

# Supplementary Information: Orientational Phase Behavior of Polymer-Grafted Nanocubes

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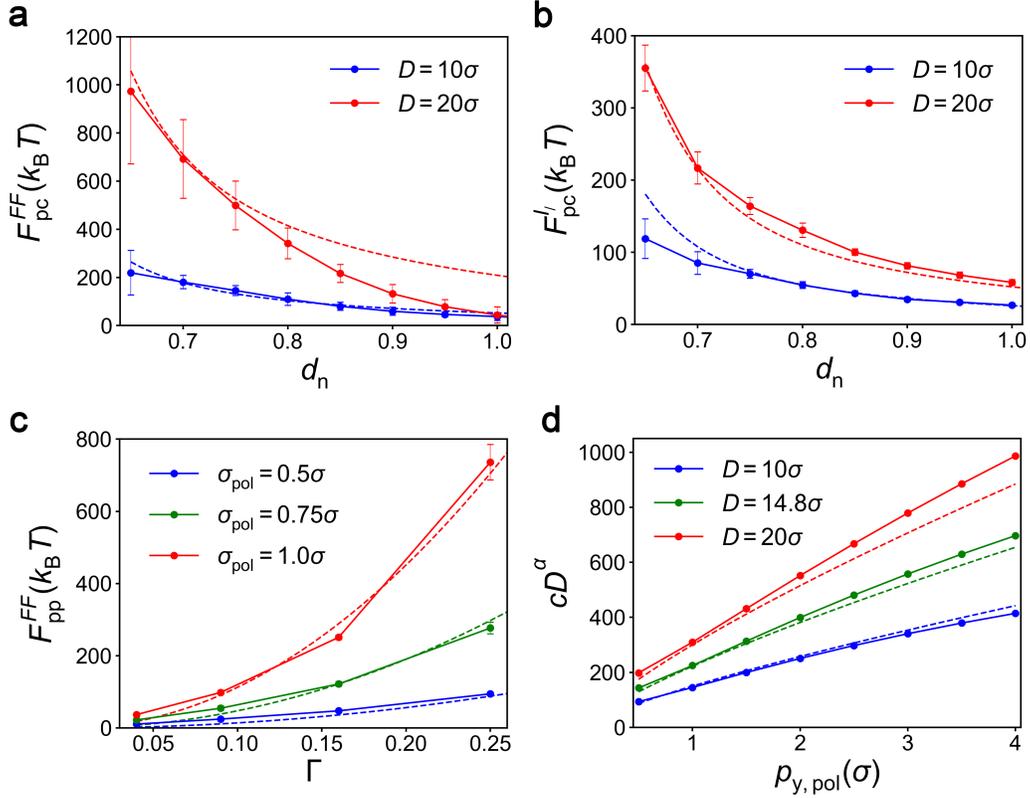


Figure S1: Effect of nanocube size on polymer-surface interaction free energies of the (a)  $FF$  phase, (b)  $I_I$  phase for nanocubes with  $\sigma_{pol} = 0.5\sigma$ ,  $\varepsilon_{pc} = 0.05 k_B T$ , and  $\Gamma = 0.04/\sigma^2$ . (c) Polymer-polymer interaction free energy  $F_{pp}^{FF}$  as a function of grafting density  $\Gamma$  for  $D = 20\sigma$  nanocubes in the terminal region. (d)  $cD^\alpha$  for the  $I_I$  phase when one nanocube contacts the other at its midpoint as a function of  $p_{y,pol}$ , which denotes the location of the most confined grafted segment.  $p_{y,pol}$ , which depends on  $\Gamma$ , was used for obtaining the representative configuration of the  $I_I$  phase. The coefficients  $c$  could be well fitted by the relationship  $c = 15p_{y,pol}^{0.78}$  and  $\alpha = 1$ .

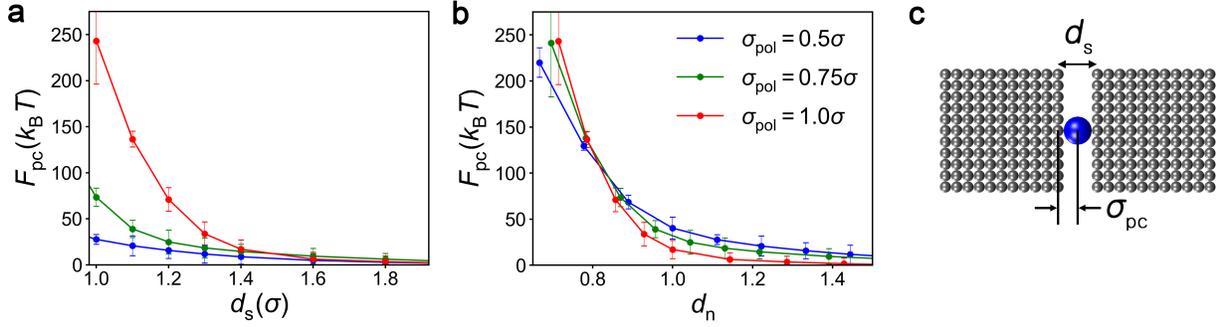


Figure S2: Distance normalization of polymer-cube interactions. Free energy  $F_{pc}$  for  $D = 10\sigma$  nanocubes with  $\Gamma = 0.04/\sigma^2$  and  $\varepsilon_{pc} = 0.05 k_B T$  is plotted with respect to (a) separation distance  $d_s$  and (b) normalized separation distance  $d_n \equiv d_s/2\sigma_{pc}$  for three different values of  $\sigma_{pol}$ . All three free energies curves roughly collapse onto a single curve when plotted with respect to  $d_n$ . (c) Schematic showing the basis for this distance normalization: the distance between the two nanocube faces at which the polymer bead (blue) bridges the two surface without getting squeezed is given by  $2\sigma_{pc} = \sigma_{pol} + \sigma_{cc}$ , where  $\sigma_{cc}$  is the size of the atoms (gray) making up the nanocubes.

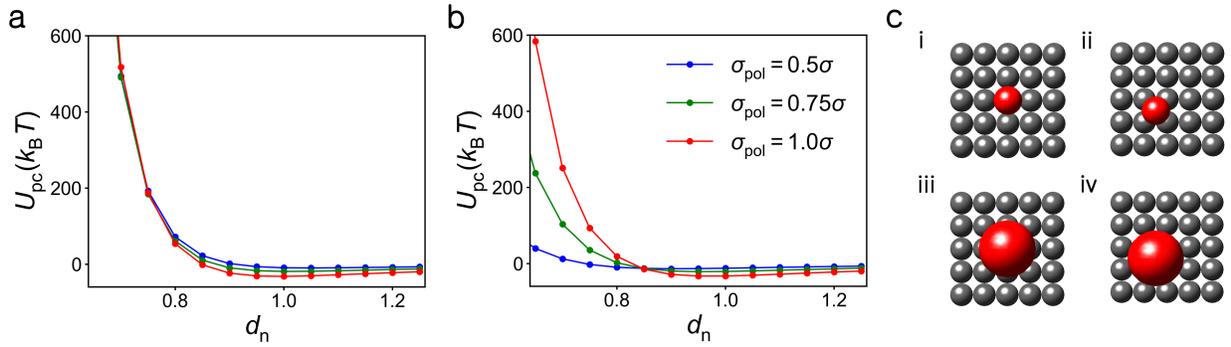


Figure S3: Effect of atomic surface roughness of nanocubes on the polymer-nanocube potential energies  $U_{pc}$ . (a) Potential energy  $U_{pc}$  of a single polymer bead hovering directly above one of the lattice atoms on the surface of the nanocube. This energy, when plotted as a function of normalized distance  $d_n$  of the bead from the surface, is largely independent of the size of the polymer bead  $\sigma_{cc}$ . (b)  $U_{pc}$  of a polymer bead located above the center of the cavity formed between four atoms of a square unit cell on the surface. Significant reduction in  $U_{pc}$  is observed when the polymer bead size becomes smaller than the size of this cavity. (c) Schematics showing a small polymer bead of  $\sigma_{pol} = 0.5\sigma$  (*i* and *ii*) and a large bead of  $\sigma_{pol} = 1.0\sigma$  (*iii* and *iv*) sitting atop (*i* and *iii*) a surface atom or and atop the cavity formed between nanocube lattice atoms (*i* and *iv*).

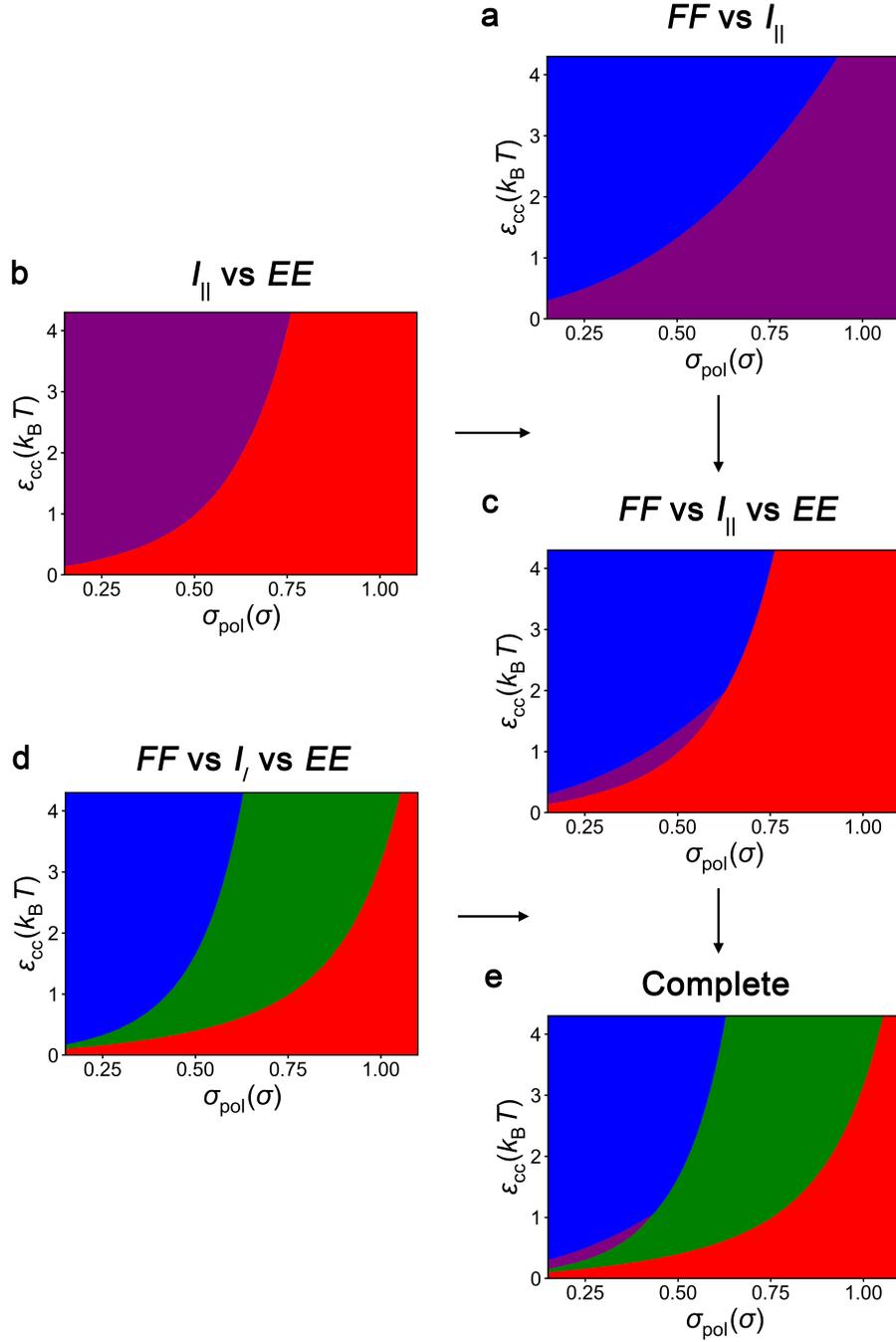


Figure S4: Intermediate phase diagram of nanocubes with  $D = 10\sigma$  and  $\Gamma = 0.16/\sigma^2$  considering only *subsets* of possible phases: (a)  $FF-I_{\parallel}$ , (b)  $I_{\parallel}-EE$ , (c)  $FF-I_{\parallel}-EE$ , and (d)  $FF-I_{\perp}-EE$ . (e) Complete phase diagram considering all four phases.

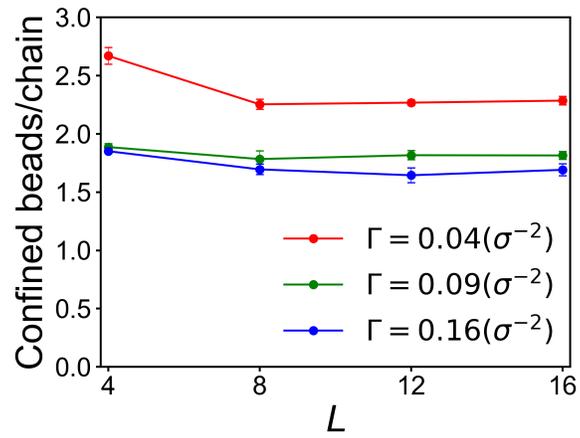


Figure S5: Number of confined beads per polymer chain in the *FF* configuration for  $D = 10\sigma$  nanocubes. Results demonstrate that for the nanocube sizes investigated increasing the chain length does not lead to increased number of confined polymer beads.