

Electronic Supplementary Information for:

**Lone Pair Electron Effect Induced Differences in Linear and
Nonlinear Optical Properties of Bismuth Borates**

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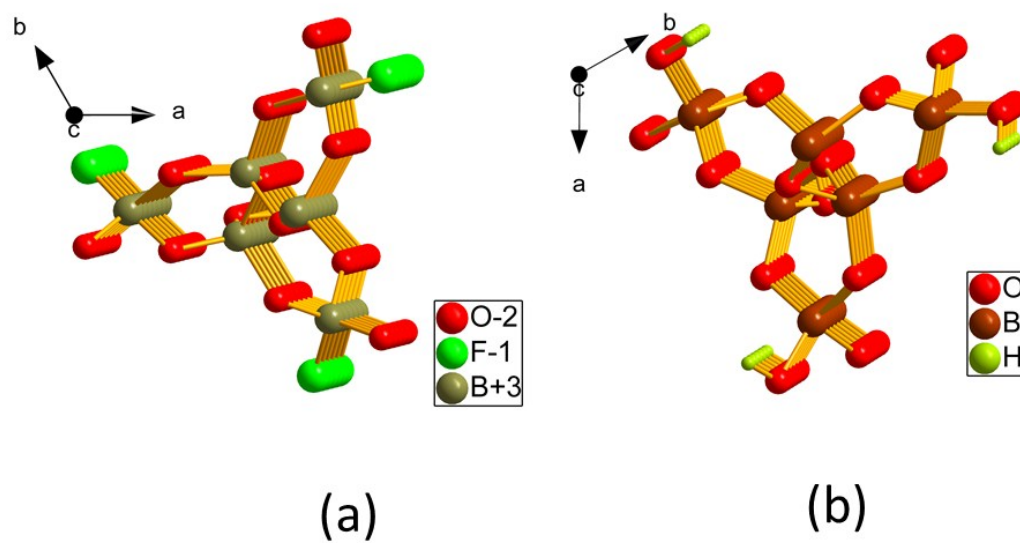


Fig. S1 Anion structure of (a) $\text{BiB}_2\text{O}_4\text{F}$, (b) $\text{BiB}_2\text{O}_4(\text{OH})$

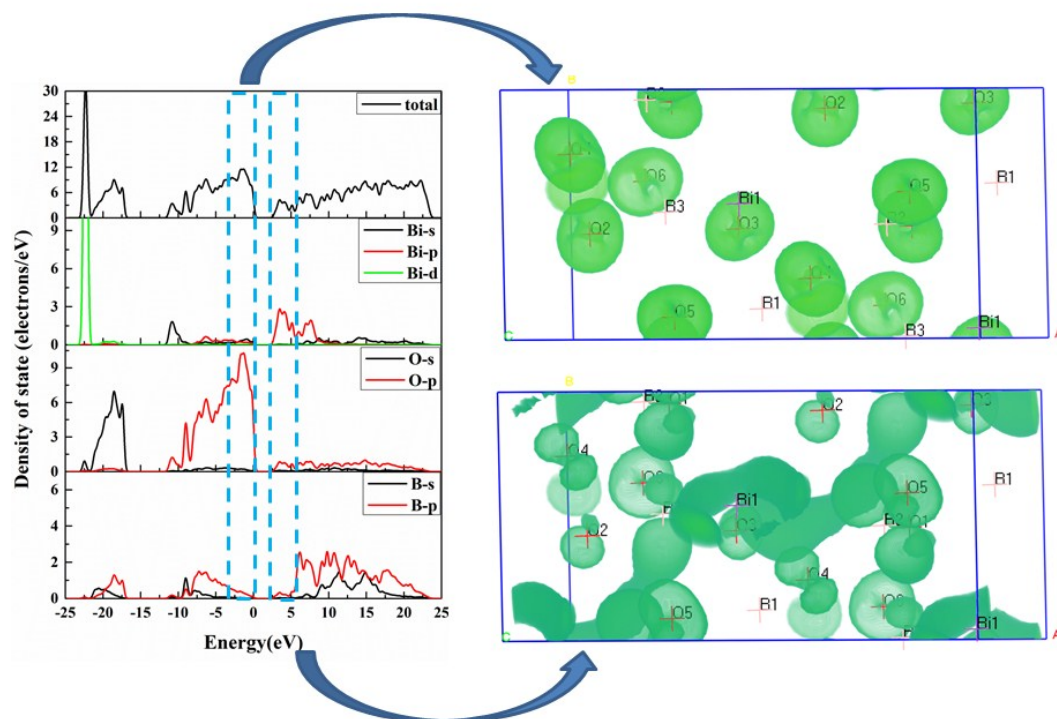


Fig. S2 PDOS/DOS as well as the orbital near the Fermi level of $\alpha\text{-BiB}_3\text{O}_6$

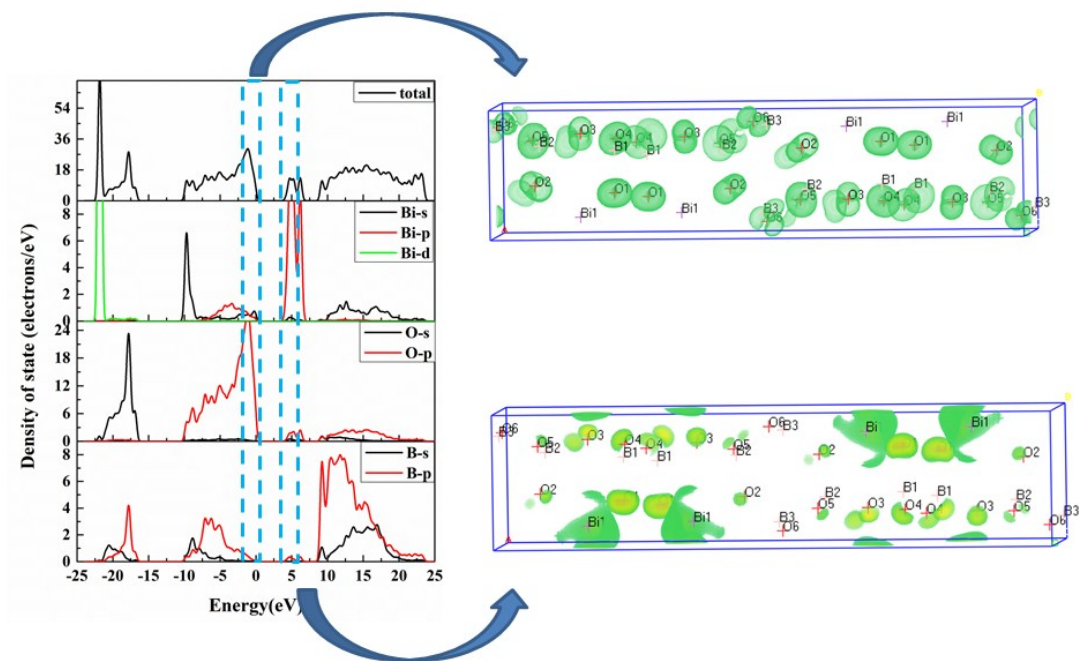


Fig. S3 PDOS/DOS as well as the orbital near the Fermi level of δ -BiB₃O₆

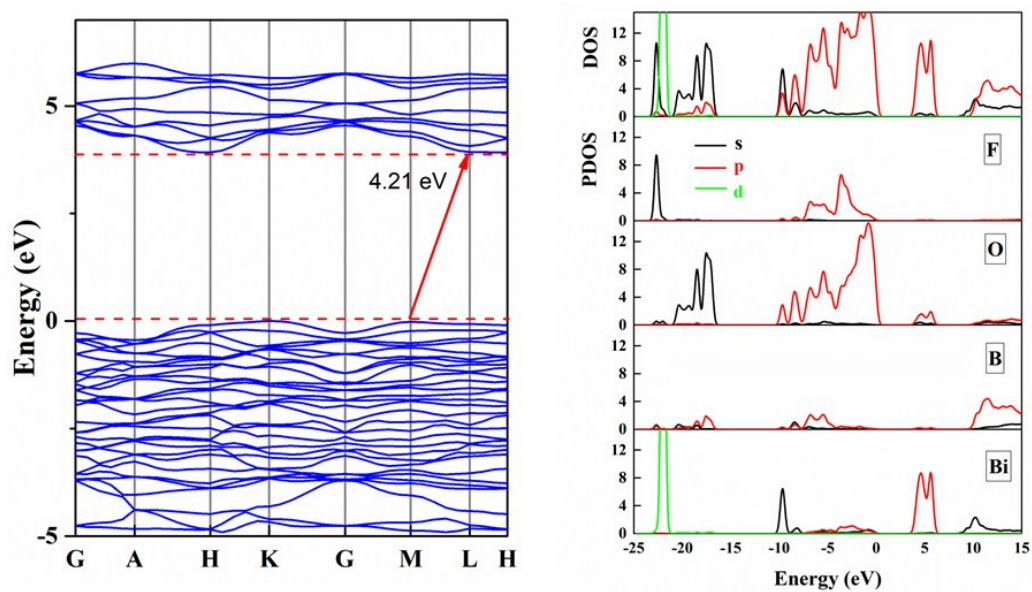


Fig. S4 Electronic band structure and DOS/PDOS of BiB₂O₄F

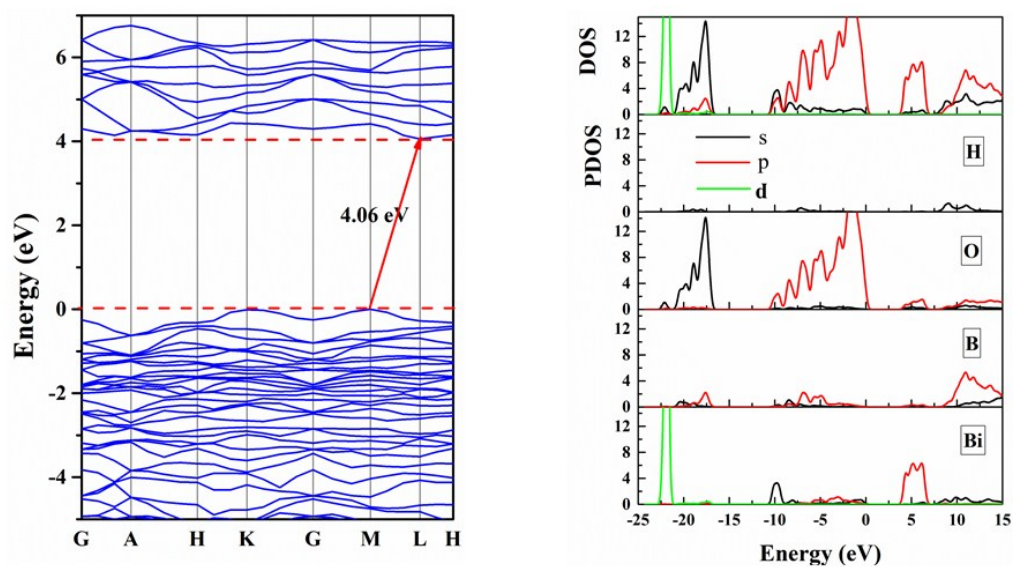


Fig. S5 Electronic band structure and DOS/PDOS of $\text{BiB}_2\text{O}_4(\text{OH})$

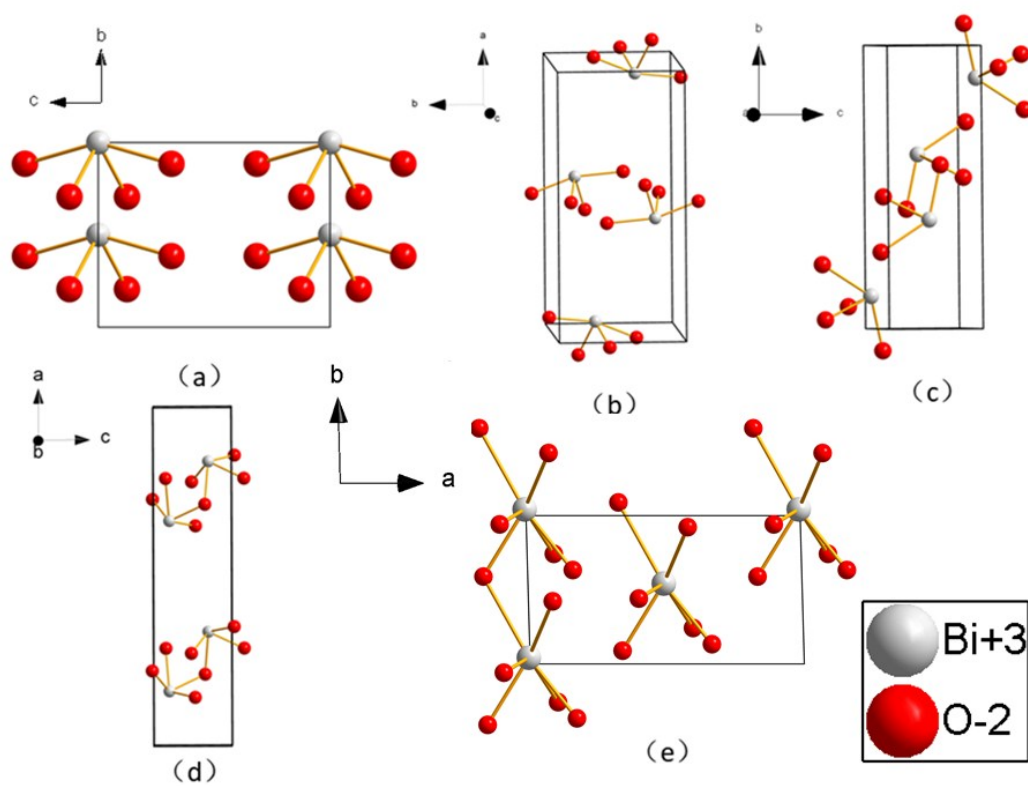


Fig. S6 The arrangement of bismuth oxygen polyhedra (a) $\alpha\text{-BiB}_3\text{O}_6$, (b) $\beta\text{-BiB}_3\text{O}_6$, (c) $\gamma\text{-BiB}_3\text{O}_6$, (d) $\delta\text{-BiB}_3\text{O}_6$, (e) $\epsilon\text{-BiB}_3\text{O}_6$

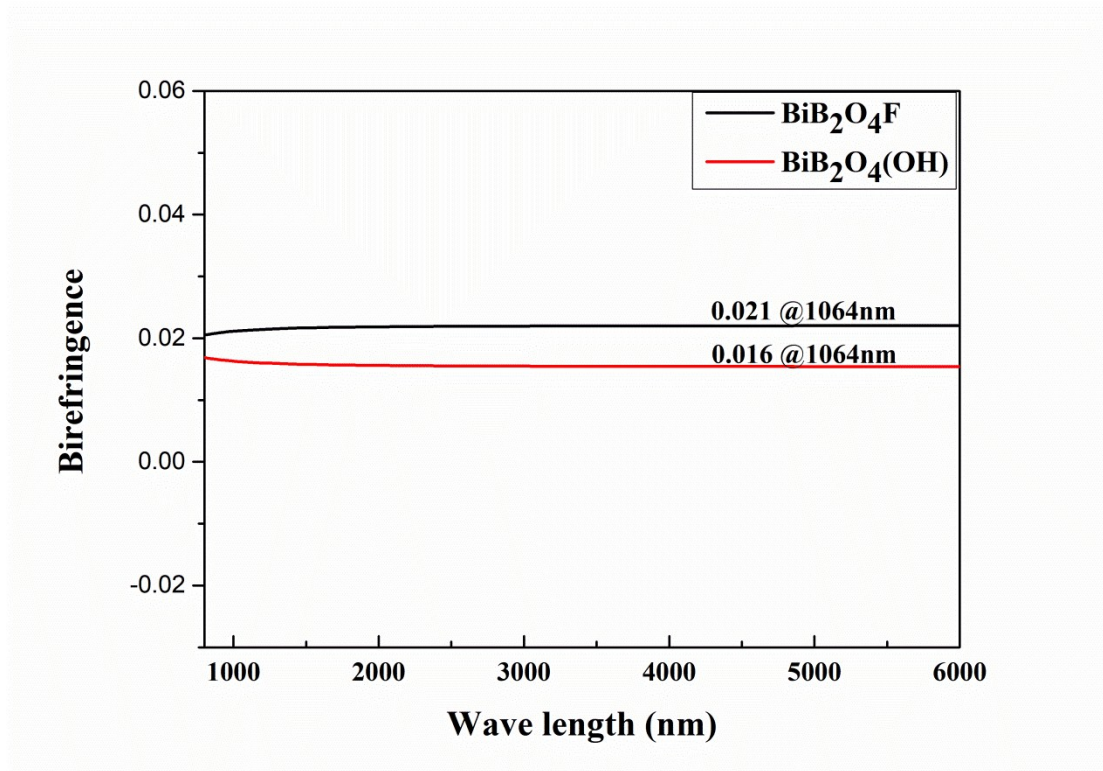


Fig. S7 Birefringence of BiB₂O₄F and BiB₂O₄(OH)

Table S1 Classification of BIBO and BiB₂O₄F and BiB₂O₄(OH) according to the type of B-O structure

compound	α -BiB ₃ O ₆	β -BiB ₃ O ₆	γ -BiB ₃ O ₆	δ -BiB ₃ O ₆	ϵ -BiB ₃ O ₆	BiB ₂ O ₄ F	BiB ₂ O ₄ (OH)
Crystal system	monoclinic	monoclinic	monoclinic	orthorhombic	triclinic	trigonal	trigonal
Space group	C2	P2 ₁ /n	P2 ₁ /n	Pna2 ₁	C1	P3 ₂	P3 ₁
structure of B-O	Layered	Layered	3D	3D	Layered	chain	chain
FBB	B ₃ O ₈	B ₃ O ₈	B ₃ O ₉	B ₃ O ₁₀	B ₃ O ₈	B ₃ O ₈ F	B ₃ O ₉ H
a(Å)	7.116	14.1664	8.4992	18.4480	7.4781	6.7147	6.6221
b(Å)	4.993	6.7514	11.7093	4.4495	3.9340	6.7147	6.6221
b(Å)	6.508	4.4290	4.2596	4.2806	6.2321	6.4688	6.6526

Table S2 Birefringence of calculation and experiment of α -BiB₃O₆ (about 1064nm)

	n ₁	n ₂	n ₃	Δn
Experiment	1.7585	1.7854	1.9190	0.1605
calculation	1.8648	1.8789	2.013	0.1482

Table S3 Range of bond length and bond angle of BO_3 , density of BO_3 in the unit cell, and distance of B atom out of O plane of BO_3 , and dihedral angle of neighbouring BO_3

	Bond length (Å)	Bond angle (°)	Density	Dihedral angle(°)	Distance (Å)
B_2O_3 (α - BiB_3O_6)	1.339-1.411	110.443-128.057	0.01796	89.335	0.044
B_1O_3 (δ - BiB_3O_6)	1.376-1.392	116.793-125.29	0.00966	79.891	0.018
B_2O_3 (ϵ - BiB_3O_6)	1.322-1.478	107.458-140.942	0.02244	47.593	0.011
B_3O_3 (ϵ - BiB_3O_6)	1.340-1.424	110.107-134.198	0.02244	47.593	0.02

Table S4 Calculated value of SHG coefficients of α - BiB_3O_6 crystal as well as the contribution of each group (unit: pm/V)

	d_{16}	d_{14}	d_{22}	d_{23}
Calculated value	-4.37	-1.59	-4.89	-1.53
Only Bi-O polyhedra	-3.15	-1.87	-3.99	-0.85
Only BO_3	-0.49	0.40	-0.54	0.09
Only BO_4	-0.2	0.34	0.13	0.33
Only Bi	-0.5	-0.67	-0.97	-0.57

Table S5 Calculated value of SHG coefficients of δ - BiB_3O_6 crystal as well as the contribution of each group (unit: pm/V)

	d_{15}	d_{24}	d_{33}
Calculated value	-1.16	-0.36	4.53
Only Bi-O polyhedra	-0.22	0.06	3.43
Only BO_4	-0.86	-0.56	1.25
Only Bi	-0.22	-0.24	0.43