

# First molecular electronic hyperpolarizability of series of $\pi$ -conjugated oxazole dyes in solution: an experimental and theoretical study

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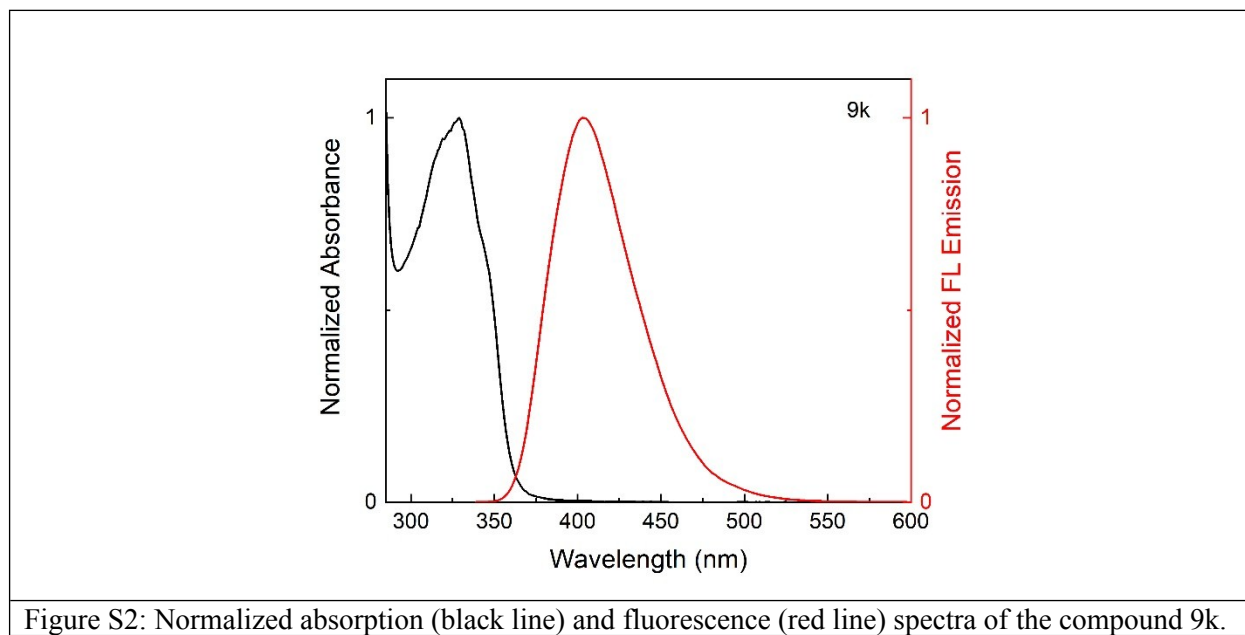
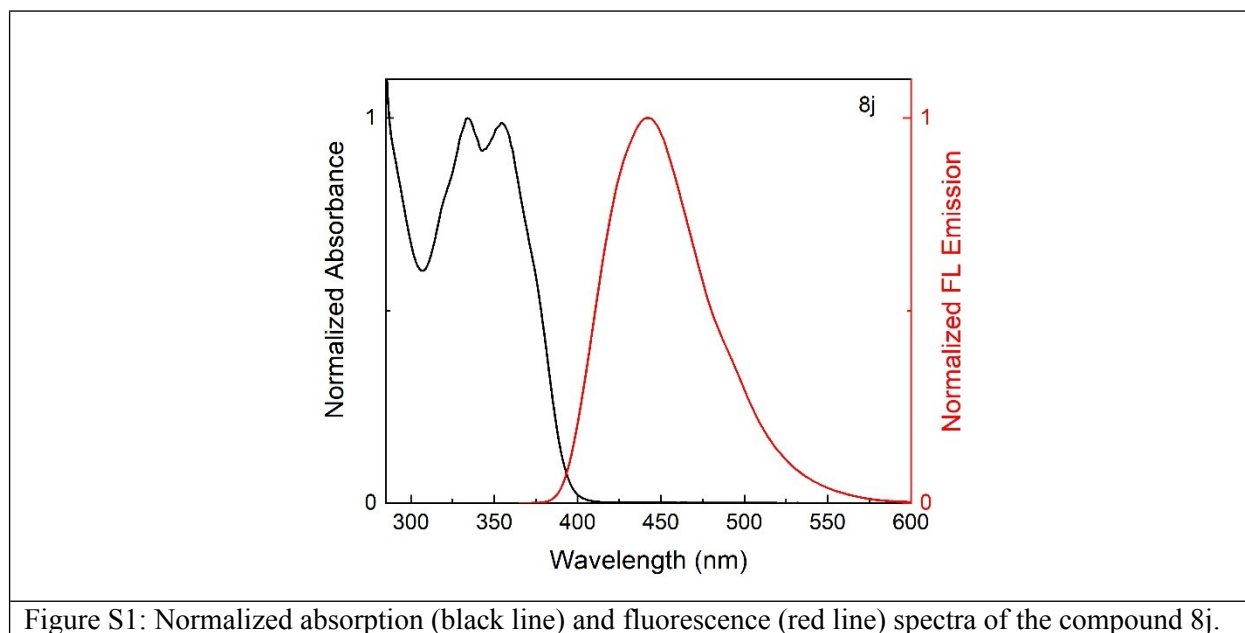
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## Supplementary Information

## Absorption e emission spectra



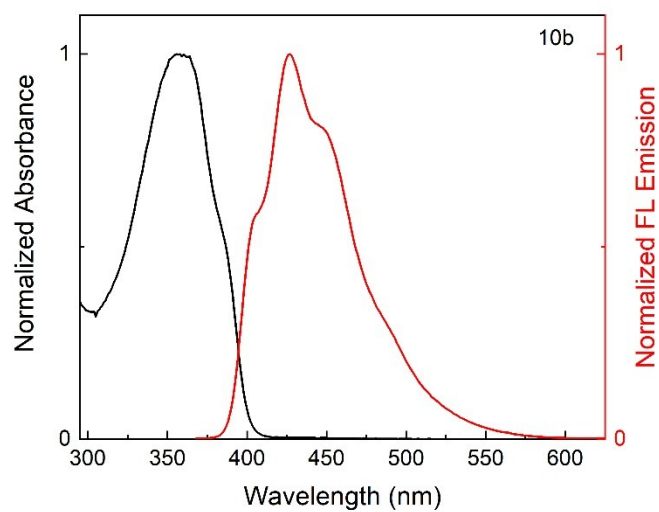


Figure S3: Normalized absorption (black line) and fluorescence (red line) spectra of the compound 10b.

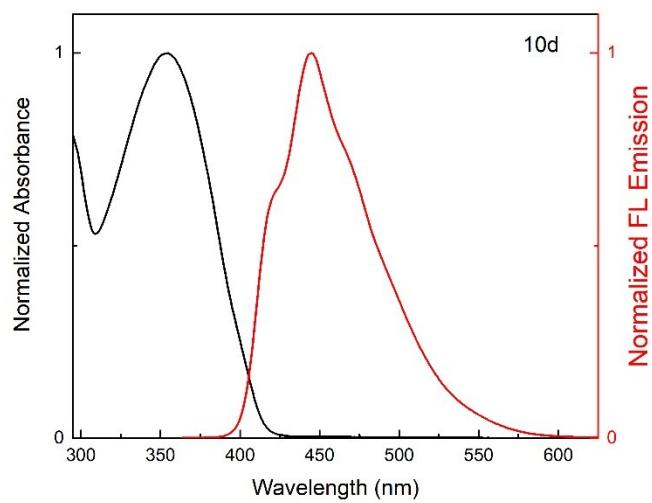


Figure S4: Normalized absorption (black line) and fluorescence (red line) spectra of the compound 10d.

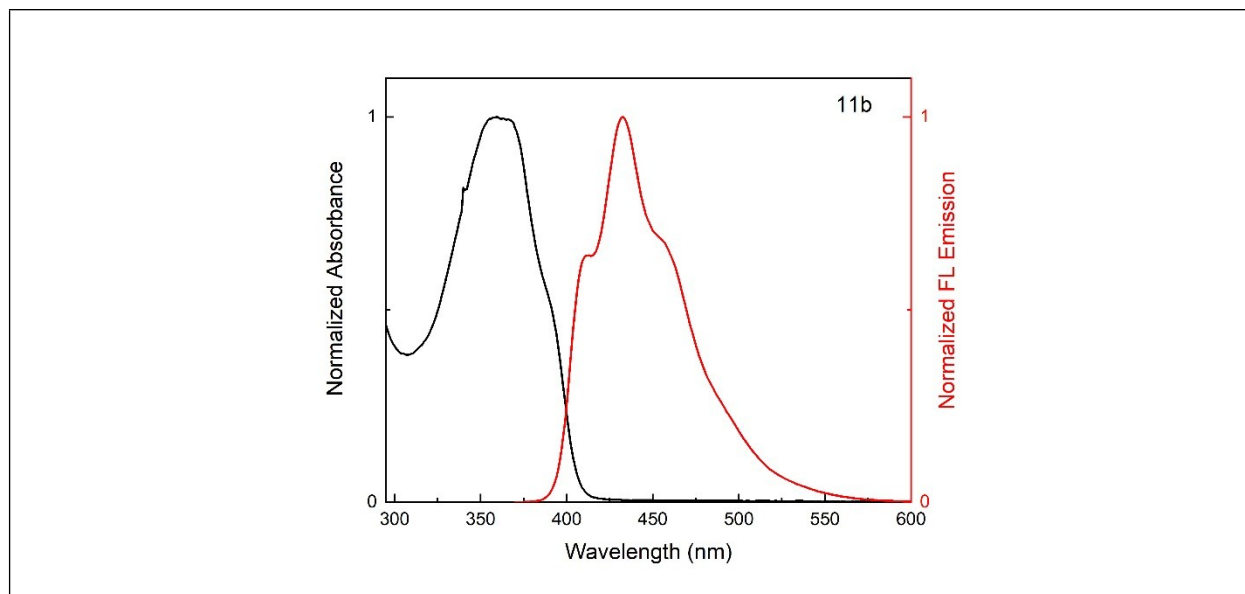


Figure S5: Normalized absorption (black line) and fluorescence (red line) spectra of the compound 11b.

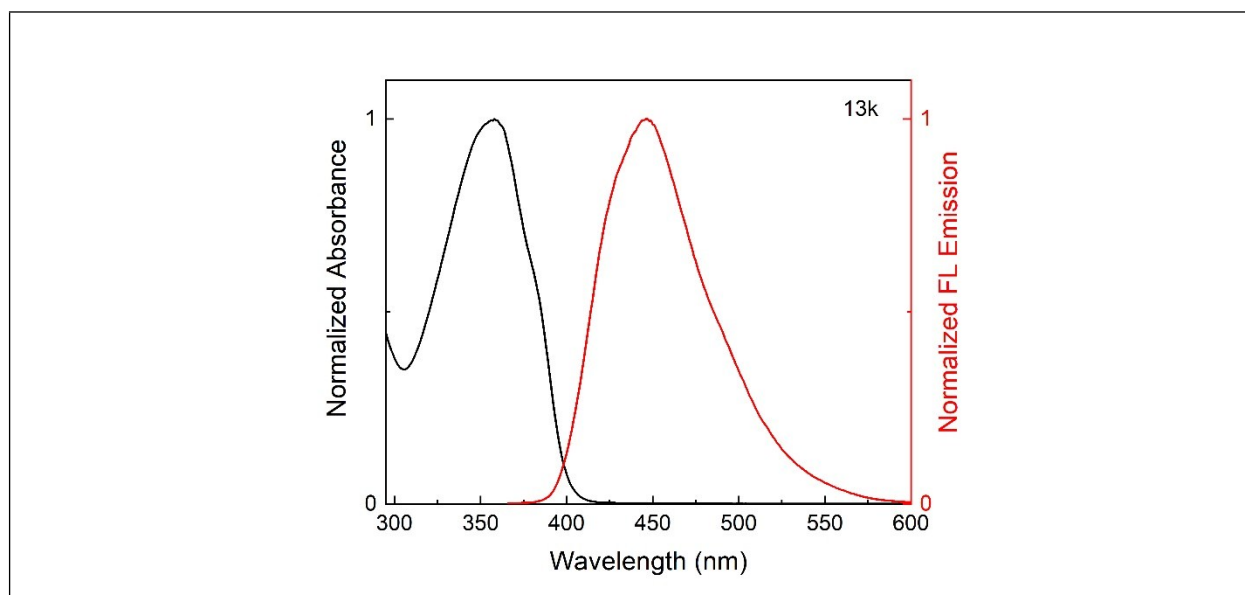


Figure S6: Normalized absorption (black line) and fluorescence (red line) spectra of the compound 13k.

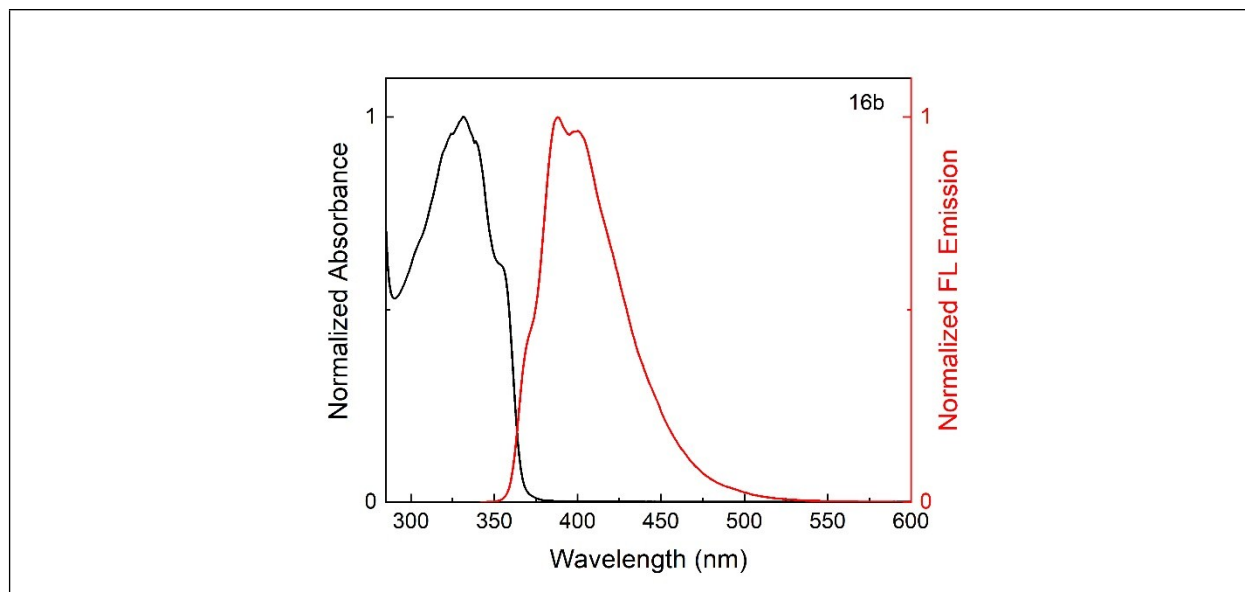


Figure S7: Normalized absorption (black line) and fluorescence (red line) spectra of the compound 16b.

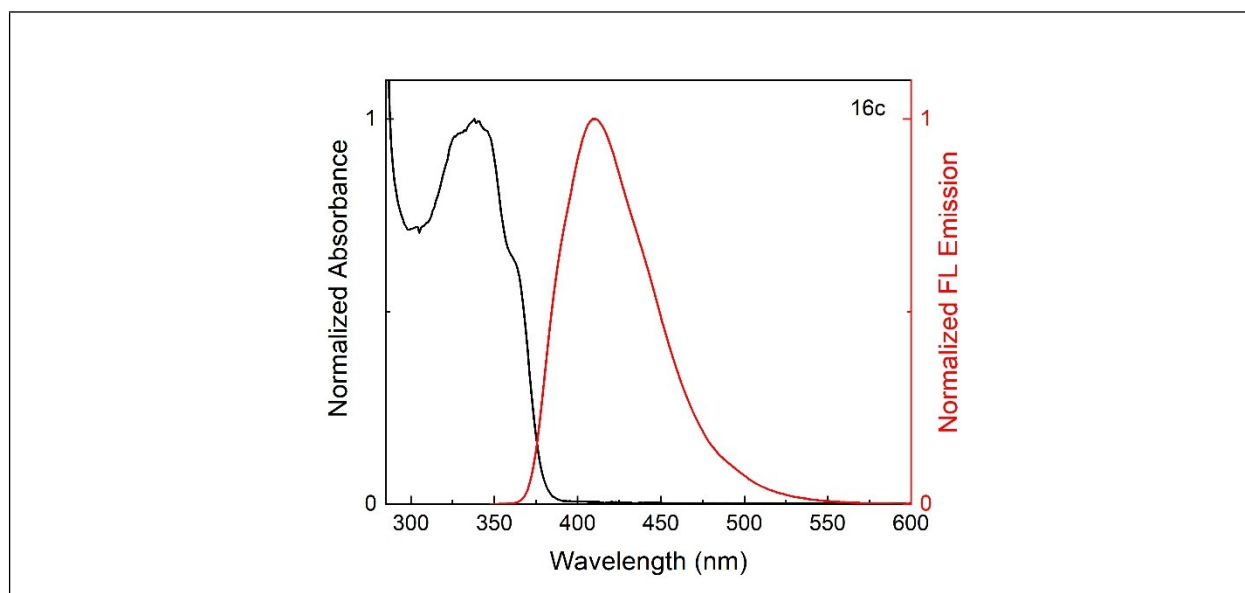


Figure S8: Normalized absorption (black line) and fluorescence (red line) spectra of the compound 16c.

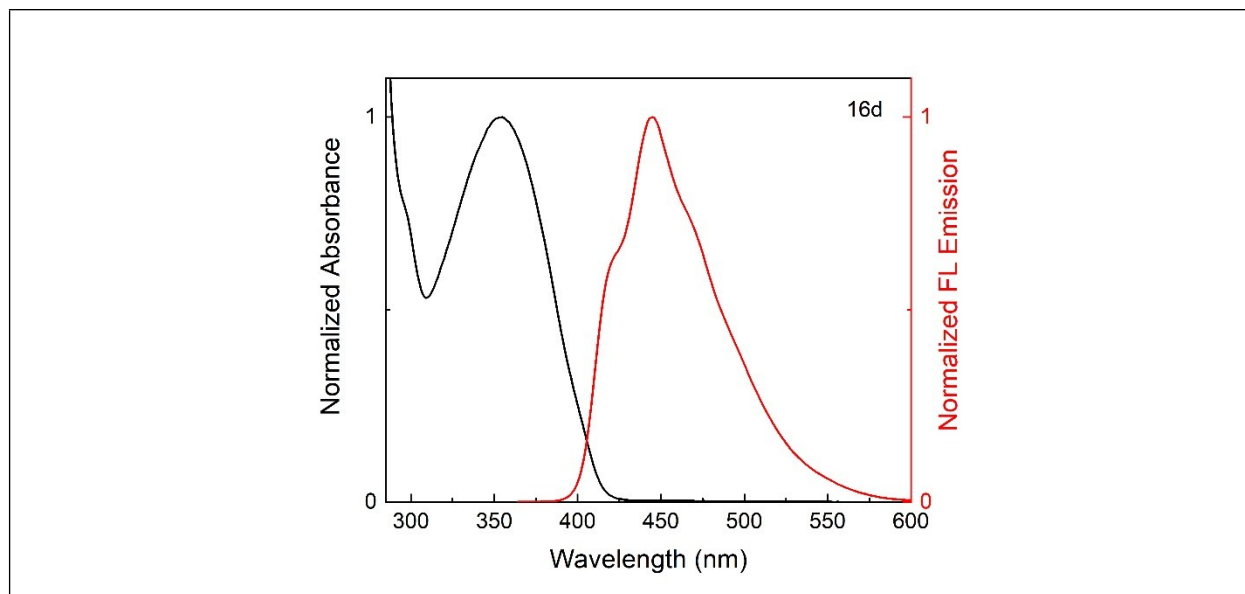


Figure S9: Normalized absorption (black line) and fluorescence (red line) spectra of the compound 16d.

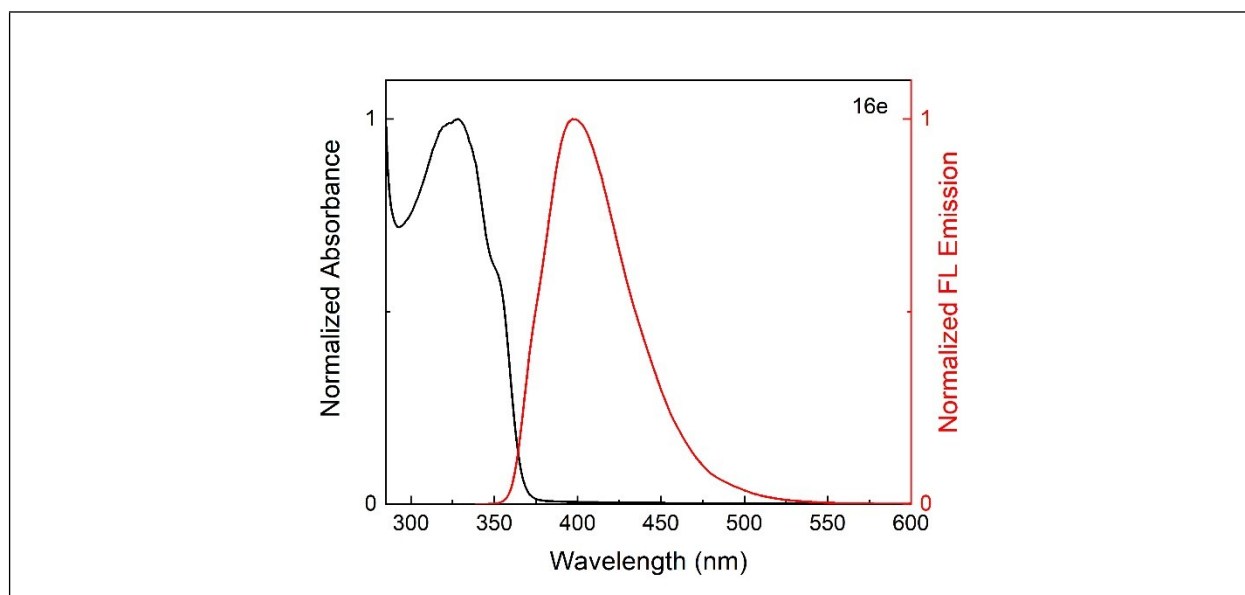


Figure S10: Normalized absorption (black line) and fluorescence (red line) spectra of the compound 16e.

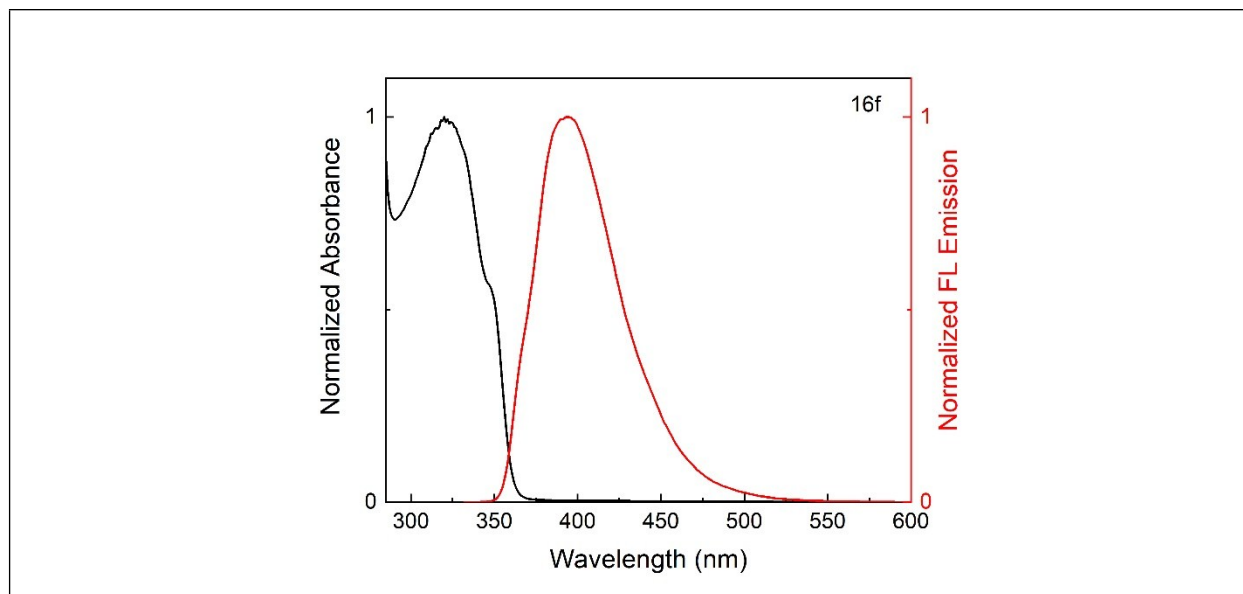


Figure S11: Normalized absorption (black line) and fluorescence (red line) spectra of the compound 16f.

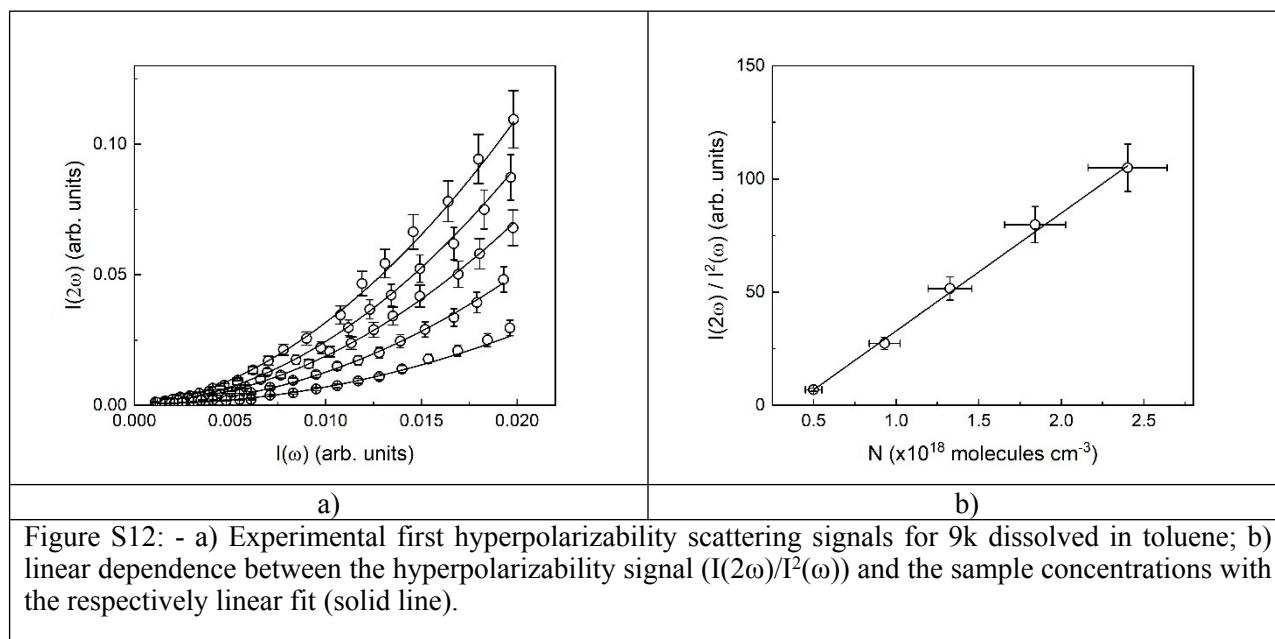
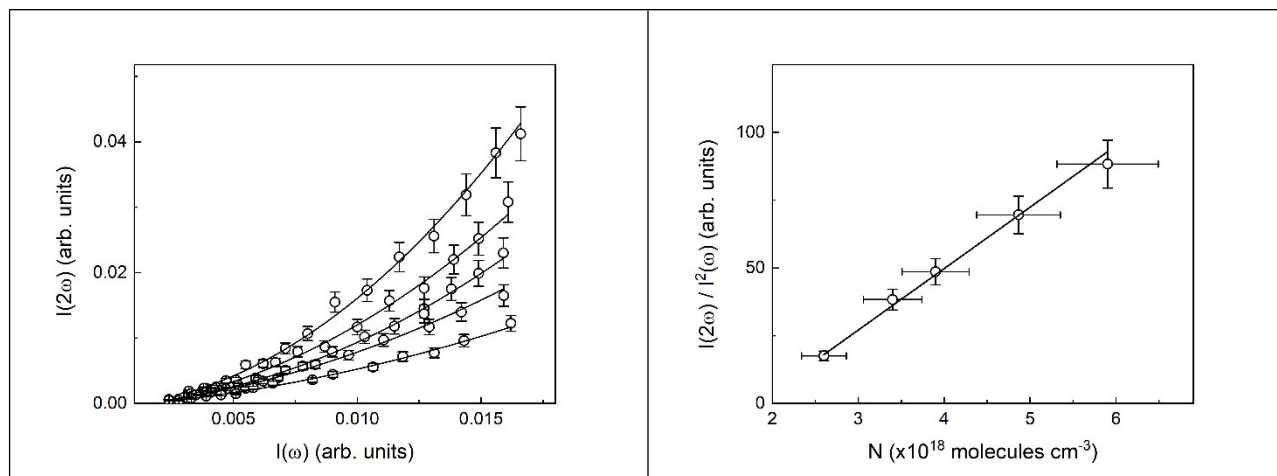


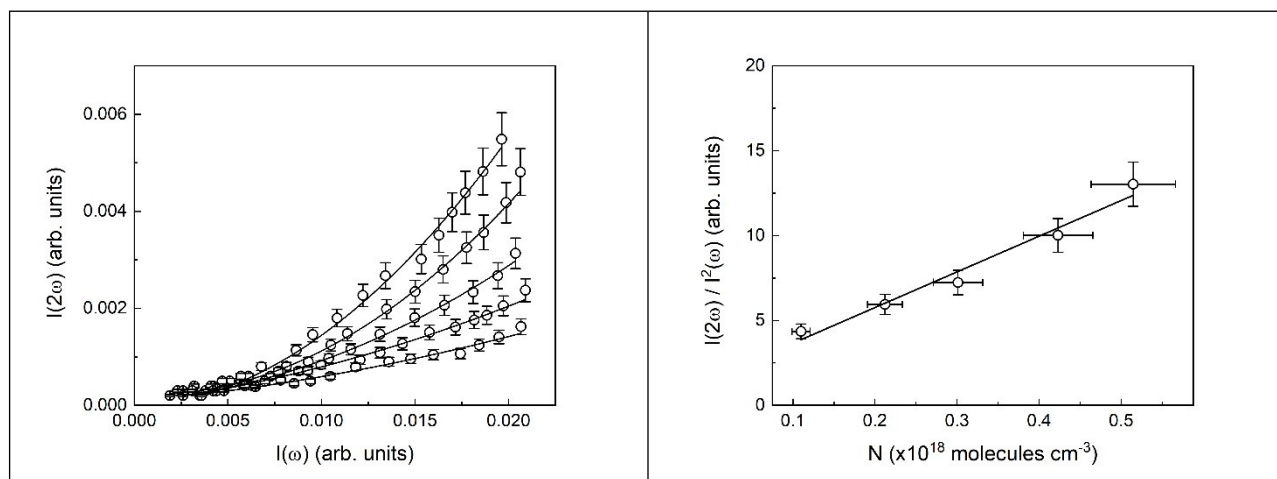
Figure S12: - a) Experimental first hyperpolarizability scattering signals for 9k dissolved in toluene; b) linear dependence between the hyperpolarizability signal ( $I(2\omega)/I^2(\omega)$ ) and the sample concentrations with the respectively linear fit (solid line).



a)

b)

Figure S13: - a) Experimental first hyperpolarizability scattering signals for 10b dissolved in toluene; b) linear dependence between the hyperpolarizability signal ( $I(2\omega)/I^2(\omega)$ ) and the sample concentrations with the respectively linear fit (solid line).

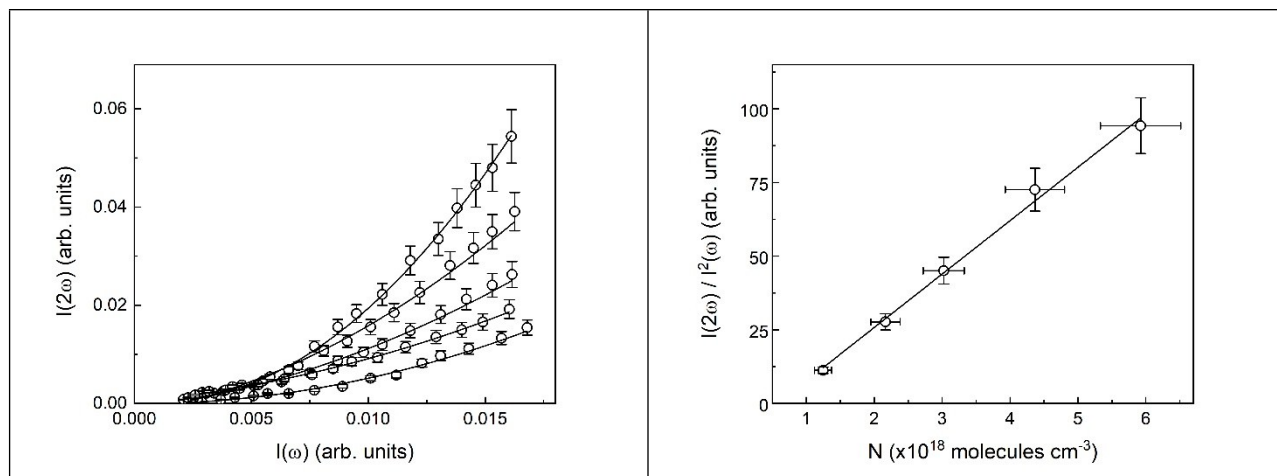


a)

b)

Figure S14: - a) Experimental first hyperpolarizability scattering signals for 10d dissolved in toluene; b) linear dependence between the hyperpolarizability signal ( $I(2\omega)/I^2(\omega)$ ) and the sample concentrations with the respectively linear fit (solid line).

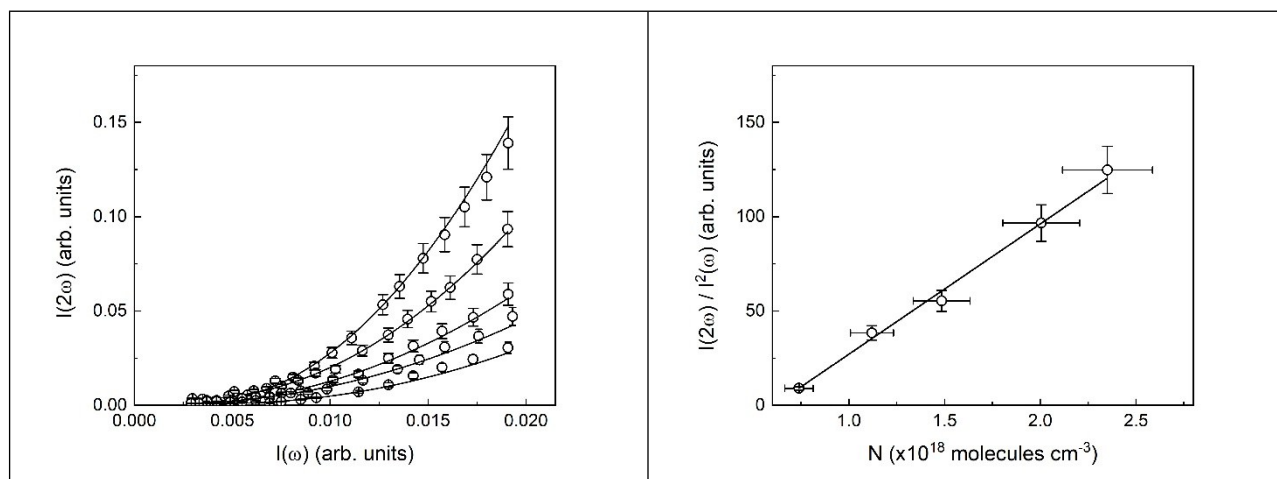




a)

b)

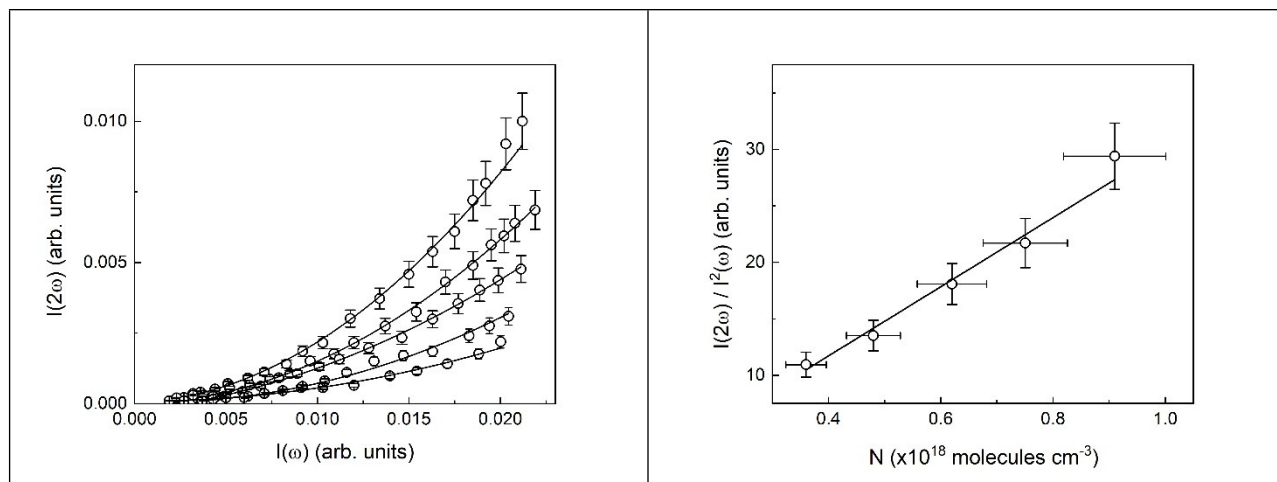
Figure S15: - a) Experimental first hyperpolarizability scattering signals for 11b dissolved in toluene; b) linear dependence between the hyperpolarizability signal ( $I(2\omega)/I^2(\omega)$ ) and the sample concentrations with the respectively linear fit (solid line).



a)

b)

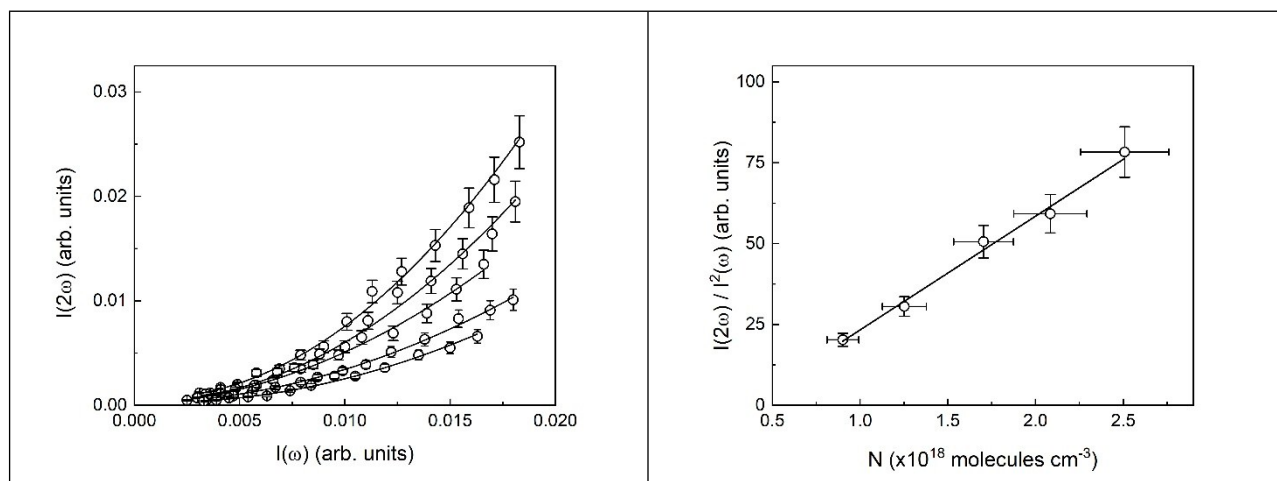
Figure S16: - a) Experimental first hyperpolarizability scattering signals for 13k dissolved in toluene; b) linear dependence between the hyperpolarizability signal ( $I(2\omega)/I^2(\omega)$ ) and the sample concentrations with the respectively linear fit (solid line).



a)

b)

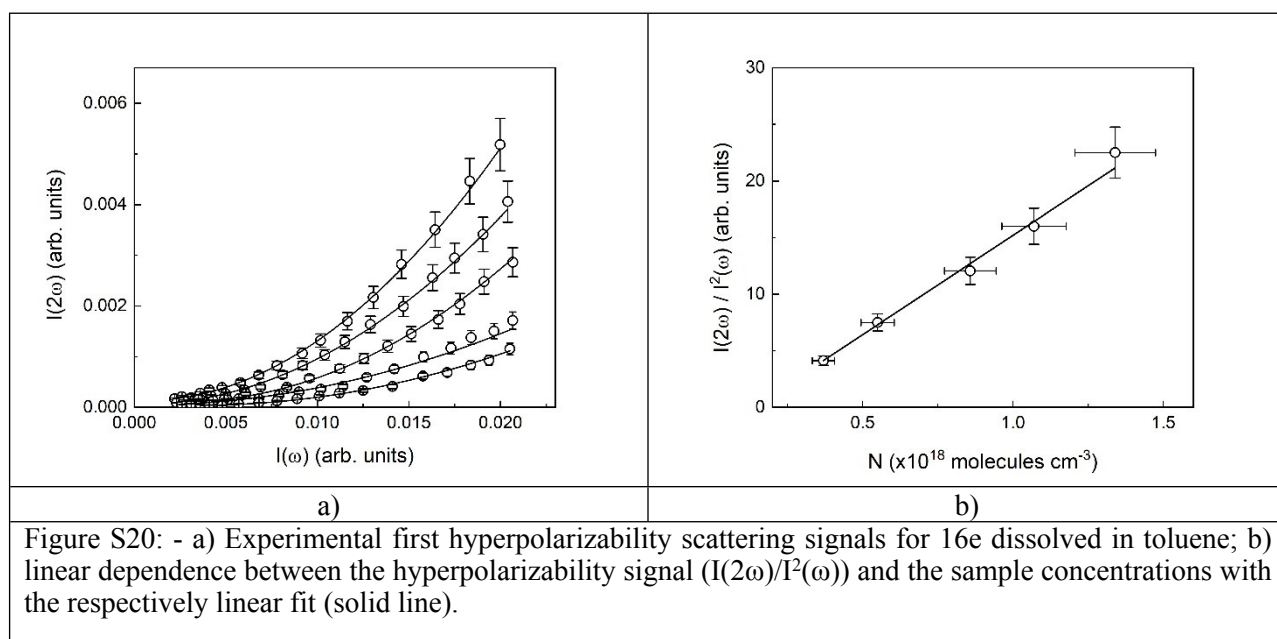
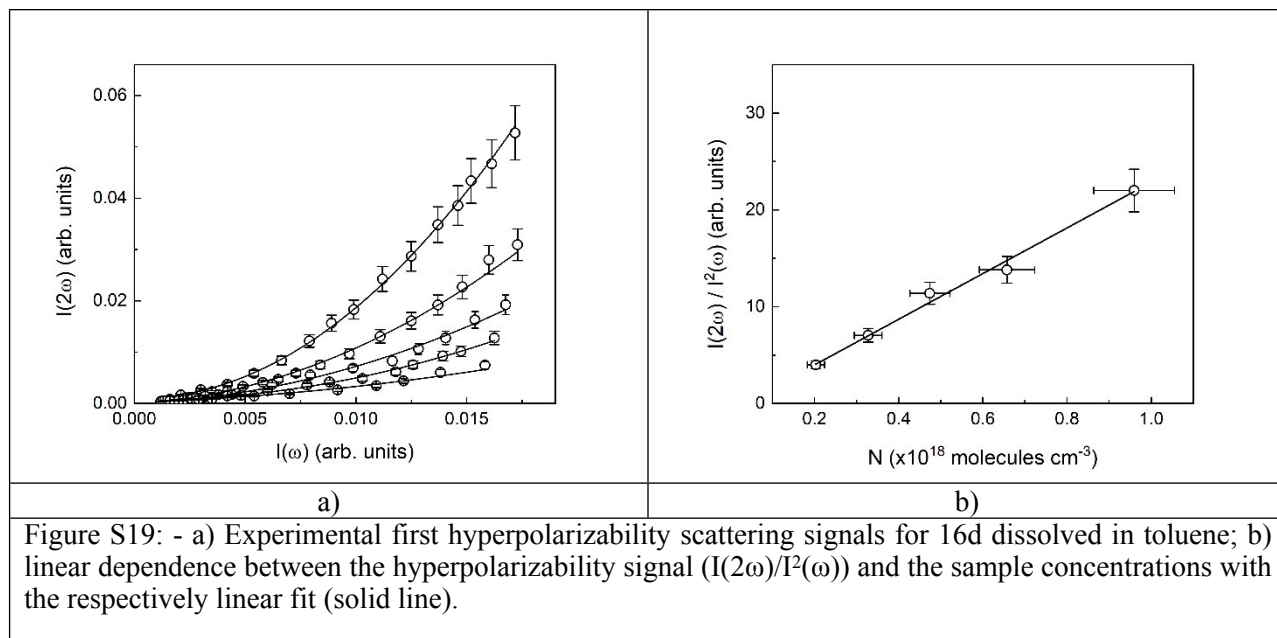
Figure S17: - a) Experimental first hyperpolarizability scattering signals for 16b dissolved in toluene; b) linear dependence between the hyperpolarizability signal ( $I(2\omega)/I^2(\omega)$ ) and the sample concentrations with the respectively linear fit (solid line).

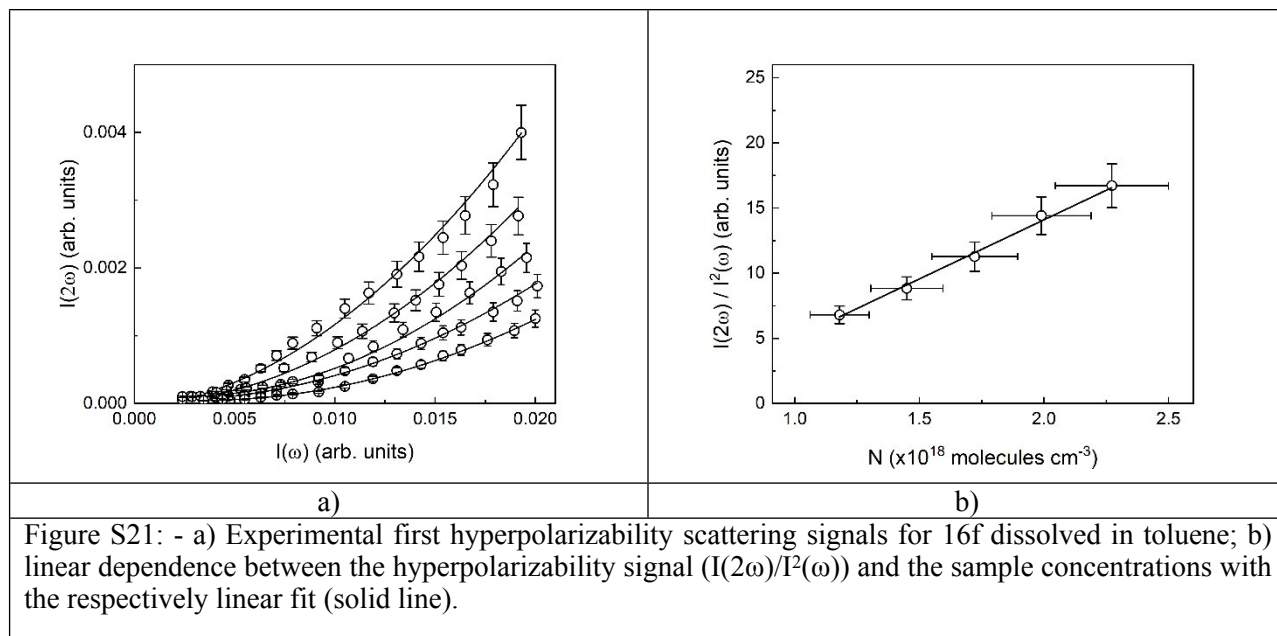


a)

b)

Figure S18: - a) Experimental first hyperpolarizability scattering signals for 16c dissolved in toluene; b) linear dependence between the hyperpolarizability signal ( $I(2\omega)/I^2(\omega)$ ) and the sample concentrations with the respectively linear fit (solid line).





**Table S1. Optimized geometry in solvent (toluene) for compounds 8j and 9k used to perform the calculation of the static ( $\beta_0$ ) and dynamic ( $\beta_{\text{HRS}}$ ) first hyperpolarizability  $\beta$  (in  $10^{-30}$  cm<sup>4</sup> statvolt<sup>-1</sup>). The values below correspond to the functional B3LYP with the basis set 6-311+G(d,p).**

Sample: 8j				Sample: 9k			
C	-3.12660	-1.33378	-0.06468	C	5.20078	-0.98391	0.08623
C	-4.34457	-0.65643	-0.10942	C	6.41404	-0.30918	0.10018
O	-5.56075	-1.26561	-0.11135	N	6.52949	1.02562	0.07285
C	-5.61313	-2.69038	-0.09675	H	7.34344	-0.86989	0.13512
H	-6.67087	-2.94545	-0.11692	C	5.39093	1.72641	0.02945
H	-5.15842	-3.09653	0.81239	C	4.12371	1.15316	0.01217
H	-5.12057	-3.11444	-0.97716	H	5.49429	2.80749	0.00729
C	-4.37660	0.74951	-0.15807	C	4.00879	-0.24378	0.04127
O	-5.56429	1.41569	-0.28031	H	3.24323	1.78109	-0.02337
C	-6.28073	1.62484	0.94581	H	5.18913	-2.06668	0.10972
H	-7.19066	2.16088	0.67836	C	2.71824	-0.90460	0.02622
H	-5.68927	2.23150	1.63828	C	2.30037	-2.20443	0.04909
H	-6.54075	0.67070	1.41150	N	0.92518	-2.25351	0.01734
C	-3.16867	1.46612	-0.15676	H	2.89779	-3.10115	0.08659
O	-3.28982	2.81969	-0.19677	C	0.53959	-1.00619	-0.02382
C	-2.10408	3.61011	-0.22737	O	1.58071	-0.12909	-0.02090
H	-2.44183	4.64386	-0.26900	C	-0.81875	-0.48259	-0.06900
H	-1.50201	3.38863	-1.11402	C	-1.88432	-1.39024	-0.07350
H	-1.50202	3.46004	0.67440	C	-3.19275	-0.91217	-0.11868
C	-1.94686	0.78943	-0.11615	H	-1.67007	-2.44801	-0.04735
C	-1.92553	-0.60963	-0.07023	O	-4.29727	-1.70499	-0.13675
H	-1.01510	1.33407	-0.11790	C	-4.11850	-3.12086	-0.14545
H	-3.10499	-2.41321	-0.03003	H	-5.12103	-3.54270	-0.18052
C	-0.65960	-1.32437	-0.02887	H	-3.60962	-3.46239	0.76104
C	-0.29337	-2.64068	0.00958	H	-3.55605	-3.44266	-1.02692
N	1.08133	-2.74372	0.03608	C	-3.44299	0.47285	-0.15296
H	-0.92367	-3.51477	0.01878	O	-4.71708	0.94985	-0.26984
C	1.51484	-1.51543	0.01366	C	-5.48447	0.97293	0.94396
O	0.50853	-0.59571	-0.02611	H	-6.46138	1.37350	0.67640
C	2.88960	-1.04533	0.02549	H	-5.01149	1.62635	1.68331
C	3.95087	-2.00068	0.05820	H	-5.59910	-0.03463	1.35068
N	5.22206	-1.68495	0.07089	C	-2.36269	1.37342	-0.14589
H	3.70005	-3.05667	0.07336	O	-2.69684	2.69019	-0.17895
C	5.56456	-0.36081	0.05196	C	-1.65134	3.65883	-0.21084
C	4.58129	0.67594	0.01914	H	-2.14902	4.62571	-0.25314
C	3.22115	0.29419	0.00613	H	-1.02219	3.53483	-1.09769
H	2.44987	1.05537	-0.01871	H	-1.03238	3.60780	0.69064
C	6.93600	-0.00977	0.06530	C	-1.05070	0.89698	-0.10683
C	7.31543	1.31291	0.04711	H	-0.21425	1.57905	-0.10126
H	7.66601	-0.81000	0.08998				
C	6.34320	2.34122	0.01482				
H	8.36745	1.57424	0.05743				
C	5.00402	2.03089	0.00107				
H	6.66107	3.37738	0.00082				
H	4.25519	2.81553	-0.02375				

**Table S2. Optimized geometry in solvent (toluene) for compounds 10b and 10d used to perform the calculation of the static ( $\beta_0$ ) and dynamic ( $\beta_{\text{HRS}}$ ) first hyperpolarizability  $\beta$  (in  $10^{-30}$  cm<sup>4</sup> statvolt<sup>-1</sup>). The values below correspond to the functional B3LYP with the basis set 6-311+G(d,p).**

Sample: 10b				Sample: 10d			
H	3.22586	1.70926	0.01009	H	7.50645	1.87339	0.86227
C	4.27022	1.42405	0.01744	C	6.60283	1.32200	0.62952
C	5.25907	2.40356	0.03869	C	6.67821	-0.01393	0.23037
H	4.97437	3.44970	0.04808	H	7.64206	-0.50400	0.15267
C	6.60667	2.04692	0.04780	C	5.52183	-0.72416	-0.06787
H	7.37466	2.81150	0.06427	H	5.59601	-1.76100	-0.37445
C	6.95974	0.69595	0.03598	C	4.26156	-0.10836	0.02649
H	8.00482	0.40772	0.04375	C	3.05598	-0.85658	-0.28974
C	5.97802	-0.28701	0.01530	C	2.79173	-2.12577	-0.72349
H	6.26878	-1.33110	0.00808	H	3.48841	-2.91774	-0.94574
C	4.61620	0.06298	0.00490	N	1.43193	-2.30124	-0.85837
C	3.59499	-0.97085	-0.01812	C	0.90366	-1.15600	-0.51211
C	3.60437	-2.33704	-0.04939	C	-0.49618	-0.81870	-0.47938
N	2.31265	-2.81581	-0.05818	H	-1.14242	-1.62984	-0.78729
C	1.55272	-1.75030	-0.03308	C	-0.97495	0.39739	-0.14625
C	0.11587	-1.70616	-0.02867	H	-0.24544	1.17274	0.07278
H	-0.34628	-2.68603	-0.04319	C	-2.36634	0.85827	-0.13726
C	-0.61501	-0.57161	-0.01013	C	-2.57153	2.19524	-0.45630
C	-2.06944	-0.45929	-0.00007	H	-1.70865	2.82591	-0.64202
C	-2.64073	0.83209	-0.02278	C	-3.86002	2.74413	-0.59407
H	-1.98003	1.68865	-0.04780	H	-3.97044	3.78637	-0.87045
C	-4.01521	1.02363	-0.01598	C	-4.96644	1.95550	-0.39317
O	-4.63223	2.23584	-0.03923	H	-5.96480	2.36266	-0.51243
C	-3.82310	3.40761	-0.06897	C	-4.82317	0.59905	-0.00211
H	-3.18870	3.47614	0.82078	C	-3.51297	0.03440	0.15549
H	-3.19917	3.43822	-0.96818	C	-3.42383	-1.29456	0.65046
H	-4.51832	4.24487	-0.08264	H	-2.45355	-1.72351	0.85462
C	-4.87397	-0.10293	0.01838	C	-4.55093	-2.03928	0.91444
O	-6.20412	0.16346	0.02749	H	-4.44953	-3.04724	1.30065
C	-7.11716	-0.93071	0.06595	C	-5.83737	-1.49780	0.70087
H	-7.00763	-1.57044	-0.81537	H	-6.71745	-2.09764	0.90286
H	-6.98271	-1.52785	0.97329	C	-5.96543	-0.20248	0.26286
H	-8.10982	-0.48479	0.06907	H	-6.94803	0.23630	0.12446
C	-4.31463	-1.38035	0.04188	O	1.83886	-0.22899	-0.15301
H	-4.95640	-2.25041	0.06933	C	4.19488	1.23526	0.42929
C	-2.93306	-1.55859	0.03275	H	3.23124	1.72238	0.50700
H	-2.54074	-2.56761	0.05519	C	5.35732	1.94047	0.72712
H	-0.07780	0.37296	-0.00306	H	5.28875	2.97721	1.03677
O	2.27187	-0.58931	-0.00810				
H	4.45297	-3.00158	-0.06694				

**Table S3. Optimized geometry in solvent (toluene) for compounds 11b and 13k used to perform the calculation of the static ( $\beta_0$ ) and dynamic ( $\beta_{\text{HRS}}$ ) first hyperpolarizability  $\beta$  (in  $10^{-30}$  cm<sup>4</sup> statvolt<sup>-1</sup>). The values below correspond to the functional B3LYP with the basis set 6-311+G(d,p).**

Sample: 11b				Sample: 13k			
C	5.94430	1.31442	0.03679	C	7.46385	0.64023	0.12111
C	4.61483	1.75585	0.03015	N	7.22342	1.95712	0.18463
C	3.57344	0.84332	0.02498	C	5.94017	2.33493	0.17633
H	4.42046	2.82170	0.02922	C	4.86867	1.45106	0.10621
C	3.82360	-0.54159	0.02621	H	5.75501	3.40396	0.22833
H	2.55194	1.20182	0.02019	C	5.12611	0.07425	0.03933
C	5.15824	-0.96874	0.03202	H	3.85365	1.82587	0.10293
C	6.21155	-0.05943	0.03773	C	6.47112	-0.32767	0.04868
H	5.38779	-2.02802	0.03090	H	6.74508	-1.37451	0.00172
H	7.22717	-0.43092	0.04169	H	8.50838	0.34302	0.12918
O	6.89717	2.28722	0.04152	C	4.05364	-0.89802	-0.03682
C	8.27002	1.90156	0.04764	C	3.99062	-2.26013	-0.13017
H	8.51490	1.32191	0.94315	N	2.67720	-2.66573	-0.17093
H	8.83806	2.82975	0.05091	H	4.80327	-2.96754	-0.17125
H	8.52319	1.32317	-0.84637	C	1.97593	-1.56086	-0.10276
C	2.73721	-1.50524	0.02163	O	2.75383	-0.44467	-0.01989
C	2.65199	-2.86996	0.04173	C	0.54300	-1.44091	-0.10654
N	1.32959	-3.25760	0.02257	C	-0.12256	-0.26985	-0.03422
H	3.45205	-3.59187	0.06938	H	0.03104	-2.39308	-0.17439
C	0.64579	-2.14338	-0.00793	C	-1.56898	-0.07423	-0.02985
O	1.44467	-1.03380	-0.00980	H	0.46316	0.64271	0.02812
C	-0.78441	-1.99844	-0.03864	C	-2.48570	-1.14242	-0.07899
C	-1.43408	-0.81670	-0.06694	C	-3.85437	-0.89981	-0.06631
H	-1.31348	-2.94395	-0.03709	H	-2.12356	-2.15909	-0.12844
C	-2.87956	-0.60713	-0.10041	C	-4.34375	0.42633	0.00763
H	-0.83432	0.08919	-0.06440	C	-3.43110	1.48574	0.03801
C	-3.81510	-1.65142	-0.12895	C	-2.05963	1.23531	0.02163
C	-5.17597	-1.37107	-0.15376	H	-1.38224	2.08022	0.06121
H	-3.48988	-2.68421	-0.13054	O	-4.80939	-1.86775	-0.11622
C	-5.64694	-0.06073	-0.15529	C	-4.39807	-3.23101	-0.20187
H	-5.90690	-2.17095	-0.17950	H	-5.31658	-3.81335	-0.23868
C	-4.72018	1.00353	-0.14349	H	-3.81417	-3.52507	0.67585
C	-3.35688	0.71824	-0.10929	H	-3.81574	-3.41172	-1.11042
H	-2.63755	1.52678	-0.10020	O	-5.68576	0.68790	-0.00973
O	-6.99702	0.15727	-0.25224	C	-6.39727	0.38847	1.20465
C	-7.63152	0.75837	0.88792	H	-6.34698	-0.67804	1.43141
H	-8.69010	0.82627	0.64055	H	-5.99040	0.97218	2.03544
H	-7.23268	1.75532	1.08159	H	-7.43163	0.67842	1.02529
H	-7.50299	0.12438	1.77133	O	-3.86212	2.78402	0.15321
O	-5.24389	2.26114	-0.18218	C	-4.50780	3.33393	-1.00730
C	-4.35196	3.37311	-0.21357	H	-4.77836	4.35588	-0.74477
H	-4.98505	4.25713	-0.25974	H	-5.40414	2.76640	-1.26298
H	-3.70876	3.33981	-1.09830	H	-3.81594	3.34608	-1.85588
H	-3.73476	3.41375	0.68954				

**Table S4. Optimized geometry in solvent (toluene) for compounds 16b and 16c used to perform the calculation of the static ( $\beta_0$ ) and dynamic ( $\beta_{\text{HRS}}$ ) first hyperpolarizability  $\beta$  (in  $10^{-30}$  cm<sup>4</sup> statvolt<sup>-1</sup>). The values below correspond to the functional B3LYP with the basis set 6-311+G(d,p).**

Sample: 16b				Sample: 16c			
C	-7.27109	0.34903	0.01241	C	-6.62859	0.25116	0.00731
C	-7.08988	1.73334	-0.00176	C	-6.52822	1.64352	0.00111
C	-6.17322	-0.50273	0.01347	C	-5.26977	2.24364	-0.00549
H	-8.27177	-0.06774	0.02307	H	-7.42375	2.25398	0.00152
C	-4.86748	0.01731	-0.00017	C	-4.11765	1.46319	-0.00604
H	-6.32933	-1.57511	0.02542	H	-5.18335	3.32417	-0.01028
C	-4.69367	1.41053	-0.01423	C	-4.21048	0.06236	0.00010
C	-5.79811	2.25756	-0.01496	H	-3.14330	1.93500	-0.01137
H	-3.69310	1.82376	-0.02476	C	-5.48265	-0.53466	0.00693
H	-5.64797	3.33119	-0.02592	H	-5.57593	-1.61423	0.01227
H	-7.94802	2.39542	-0.00236	H	-7.60308	-0.22339	0.01268
C	-3.72278	-0.87997	0.00021	C	-3.01556	-0.76677	-0.00072
C	-3.56009	-2.23834	0.00099	C	-2.77597	-2.11633	-0.00233
N	-2.21975	-2.55221	0.00039	N	-1.42204	-2.35130	-0.00293
H	-4.31696	-3.00586	0.00144	H	-3.48731	-2.92612	-0.00354
C	-1.60351	-1.39937	-0.00094	C	-0.87385	-1.16521	-0.00144
O	-2.46332	-0.33343	-0.00114	O	-1.79200	-0.15053	-0.00039
C	-0.22539	-1.13623	-0.00145	C	0.48809	-0.82760	-0.00106
C	0.96534	-0.91329	-0.00152	C	1.66415	-0.54187	-0.00064
C	2.35939	-0.65267	-0.00135	C	3.04325	-0.21097	-0.00016
C	3.28474	-1.70077	-0.00405	C	4.01939	-1.22619	-0.00146
C	4.65205	-1.42868	-0.00367	C	5.36663	-0.90345	-0.00096
H	2.93824	-2.72625	-0.00644	H	3.70933	-2.26337	-0.00286
C	5.11972	-0.11641	-0.00055	C	5.76564	0.44244	0.00087
H	5.35132	-2.25331	-0.00584	H	6.11437	-1.68644	-0.00195
C	4.18712	0.95532	0.00222	C	4.79923	1.46068	0.00218
C	2.82855	0.68080	0.00175	C	3.45241	1.13663	0.00166
H	2.10770	1.48578	0.00379	H	5.11027	2.49771	0.00361
O	6.42605	0.24071	0.00015	H	2.70591	1.92066	0.00268
C	7.41517	-0.78726	-0.00275	C	7.15554	0.77615	0.00143
H	8.37328	-0.27163	-0.00186	N	8.27965	1.04644	0.00189
H	7.33649	-1.41009	-0.89912				
H	7.33721	-1.41446	0.89064				
O	4.72506	2.20234	0.00517				
C	3.84201	3.32140	0.00898				
H	4.48280	4.20089	0.01158				
H	3.21169	3.32643	0.90394				
H	3.21113	3.33212	-0.88553				



**Table S5. Optimized geometry in solvent (toluene) for compounds 16d and 16e used to perform the calculation of the static ( $\beta_0$ ) and dynamic ( $\beta_{\text{HRS}}$ ) first hyperpolarizability  $\beta$  (in  $10^{-30}$  cm<sup>4</sup> statvolt<sup>-1</sup>). The values below correspond to the functional B3LYP with the basis set 6-311+G(d,p).**

Sample: 16d				Sample: 16e			
C	-6.65893	0.45572	0.00061	C	7.56503	0.36203	0.04572
C	-6.42047	1.83140	0.00032	C	7.42493	1.75063	0.01388
C	-5.10832	2.30241	-0.00010	C	6.15001	2.31380	-0.02186
H	-7.25065	2.52820	0.00044	H	8.30246	2.38672	0.01723
C	-4.03981	1.41066	-0.00024	C	5.02080	1.50045	-0.02609
H	-4.91422	3.36897	-0.00033	H	6.03269	3.39116	-0.04653
C	-4.27135	0.02586	0.00004	C	5.15366	0.10322	0.00558
H	-3.02318	1.78270	-0.00058	H	4.03346	1.94357	-0.05437
C	-5.59709	-0.44056	0.00049	C	6.44217	-0.45644	0.04206
H	-5.79689	-1.50572	0.00076	H	6.56599	-1.53265	0.06864
H	-7.67596	0.08060	0.00096	H	8.55252	-0.08402	0.07431
C	-3.16488	-0.91808	-0.00013	C	3.98319	-0.76023	0.00095
C	-3.05991	-2.28296	-0.00052	C	3.78300	-2.11560	0.00427
N	-1.73468	-2.65236	-0.00070	N	2.43591	-2.38997	-0.00376
H	-3.84860	-3.01766	-0.00075	H	4.51768	-2.90422	0.01091
C	-1.07075	-1.52663	-0.00030	C	1.85368	-1.22049	-0.01190
O	-1.88451	-0.42538	0.00008	O	2.74197	-0.17953	-0.01006
C	0.31749	-1.32350	-0.00028	C	0.48218	-0.92188	-0.02018
C	1.51681	-1.15450	-0.00010	C	-0.70131	-0.66997	-0.02509
C	2.92415	-0.97705	0.00007	C	-2.09102	-0.37943	-0.02890
C	3.75335	-2.09232	0.00030	C	-3.03607	-1.42174	-0.02568
C	5.15348	-1.95166	0.00047	C	-4.39413	-1.13593	-0.02762
H	3.30926	-3.08017	0.00036	H	-2.69660	-2.44968	-0.02263
C	5.72707	-0.70129	0.00039	C	-4.82757	0.19131	-0.03682
H	5.77590	-2.83878	0.00064	H	-5.11466	-1.94379	-0.02898
C	4.92270	0.46781	0.00016	C	-3.89949	1.23495	-0.03987
H	6.80637	-0.59265	0.00051	C	-2.54077	0.95388	-0.03762
C	3.49780	0.34221	0.00000	H	-4.23691	2.26361	-0.05061
C	2.70843	1.51946	-0.00024	H	-1.81920	1.76096	-0.04371
C	3.29806	2.76265	-0.00033	C	-6.29761	0.49984	0.01691
H	1.62883	1.42856	-0.00037	F	-7.04990	-0.47400	-0.54337
C	4.70607	2.88926	-0.00017	F	-6.60508	1.65444	-0.61766
H	2.67966	3.65306	-0.00052	F	-6.73933	0.63777	1.29615
C	5.49806	1.76640	0.00007				
H	5.15745	3.87482	-0.00024				
H	6.57919	1.85585	0.00020				

**Table S6. Optimized geometry in solvent (toluene) for compound 16f used to perform the calculation of the static ( $\beta_0$ ) and dynamic ( $\beta_{\text{HRS}}$ ) first hyperpolarizability  $\beta$  (in  $10^{-30}$  cm<sup>4</sup> statvolt<sup>-1</sup>). The values below correspond to the functional B3LYP with the basis set 6-311+G(d,p).**

<b>Sample: 16f</b>			
C	5.89663	0.05356	0.00005
C	5.86291	1.44920	0.00019
C	4.63437	2.10826	0.00024
H	6.78653	2.01629	0.00025
C	3.44645	1.38329	0.00015
H	4.59903	3.19170	0.00034
C	3.47216	-0.02037	0.00001
H	2.49562	1.90089	0.00019
C	4.71463	-0.67701	-0.00004
H	4.75669	-1.75989	-0.00014
H	6.84742	-0.46697	0.00001
C	2.23857	-0.79113	-0.00008
C	1.93348	-2.12628	-0.00023
N	0.56856	-2.29533	-0.00026
H	2.60430	-2.96989	-0.00033
C	0.07932	-1.08402	-0.00012
O	1.04545	-0.11543	-0.00002
C	-1.26563	-0.68105	-0.00009
C	-2.42775	-0.34385	-0.00006
C	-3.79089	0.04740	-0.00001
C	-4.82914	-0.89875	0.00050
C	-6.14179	-0.44943	0.00053
H	-4.59808	-1.95697	0.00086
C	-6.38281	0.92379	0.00006
H	-6.96877	-1.14893	0.00091
N	-5.40720	1.84112	-0.00044
H	-7.39940	1.30471	0.00008
C	-4.14810	1.41034	-0.00047
H	-3.37091	2.16820	-0.00088

**Table S7: Theoretical values for static ( $\beta_0$ ) and dynamic ( $\beta_{\text{HRS}}$ ) first hyperpolarizability  $\beta$  (in  $10^{-30} \text{ cm}^4 \text{ statvolt}^{-1}$ ) in toluene medium of the investigated compounds. These results were obtained by using the basis set 6-311+G(d,p).**

Molecule	B3LYP		CAM-B3LYP		M06-2X		Experimental
	$\beta_0$	$\beta_{\text{HRS}}$	$\beta_0$	$\beta_{\text{HRS}}$	$\beta_0$	$\beta_{\text{HRS}}$	$\beta_{\text{HRS}}$
8j	29.4	99.8	12.2	24.5	13.0	26.4	42 ± 4
9k	18.9	45.5	11.2	18.8	11.0	18.3	35 ± 4
10b	20.3	68.6	12.4	24.3	11.5	22.6	34 ± 3
10d	8.5	25.6	3.5	6.2	4.3	8.2	15 ± 2
11b	18.5	73.7	7.9	17.7	8.7	20.1	30 ± 3
13k	24.4	82.2	13.6	26.6	12.3	23.6	38 ± 4
16b	20.2	55.5	11.7	20.5	10.9	19.3	29 ± 3
16c	54.0	187.7	23.3	48.7	24.6	51.5	48 ± 5
16d	11.9	40.0	4.6	9.7	5.7	12.1	17 ± 2
16e	32.2	96.7	14.0	28.4	15.1	30.3	31 ± 3
16f	21.8	61.8	9.6	19.1	10.2	20.4	22 ± 2

**Table S8: Theoretical values for static ( $\beta_0$ ) and dynamic ( $\beta_{\text{HRS}}$ ) first hyperpolarizability  $\beta$  (in  $10^{-30} \text{ cm}^4 \text{ statvolt}^{-1}$ ) in toluene medium of the investigated compounds. These results were obtained by using the basis set 6-311++G(d,p).**

Molecule	B3LYP		CAM-B3LYP		M06-2X		Experimental
	$\beta_0$	$\beta_{\text{HRS}}$	$\beta_0$	$\beta_{\text{HRS}}$	$\beta_0$	$\beta_{\text{HRS}}$	$\beta_{\text{HRS}}$
8j	29.2	99.5	13.8	29.3	14.5	31.3	42 ± 4
9k	18.8	45.2	13.2	21.4	12.0	20.9	35 ± 4
10b	20.1	68.1	13.7	28.6	12.8	26.9	34 ± 3
10d	8.4	25.6	4.1	8.1	5.0	10.4	15 ± 2
11b	18.4	73.7	9.0	22.3	9.7	24.6	30 ± 3
13k	24.4	81.8	15.6	32.7	14.8	31.0	38 ± 4
16b	20.0	51.1	12.7	23.5	11.9	22.0	29 ± 3
16c	54.0	187.7	28.1	62.9	29.7	66.6	48 ± 5
16d	11.9	40.0	5.5	12.6	6.6	15.0	17 ± 2
16e	32.2	96.7	17.2	36.8	18.7	39.8	31 ± 3
16f	21.8	61.8	11.3	23.9	11.9	25.0	22 ± 2

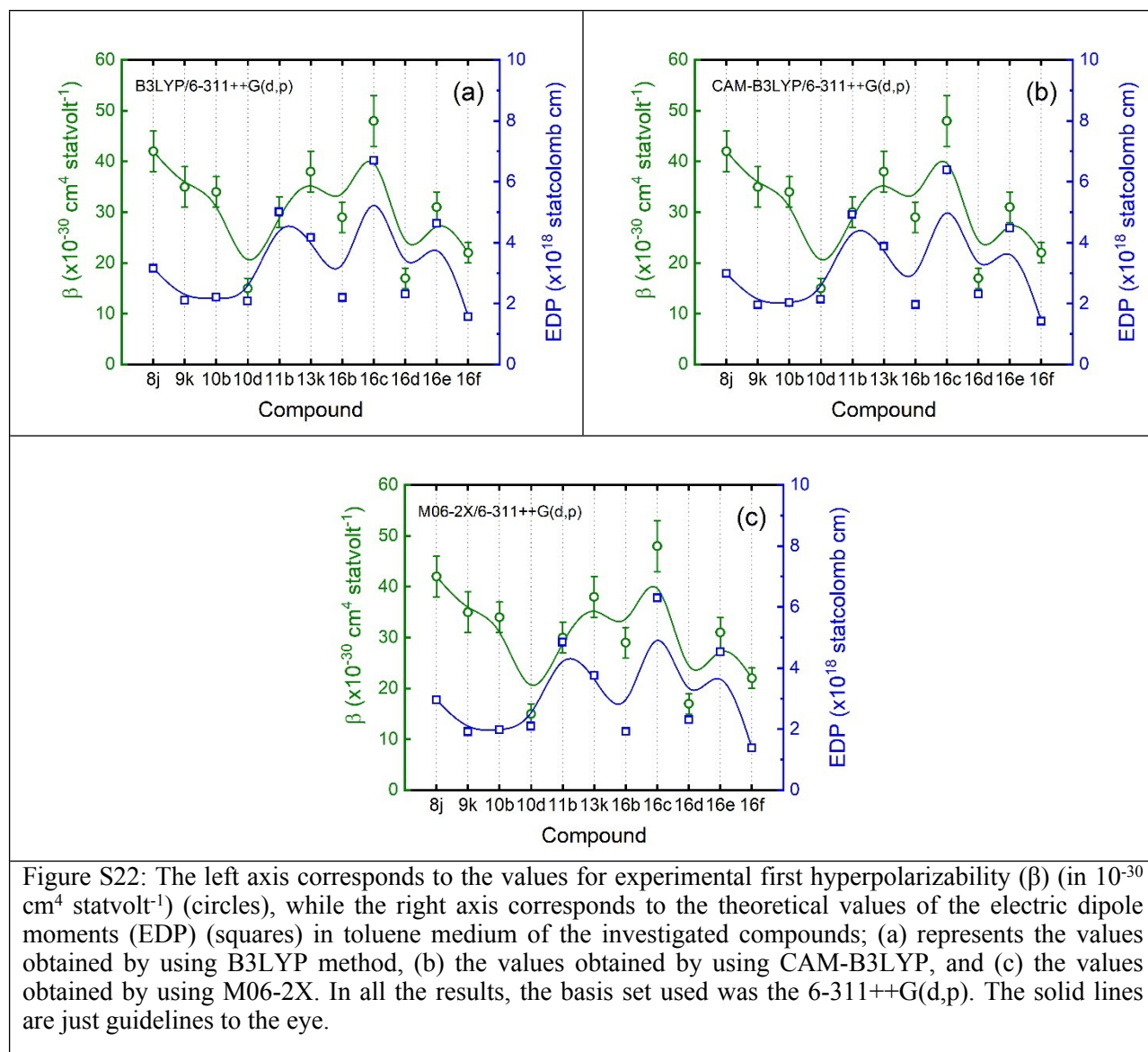


Figure S22: The left axis corresponds to the values for experimental first hyperpolarizability ( $\beta$ ) (in  $10^{-30} \text{ cm}^4 \text{ statvolt}^{-1}$ ) (circles), while the right axis corresponds to the theoretical values of the electric dipole moments (EDP) (squares) in toluene medium of the investigated compounds; (a) represents the values obtained by using B3LYP method, (b) the values obtained by using CAM-B3LYP, and (c) the values obtained by using M06-2X. In all the results, the basis set used was the 6-311++G(d,p). The solid lines are just guidelines to the eye.