

## Supporting Information

# Pressure induced semiconductor-semimetal-superconductor transition for magnesium hexaborides

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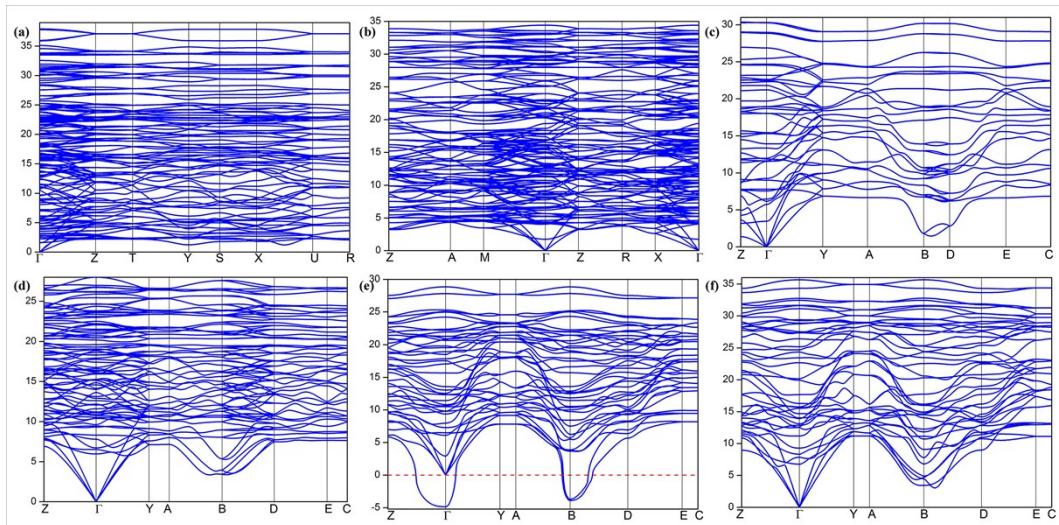


Fig. S1 Phonon dispersion curves of (a)  $Cmcm$ , (b)  $I4/mmm$ , (c)  $C2/m\text{-I}$ , (d)  $C2/m\text{-II}$  and (e)  $P2_1/m$  at zero pressure, (f)  $P2_1/m$  at 70GPa for  $MgB_6$ .

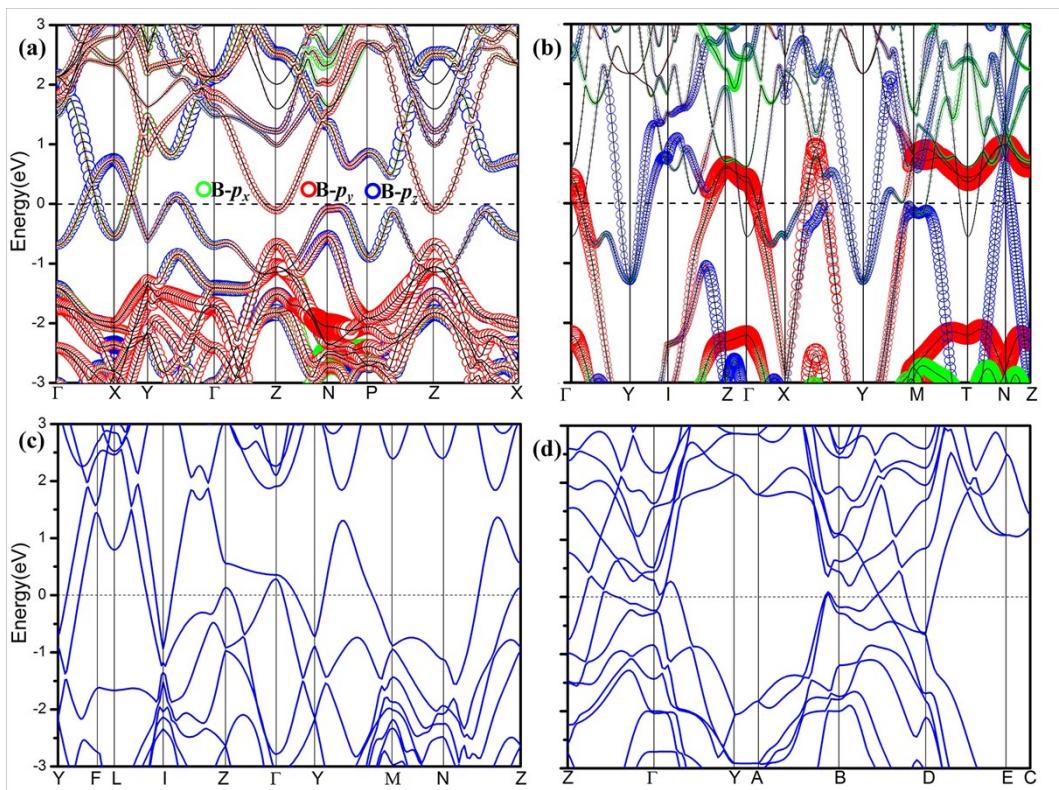


Fig. S2 Bands structure of (a)  $I4/mmm$ , (b)  $C2/m\text{-I}$ , (c)  $C2/m\text{-II}$ , (d)  $P2_1/m$  of  $MgB_6$ .

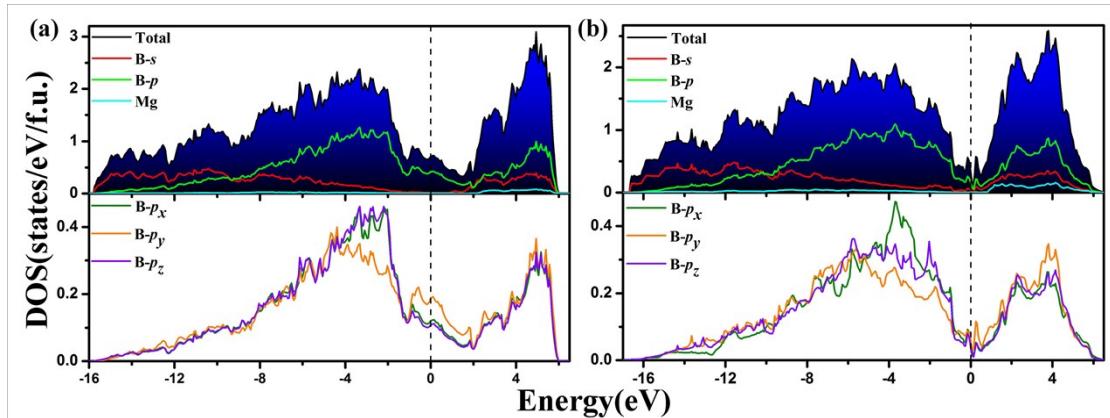


Fig. S3 The densities of states calculated by PBE (a)  $C2/m\text{-II}$ , (b)  $P2_1/m$  at ambient pressure.

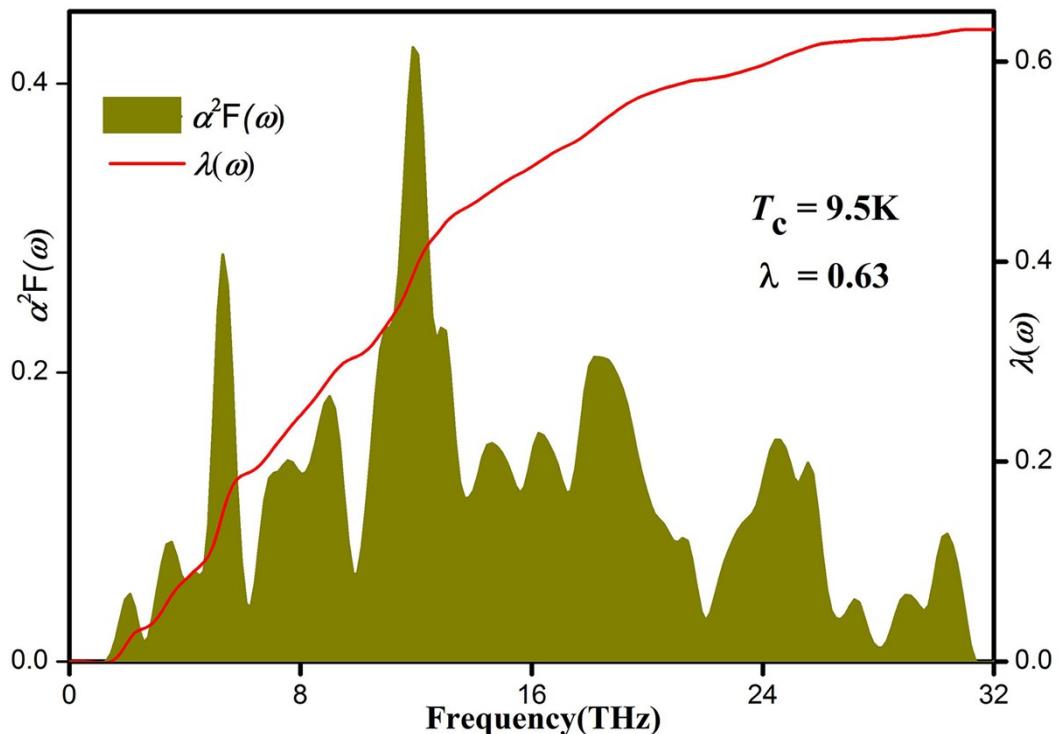


Fig. S4 Eliashberg spectral function  $\alpha^2F(\omega)$  (dark yellow area) and electron-phonon coupling parameters  $\lambda(\omega)$  (red line) of  $C2/m\text{-I}$  for  $MgB_6$ .

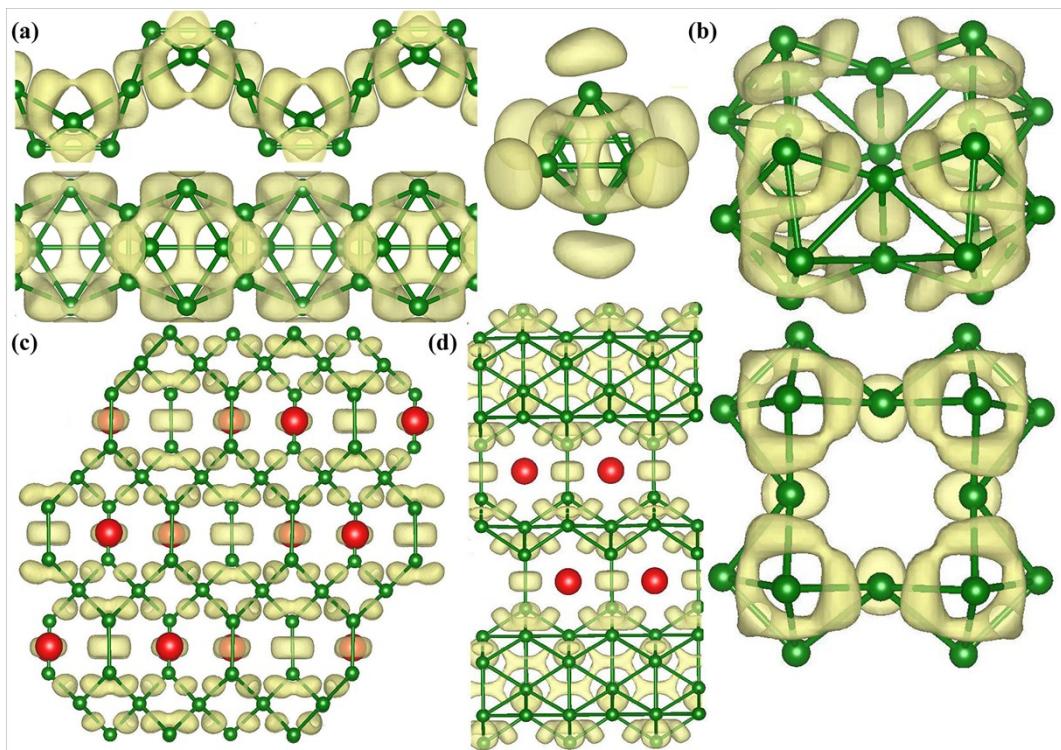


Fig. S5 The ELF with isosurfaces 0.75 (a)  $B_8$  cluster and  $B_6$  octahedra of  $Cmcm$  structure, (b)  $B_{24}$  cluster of  $I4/mmm$  structure, (c)  $C2/m$ -II, (d)  $P2_1/m$ .

Born-Huang criteria for

orthorhombic phase:

$$C_{ii} > 0 \quad (i=1 \sim 6),$$

$$(C_{11} + C_{22} - 2C_{12}) > 0, \quad (C_{11} + C_{33} - 2C_{13}) > 0, \quad (C_{22} + C_{33} - 2C_{23}) > 0,$$

$$[C_{11} + C_{22} + C_{33} + 2(C_{12} + C_{13} + C_{23})] > 0.$$

tetragonal phase:

$$C_{ii} > 0 \quad (i=3, 4, 6),$$

$$C_{11} - C_{12} > 0,$$

$$C_{11} + C_{33} - 2C_{13} > 0,$$

$$2C_{11} + C_{33} + 2C_{12} + 4C_{13} > 0.$$

monoclinic structure:

$$C_{ii} > 0 \quad (i=1, 2, 3, 4, 5, 6),$$

$$[C_{11} + C_{22} + C_{33} + 2(C_{12} + C_{13} + C_{23})] > 0,$$

$$(C_{33}C_{55} - C_{35}^2) > 0, \quad (C_{44}C_{66} - C_{46}^2) > 0, \quad (C_{22} + C_{33} - 2C_{23}) > 0,$$

$$[C_{22}(C_{33}C_{55} - C_{35}^2) + 2C_{23}C_{25}C_{35} - C_{23}^2C_{55} - C_{25}^2C_{33}] > 0,$$

$$\{2[aC_{15}C_{25} + bC_{15}C_{35} + cC_{25}C_{35}] - [dC_{15}^2 + eC_{25}^2 + fC_{35}^2]\} + gC_{55} > 0,$$

$$a = C_{33}C_{12} - C_{13}C_{23}, \quad b = C_{22}C_{13} - C_{12}C_{23}, \quad c = C_{11}C_{23} - C_{12}C_{13},$$

$$d = C_{22}C_{33} - C_{23}^2, \quad e = C_{11}C_{33} - C_{13}^2, \quad f = C_{11}C_{22} - C_{12}^2,$$

$$g = C_{11}C_{22}C_{33} - C_{11}C_{23}^2 - C_{22}C_{13}^2 - C_{33}C_{12}^2 + 2C_{12}C_{13}C_{23}.$$

Table S1. The Wyckoff positions of the proposed MgB<sub>6</sub> structures are listed.

	atoms	x	y	z	site
<i>Cmcm</i>	Mg	-0.29123	-0.63821	0.75000	8g
	B1	-0.35423	-0.35694	0.75000	8g
	B2	0.16798	-0.42073	0.75000	8g
	B3	-0.00000	-0.64058	1.41019	8f
	B4	0.00000	-0.93983	-0.93983	8f
	B5	-0.00000	-0.22821	1.09012	8f
	B6	-0.09786	-0.50000	0.50000	8e
<i>I4/mmm</i>	Mg1	0.00000	0.00000	0.81648	4e
	Mg2	-0.00000	0.50000	0.25000	4d
	B1	0.28091	0.50000	0.08942	16n
	B2	0.27527	0.27527	0.16088	16m
	B3	0.12371	0.70010	-0.00000	16l
<i>C2/m-I</i>	Mg	-0.50000	-0.00000	-0.00000	2b
	B1	0.52215	-0.50000	0.27674	4i
	B2	0.66639	-0.00000	0.73943	4i
	B3	0.65047	-0.00000	0.49065	4i
<i>C2/m-II</i>	Mg	-0.33501	-0.00000	0.82714	4i
	B1	-0.66187	-0.25878	0.67179	8j
	B2	-0.12456	0.00000	0.02290	4i
	B3	-0.20420	-0.00000	0.32761	4i
	B4	-0.53754	-0.00000	0.65646	4i
	B5	-0.50000	0.25921	-0.00000	4g
<i>P2<sub>1</sub>/m</i>	Mg	-0.68671	-0.25000	1.15591	2e
	B1	-0.22485	-0.25000	0.34295	2e
	B2	-0.49698	-0.25000	0.79945	2e
	B3	-0.40498	-0.25000	1.33352	2e
	B4	-0.13181	-0.75000	0.48382	2e
	B5	-0.04557	-0.75000	1.04339	2e
	B6	-0.86741	-0.75000	1.13269	2e

Table S2. The elastic constants  $C_{ij}$  (GPa), bulk moduli  $B$  (GPa), the shear moduli  $G$  (GPa), Young's modulus  $E$  (GPa), the  $B/G$  value and Poisson ratio  $\nu$  for the  $C2/m$ -II and  $P2_1/m$  of MgB<sub>6</sub>.

	$C2/m$ -II	$P2_1/m$ (70 GPa)
$C_{11}$	478	771
$C_{22}$	371	757
$C_{33}$	458	753
$C_{44}$	229	262
$C_{55}$	188	344
$C_{66}$	230	260
$C_{12}$	136	200
$C_{13}$	67	193
$C_{15}$	-39	44
$C_{23}$	118	152
$C_{25}$	69	-48
$C_{35}$	-39	57
$C_{46}$	32	-18
$B$	213	
$G$	179	
$E$	420	
$B/G$	1.19	
$\nu$	0.171	