Electronic Supplementary Information

Synthesis of crystalline $Na_2P_2S_6$ via a ball milling route and comparison of its local structure to the amorphous phase

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Table S1: Refined structural parameters obtained from powder diffraction of crystalline $Na_2P_2S_6$ at room temperature compared to those of a single crystal measurement from Ref. ¹³.

	Na ₂ P ₂ S ₆ synthesized by ballmilling and subsequent thermal annealing	$Na_2P_2S_6$ synthesized by solid state reaction by Lotsch et al. ^[9]
Space group	P2 ₁ /m (11)	P2 ₁ /m (11)
Lattice parameters		
a / Å	6.6861(3)	6.6752(3)
b / Å	7.8314 (4)	7.7968(4)
c / Å	9.0418 (4)	9.0379(4)
β/°	90.223 (4)	90.151(1)
Cell volume	473.44 (4)	470.38(4)
Atomic coordinates Na		
х	0.2829 (0.0028)	0.2863(2)
У	0.0136 (0.0017)	0.01241(9)
Z	0.7130 (0.0016)	0.71003(7)
Structural strain	34.34 (0.12)	-
dD/D *10E-4		
GOF	2.458	1.090



Figure S1: Zoom into the short range region of the pair distribution functions of amorphous $Na_2P_2S_6$ compared with modeled PDFs of single $[PS_4]^{3-}$, $[P_2S_6]^{4-}$, $[P_2S_7]^{4-}$ and $[P_2S_6]^{2-}$ structural building blocks. Atomic distances are marked with yellow, green and blue arrows.



Figure S2: FigureS1-SEM image of amorphous Na₂P₂S₆.



Figure 10: Figure S2-SEM image of crystalline Na₂P₂S_{6.}

Comparison of crystal structures of the same symmetry $P2_1/m$ (No. 11) [unique axis b]

Structure #1

11						
6.6789	6.67893 7.81782 9.05651 90.00000 90.35290 90.00000					
8						
Р	1	2e	0.210080 0.250000 0.390070			
Р	3	2e	0.322040 0.250000 0.082430			
S	1	4f	0.228740 0.448750 0.226260			
S	5	2e	0.618980 0.250000 0.043230			
S	7	2e	0.447430 0.250000 0.519680			
S	9	2e	0.147200 0.250000 0.899310			
S	11	2e	0.944070 0.250000 0.486700			
Na	1	4f	0.287390 0.990860 0.700950			

Structure #2

11 6.68609 7.83137 9.04181 90.0000 90.2232 90.0000 8

P 1 2e 0.786600 0.250000 0.613400

Р	2	2e	0.684100	0.250000	0.925800
S	1	4f	0.237800	0.549100	0.225300
S	2	2e	0.385500	0.250000	0.949900
S	3	2e	0.545700	0.250000	0.483800
S	4	2e	0.854600	0.250000	0.089600
S	5	2e	0.046000	0.250000	0.515000
Na	1	4f	0.282900	0.013600	0.713000

Description of Structure #2 in the most similar configuration to Structure #1

011					
6.6860	6.686090 7.831370 9.041810 90.000000 90.223198 90.000000				
8					
Р	1	2e	0.213400	0.250000	0.386600
Р	2	2e	0.315900	0.250000	0.074200
S	1	4f	0.237800	0.450900	0.225300
S	2	2e	0.614500	0.250000	0.050100
S	3	2e	0.454300	0.250000	0.516200
S	4	2e	0.145400	0.250000	0.910400
S	5	2e	0.954000	0.250000	0.485000
Na	1	4f	0.282900	0.986400	0.713000

Transformation matrix (P, p): a,b,c ; 0,1/2,0

Matrix form:

 $(\mathbf{P}, \mathbf{p}) = \begin{pmatrix} 1 & 0 & 0 & 0 \\ 0 & 1 & 0 & 1/2 \\ 0 & 0 & 1 & 0 \end{pmatrix}$

Atom pairings and distances

	Atom Mappings						
WP Atom			Coordinates in S ₁	in S ₁ Atom Coordinates in			
2e	(x,1/4,z)	P1	(0.210080,0.250000,0.390070)	P1	(0.213400,0.250000,0.386600)		
2e	(x,1/4,z)	Р3	(0.322040,0.250000,0.082430)	P2	(0.315900,0.250000,0.074200)		
4f	(x,y,z)	S1	(0.228740,0.448750,0.226260)	S1	(0.237800,0.450900,0.225300)		

2e	(x,1/4,z)	S5	(0.618980,0.250000,0.043230)	S2	(0.614500,0.250000,0.050100)
2e	(x,1/4,z)	S7	(0.447430,0.250000,0.519680)	S3	(0.454300,0.250000,0.516200)
2e	(x,1/4,z)	S9	(0.147200,0.250000,0.899310)	S4	(0.145400,0.250000,0.910400)
2e	(x,1/4,z)	S11	(0.944070,0.250000,0.486700)	S5	(0.954000,0.250000,0.485000)
4f	(x,y,z)	Na1	(0.287390,0.990860,0.700950)	Na1	(0.282900,0.986400,0.713000)

WP		Atom	Atomic Displacements				
		Atom	u _x	u _y	uz	u	
2e	(x,1/4,z)	P1	0.0033	0.0000	-0.0035	0.0386	
2e	(x,1/4,z)	Р3	-0.0061	0.0000	-0.0082	0.0849	
4f	(x,y,z)	S1	0.0091	0.0022	-0.0010	0.0635	
2e	(x,1/4,z)	S5	-0.0045	0.0000	0.0069	0.0692	
2e	(x,1/4,z)	S7	0.0069	0.0000	-0.0035	0.0558	
2e	(x,1/4,z)	S9	-0.0018	0.0000	0.0111	0.1012	
2e	(x,1/4,z)	S11	0.0099	0.0000	-0.0017	0.0682	
4f	(x,y,z)	Na1	-0.0045	-0.0045	0.0120	0.1186	

NOTE: u_x , u_y and u_z are given in relative units. |u| is the absolute distance given in Å

Evaluation of the structure similarity

S	d _{max.} (Å)	d _{av.} (Å)	Δ
0.0010	0.1186	0.0782	0.016

- Lattice and atomic position criteria:
 - The <u>degree of lattice distortion (S)</u> is the spontaneous strain (sum of the squared eigenvalues of the strain tensor divided by 3). For the given two structures, the **degree of lattice distortion (S)** is **0.0010**.
 - The maximum distance (d_{max}) shows the maximal displacement between the atomic positions of the paired atoms. The maximum distance (d_{max}) in this case is: 0.1186 Å
- The <u>arithmetic mean (d_{av})</u> of the distance. In this case, the arithmetic mean (d_{av}) is
 0.0782 Å
- The measure of similarity (Δ) (Bergerhoff *et al.*, 1998) is a function of the differences in atomic positions (weighted by the multiplicities of the sites) and the ratios of the

corresponding lattice parameters of the structures. The measure of similarity (Δ) calculated for this case is **0.016**.