## Supplementary material

# 3.3 nm-sized $\mathrm{TiO}_{2} /$ carbon hybrid spheres endowed with pseudocapacitance-dominated superhigh-rate Li-ion and Na-ion storages <br> Hao Luo, Yuxi Chen,* Jing Huang, Zhanglong Chen, Xiaohong Xia, Jin Li, Hongbo Liu 

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## Supporting Notes

1. Calculation of electrical conductivity: 10 measurements of the electrical resistivity $\rho(\Omega \mathrm{cm})$ of 3.3-TO/C have been conducted, and the values are depicted in the following table. The electrical conductivity $\sigma\left(\mathrm{S} \mathrm{cm}^{-1}\right)$ is calculated based on the following equation,

$$
\sigma=1 / \rho .
$$

The reported $\sigma$ is an average of 8 values except the largest and the lowest ones. The standard division is given.

| $1^{\text {st }}$ | $2^{\text {nd }}$ | $3^{\text {rd }}$ | $4^{\text {th }}$ | $5^{\text {th }}$ | $6^{\text {th }}$ | $7^{\text {th }}$ | $8^{\text {th }}$ | $9^{\text {th }}$ | $10^{\text {th }}$ |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| 72.01 | 85.98 | 75.05 | 79.26 | 69.25 | 78.22 | 71.67 | 73.51 | 70.06 | 78.52 |

## 2. Determination of intersection potential of the domain I and the domain II:

The mathematically smoothed $C_{d}$ data in a potential range of 0.01 to $0.12 \mathrm{~V}\left(v s \mathrm{Li} / \mathrm{Li}^{+}\right)$ have been linearly fitted as fitting line 1 (Figure a in the following image), i.e.,

$$
\begin{equation*}
y 1=2016.3-7600.5 x . \tag{1}
\end{equation*}
$$

The coefficient of determination $\mathrm{R}^{2}$ is 0.99 . Fitting line 2 is derived from the smoothed $C_{d}$ data in a potential range of 0.41 to 0.50 V (Figure b), i.e.,

$$
\begin{equation*}
y 2=824.5-383.1 x . \tag{2}
\end{equation*}
$$

The coefficient of determination $\mathrm{R}^{2}$ is 0.98 . The intersection potential thus can be determined by the solution of Equations (1) and (2), i.e.,

$$
x=0.17 \mathrm{~V} .
$$


3. Calculation of average voltage $V_{a}$ : The calculation is based on the voltage profiles of $3.3-\mathrm{TO} / \mathrm{C}$ at 2 C (Figure 4e). The energy $E$ is a product of electric charge $Q$ and voltage $V$, i.e.,

$$
\begin{equation*}
E=Q V . \tag{3}
\end{equation*}
$$

Thus for a given voltage profile, $E$ is an integration of $V$ in a full scale of $Q$, i.e.,

$$
\begin{equation*}
E=\int_{0}^{Q} V d Q=\int_{0}^{C} 3.6 V d C . \tag{4}
\end{equation*}
$$

The average voltage $V_{a}$ is defined as

$$
\begin{equation*}
V_{a}=\frac{E}{Q}=\frac{\int_{0}^{C} 3.6 V d C}{3.6 C}=\frac{\int_{0}^{C} V d C}{C} . \tag{5}
\end{equation*}
$$

## Supporting Figures



Fig. S1. XRD patterns of 3.3-TO/C and 17/5.3-TO.


Fig. S2. Pseudocapacitive performance of 17/5.3-TO for Li-ion storage. (a) CV curves at various scanning rates. (b) Plots and linear fittings of logarithmic peak current as a function of logarithmic scanning rate of the anodic and the cathodic CV peaks. (c) CV profile and pseudocapacitance contribution represented by the red slashed area at $0.5 \mathrm{mV} \mathrm{s}^{-1}$. (d) Variation of the pseudocapacitance contribution with an increase of the CV scanning rate.


Fig. S3. Pseudocapacitive performance of 3.3-TO/C for Na-ion storage. (a) CV curves at various scanning rates. (b) Plots and linear fittings of logarithmic peak current as a function of logarithmic scanning rate of the anodic and the cathodic CV peaks. (c) CV profile and pseudocapacitance contribution represented by the red slashed area at 5 $\mathrm{mV} \mathrm{s}^{-1}$. (d) Variation of the pseudocapacitance contribution with an increase of the CV scanning rate.


Fig. S4. Microstructures of 3.3-TO/C and 17/5.3-TO after 600 discharge/charge
cycles of Li-ion stroage. (a) TEM and (b) HREM of 3.3-TO/C. (c) TEM and (d) HREM images of 17/5.3-TO.


Fig. S5. Microstructure and element distributions of 3.3-TO/C after 500
discharge/charge cycles for Na -ion stroage. (a) TEM and (b) HAADF image of 3.3TO/C. Element mappings of (c) sodium, (d) titanium, (e) oxygen and (f) carbon.

