## Supporting Information

## Table of Contents

Experimental Section ..... S2
Table S1: Crystallographic data and structure refinements for $\mathbf{1 E r}$ and $2 \mathbf{E r}$ ..... S5
Table S2: Selected bond lengths and angles of $\mathbf{1 E r}$ and $2 \mathbf{E r}$ ..... S6
Table S3: Kramers doublets (KDs) energy spectrum ( $\mathrm{cm}^{-1}$ ) and g tensors of the ground states for $\mathbf{1 E r}$ and $2 \mathbf{E r}$ - ..... S7
Table S4: Kramers doublets (KDs) energy spectrums $\left(\mathrm{cm}^{-1}\right)$ and g tensors corresponding to modified $\mathbf{1 E r}$ - ..... S8
Figure S1: $\chi_{m} T$ vs $T$ plots ..... S9
Figure S2: Hysteresis under different field-sweeping rates for 1Er at 2 K ..... S10
Figure S3: Temperature dependence ac susceptibilities for $\mathbf{1 E r} \cdot$ ..... S11
Figure S4: Frequency-dependent out-of-phase susceptibilities for 1Er ..... S12
Figure S5: Cole-Cole plots for 1Er ..... S13
Figure S6: Frequency-dependent out-of-phase susceptibilities for 2Er- ..... S14
Figure S7: Cole-Cole plots for 2Er ..... S15
Figure. S8 Ab initio calculated easy axis for $\mathbf{1 E r}$ ..... S16
Figure. S9 $A b$ initio calculated easy axis for $2 \mathbf{E r}$ ..... S17
Figure. S10 The blocking barriers for $\mathbf{1 E r}$ (a) and $2 \mathbf{E r}$ (b). ..... S18
Figure S11: Near-IR emissive spectra of 1Er at 77 K ..... S19

## Experimental Section

The synthesis of air and/or moisture sensitive compounds was carried out under an atmosphere of argon using Schlenk techniques or in an Argon filled glovebox. THF was dried in solvent purification system, transferred under vacuum, and stored in the glovebox. Cyclooctatetraene (COT) was degassed after dried over activated $4 \AA$ molecular sieves overnight. $\left[(\mathrm{COT}) \operatorname{ErCl}(\mathrm{THF})_{\mathrm{x}}\right]$ was prepared according to literature procedures. ${ }^{1}$ Unless otherwise noted, all starting materials were commercially available and were used without further purification. Elemental analysis was performed by Elementar Vario MICRO CUBE (Germany).

1Er [(LOMe)Er(COT)] (LOMe: (cyclopentadienyl)tris(di(methyl)phosphito) cobaltate): A THF solution ( 3 mL ) of LOMeNa ( $237 \mathrm{mg}, 0.5 \mathrm{mmol}$ ) was slowly added to the slurry of $\left[(C O T) E r C l(T H F){ }_{\mathrm{x}}\right]$ ( $189 \mathrm{mg}, 0.5 \mathrm{mmol}$ ) in THF and stirred overnight. The solution was filtered and solvent was removed under vacuum. The residue was redissolved in toluene and stored in $-25^{\circ} \mathrm{C}$. Red crystals were obtained suitable for X-ray diffraction analysis after two days. Anal. Calcd (\%) for $\mathrm{C}_{19} \mathrm{H}_{31} \mathrm{CoErO}_{9} \mathrm{P}_{3}$ : C, 31.48; H, 4.32. Found: C, 31.00; H, 4.15.

2Er [(ArO)Er(COT)] (Ar $\left.=-\mathrm{C}_{6} \mathrm{H}_{3}-2,6-\left(2^{\prime}, 6^{\prime}{ }^{i} \mathrm{P}_{2} \mathrm{C}_{6} \mathrm{H}_{3}\right)_{2}\right)$ : KOAr was prepared from ArOH and KH in toluene in a quantitative yield according to literature. ${ }^{2}$ In a glovebox KOAr ( $45.3 \mathrm{mg}, 0.10 \mathrm{mmol}$ ) was mixed with $\operatorname{COTErCl}(\mathrm{thf})_{\mathrm{x}}(75.4 \mathrm{mg}$, ca. 0.2 mmol ) in a Schlenk tube. When THF (ca. 10 mL ) was added to the mixture and stirred at room temperature a suspension formed. This Schlenk tube was sealed and taken outside of the glovebox. Then it was warmed to $90^{\circ} \mathrm{C}$ in an oil bath and stirred for 12 h . When it cooled to room temperature this Schlenk tube was taken inside the glovebox. The solution was concentrated to ca. 1.5 mL and then filtered. The pink crystals of 2Er can be obtained from its THF/hexane solution. Anal. Calcd (\%) for $\mathrm{C}_{46} \mathrm{H}_{61} \mathrm{ErO}_{3}$ : C, 66.63; H, 7.41. Found: C, 66.35; H, 7.51.

## X-ray crystallography and magnetic measurement

All crystals were manipulated under a nitrogen atmosphere and were covered in grease. Data collections were performed at 180 K on a Aglient technologies Super Nova Atlas Dual System, with a (Mo $\mathrm{K} \alpha=0.71073 \AA$ ) microfocus source and focusing multilayer mirror optics. The structures were solved with the Superflip structure solution program using Charge Flipping and refined with the XL refinement package using Least Squares minimization that implanted in Olex2., 2,3 All non-hydrogen atoms were refined anisotropically. Hydrogen atoms were placed at the calculation positions.

Samples were fixed by N -grease to avoid moving and decaying during measurement. Direct current susceptibility experiment was performed on Quantum Design MPMS XL-5 SQUID magnetometer on polycrystalline samples. Alternative current susceptibility measurement with frequencies ranging from 100 Hz to 10000 Hz was performed on Quantum Design PPMS on polycrystalline samples. All dc susceptibilities were corrected for diamagnetic contribution from the sample holder, N -grease and diamagnetic contributions from the molecule using the pascal's constants.

## $A b$ initio calculations

Complete-active-space self-consistent field (CASSCF) calculations on the complete structures of complexes $\mathbf{1 E r}$ and $2 \mathbf{E r}$ on the basis of X-ray determined geometry have been carried out with MOLCAS 8.0 program package. ${ }^{4}$ For CASSCF calculations, the basis sets for all atoms are atomic natural orbitals from the MOLCAS ANO-RCC library: ANO-RCC-VTZP for Er ${ }^{\text {III }}$ ion; VTZ for close C and O ; VDZ for distant atoms. The calculations employed the second order Douglas-Kroll-Hess Hamiltonian, where scalar relativistic contractions were taken into account in the basis set and the spin-orbit coupling was handled separately in the restricted active space state interaction (RASSI-SO) procedure. The active electrons in 7 active spaces included all f electrons (CAS(11 in 7)) in the CASSCF calculation. To exclude all the doubts we calculated all the roots in the active space. We have mixed the maximum number of spin-free states which
was possible with our hardware (all from 35 quadruplets and all from 112 doublets.

## Near-IR emission spectrum measurement.

Steady state emission spectra was acquired on an Edinburgh Analytical Instruments FLS920 lifetime and steady-state spectrometer (450 W Xe lamp, Ge detector for NIR emission spectrum, Hamamatsu R5509-73 PMT with C9940-02 cooler) on frozen glasses of solutions of the 1Er (2-methyl-tetrahydrofurnan) using a dewar cuvette filled with liquid $\mathrm{N}_{2}(\mathrm{~T}=77 \mathrm{~K})$.

## References

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Table S1 Crystallographic data and structure refinements for 1Er and 2Er.

| formula | $\mathrm{C}_{19} \mathrm{H}_{31} \mathrm{CoErO}_{9} \mathrm{P}_{3}$ | $\mathrm{C}_{46} \mathrm{H}_{61} \mathrm{ErO}_{3}$ |
| :--- | :--- | :--- |
| Mr | 722.54 | 570.27 |
| cryst syst | orthorhombic | orthorhombic |
| space group | Pnma | $P 2_{1} 2_{1} 2_{1}$ |
| $a, \AA$ | $20.9027(2)$ | $12.4119(3)$ |
| $b, \AA$ | $11.96320(14)$ | $16.2512(4)$ |
| $c, \AA$ | $22.3054(2)$ | $20.0292(5)$ |
| $V, \AA^{3}$ | $5577.75(11)$ | $4040.05(18)$ |
| $\alpha$, deg | 90 | 90 |
| $\beta$, deg | 90 | 90 |
| $\gamma$, deg | 90 | 90 |
| $Z$ | 8 | 4 |
| $T, \mathrm{~K}$ | $180(2)$ | $180(2)$ |
| $\mu, \mathrm{mm}^{-1}$ | 3.797 | 2.115 |
| $\lambda, \AA$ | 0.71073 | 0.71073 |
| Cryst size, mm | $0.31 * 0.18 * 0.11$ | $0.3^{*} 0.15^{*} 0.15$ |
| GOF | 1.091 | 1.050 |
| $R_{\text {int }}$ | 0.0424 | 0.0408 |
| $R_{1}, w R_{2}[\mathrm{I}>2 \sigma(\mathrm{I})]$ | $0.0481,0.1545$ | $0.0281,0.0486$ |
| $R_{1}, w R_{2}[$ all data $]$ | $0.0569,0.1637$ | $0.0387,0.0530$ |
| CCDC code | 1900286 | 1900287 |

Table S2 Selected bond lengths and angles of 1Er and 2Er.

|  | $\mathbf{1 E r}(\mathbf{A})$ | $\mathbf{1 E r}(\mathbf{B})$ | $\mathbf{2 E r}$ |
| :---: | :---: | :---: | :---: |
| Er-O(1), $\AA$ | 2.236 | 2.231 | 2.409 |
| Er-O(2), $\AA$ | 2.236 | 2.231 | 2.428 |
| Er-O(3), $\AA$ | 2.245 | 2.256 | 2.132 |
| Er-C(COT), $\AA$ | $2.564-2.585$ | $2.550-2.586$ | $2.555-2.573$ |
| Er-centroid (COT), $\AA$ | 1.805 | 1.802 | 1.826 |
| Er-centroid (O), $\AA$ | 1.489 | 1.477 | 1.498 |
| $\angle \mathrm{O}(1)-$-Er-O(2), ${ }^{\circ}$ | 81.5 | 82.3 | 76.0 |
| $\angle \mathrm{O}(2)-E r-\mathrm{O}(3),{ }^{\circ}$ | 80.1 | 80.7 | 86.8 |
| $\angle \mathrm{O}(3)-$-Er-O(1), ${ }^{\circ}$ | 80.1 | 80.7 | 86.8 |
| $\angle$ centroid (O)-Er-centroid | 176.4 | 176.7 | 163.3 |
| (COT), ${ }^{\circ}$ |  |  |  |
| Dihedral angle, ${ }^{\circ}$ | 4.8 | 5.1 | 3.7 |

Table S3 Kramers doublets (KDs) energy spectrums $\left(\mathrm{cm}^{-1}\right)$ and $g$ tensors of the ground states

|  | 1Er | 2Er |
| :---: | :---: | :---: |
|  | Kramers doublets (KDs) energy spectrum |  |
| 1 | 0 | 0 |
| 2 | 111.6 | 55.5 |
| 3 | 199.4 | 94.8 |
| 4 | 223.6 | 138.1 |
| 5 | 227.4 | 236.4 |
| 6 | 268.2 | 261.3 |
| 7 | 290.0 | 304.3 |
| 8 | 300.7 | 396.5 |
|  | $g$ tensor of the ground state |  |
| $g_{x}$ | $1 \times 10^{-5}$ | 0.0595 |
| $g_{y}$ | $1 \times 10^{-5}$ | 0.0960 |
| $g_{z}$ | 17.92 | 17.44 |

Table S4 Kramers doublets (KDs) energy spectrums ( $\mathrm{cm}^{-1}$ ) and $g$ tensors corresponding to modified 1Er.

| KDs | Er-Centroid (O): 1.389 A |  |  | Er-Centroid (O): 1.589 A |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | E |  |  | E |  |  |
| 1 | 0 |  |  | 0 |  |  |
| 2 | 113.6 |  |  | 114.2 |  |  |
| 3 | 198.4 |  |  | 223.3 |  |  |
| 4 | 224.0 |  |  | 231.7 |  |  |
| 5 | 227.5 |  |  | 250.1 |  |  |
| 6 | 268.0 |  |  | 288.4 |  |  |
| 7 | 291.2 |  |  | 303.2 |  |  |
| 8 | 300.9 |  |  | 317.0 |  |  |
| KDs | $g_{x}$ | $g_{y}$ | $g_{z}$ | $g_{x}$ | $g_{y}$ | $g_{z}$ |
| 1 | 2.018E-5 | 2.808E-5 | 17.9211 | 1.146E-5 | 1.418E-5 | 17.9362 |
| 2 | 0.0051 | 0.0053 | 15.4853 | 0.0018 | 0.0019 | 15.5167 |
| 3 | 9.8248 | 9.3993 | 1.1648 | 9.8254 | 9.15082 | 0.9802 |
| 4 | 0.2319 | 0.5468 | 9.2977 | 0.0112 | 0.3389 | 12.774 |
| 5 | 0.3942 | 0.7952 | 7.4455 | 0.1871 | 0.8465 | 3.6579 |
| 6 | 0.1508 | 0.8837 | 6.6792 | 0.2514 | 0.8234 | 6.6989 |
| 7 | 0.0154 | 0.3290 | 10.6106 | 0.0223 | 0.2775 | 10.3896 |
| 8 | 0.25255 | 0.8053 | 10.4391 | 0.3715 | 0.7654 | 9.5182 |
| KDs | Er-Centroid (O): 1.689 A |  |  | Er-Centroid (O): $\infty$ |  |  |
|  | E |  |  | E |  |  |
| 1 | 0 |  |  | 0 |  |  |
| 2 | 108.3 |  |  | 140.0 |  |  |
| 3 | 206.1 |  |  | 305.1 |  |  |
| 4 | 222.9 |  |  | 428.7 |  |  |
| 5 | 233.5 |  |  | 485.3 |  |  |
| 6 | 273.6 |  |  | 492.1 |  |  |
| 7 | 291.3 |  |  | 498.2 |  |  |
| 8 | 304.1 |  |  | 507.8 |  |  |
| KDs | $g_{x}$ | gy | $g_{z}$ | $g_{x}$ | $g_{y}$ | $g_{z}$ |
| 1 | 8.403E-6 | 9.442E-6 | 17.9451 | 2.38E-7 | 4.77E-7 | 17.9510 |
| 2 | 0.0011 | 0.0011 | 15.5314 | 5.255E-5 | 5.287E-5 | 15.5418 |
| 3 | 10.2876 | 8.9837 | 1.1714 | 4.971E-4 | 5.074E-4 | 13.1275 |
| 4 | 0.0117 | 0.0578 | 13.0222 | 0.0161 | 0.0165 | 10.7333 |
| 5 | 0.5148 | 0.8811 | 3.6421 | 12.1359 | 7.1011 | 1.1427 |
| 6 | 0.3266 | 0.6357 | 6.4768 | 0.94603 | 1.22719 | 7.95135 |
| 7 | 0.0195 | 0.1366 | 10.5757 | 3.89918 | 2.88171 | 1.79195 |
| 8 | 0.2922 | 0.5939 | 10.1354 | 0.56614 | 1.24625 | 5.97921 |



Fig. S1 $\chi_{m} T$ vs $T$ plots for 1Er (black circles) and 2Er (red circles). The solid lines represent the $a b$ initio calculated results.


Fig. S2 Hysteresis measurement under different field sweeping rates for $\mathbf{1 E r}$ at 2 K.


Fig. S3 Temperature dependence ac susceptibility in the absence of dc field for 1Er.


Fig. S4 Frequency-dependent out-of-phase susceptibilities for 1Er
(a)

(b)


Fig. S5 Cole-Cole plots fitted by utilizing generalized Debye model for 1Er. (a) presents the data from MPMS in the frequency range of $1-1000 \mathrm{~Hz}$. (b) represents the data from PPMS in the frequency range of $100-10000 \mathrm{~Hz}$.
(a)

(b)


Fig. S6 Frequency-dependent out-of-phase susceptibilities for 2Er.
(a)

(b)


Fig. S7 Cole-Cole plots fitted by utilizing generalized Debye model for 2Er. (a) presents the data from MPMS in the frequency range of $1-1000 \mathrm{~Hz}$. (b) represents the data from PPMS in the frequency range of $100-10000 \mathrm{~Hz}$.


Fig. S8 Ab initio calculated easy axis for 1Er.


Fig. S9 $A b$ initio calculated easy axis for 2Er.


Fig. S10 The blocking barriers for 1Er (a) and 2Er (b). The thick black lines represent the exchange Kramers doublets as a function of their magnetic moment along the magnetic axis. The green lines correspond to diagonal quantum tunneling of magnetization (QTM), the blue lines represent off-diagonal relaxation process. The numbers at each arrow stand for the mean absolute value of the corresponding matrix element of transition magnetic moment.


Fig. S11 Near-IR emissive spectra of $\mathbf{1 E r}$ at 77 K . The blue lines represented the position the emissive peaks.

