# SUPPLEMENTRAY INFORMATION

### Short Period Sinusoidal Thermal Modulation for Quantitative

### **Identification of Gas Species**

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#### **Supplementary Figures**



Fig. S1 Schematic illustration for gas sensing experimental device.



Fig. S2 (a) XRD spectra, (b) Raman spectra, and SEM images of (c)  $CeO_2$  and (d) Au-CeO<sub>2</sub>.



Fig. S3 EDS (point scan) of the pristine and functionalized CeO<sub>2</sub> samples.



**Fig. S4** (a) STEM Ce, O and Au mixed mapping image. (b) Ce, (c) O, (d) Au individual element mapping images of the as-prepared Au-CeO<sub>2</sub>.



Fig. S5 EDS (mapping scan) of Au-CeO<sub>2</sub> sample.



**Fig. S6** The most stable adsorption structure of  $H_2S$  adsorbed on (a) pure ceria and (b) Au doped ceria. Density of states of  $H_2S$  adsorbed on (c) pure ceria and (d) Au doped ceria. (e) The probable mechanism of  $H_2S$  adsorption on the Au doped ceria surface in the presence of air. (Relevant atoms and molecules are represented at the bottom of the Figure.)



**Fig. S7** The most stable adsorption structure of  $SO_2$  adsorbed on (a) pure ceria and (b) Au doped ceria. Density of states of  $SO_2$  adsorbed on (c) pure ceria and (d) Au doped ceria. (e) The probable mechanism of  $SO_2$  adsorption on the Au doped ceria surface in the presence of air. (Relevant atoms and molecules are represented at the bottom of the Figure.)



**Fig. S8** Under DC heating voltage, the response-recovery curves of Au-CeO<sub>2</sub> sensor to various concentrations of (a)  $H_2S$  and (b)  $SO_2$  at 100°C. Experimental results and fitting curves toward (c)  $H_2S$  and (d)  $SO_2$ , respectively.



Fig. S9 (a) The responses of the sensor toward various concentrations of  $H_2S$  in the dynamic sensing experiment. (b) Current and voltage curves applied to the sensor's heating film.



**Fig. S10** During one sinusoidal heating cycle, (a) the corresponding temperature change monitored by the IR camera. (b) The maximum surface temperatures of the sensor at different sampling N.



**Fig. S11** The dynamic curves for sensing 50 ppm (a) H<sub>2</sub>S and (b) SO<sub>2</sub>. (c) Recovery capability of the sensor at different sampling N. (d) Noise assessment of the sensor current curve. The recovery capability of IN curve can be defined by: Recovery<sub>N</sub> =  $\frac{I_{Ng}-I_{Na'}}{I_{Ng}-I_{Na}}$ , where  $I_{Ng}$  represents the saturation sampling current value under the detected gas,  $I_{Na}$  represents the initial sampling current value under the background gas, and  $I_{Na'}$  represents the final sampling current value under the background gas.



Fig. S12 The long-term stability of Au-CeO<sub>2</sub> sensor upon exposure to (a) 50 ppm  $H_2S$  and (b) 50 ppm SO<sub>2</sub>.



**Fig. S13** Derivative curves at different sampling N for (a) test-1, (b) test-2, (c) test-3, (d) test-4.



**Fig. S14** (a) Variation of sensor current for different concentrations of  $H_2S$  and  $SO_2$  (test gases) for four different test cases (i.e., test-5 through test-8). (b) The prejudgements of the possible gases deduced by  $\tau_m$ . The verifications of the prejudgements by using radar charts of (c)  $H_2S$  and (d)  $SO_2$ .



**Fig. S15** The variation of sensor current for sensing (a)  $NO_2$  and (c)  $NH_3$  with various concentrations. (b), (d) The variation of sensor current toward unknown test gases (test- $n1\sim n6$ ) with different concentrations.



Fig. S16 (a) The pre-judgements of the possible gases deduced by  $\tau_m$ . The verifications of the pre-judgements by using radar charts of (b) NO<sub>2</sub> and (c) NH<sub>3</sub>.

# Supplementary Tables

Table S1 The adsorption energy, the nearest distance,	, charge transfer and work function
modification of H <sub>2</sub> S adsorbed on both substrates	

System	$E_{ads}/eV$	dgas-ceria/Å	Q/e	$\Delta \Phi/eV$	
H <sub>2</sub> S/ceria	-0.424	(H_O)2.021	0.0025	-0.199	
H <sub>2</sub> S/Au-ceria	-2.175	(S_Au)2.253	0.2126	-0.564	

modification of 502 adsorbed on both substrates						
System	E <sub>ads</sub> /eV	dgas-ceria/Å	Q/e	$\Delta \Phi/eV$		
SO <sub>2</sub> /ceria	-1.216	(O_Ce)2.490	0.3355	-0.371		
SO <sub>2</sub> /Au-ceria	-2.783	(S_O)1.610	0.4676	0.194		

**Table S2** The adsorption energy, the nearest distance, charge transfer and work functionmodification of  $SO_2$  adsorbed on both substrates

Table S3 The relationship between  $\tau_N$  and the H<sub>2</sub>S concentration at different sampling N

- (-)	Concentration					
tn (S)	5 ppm	10 ppm	20 ppm	30 ppm	40 ppm	50 ppm
τ4	75.32	62.126	48.554	46.152	44.868	43.44
τ5	76.5	63.407	49.12	45.521	44.618	44.598
τ6	77.262	63.703	49.698	45.11	44.076	42.78
τ7	78.218	58.577	47.994	43.656	43.243	41.179
τ8	83.913	56.311	49.323	44.1	41.326	39.575
τ <sub>m</sub>	78.2426	60.8248	48.9378	44.9078	43.6262	42.3144

Table S4 The relationship between  $\tau_N$  and the SO<sub>2</sub> concentration at different sampling N

- (-)	Concentration					
τn (S)	50 ppm	60 ppm	70 ppm	80 ppm	90 ppm	100 ppm
τ4	67.52	48.291	46.856	46.063	45.86	48.716
τ5	61.494	47.643	47.5	46.4102	46.19	44.826
τ6	58.577	50.731	49.11	48.343	47.45	45.085
τ7	55.474	47.76	47.065	48.641	45.86	44.604
τ8	55.569	50.291	49.45	45.62	45.233	42.9
$ au_{\mathrm{m}}$	59.7268	48.9432	47.9962	47.01544	46.1186	45.2262

Test	Pre-judgement	Identification	True value	Error (%)	
n1	93ppm NO <sub>2</sub>	93ppm NO <sub>2</sub>	90ppm NO <sub>2</sub>	3.33	
	72ppm NO <sub>2</sub>				
n2	26ppm H <sub>2</sub> S	72ppm NO <sub>2</sub>	70ppm NO <sub>2</sub>	2.86	
	87ppm SO <sub>2</sub>				
n3	23ppm NO <sub>2</sub>	23ppm NO <sub>2</sub>	20ppm NO <sub>2</sub>	15.00	
n4	43ppm NO <sub>2</sub>		85ppm NH <sub>3</sub>	2.35	
	83ppm NH <sub>3</sub>	83ppm NH <sub>3</sub>			
	8ppm H <sub>2</sub> S				
n5	40ppm NO <sub>2</sub>				
	68ppm NH <sub>3</sub>	68ppm NH <sub>3</sub>	65ppm NH <sub>3</sub>	4.62	
	7ppm H <sub>2</sub> S				
n6	32ppm NO <sub>2</sub>	20	25	12.00	
	28ppm NH <sub>3</sub>	28ppm NH <sub>3</sub>	25ppm NH <sub>3</sub>		

**Table S5** Summary of identification results (test n1~n6).

#### Supplementary Texts

Under the action of sinusoidal heating voltage, the response value of the sensor is defined as follows:

$$S_{sine} = I_{Ng\_max} / I_{Na\_min}$$
(S1)

where  $I_{Na\_min}$  is the minimum value of  $I_N$  curves in the background gas, and  $I_{Ng\_max}$  is the maximum value of  $I_N$  curves in the detected gas.

For evaluating the detection limits (DL) of the sensor toward H<sub>2</sub>S, the noise formula is given as follows:

$$S_{DL} = (1 + 3 * Noise_6) * \frac{M_6}{M_1}$$
 (S2)

where  $M_6$  is the mean of the  $I_N$  curve at sampling sixth in air, and  $M_1$  is the mean of the  $I_N$  curve at sampling first in air. Noise<sub>6</sub> is calculated to 0.202% as shown in Table 1 of main manuscript.

The adsoption energy ( $E_{ads}$ ), basically used to characterize the adsorption intensity, is defined as <sup>1</sup>:

$$E_{ads} = E_{molecule/substrate} - E_{molecule} - E_{substrate}$$
(S3)

where  $E_{molecule/substrate}$ ,  $E_{molecule}$  and  $E_{substrate}$  represent the energies of the substrate with the gas molecule, isolated gas molecule, and the substrate, respectively. By this definition, a negative adsorption energy mean that the adsorption was exothermic, and higher negative values correspond to stronger adsorptions.

The modification of work function energy of the substrate with and without the gas molecule adsorbed was also an important indicator of adsorption. The definition of work function energy is <sup>2</sup>:

$$\Phi = E_{\text{vacuum}} - E_{\text{Fermi}} \tag{S4}$$

in which,  $E_{\text{vacuum}}$  and  $E_{\text{Fermi}}$  refer to vacuum energy and Fermi energy respectively.

**Fig. S7**a and E<sub>ads</sub> of SO<sub>2</sub> adsorbed on ceria (111) listed in Table S2 show that SO<sub>2</sub> is chemically adsorbed on pure ceria surface, with 0.3355 electrons transferring to the substrate. While, the interaction between SO<sub>2</sub> and Au-ceria (111) was stronger for the larger adsorption energy and charge transfer value (**Fig. S7**b). Besides, the peak of the 2p orbital near Fermi level of SO<sub>2</sub> in plot of DOS (**Fig. S7**c) indicates a tight interaction occurring between SO<sub>2</sub> and ceria (111) surface. Similar to the adsorption of H<sub>2</sub>S, the Fermi level of TDOS in **Fig. S7**d is upshifted compared with that in Fig. S4c, which indicates greater electron transfer from gas molecules to substrate when SO<sub>2</sub> molecules interacted with the Au-ceria (111) surface. **Fig. S7**e is a possible adsorption mechanism of SO<sub>2</sub> on the Au-ceria (111) surface in the presence of air (oxygen).

To prove the broad application of this two-steps judgement process, we have supplemented experiments for quantitatively detecting  $NO_2$  and  $NH_3$  with concentrations ranging from 20ppm to 100ppm, respectively. Experimental conditions are consistent with those described in the manuscript. Firstly, the recognition library is established based on the known gas concentrations (100ppm, 80ppm, 50ppm, 20ppm). Fig. S15a and S15c presents the variation of sensor current for sensing  $NO_2$  and  $NH_3$  with various concentrations.

Similarly, the  $\tau_m$  values of Au-CeO<sub>2</sub> sensor for NO<sub>2</sub> and NH<sub>3</sub> detection are respectively given in **Fig. S16**a, it's obvious that there are obvious differences between these two curves. Extracting S<sub>N</sub> by sampling from the sampling fourth (N=4) to the sampling eighth (N=8), we can develop an envelope by sequentially connecting every S<sub>N</sub> at a fixed gas concentration, and then a radar chart is constituted by a series of envelopes at various concentrations, as shown in **Fig. S16**b and **S16**c. With this, the dependence of  $\tau_m$  on gas concentration and the radar chart, together constitute the gas recognition library, which could be used to quantitatively identify NO<sub>2</sub> and NH<sub>3</sub>.

To evaluate the accuracy of recognition library, we have also measured a series of sensor current curves when exposed to test gases (test n1~n6), as presented in Fig. S15b and S15d. Then, we use the library to discriminate the concentration of unknown gas via a two-step judgment. Take test-n2 and test-n5 as examples, the reliability of library is evaluated. For test-n2,  $\tau_m$  is 45.36s and it is evident that the test gas is ~72 ppm NO<sub>2</sub>, ~26ppm H<sub>2</sub>S or ~87ppm SO<sub>2</sub>. As shown in **Fig. S16**b, the green envelope for test-n2 is between 50ppm and 80 ppm NO<sub>2</sub>, and it's very closed to 80ppm. Conversely, it doesn't match with the H<sub>2</sub>S envelopes in Fig. 4c or the SO<sub>2</sub> envelopes in Fig. 4d. Therefore, test-n2 can be identified as ~72ppm NO<sub>2</sub>, ~68ppm NH<sub>3</sub>, or ~7ppm H<sub>2</sub>S. Then, NO<sub>2</sub>, NH<sub>3</sub> and H<sub>2</sub>S radar charts are analyzed to verify the pre-judgements of test-n5. In **Fig. S16**c, we can find that the green envelope is located between 50ppm and 80ppm NH<sub>3</sub>, yet it can't be matched with the NO<sub>2</sub> envelopes in **Fig. S16**b or the H<sub>2</sub>S envelopes in Fig. 4c. So, test-n5 is detected as ~68ppm NH<sub>3</sub>, which is relatively consistent with the actual concentration (65ppm NH<sub>3</sub>).

We have summarized the identification results of test-n1 through test-n6 in **Table S5**. It is evident that the gas recognition library can be used to discriminate  $NO_2$  and  $NH_3$  in a facile manner and the maximum recognition error is less than 15%. Therefore, the supplemented experiments have verified that the short period sinusoidal thermal modulation strategy has ability to be broad application for quantitatively detecting sorts of gases.

## **Supplementary References**

- 1 J. Zhang, X. Q. Gong and G. Z. Lu, *Chinese J. Catal.*, 2014, **35**, 1305-1317.
- 2 D. W. Wang, X. H. Wang, A. J. Yang and P. Lv, *Mater. Chem. Phys.*, 2018, **212**, 453-460.