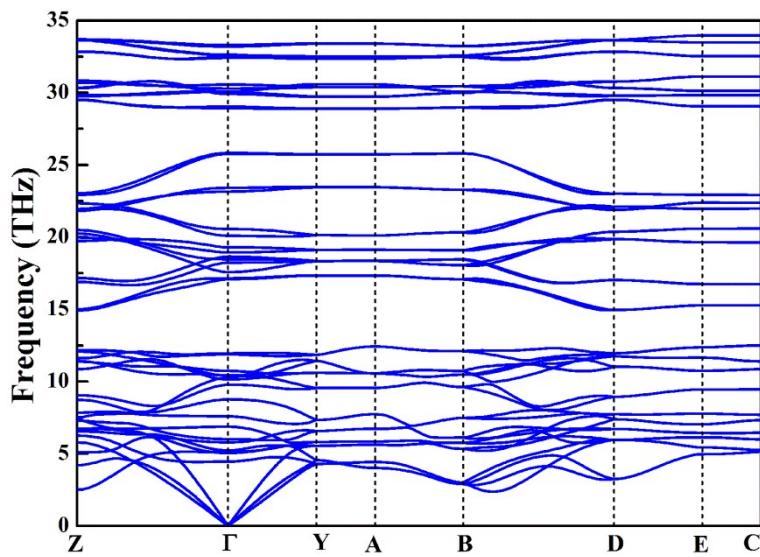


Fig. S12 Phonon dispersion curves for the $C2/m$ -SrN₃ at P = 60 GPa.

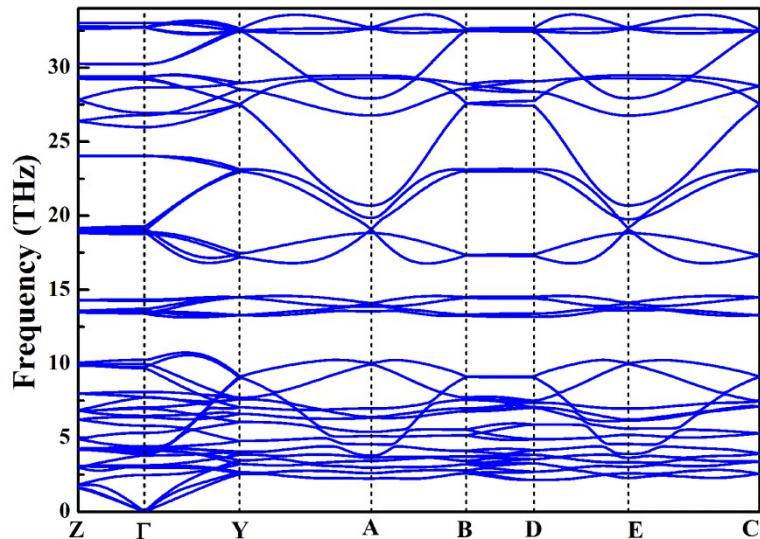


Fig. S13 Phonon dispersion curves for the $C2/c$ -SrN₄ at ambient pressure.

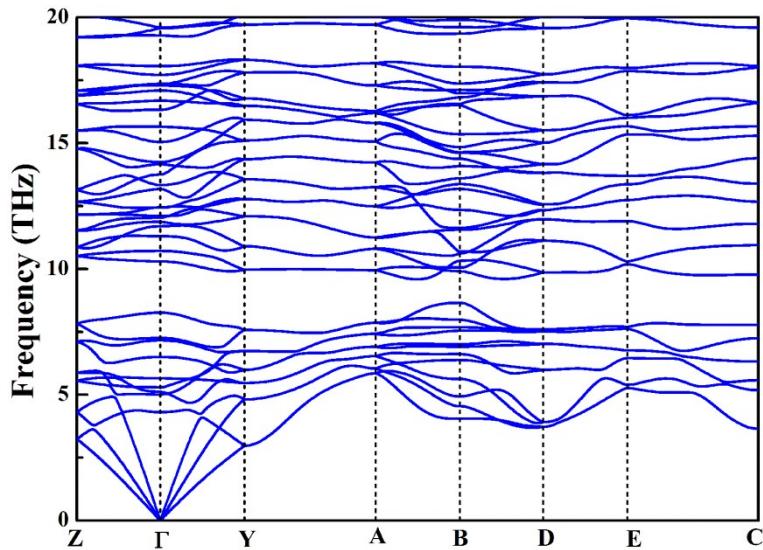


Fig. S14 Phonon dispersion curves for the $P2_1/c$ -SrN₄ at P = 60 GPa.

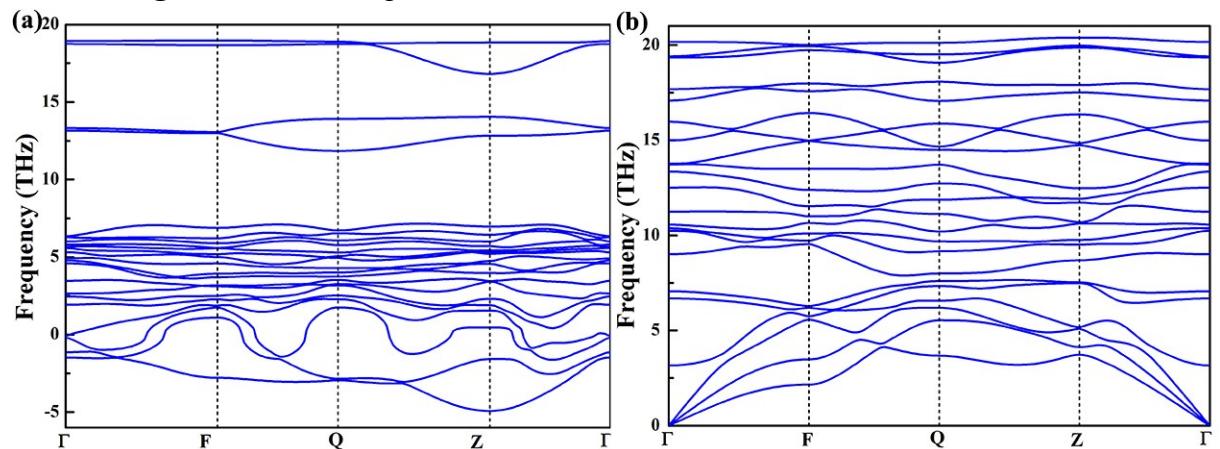


Fig. S15 Phonon dispersion curves for the $P-1$ -SrN₅ at P = 0 GPa(a) and P = 60 GPa(b).

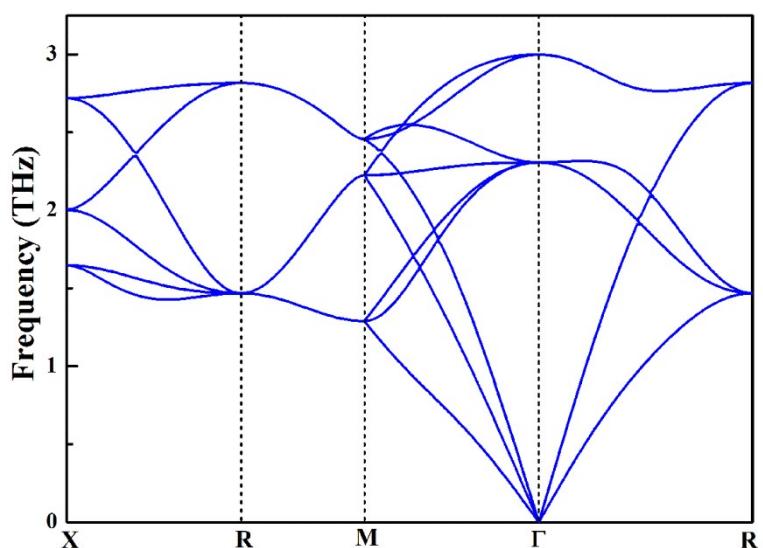


Fig. S16 Phonon dispersion curves for the $Fm\text{-}3m$ -Sr at $P = 0$ GPa.

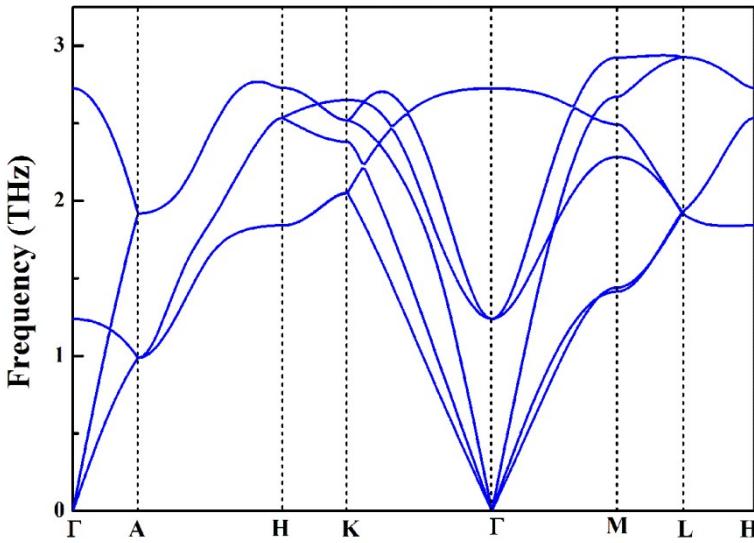


Fig. S17 Phonon dispersion curves for the $P6_3/mmc$ -Sr at $P = 5$ GPa.

Crystal orbital Hamilton population (COHP) curves

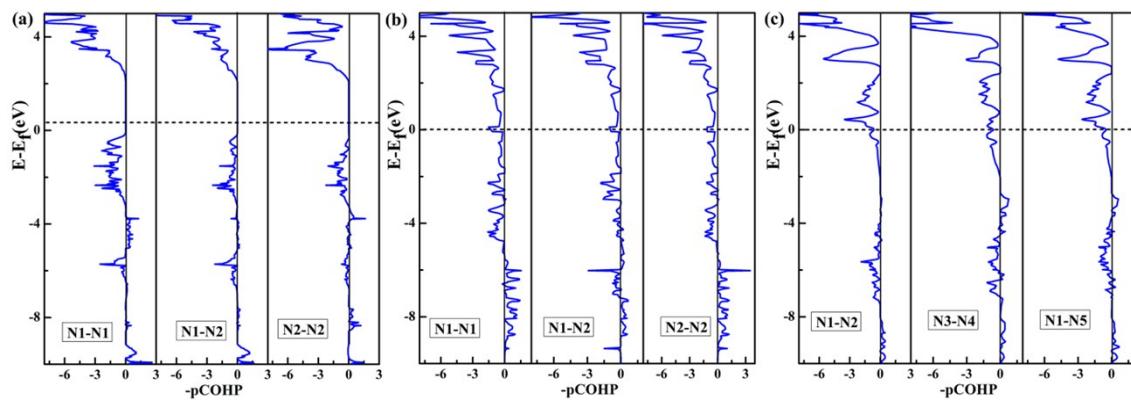


Fig. S18 Crystal orbital Hamilton population (COHP) analyses for $C2/m$ - SrN_3 at $P = 60$ GPa(a), $C2/c$ - SrN_4 at $P = 20$ GPa(b), and $P-1$ - SrN_5 at $P = 60$ GPa(c). The horizontal line at zero is the Fermi level.

Total density of states considering spin of the electron

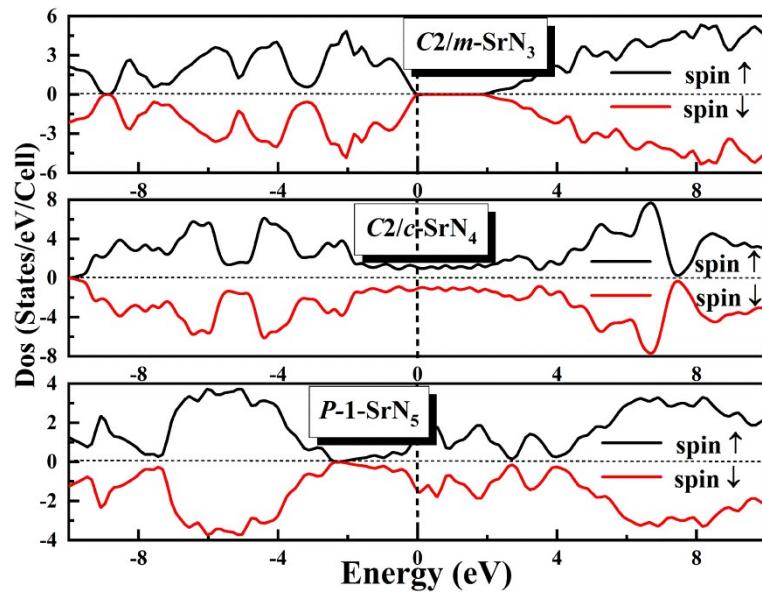


Fig. S19. Total density of states considering spin of the electron for $C2/m\text{-SrN}_3$ at $P = 60\text{GPa}$ (a), $C2/c\text{-SrN}_4$ at $P = 20\text{ GPa}$ (b), and $P-1\text{-SrN}_5$ at $P = 60\text{ GPa}$ (c).