# Theoretical Study on the Electronic Structure and Second-Order Nonlinear <br> Optical Properties of Benzannulated or Selenophene-annulated Expanded 

Li-jing Gong, ${ }^{*, a, \ddagger}$ Chun-yu Liu, ${ }^{\text {b }} \ddagger$ Cheng Ma, ${ }^{a}$ Wan-feng Lin, ${ }^{\text {a }}$ Jin-kai Lv, ${ }^{\text {a }}$ and Xiang-yu Zhanga ${ }^{a}$ Aviation University of Air Force, Changchun 130022, China<br>${ }^{b}$ Institute of Functional Material Chemistry, National \& Local United Engineering Lab for Power Battery, Faculty of Chemistry, Northeast Normal University, Changchun, 130024 Jilin, China

## Contents

Index Page

1. The selected bond lengths for helicene $\mathbf{H} \mathbf{1}$ between experiment and calculation ..... S2
2. Contour plots of the HOMO and LUMO for the studied helicenes $\mathbf{H} 2-\mathrm{H} 4, \mathbf{H} 6-\mathrm{H} 9, \mathrm{H} 11, \mathrm{H} 16-\mathrm{H} \mathbf{1 8}$ and $\mathbf{H} 20-\mathrm{H} 23$, and $\mathbf{H} 25$ ..... S4
3. The computed main energy absorption band using the different basis sets level for helicene $\mathbf{H} 1$ ..... S4
4. The computed main energy absorption band using the different functionals for helicene H1 ..... S4
5. Electron density difference maps of helicenes $\mathbf{H} 2-\mathrm{H} 9, \mathbf{H} 11-\mathrm{H} 14, \mathbf{H} \mathbf{1 6}-\mathrm{H} 23$ and $\mathrm{H} 25-\mathrm{H} 28$ ..... S5
6. The calculated $B_{\text {HRS }}$ values ( $\times 10^{-30}$ esu) of helicenes $\mathbf{H 1}-\mathbf{H} 28$ by using four DFT functionals. ..... S6

Table S1. The selected bond lengths for helicene $\mathbf{H 1}$ between experiment and calculation.


Optimized geometry of helicene $\mathbf{H 1}$ (not show hydrogens)

| Bond | B3LYP | Experiment | Difference |
| :---: | :---: | :---: | :---: |
| $\mathbf{1}$ | 1.399 | 1.405 | 0.006 |
| $\mathbf{2}$ | 1.384 | 1.390 | -0.006 |
| $\mathbf{3}$ | 1.411 | 1.425 | -0.014 |
| $\mathbf{4}$ | 1.420 | 1.417 | 0.003 |
| $\mathbf{5}$ | 1.469 | 1.487 | -0.018 |
| $\mathbf{6}$ | 1.427 | 1.420 | 0.007 |
| $\mathbf{7}$ | 1.468 | 1.463 | 0.005 |
| $\mathbf{8}$ | 1.397 | 1.396 | 0.001 |
| $\mathbf{9}$ | 1.400 | 1.397 | 0.003 |
| $\mathbf{1 0}$ | 1.429 | 1.426 | 0.003 |
| $\mathbf{1 1}$ | 1.398 | 1.396 | 0.002 |
| $\mathbf{1 2}$ | 1.400 | 1.378 | 0.002 |
| $\mathbf{1 3}$ | 1.434 | 1.434 | 0.000 |
| $\mathbf{1 4}$ | 1.365 | 1.365 | 0.000 |
| $\mathbf{1 5}$ | 1.439 | 1.424 | 0.015 |
| $\mathbf{1 6}$ | 1.425 | 1.408 | 0.017 |
| $\mathbf{1 7}$ | 1.462 | 1.456 | 0.006 |
|  |  |  | 2 |


| 18 | 1.398 | 1.405 | -0.007 |
| :---: | :---: | :---: | :---: |
| 19 | 1.396 | 1.385 | 0.011 |
| 20 | 1.427 | 1.431 | -0.004 |
| 21 | 1.399 | 1.379 | 0.020 |
| 22 | 1.400 | 1.410 | -0.010 |
| 23 | 1.471 | 1.476 | -0.005 |
| 24 | 1.419 | 1.416 | 0.003 |
| 25 | 1.473 | 1.472 | 0.001 |
| 26 | 1.440 | 1.442 | -0.002 |
| 27 | 1.473 | 1.471 | 0.002 |
| 28 | 1.390 | 1.389 | 0.001 |
| 29 | 1.408 | 1.422 | 0.014 |
| 30 | 1.431 | 1.416 | 0.015 |
| 31 | 1.408 | 1.402 | 0.006 |
| 32 | 1.391 | 1.378 | 0.013 |
| 33 | 1.423 | 1.419 | 0.004 |
| 34 | 1.374 | 1.363 | 0.011 |
| 35 | 1.420 | 1.404 | 0.016 |
| 36 | 1.374 | 1.374 | 0.000 |
| 37 | 1.423 | 1.430 | -0.007 |
| 38 | 1.392 | 1.384 | 0.008 |
| 39 | 1.360 | 1.393 | -0.033 |
| 40 | 1.410 | 1.419 | -0.009 |
| 41 | 1.385 | 1.396 | -0.011 |
| 42 | 1.399 | 1.404 | -0.005 |
| 43 | 1.385 | 1.398 | -0.013 |
| 44 | 1.410 | 1.414 | -0.004 |

Note: the difference is equal to calculation value minus experimental value


Fig. S1. Contour plots of the HOMO and LUMO for the studied helicenes $\mathrm{H} 2-\mathrm{H} 4, \mathrm{H} 6-\mathrm{H} 9, \mathrm{H} 11, \mathrm{H} 16-\mathrm{H} 18$ and $\mathrm{H} 20-\mathrm{H} 23$, and H 25 .

Table S2. The computed main energy absorption band ( $\lambda, \mathrm{nm}$ ) using the B3LYP functional at the different basis sets level for helicene

H1.

| Basis set | $6-31 \mathrm{G}(\mathrm{d})$ | $6-31 \mathrm{G}(\mathrm{d}, \mathrm{p})$ | $6-31+\mathrm{G}(\mathrm{d})$ | $6-311+\mathrm{G}(\mathrm{d})$ |
| :---: | :---: | :---: | :---: | :---: |
| $\lambda$ | 311.90 | 312.22 | 318.21 | 319.91 |

Table S3. The computed main energy absorption band $(\lambda, \mathrm{nm})$ using the different functionals at 6-31+G(d) basis set level for helicene H1.

| Functional | B3LYP | M06-2X | CAM-B3LYP | BH\&HLYP |
| :---: | :---: | :---: | :---: | :---: |
| $\lambda$ | 318.21 | 301.10 | 300.13 | 298.83 |



Fig. S2. Electron density difference maps of helicenes $\mathbf{H} \mathbf{2}-\mathbf{H} 9, \mathbf{H 1 1}-\mathbf{H} 14, \mathbf{H} 16-\mathrm{H} \mathbf{2 3}$ and $\mathbf{H} \mathbf{2 5}-\mathbf{H} \mathbf{2 8}$. Blue and purple colours indicate depletion and accumulation of electron density, respectively.

Table S4. The calculated $B_{\text {HRS }}$ values $\left(\times 10^{-30}\right.$ esu) of helicenes $\mathbf{H 1}-\mathrm{H} 14$ by using four DFT functionals associated with the $6-31+G(d)$ basis set and the calculated $B_{\text {HRS }}$ values ( $\times 10^{-30} \mathrm{esu}$ ) of the helicenes $\mathbf{H 1 5 - H 2 8}$ by using four DFT functionals associated with the 6 $31+G(d)$ for $\mathrm{O}, \mathrm{N}, \mathrm{C}$ and H atoms and LANL2DZ basis set for Se atom.

| Compound | B3LYP | CAM-B3LYP | M06-2X | BH\&HLYP |
| :---: | :---: | :---: | :---: | :---: |
| H1 | 7.67 | 5.26 | 5.52 | 4.97 |
| H2 | 17.61 | 10.57 | 11.26 | 10.36 |
| H3 | 7.87 | 4.86 | 5.18 | 4.80 |
| H4 | 6.55 | 5.02 | 5.28 | 4.83 |
| H5 | 14.99 | 9.41 | 10.07 | 9.93 |
| H6 | 7.03 | 5.59 | 6.06 | 5.48 |
| H7 | 15.93 | 8.39 | 7.77 | 9.12 |
| H8 | 22.67 | 11.04 | 10.31 | 10.71 |
| H9 | 16.08 | 9.70 | 10.19 | 9.64 |
| H10 | 62.78 | 28.88 | 28.66 | 31.46 |
| H11 | 24.64 | 14.11 | 14.34 | 14.47 |
| H12 | 16.28 | 10.16 | 10.99 | 10.05 |
| H13 | 46.40 | 22.23 | 23.74 | 24.03 |
| H14 | 50.51 | 18.21 | 19.26 | 19.65 |
| H15 | 8.79 | 5.89 | 6.10 | 5.58 |
| H16 | 14.72 | 8.50 | 8.84 | 8.46 |
| H17 | 8.93 | 5.79 | 6.23 | 5.74 |
| H18 | 7.78 | 5.72 | 5.78 | 5.44 |
| H19 | 16.14 | 10.11 | 10.72 | 10.82 |
| H2O | 8.84 | 5.90 | 6.27 | 5.87 |
| H21 | 15.30 | 7.89 | 8.13 | 8.28 |
| H22 | 17.31 | 7.96 | 7.47 | 7.58 |
| H23 | 12.43 | 7.82 | 8.30 | 7.54 |
| H24 | 65.19 | 29.95 | 29.80 | 32.47 |
| H25 | 25.35 | 15.10 | 15.52 | 15.17 |


| H26 | 13.54 | 8.30 | 8.63 | 8.67 |
| ---: | ---: | ---: | ---: | ---: |
| H27 | 52.45 | 26.10 | 27.31 | 27.62 |
| H28 | 38.33 | 15.29 | 16.21 | 16.28 |

