Ligand Ratio/Solvent-Influenced Syntheses, Crystal Structures, Magnetic Properties of Polydentate Schiff Base Ligand-Dy^{III} Compounds with β -Diketonate Ligand as Co-Ligand

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1 The synthesis ligand H₂L

1.1 2-Hydroxy-3-(chloromethyl)-5-methyl-benzaldehyde (HCMB)

HCMB was prepared by a direct chloromethylation of HMB. In a 250 mL round bottom flask, a mixture of 6.4 g (4.7 mmol) of HMB, 7.5 mL of formaldehyde and 25 mL of HCl (12 mol/L) was heated under magnetic stirring to reflux for 15 min. After cool down the reaction to 0 °C, a solid mass was formed in the bottom. The solid was separated from the reaction solution and recrystallized in hot ethanol, yielding 5 g of HCMB (70% yield). The residual solutions were basified with NaOH (pH > 9) prior to discard them. ¹H NMR (400 MHz, CDCl₃) δ 11.24 (s, 1H), 9.80 (s, 1H), 7.42 (d, *J* = 2.1 Hz, 1H), 7.30 (d, *J* = 1.4 Hz, 1H), 4.64 (s, 2H), 2.31 (d, *J* = 4.4 Hz, 3H). ¹H NMR (100 MHz, CDCl₃) δ 196.7, 196.5, 159.5, 157.3, 138.6, 138.1, 134.1, 133.5, 129.3, 129.2, 125.7, 120.4, 120.4, 117.4, 39.9, 20.3, 20.2.



Fig. S1 ¹³C NMR spectra of HCMB.



Fig. S2¹H NMR spectra of HCMB.

1.2 N,N'-bis(pyridin-2-ylmethyl)ethylenediamine (py2en)

Py₂en was prepared by a condensation reaction between 2-pyridinecarboxaldehyde and ethylenediamine, followed by reduction with NaBH₄. In a 100 mL round bottom flask, 3.0 mL of pyridine-2-carboxaldehyde (31 mmol) were dissolved in 30 mL of methanol at 0 °C, followed by the addition of 1.0 mL of ethylenediamine (15.5 mmol), under magnetic stirring. After 1 h, 1.2 g of sodium borohydride (31 mmol) was added in small portions and left to react for another 1 h. Then, HCl 6 mol/L was added dropwise up to pH < 2. After removing the solvent, 30 mL of distilled water was added and the pH adjusted to 9–10 with NaOH. The product was extracted with dichloromethane (6 × 50 mL); the organic layers were dried under MgSO4 and the solvent was removed under vacuum, yielding 2.8 g of a yellow oil of py₂en (85 % yield). ¹H NMR (400 MHz, CDCl₃) δ 8.57-8.51 (m, 2H), 7.62 (td, *J* = 7.7, 1.8 Hz, 2H), 7.32 (d, *J* = 7.8 Hz, 2H), 7.14 (ddd, *J* = 7.4, 4.9, 0.9 Hz, 2H), 3.92 (s, 4H), 2.82 (s, 4H). ¹³C NMR (100 MHz, CDCl₃) δ 159.8, 149.1, 136.3, 122.1, 121.7, 55.1, 49.0.



Fig. S3 ¹³C NMR spectra of py₂en.



Fig. S4 ¹H NMR spectra of HCMB.

1.3

 $N,N'-bis(2-hydroxy-5-methyl-3-formylbenzyl)-N,N'-bis-(pyridin-2-ylmethyl)ethylene \ diamine, \ H_2L$

In a 100 mL round bottom flask, 4.6 g of HCMB (25 mmol) and 3.0 g of py₂en (12 mmol) were dissolved in 40 mL of dichloromethane. Then, 3.5 mL of triethylamine (25 mmol) was added dropwise. After 24 h at room temperature, the reaction solution was washed with a saturated solution of NaHCO₃ and the organic layers dried with MgSO₄. After removing the solvent under vacuum, 6.4 g of H₂L were obtained, as viscous yellow oil (96% yield). ¹H NMR (400 MHz, CDCl₃) δ 10.19 (d, *J* = 2.2 Hz, 2H), 8.53 (dd, *J* = 2.8, 2.0 Hz, 2H), 7.59 (dd, *J* = 10.6, 4.7 Hz, 2H), 7.37 (s, 2H), 7.25 (d, *J* = 7.7 Hz, 2H), 7.16 (dd, *J* = 12.7, 7.6 Hz, 4H), 3.74 (s, 4H), 3.66 (s, 4H), 2.75 (s, 4H), 2.23 (s, 6H). ¹³C NMR (100 MHz, CDCl₃) δ 192.6, 159.0, 157.9, 148.9, 137.5, 136.7, 128.8, 128.1, 125.0, 123.2, 122.3, 122.2, 59.4, 54.9, 50.5, 20.3. HRMS (ESI) for C₃₂H₃₅N₄O₄ [M+H⁺]: Calcd: 539.2209; Found: 539.2202. IR (KBr): 2958, 2844, 1590, 1471, 1240, 1083, 989, 871.



Fig. S5 ¹³C NMR spectra of H₂L.







Fig. S7 HRMS spectra of H₂L.



2. The structure information of 1-3, 1a-3a and 3b.

Table S1. Crystallographic Data and Structural Refinements for 1a, 2a, 3a and 3b.

Compound	1a	2a	3 a	3 b
molecular formula	C53DyN0.12O13	C51DyN0.25O14	C77H65Dy2N4O10	C65Dy2N17O24
formula weight	1008.78	1002.51	1531.33	1727.82
temperature	293(2)	293(2)	293(2)	293(2)
crystal system	monoclinic	monoclinic	cubic	cubic
space group	C2/c	$P2_{1/c}$	Pa3	Pa3
<i>a</i> (Å)	28.071(2)	22.8242(5)	35.3274(5)	35.3274(5)
<i>b</i> (Å)	14.8132(10)	15.3037(4)	35.3274(5)	35.3274(5)
<i>c</i> (Å)	20.9718(12)	11.8447(3)	35.3274(5)	35.3274(5)
α (deg)	90	90	90	90
β (deg)	96.366(6)	90.236(2)	90	90
γ (deg)	90	90	90	90
$V(\text{\AA}^3)$	8666.9(10)	4137.28(16)	44090(2)	43953(2)
Ζ	8	4	24	24
$D_{\text{calc}}(\text{g cm}^{-3})$	1.546	1.609	1.384	1.562
<i>F</i> (000)	3911	1943	18408	19992
μ/mm^{-1}	9.825	10.305	11.219	11.512

heta min-max/°	3.895-67.246	3.477-67.236	3.064-67.216	3.064-67.216		
reflections collected	18385	30251	39571	39571		
GOF on F^2	1.029	1.015	0.853	1.036		
$R_1/wR_2 [I \ge 2\sigma(I)]$	0.0710/0.1815	0.0959/0.2397	0.0730/0.1939	0.0935/0.2579		
R_1/wR_2 [all data]	0.1115/0.2161	0.1090/0.2545	0.1640/0.2709	0.1915/0.3255		
${}^{a}R_{1} = \Sigma F_{o} - F_{C} / \Sigma F_{o} . {}^{b}wR_{2} = [\Sigma w(F_{o}^{2} - F_{c}^{2})^{2} / \Sigma w(F_{o}^{2})^{2}]^{1/2}.$						

 Table S2. Selected bond lengths (Å) and angles (°) for 1-3.

Compound	1		
Dy(1)-O(1)	2.223(3)	O(1)-Dy(1)-N(4)	74.93(12)
Dy(1)-O(3)	2.268(3)	O(3)-Dy(1)-N(4)	132.64(12)
Dy(1)-O(6)	2.299(3)	O(6)-Dy(1)-N(4)	113.43(13)
Dy(1)-O(5)	2.334(3)	O(5)-Dy(1)-N(4)	69.68(12)
Dy(1)-N(1)	2.594(4)	N(1)-Dy(1)-N(4)	144.87(12)
Dy(1)-N(4)	2.604(4)	O(1)-Dy(1)-N(2)	76.55(13)
Dy(1)-N(2)	2.626(4)	O(3)-Dy(1)-N(2)	92.62(12)
Dy(1)-N(3)	2.637(4)	O(6)-Dy(1)-N(2)	140.54(12)
O(1)-Dy(1)-O(3)	151.29(12)	O(5)-Dy(1)-N(2)	148.25(12)
O(1)-Dy(1)-O(6)	81.08(12)	N(1)-Dy(1)-N(2)	66.01(12)
O(3)-Dy(1)-O(6)	91.69(13)	N(4)-Dy(1)-N(2)	91.63(12)
O(1)-Dy(1)-O(5)	119.99(12)	O(1)-Dy(1)-N(3)	124.02(12)
O(3)-Dy(1)-O(5)	82.89(12)	O(3)-Dy(1)-N(3)	74.61(12)
O(6)-Dy(1)-O(5)	71.17(11)	O(6)-Dy(1)-N(3)	148.05(12)
O(1)-Dy(1)-N(1)	73.70(12)	O(5)-Dy(1)-N(3)	78.46(12)
O(3)-Dy(1)-N(1)	77.60(12)	N(1)-Dy(1)-N(3)	126.04(13)
O(6)-Dy(1)-N(1)	76.74(12)	N(4)-Dy(1)-N(3)	62.79(12)
O(5)-Dy(1)-N(1)	141.68(12)	N(2)-Dy(1)-N(3)	70.09(12)
Compound 2	·		
Dy(1)-O(3)	2.219(4)	O(3)-Dy(1)-N(1)	78.17(13)
Dy(1)-O(1)	2.224(4)	O(1)-Dy(1)-N(1)	73.48(13)
Dy(1)-O(5)	2.295(3)	O(5)-Dy(1)-N(1)	77.59(13)
Dy(1)-O(6)	2.302(3)	O(6)-Dy(1)-N(1)	145.41(13)
Dy(1)-N(4)	2.598(4)	N(4)-Dy(1)-N(1)	144.43(13)
Dy(1)-N(1)	2.628(4)	O(3)-Dy(1)-N(2)	94.68(14)
Dy(1)-N(2)	2.648(4)	O(1)-Dy(1)-N(2)	77.03(14)
Dy(1)-N(3)	2.652(4)	O(5)-Dy(1)-N(2)	140.74(13)
O(3)-Dy(1)-O(1)	151.35(13)	O(6)-Dy(1)-N(2)	147.12(13)
O(3)-Dy(1)-O(5)	87.47(13)	N(4)-Dy(1)-N(2)	91.14(14)
O(1)-Dy(1)-O(5)	82.52(13)	N(1)-Dy(1)-N(2)	64.65(14)

O(3)-Dy(1)-O(6)	84.11(13)	O(3)-Dy(1)-N(3)	74.68(13)
O(1)-Dy(1)-O(6)	117.65(13)	O(1)-Dy(1)-N(3)	125.33(13)
O(5)-Dy(1)-O(6)	72.13(12)	O(5)-Dy(1)-N(3)	147.16(13)
O(3)-Dy(1)-N(4)	132.16(13)	O(6)-Dy(1)-N(3)	78.68(13)
O(1)-Dy(1)-N(4)	75.97(13)	N(4)-Dy(1)-N(3)	63.26(14)
O(5)-Dy(1)-N(4)	115.98(13)	N(1)-Dy(1)-N(3)	123.56(14)
O(6)-Dy(1)-N(4)	66.84(12)	N(2)-Dy(1)-N(3)	69.40(14)
Compound 3			
Dy(1)-O(2)	2.300(7)	O(2)-Dy(1)-Dy(2)	156.6(2)
Dy(1)-O(3)	2.304(7)	O(3)-Dy(1)-Dy(2)	88.5(2)
Dy(1)-O(8)	2.310(7)	O(8)-Dy(1)-Dy(2)	31.98(17)
Dy(1)-O(1)	2.319(7)	O(1)-Dy(1)-Dy(2)	113.2(2)
Dy(1)-O(4)	2.336(7)	O(4)-Dy(1)-Dy(2)	111.90(18)
Dy(1)-O(9)	2.370(7)	O(9)-Dy(1)-Dy(2)	32.87(16)
Dy(1)-O(10)	2.449(8)	O(10)-Dy(1)-Dy(2)	81.0(2)
Dy(1)-O(7)	2.480(8)	O(7)-Dy(1)-Dy(2)	82.17(19)
Dy(1)-Dy(2)	3.9031(9)	O(6)-Dy(2)-O(5)	72.7(3)
Dy(2)-O(6)	2.275(8)	O(6)-Dy(2)-O(8)	133.2(3)
Dy(2)-O(5)	2.287(8)	O(5)-Dy(2)-O(8)	83.4(3)
Dy(2)-O(8)	2.297(7)	O(6)-Dy(2)-O(9)	80.5(3)
Dy(2)-O(9)	2.305(7)	O(5)-Dy(2)-O(9)	100.4(3)
Dy(2)-N(2)	2.575(9)	O(8)-Dy(2)-O(9)	64.8(2)
Dy(2)-N(1)	2.585(9)	O(6)-Dy(2)-N(2)	149.3(3)
Dy(2)-N(4)	2.590(11)	O(5)-Dy(2)-N(2)	133.8(3)
Dy(2)-N(3)	2.616(9)	O(8)-Dy(2)-N(2)	73.2(3)
O(2)-Dy(1)-O(3)	114.7(3)	O(9)-Dy(2)-N(2)	104.4(3)
O(2)-Dy(1)-O(8)	142.9(3)	O(6)-Dy(2)-N(1)	122.2(3)
O(3)-Dy(1)-O(8)	82.4(3)	O(5)-Dy(2)-N(1)	76.4(3)
O(2)-Dy(1)-O(1)	73.3(3)	O(8)-Dy(2)-N(1)	88.7(3)
O(3)-Dy(1)-O(1)	73.6(3)	O(9)-Dy(2)-N(1)	153.5(3)
O(8)-Dy(1)-O(1)	81.5(3)	N(2)-Dy(2)-N(1)	64.0(3)
O(2)-Dy(1)-O(4)	79.5(3)	O(6)-Dy(2)-N(4)	69.3(3)
O(3)-Dy(1)-O(4)	73.0(3)	O(5)-Dy(2)-N(4)	104.7(3)
O(8)-Dy(1)-O(4)	137.5(2)	O(8)-Dy(2)-N(4)	157.3(3)
O(1)-Dy(1)-O(4)	121.9(3)	O(9)-Dy(2)-N(4)	132.0(3)
O(2)-Dy(1)-O(9)	146.4(3)	N(2)-Dy(2)-N(4)	86.5(3)
O(3)-Dy(1)-O(9)	83.4(3)	N(1)-Dy(2)-N(4)	73.1(3)
O(8)-Dy(1)-O(9)	63.5(2)	O(6)-Dy(2)-N(3)	81.1(3)
O(1)-Dy(1)-O(9)	140.3(3)	O(5)-Dy(2)-N(3)	153.8(3)
O(4)-Dy(1)-O(9)	79.4(2)	O(8)-Dy(2)-N(3)	116.2(3)
O(2)-Dy(1)-O(10)	81.2(3)	O(9)-Dy(2)-N(3)	75.3(3)
O(3)-Dy(1)-O(10)	144.3(3)	N(2)-Dy(2)-N(3)	71.3(3)
O(8)-Dy(1)-O(10)	104.2(3)	N(1)-Dy(2)-N(3)	118.8(3)

O(1)-Dy(1)-O(10)	141.6(3)	N(4)-Dy(2)-N(3)	64.2(3)
O(4)-Dy(1)-O(10)	79.5(3)	O(6)-Dy(2)-Dy(1)	104.7(2)
O(9)-Dy(1)-O(10)	69.4(3)	O(5)-Dy(2)-Dy(1)	85.2(2)
O(2)-Dy(1)-O(7)	77.9(3)	O(8)- $Dy(2)$ - $Dy(1)$	32.19(16)
O(3)-Dy(1)-O(7)	140.4(3)	O(9)-Dy(2)-Dy(1)	33.92(17)
O(8)-Dy(1)-O(7)	69.5(2)	N(2)-Dy(2)-Dy(1)	94.2(2)
O(1)-Dy(1)-O(7)	75.0(3)	N(1)-Dy(2)-Dy(1)	120.1(2)
O(4)-Dy(1)-O(7)	145.8(3)	N(4)-Dy(2)-Dy(1)	165.5(2)
O(9)-Dy(1)-O(7)	106.8(3)	N(3)-Dy(2)-Dy(1)	102.3(2)
O(10)-Dy(1)-O(7)	71.9(3)		

Table S3 Dy^{III} ion geometry analysis by SHAPE 2.1 software.

Configuration	ABOXIY,	ABOXIY,	ABOXIY, 3	
	1	2	Dy1	Dy2
Octagon(D8h)	31.594	31.307	31.581	32.874
Heptagonal pyramid(C7v)	21.493	20.923	23.065	23.596
Hexagonal bipyramid(D6h)	12.285	12.168	16.750	12.324
Cube(Oh)	8.272	8.763	9.846	5.044
Square antiprism (D_{4d})	2.401	2.149	0.629	2.679
Triangular dodecahedron (D_{2d})	1.256	1.765	2.480	1.308
Johnson gyrobifastigium J26 (D _{2d})	12.163	11.526	16.448	15.694
Johnson elongated triangular bipyramid J14 (D_{3h})	26.847	26.775	27.866	27.158
Biaugmented trigonal prism J50 (C_{2v})	2.042	1.983	2.874	4.334
Biaugmented trigonal prism (C_{2v})	2.042	2.128	2.248	3.739
Snub siphenoid J84 (D _{2d})	4.272	4.258	5.082	5.166
Triakis tetrahedron(Td)	9.029	9.554	10.699	5.931
Elongated trigonal bipyramid(D3h)	24.373	23.312	24.149	23.932

SHAPE	v2.1	Cor	tinuous Shape Measures calculation
(c) 2013	Electronic	Structure G	roup, Universitat de Barcelona
		Contact:	llunell@ub.edu

Dy structures of 1		
OP-8	1 D8h	Octagon
HPY-8	2 C7v	Heptagonal pyramid
HBPY-8	3 D6h	Hexagonal bipyramid
CU-8	4 Oh	Cube
SAPR-8	5 D4d	Square antiprism
TDD-8	6 D2d	Triangular dodecahedron
JGBF-8	7 D2d	Johnson gyrobifastigium J26

JETBPY-8	8 D3h	Johnson elo	ngated triangula	ar bipyramid J	14				
JBTPR-8	9 C2v	Biaugmentee	Biaugmented trigonal prism J50						
BTPR-8	10 C2v	Biaugmente	Biaugmented trigonal prism						
JSD-8	11 D2d	Snub diphen	Snub diphenoid J84						
TT-8	12 Td	Triakis tetrah	edron						
ETBPY-8	13 D3h	Elongated t	rigonal bipyram	iid					
Structure [MI	L8]	OP-8	HPY-8	HBPY-8	CU-8	SAPR-8			
TDD-8	JGBF-8	JETBPY-8	JBTPR-8	BTPI	R-8 JS	D-8 1	T-8		
ETBPY-8									
ABOXIY,	31.594,	21.493,	12.285,	8.272,	2.401,	1.256,	12.163,		
26.847,	2.042,	2.042,	4.272,	9.029,	24.373				
 S H A P E	v2.1	Continuous S	hape Measures	calculation					
(c) 2013 Ele	ectronic Struct	ure Group, Uni	versitat de Barc	elona					
. ,	Con	tact: llunell@	ub.edu						
Dy structures	of 2								
OP-8	1 D8h	Octagon							
HPY-8	2 C7v	Heptagonal	pyramid						
HBPY-8	3 D6h	Hexagonal b	pipyramid						
CU-8	4 Oh	Cube							
SAPR-8	5 D4d	Square antip	orism						
TDD-8	6 D2d	Triangular d	lodecahedron						
JGBF-8	7 D2d	Johnson gyr	obifastigium J2	6					
JETBPY-8	8 D3h	Johnson elos	ngated triangula	ır bipyramid J	14				
JBTPR-8	9 C2v	Biaugmente	l trigonal prism	J50					
BTPR-8	10 C2v	Biaugmente	d trigonal prism	l					
JSD-8	11 D2d	Snub diphene	oid J84						
TT-8	12 Td	Triakis tetrah	edron						
ETBPY-8	13 D3h	Elongated tr	rigonal bipyram	id					
Structure [M	[L8]	OP-8	HPY-8	HBF	PY-8	CU-8	SAPR-8		
TDD-8	JGBF-8	JETBPY-8	3 JBTPF	R-8 I	BTPR-8	JSD-8	TT-8		
ETBPY-8									
ABOXIY,	31.307,	20.923,	12.168,	8.763,	2.149,	1.765,	11.526,		
26.775,	1.983,	2.128,	4.258,	9.554,	23.312				
S H A P E (c) 2013 Ele	v2.1 ectronic Struct Con	Continuous S ure Group, Uni tact: llunell@	hape Measures versitat de Barc 9ub.edu	calculation celona					

Dy structures of 3	(Dy1)	
OP-8	1 D8h	Octagon
HPY-8	2 C7v	Heptagonal pyramid
HBPY-8	3 D6h	Hexagonal bipyramid
CU-8	4 Oh	Cube
SAPR-8	5 D4d	Square antiprism
TDD-8	6 D2d	Triangular dodecahedron
JGBF-8	7 D2d	Johnson gyrobifastigium J26
JETBPY-8	8 D3h	Johnson elongated triangular bipyramid J14
JBTPR-8	9 C2v	Biaugmented trigonal prism J50
BTPR-8	10 C2v	Biaugmented trigonal prism
JSD-8	11 D2d	Snub diphenoid J84
TT-8	12 Td	Triakis tetrahedron
ETBPY-8	13 D3h	Elongated trigonal bipyramid

Structure []	ML8]	OP-8	HPY-8	HBF	PY-8	CU-8	SAPR-8
TDD-8	JGBF-8	JETBPY-8	JBTP	R-8 I	BTPR-8	JSD-8	TT-8
ETBPY-8							
ABOXIY,	31.581,	23.065,	16.750,	9.846,	0.629,	2.480,	16.448,
27.866,	2.874,	2.248,	5.082,	10.699,	24.149		

S H A P E v2.1 Continuous Shape Measures calculation

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TDD-8

ETBPY-8

JGBF-8

JETBPY-8

0.0.0	1 001	0						
OP-8	I D8h	Octagon	Jetagon					
HPY-8	2 C7v	Heptagonal p	Heptagonal pyramid					
HBPY-8	3 D6h	Hexagonal bi	Hexagonal bipyramid					
CU-8	4 Oh	Cube						
SAPR-8	5 D4d	Square antipr	ism					
TDD-8	6 D2d	Triangular do	odecahedron					
JGBF-8	7 D2d	Johnson gyrol	bifastigium J26					
JETBPY-8	8 D3h	Johnson elong	Johnson elongated triangular bipyramid J14					
JBTPR-8	9 C2v	Biaugmented	Biaugmented trigonal prism J50					
BTPR-8	10 C2v	Biaugmented	Biaugmented trigonal prism					
JSD-8	11 D2d	Snub diphenoi	Snub diphenoid J84					
TT-8	12 Td	Triakis tetrahe	Triakis tetrahedron					
ETBPY-8	13 D3h	Elongated trig	gonal bipyramid					
Structure [ML	.8]	OP-8	HPY-8	HBPY-8	CU-8	SAPR-8		

JBTPR-8

BTPR-8

JSD-8

TT-8



Fig. S10 XRPD curves of 2.



Fig. S12 XRPD curves of 1a.



Fig. S12 XRPD curves of 3a and 3b.

3. Magnetic hysteresis loop for 1 at 5 K



Fig. S15 Magnetic hysteresis loop for **1** at 5 K.

4. Relaxation fitting parameters of 1-3

The magnetic susceptibility data of **1-3** under a zero dc field were described by the modified Debye functions:

$$\chi'(\omega) = \chi_{\rm S} + (\chi_{\rm T} - \chi_{\rm S}) \frac{1 + (\omega\tau)^{1-\alpha} \sin(\frac{\pi}{2}\alpha)}{1 + 2(\omega\tau)^{1-\alpha} \sin(\frac{\pi}{2}\alpha) + (\omega\tau)^{(2-2\alpha)}}$$
$$\chi''(\omega) = (\chi_{\rm T} - \chi_{\rm S}) \frac{(\omega\tau)^{1-\alpha} \cos(\frac{\pi}{2}\alpha)}{1 + 2(\omega\tau)^{1-\alpha} \sin(\frac{\pi}{2}\alpha) + (\omega\tau)^{(2-2\alpha)}}$$
$$\chi''_{\omega=\tau^{-1}} = (\chi_{\rm T} - \chi_{\rm S}) \frac{\cos(\frac{\pi}{2}\alpha)}{2 + 2\sin(\frac{\pi}{2}\alpha)} = \frac{1}{2} (\chi_{\rm T} - \chi_{\rm S}) \tan\frac{\pi}{4} (1-\alpha)$$

	s appliea ae liela.			
Τ	$\Delta \chi_1 \text{ (cm}^3 \text{mol}^{-1}\text{)}$	$\Delta \chi_2 (\mathrm{cm}^3\mathrm{mol}^{-1})$	$\tau(s)$	α
2.0	0.261391E+00	0.361211E+01	0.175656E-02	0.140216E+00
2.2	0.238414E+00	0.327639E+01	0.175393E-02	0.140658E+00
2.4	0.219778E+00	0.299739E+01	0.174849E-02	0.140183E+00
2.6	0.203631E+00	0.275428E+01	0.173895E-02	0.139988E+00
2.8	0.190634E+00	0.256450E+01	0.173304E-02	0.139880E+00
3.0	0.241180E+00	0.320769E+01	0.145563E-02	0.134667E+00
3.2	0.168410E+00	0.224433E+01	0.171481E-02	0.139552E+00
3.6	0.152109E+00	0.199434E+01	0.169600E-02	0.138781E+00
4.0	0.138250E+00	0.179388E+01	0.167278E-02	0.138328E+00
4.4	0.128098E+00	0.163083E+01	0.164985E-02	0.136957E+00
4.8	0.119174E+00	0.149417E+01	0.162239E-02	0.135712E+00
5.2	0.112107E+00	0.137857E+01	0.159383E-02	0.133974E+00
5.6	0.104950E+00	0.128026E+01	0.156388E-02	0.133034E+00
6.0	0.989626E-01	0.119526E+01	0.153371E-02	0.132015E+00
6.5	0.931221E-01	0.110274E+01	0.149254E-02	0.129260E+00
7.0	0.879650E-01	0.102420E+01	0.145102E-02	0.126618E+00
7.5	0.832263E-01	0.955982E+00	0.140595E-02	0.123585E+00
8.0	0.786051E-01	0.896620E+00	0.135879E-02	0.122136E+00
9.0	0.719128E-01	0.797233E+00	0.126102E-02	0.115251E+00
10	0.662030E-01	0.718566E+00	0.115962E-02	0.108454E+00
11	0.617714E-01	0.652911E+00	0.105188E-02	0.100305E+00
12	0.576881E-01	0.599437E+00	0.943958E-03	0.930296E-01
14	0.502664E-01	0.514226E+00	0.728314E-03	0.778799E-01
16	0.439224E-01	0.452475E+00	0.538635E-03	0.686484E-01
18	0.378291E-01	0.404149E+00	0.377124E-03	0.676439E-01
20	0.333472E-01	0.365050E+00	0.245487E-03	0.735590E-01
25	0.346309E-01	0.294894E+00	0.526036E-04	0.106273E+00
30	0.149166E-06	0.248538E+00	0.702782E-05	0.428005E-01

Table S4 Relaxation fitting parameters from Least-Squares Fitting of $\chi(\omega)$ data for **1** under a zero applied dc field.

Table S5 Relaxation fitting parameters from Least-Squares Fitting of $\chi(\omega)$ data for **2** under a zero applied dc field.

Т	$\Delta \chi_1 \ (\text{cm}^3 \text{mol}^{-1})$	$\Delta \chi_2 (\mathrm{cm}^3\mathrm{mol}^{-1})$	$\tau(s)$	α
2.0	0.465942E-01	0.289863E+01	0.197708E-01	0.215831E+00
2.2	0.425992E-01	0.263810E+01	0.198260E-01	0.216843E+00
2.4	0.394299E-01	0.242025E+01	0.198487E-01	0.216996E+00
2.6	0.366161E-01	0.223006E+01	0.198124E-01	0.218369E+00
2.8	0.340803E-01	0.207884E+01	0.198187E-01	0.219241E+00
3.0	0.348816E-01	0.209333E+01	0.196503E-01	0.219665E+00
3.4	0.286720E-01	0.171768E+01	0.195513E-01	0.221349E+00
3.8	0.261757E-01	0.154193E+01	0.193488E-01	0.222135E+00

4.2	0.248469E-01	0.139581E+01	0.189757E-01	0.220758E+00
4.6	0.232428E-01	0.127673E+01	0.186536E-01	0.220674E+00
5.0	0.225191E-01	0.117522E+01	0.182546E-01	0.219616E+00
6.0	0.210690E-01	0.980746E+00	0.171252E-01	0.212692E+00
7.0	0.206185E-01	0.838673E+00	0.157228E-01	0.202344E+00
8.0	0.198936E-01	0.731708E+00	0.142334E-01	0.188511E+00
9.0	0.192121E-01	0.649344E+00	0.127696E-01	0.176043E+00
10	0.186252E-01	0.581887E+00	0.112805E-01	0.161074E+00
12	0.155628E-01	0.482084E+00	0.855062E-02	0.136948E+00
14	0.132252E-01	0.411135E+00	0.632224E-02	0.116947E+00
16	0.948164E-02	0.359856E+00	0.456981E-02	0.104106E+00
18	0.921472E-02	0.320504E+00	0.320975E-02	0.982376E-01
20	0.868805E-02	0.288662E+00	0.216889E-02	0.969097E-01
22	0.847249E-02	0.261811E+00	0.139808E-02	0.761193E-01
24	0.806337E-02	0.239134E+00	0.790216E-03	0.811517E-01
26	0.788403E-02	0.221633E+00	0.381680E-03	0.841454E-01
28	0.768594E-02	0.208025E+00	0.171161E-03	0.806470E-01
30	0.752449E-02	0.194947E+00	0.844968E-04	0.826842E-01
35	0.717969E-02	0.167564E+00	0.441949E-04	0.783574E-01

Table S6 Relaxation fitting parameters from Least-Squares Fitting of $\chi(\omega)$ data for **3** under a zero applied dc field.

Т	$\Delta \chi_1 \text{ (cm}^3 \text{mol}^{-1}\text{)}$	$\Delta \chi_2 (\mathrm{cm}^3\mathrm{mol}^{-1})$	$\tau(s)$	α
2.0	0.121077E+01	0.673671E+01	0.796071E-03	0.397530E+00
2.2	0.109801E+01	0.607124E+01	0.756133E-03	0.399594E+00
2.4	0.996063E+00	0.552736E+01	0.718862E-03	0.401859E+00
2.6	0.914338E+00	0.505993E+01	0.688912E-03	0.403261E+00
2.8	0.855042E+00	0.468149E+01	0.668629E-03	0.404206E+00
3.0	0.860441E+00	0.439862E+01	0.821137E-03	0.413667E+00
3.2	0.745063E+00	0.407136E+01	0.626539E-03	0.407282E+00
3.4	0.700888E+00	0.382056E+01	0.609033E-03	0.408323E+00
3.6	0.662317E+00	0.359830E+01	0.591768E-03	0.409957E+00
3.8	0.648599E+00	0.339939E+01	0.587118E-03	0.409511E+00
4.0	0.623371E+00	0.322213E+01	0.574380E-03	0.411000E+00
4.2	0.600968E+00	0.306109E+01	0.559941E-03	0.411077E+00
4.4	0.568168E+00	0.292034E+01	0.542438E-03	0.414651E+00
4.6	0.554784E+00	0.278905E+01	0.533813E-03	0.415430E+00
4.8	0.545100E+00	0.266777E+01	0.525098E-03	0.415851E+00
5.0	0.540499E+00	0.255663E+01	0.520293E-03	0.415488E+00
5.5	0.531911E+00	0.231441E+01	0.507471E-03	0.413589E+00
6.0	0.536898E+00	0.211610E+01	0.505842E-03	0.409592E+00
6.5	0.554169E+00	0.194685E+01	0.513723E-03	0.400435E+00
7.0	0.571697E+00	0.180202E+01	0.523581E-03	0.387980E+00

8.0	0.594646E+00	0.156763E+01	0.521257E-03	0.352869E+00
10	0.578048E+00	0.124204E+01	0.341513E-03	0.274351E+00

5. Computational details

For compounds **1** and **2**, there is only one magnetic center Dy^{III} ion. For binuclear compound **3**, it has two types of Dy^{III} fragments, and thus two Dy^{III} fragments were calculated. Complete-active-space self-consistent field (CASSCF) calculations on compounds **1-3** (seen Fig. S8 for the calculated complete structures of compounds **1** and **2**, and the model structure of compound **3**) extracted from the compounds on the basis of single-crystal X-ray determined geometry have been carried out with MOLCAS 8.2^{S1} program package. For compound **3**, each Dy^{III} fragment was calculated keeping the experimentally determined structure of the corresponding compound while replacing the neighbouring Dy^{III} ion by diamagnetic Lu^{III}.

The basis sets for all atoms are atomic natural orbitals from the MOLCAS ANO-RCC library: ANO-RCC-VTZP for Dy^{III} ion; VTZ for close N and O; VDZ for distant atoms. The calculations employed the second order Douglas-Kroll-Hess Hamiltonian, where scalar relativistic contractions were taken into account in the basis set and the spin-orbit couplings were handled separately in the restricted active space state interaction (RASSI-SO) procedure. For individual Dy^{III} fragment, active electrons in 7 active spaces include all *f* electrons (CAS(9 in 7)) in the CASSCF calculation. To exclude all the doubts, we calculated all the roots in the active space. We have mixed the maximum number of spin-free state which was possible with our hardware (all from 21 sextets, 128 from 224 quadruplets, 130 from 490 doublets). SINGLE–ANISO^{S2} program was used to obtain the energy levels, *g* tensors, *m_J* values, magnetic axes, *et al.*, based on the above CASSCF/RASSI-SO calculations.





Fig. S16 Calculated structures of compounds 1-3 (a-c); H atoms are omitted.

To fit the exchange interaction in compound **3**, we took two steps to obtain them. Firstly, we calculated individual Dy^{III} fragments using CASSCF to obtain the corresponding magnetic properties. Then, the exchange interaction between the magnetic centers is considered within the Lines model,^{S3} while the account of the dipole-dipole magnetic coupling is treated exactly. The Lines model is effective and has been successfully used widely in the research field of *f*-element single-molecule magnets.^{S4}

For compound **3**, there is only one type of *J*.

The exchange Ising Hamiltonian is:

$$\hat{H}_{exch} = -J_1 \hat{S}_{y_1} \hat{S}_{y_2}$$
(S1)

The J_{total} is the parameter of the total magnetic interaction ($J_{total} = J_{diploar} + J_{exchange}$)

between magnetic center ions. The $\$_{by} = \pm 1/2$ are the ground pseudospin on the Dy^{III} sites. The dipolar magnetic coupling can be calculated exactly, while the exchange coupling constants were fitted through comparison of the computed and measured magnetic susceptibility using the Poly_Aniso program.^{S2}.

Table S7 E	xchange	energies	(cm^{-1})	and	main	values	of	the	g_z	for	the	lowest	two
exchange do	oublets of	compour	nd 3 .										

	3				
	E/cm^{-1}	gz			
Dy1	0.0	33.718			
Dy2	0.5	17.959			



Fig. S17 Calculated (red solid line) and experimental (black circle dot) data of magnetic susceptibilities of compounds 1-3 (a-c). The intermolecular interactions zJ' of 1-3 were fitted to -0.10, -0.08 and -0.00 cm⁻¹, respectively.

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