# **Electronic Supplementary Information**

# Planar Graphitic ZnS, Buckling ZnS Monolayers and Rolled-up Nanotubes as Nonlinear Optical Materials: First-Principles Simulation

Lei Hu<sup>1\*</sup>, Wencai Yi<sup>2</sup>, Jianting Tang<sup>1</sup>, Tongde Rao<sup>1</sup>, Zuju Ma<sup>3</sup>, Chuanbo Hu<sup>1</sup>, Lei Zhang Tingzhen Li<sup>1\*</sup>

<sup>1</sup>School of Environmental and Chemical Engineering, Chongqing Three Gorges University, Chongqing, 404100, China

<sup>2</sup>Laboratory of High Pressure Physics and Material Science, School of Physics and Physical

Engineering, Qufu Normal University, Qufu, 273165, China

<sup>3</sup>School of Materials Science and Engineering, Anhui University of Technology, Maanshan, 243

002, China

Email: huleisanxu@163.com, leihu@sanxiau.edu.cn, litingzhen@163.com

Keywords: planar ZnS monolayer; buckling ZnS monolayer; ZnS single-walled nanotube; second harmonic generation; nonlinear optical property; first-principles; mid-infrared

## 1. Band structure and interlayer distance of wurtzite ZnS



**Figure S1** (a) band structure calculated with HSE06 functional and (b) interlayer distance of wurtzite ZnS

As can be seen, wurtzite ZnS crystal exhibits a direct bandgap, with the VBM and CBM both

located at the  $\Gamma$  (0.0, 0.0, 0.0) point. The band gap of wurtzite ZnS crystal is 3.51 eV, which is close to the experimental value 3.77 eV<sup>1</sup>. As shown in Figure 1S(b), similar to planar g-SiC<sup>2</sup>, the effective thickness of planar g-ZnS is set as the interlayer distance 3.898 Å of wurtzite ZnS crystal.

# 2. Band structure of planar g-ZnS



**Figure S2** (a) Band structure of planar g-ZnS monolayer calculated using HSE06 functional, and (b) high symmetry k-point path in the Brillouin zone path  $\Gamma$  (0, 0, 0)  $\rightarrow$  K (-1/3, 2/3, 0)  $\rightarrow$  M (0, 1/2, 0)  $\rightarrow$   $\Gamma$  (0, 0, 0).

As suggested by Figure S2, planar g-ZnS monolayer has a direct band gap of 3.80 eV at the  $\Gamma$  point.

## 3. Band structure of buckling R-ZnS monolayer

Figure S3 suggests buckling R-ZnS monolayers have direct bandgaps with the VBM and CMB located at the  $\Gamma$  point. The bandgaps of buckling R-ZnS are steady around 3.90 eV with a small variance of ~ 0.10 eV.



**Figure S3** Band structure of buckling R<sub>1</sub>-ZnS, R<sub>2</sub>-ZnS, R<sub>3</sub>-ZnS, R<sub>4</sub>-ZnS and R<sub>5</sub>-ZnS calculated using HSE06 functional. The high symmetry k-point path in the Brillouin Zone, as shown in (c), is chosen as  $\Gamma(0, 0, 0) \rightarrow K(-1/3, 2/3, 0) \rightarrow M(0, 1/2, 0) \rightarrow \Gamma(0, 0, 0)$ .

## 4. Band structure and total density of electronic states of a representative (12, 0) ZnS SWNT

Zigzag and chiral ZnS SWNTs show similar electronic structures. As a representative, the band structure and total density of electronic states are given in Figure S4. As can be seen, ZnS (12, 0) SWNT exhibits a direct band gap at the  $\Gamma$  (0.0, 0.0, 0.0) point, and a sharp peak in the top of valence bands.



Figure S4 Band structure and total density of electronic states of a (12, 0) ZnS SWNT

## 5. SHG intensity estimation of planar g-ZnS, buckling R-ZnS and ZnS SWNTs

According to the electric dipole theory, the SHG intensity  $I_{2\omega}$  is proportional to  $\frac{[\chi^{(2)}]^2 d^2 \omega^2}{n_{\omega} n_{2\omega}^2}$ , where d is the effective thickness of monolayers,  $n_{\omega}$  and  $n_{2\omega}$  are respectively the refractive index at frequency  $\omega$  of excitation laser and at frequency  $2\omega$  of SHG field <sup>3</sup>. Previous experiments demonstrate the nonresonant SHG intensity of monolayer GaSe is stronger than that of monolayer MoS<sub>2</sub>, WS<sub>2</sub>, WSe<sub>2</sub> and BN <sup>3</sup>. Here, we make a comparison of SHG intensities of monolayer g-ZnS, GaSe and MoS<sub>2</sub>. The theoretical  $n_{\omega}$ ,  $n_{2\omega}$  at 1600 nm and effective thickness of planar g-ZnS in Table S1, and that of monolayer GaSe <sup>4</sup> and MoS<sub>2</sub> <sup>3</sup> is also shown for comparison. The theoretical SHG coefficients  $\chi^{(2)}_{xxy}$  at an excitation wavelength of 1600 nm for monolayer GaSe and planar g-ZnS are 75 pm/V <sup>4</sup> and 42 pm/V, respectively. The estimated ration of SHG intensities at 1600 nm between monolayer g-ZnS and GaSe is ~0.2. Experiments show the SHG intensity of single-layer MoS<sub>2</sub> at 1600 nm is less than 1/10 that of single-layer GaSe <sup>3</sup>. Therefore, the nonresonant SHG intensity of planar g-ZnS at 1600 nm is stronger than that of single-layer  $MoS_2$ , which mainly originates from smaller optical refractive indices of planar g-ZnS.

Materials	GaSe	g-ZnS	$MoS_2$	R <sub>1</sub> -ZnS	R <sub>2</sub> -ZnS	R <sub>3</sub> -ZnS	R <sub>4</sub> -ZnS	R <sub>5</sub> -ZnS
d	7.99	3.90	6.0	3.92	3.93	4.18	4.25	4.35
n <sub>ω</sub>	2.70	2.15	4.0	2.16	2.16	2.15	2.16	2.17
$n_{2\omega}$	2.77	2.18	4.5	2.19	2.19	2.17	2.18	2.20

**Table S1**.  $n_{\omega}$ ,  $n_{2\omega}$  at 1600 nm and effective thickness d (Å) of monolayer GaSe, planar g-ZnS, MoS<sub>2</sub> and buckling R-ZnS

As shown in Figure 2 of the main manuscript, the SHG coefficient of planar g-ZnS nearly keeps constant from zero to 1.0 eV, e.g. 42 pm/V at 1600 nm versus 37.4 pm/V at the static limit, which indicating their nonresonant SHG intensities nearly keep constant. Moreover, the nonresonant SHG regime of planar g-ZnS covers the whole mid-infrared regime (2-8  $\mu$ m), so planar g-ZnS has a potential application in the mid-infrared regime.

<b>Table S2.</b> $n_{\omega}$ and $n_{2\omega}$ at 1600 nm of ZnS SWN1s												
Materials	(6, 0)	(8,0)	(9,0)	(12,0)	(16,0)	(18,0)	(20,0)	(4,2)	(6,3)			
n <sub>ω</sub>	2.15	2.16	2.15	2.15	2.16	2.14	2.13	2.16	2.17			
$n_{2\omega}$	2.19	2.20	2.18	2.19	2.20	2.17	2.16	2.19	2.21			

**Table S2**.  $n_{\omega}$  and  $n_{2\omega}$  at 1600 nm of ZnS SWNTs

Furthermore, the optical refractive indices  $n_{\omega}$  and  $n_{2\omega}$  of buckling R-ZnS [cf. Table S1] and ZnS SWNTs [cf. Table S2] are nearly not modified in comparison with that of planar g-ZnS. Resultantly, small refractive indices will also enhance SHG signals of buckling R-ZnS and ZnS SWNTs.

#### References

- 1. J. X. Ding, J. A. Zapien, W. W. Chen, Y. Lifshitz, S. T. Lee and X. M. Meng, *Lasing in ZnS nanowires grown on anodic aluminum oxide templates*, *Appl. Phys. Lett.*, 2004, **85**, 2361.
- 2. I. J. Wu and G. Y. Guo, *Second-harmonic generation and linear electro-optical coefficients of SiC polytypes and nanotubes*, *Phys. Rev. B*, 2008, **78**, 035447.
- 3. X. Zhou, J. Cheng, Y. Zhou, T. Cao, H. Hong, Z. Liao, S. Wu, H. Peng, K. Liu and D. Yu, *Strong Second-Harmonic Generation in Atomic Layered GaSe*, J. Am. Chem. Soc., 2015, **137**, 7994.

4. L. Hu, X. Huang and D. Wei, Layer-independent and layer-dependent nonlinear optical properties of two-dimensional GaX (X = S, Se, Te) nanosheets, Phys. Chem. Chem. Phys., 2017, **19**, 11131.