

## Supporting Information

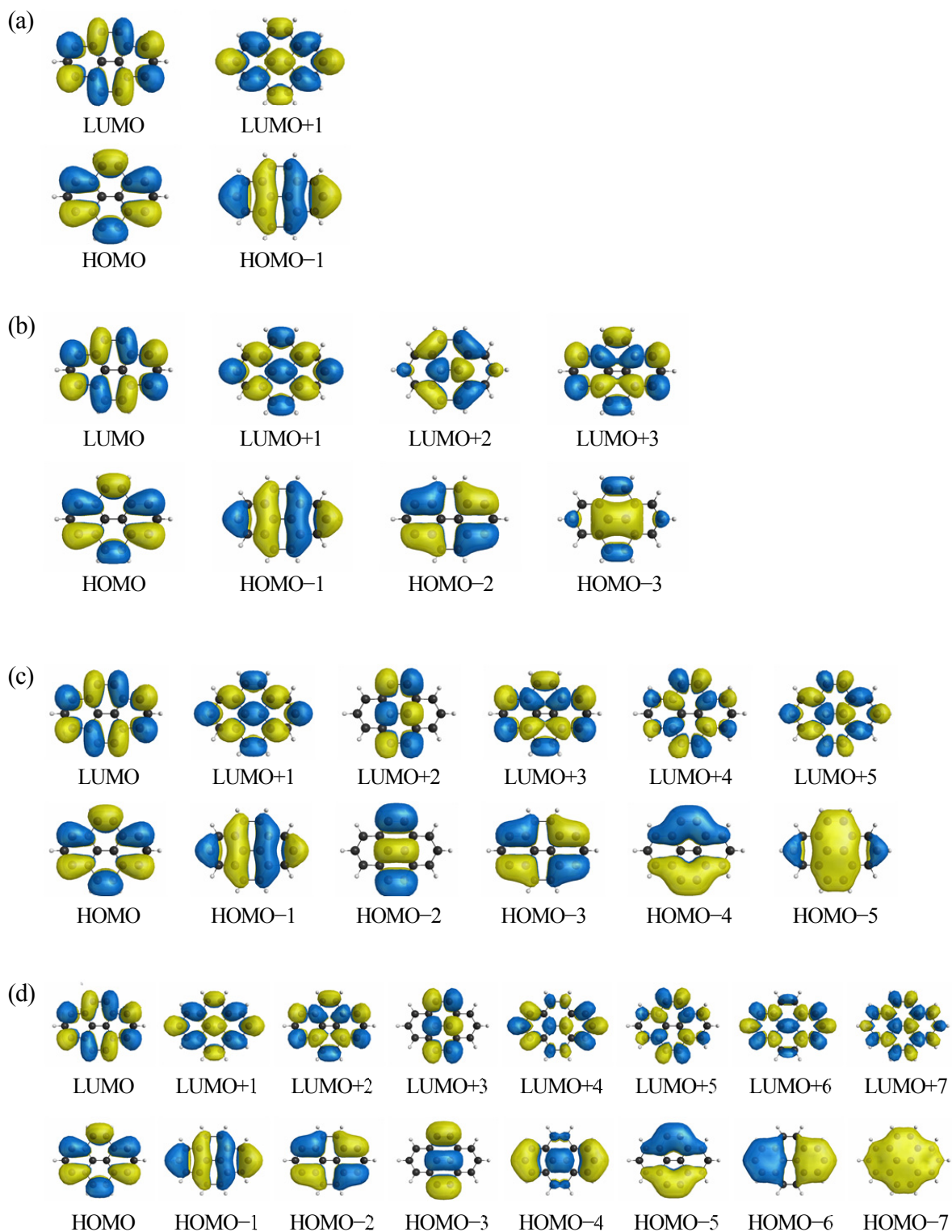
### **Ab initio study on the excited states of pyrene and its derivatives using multi-reference perturbation theory methods**

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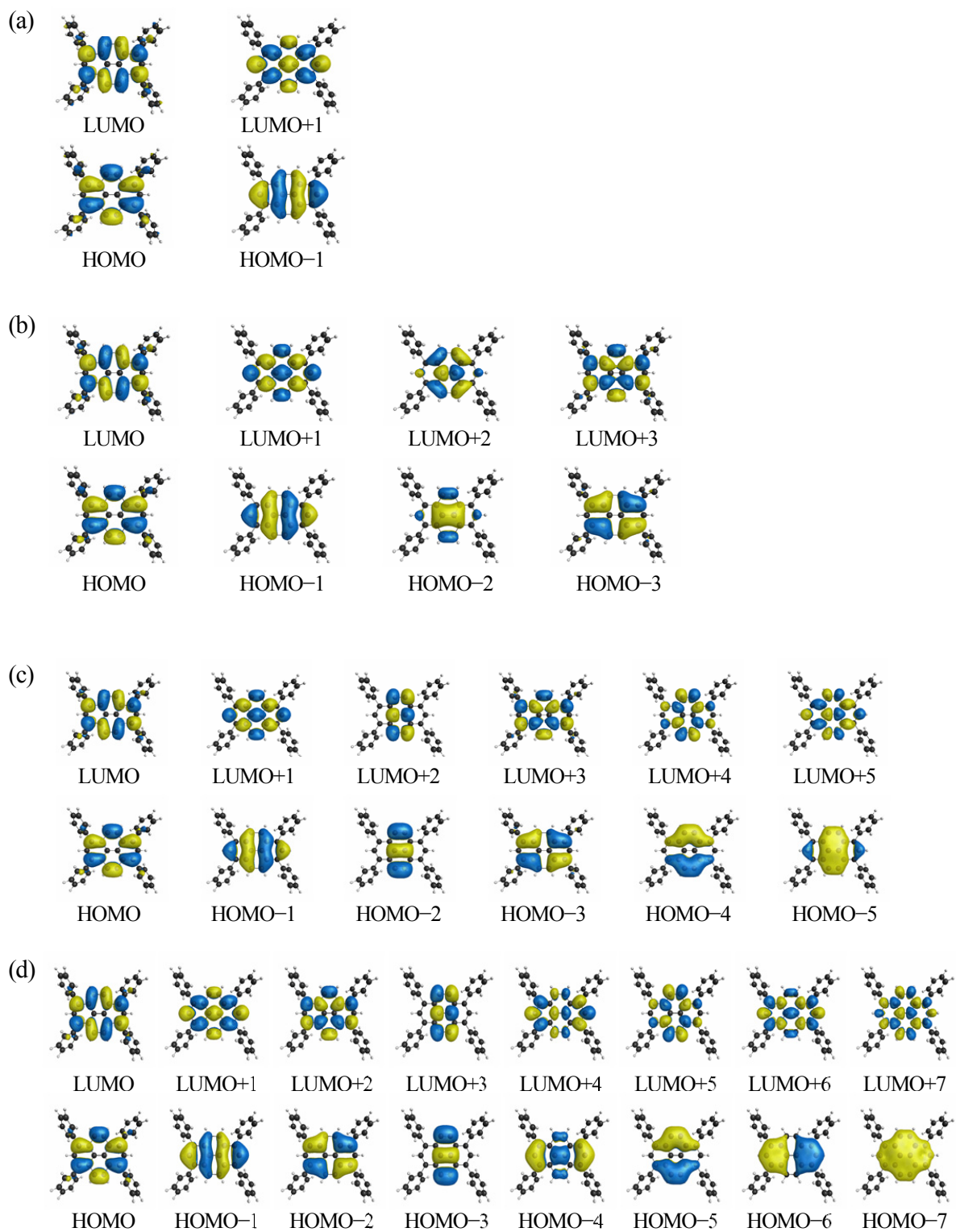
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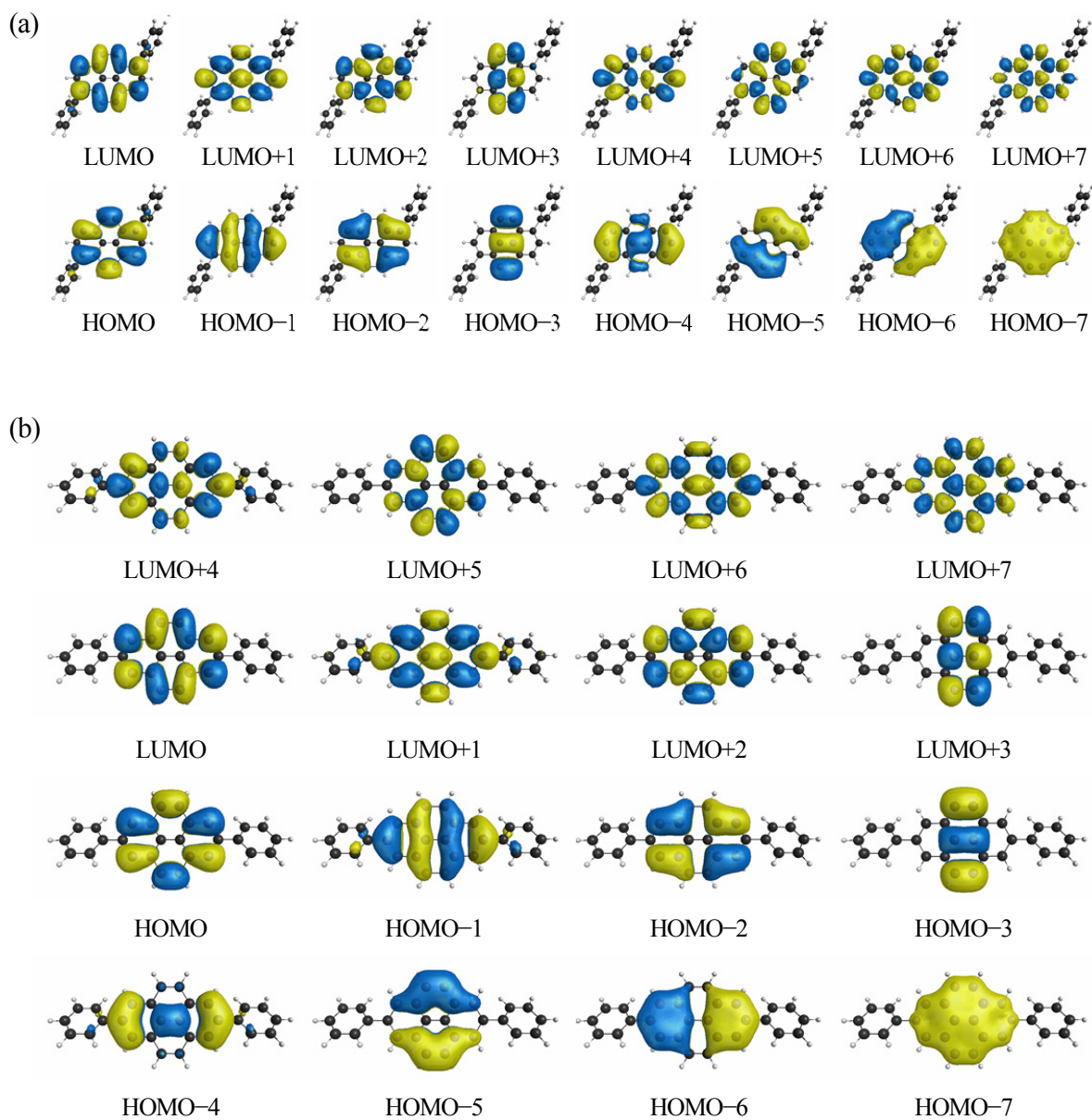
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**Fig. S1** Natural orbitals of pyrene from MCSCF wave functions:  
 (a) CAS( $4\pi e$ ,  $4\pi o$ ), (b) CAS( $8\pi e$ ,  $8\pi o$ ), (c) CAS( $12\pi e$ ,  $12\pi o$ ) and (d) MRX(4).



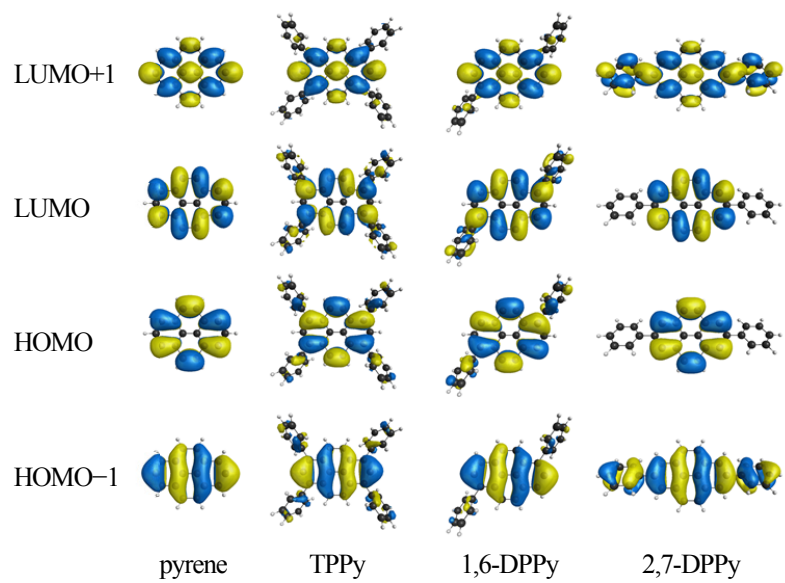
**Fig. S2** Natural orbitals of 1,3,6,8-tetraphenylpyrene (TPPy) from MCSCF wave functions:  
(a) CAS( $4\pi e$ ,  $4\pi o$ ), (b) CAS( $8\pi e$ ,  $8\pi o$ ), (c) CAS( $12\pi e$ ,  $12\pi o$ ) and (d) MRX(4).



**Fig. S3** Natural orbitals of (a) 1,6-diphenylpyrene (1,6-DPPy) and (b) 2,7-diphenylpyrene (2,7-DPPy) from MCSCF wave functions with MRX(4) configuration space.

**Table S1.** Calculated electronic total energies and excitation energies.

molecule	method	reference space	electronic state total energy			excitation energy	
			ground state	$^1L_a$	$^1L_b$	$^1L_a$	$^1L_b$
pyrene	GMCSCF	MRX(2)	-611.963398	-611.683908	-611.732426	7.61	6.28
		MRX(3)	-611.969412	-611.773601	-611.827047	5.33	3.87
		MRX(4)	-611.998334	-611.786239	-611.854412	5.77	3.92
	CASSCF	CAS(4 $\pi e$ , 4 $\pi o$ )	-611.826258	-611.630826	-611.633173	5.32	5.25
		CAS(8 $\pi e$ , 8 $\pi o$ )	-611.873724	-611.673541	-611.698314	5.45	4.77
		CAS(12 $\pi e$ , 12 $\pi o$ )	-611.938240	-611.733420	-611.773669	5.57	4.48
	GMCQDPT	MRX(2)	-613.895808	-613.757849	-613.779477	3.75	3.17
		MRX(3)	-613.898739	-613.758249	-613.777274	3.82	3.31
		MRX(4)	-613.904548	-613.763264	-613.779616	3.84	3.40
	MCQDPT	CAS(4 $\pi e$ , 4 $\pi o$ )	-613.888464	-613.758129	-613.784435	3.55	2.83
		CAS(8 $\pi e$ , 8 $\pi o$ )	-613.895007	-613.757183	-613.775339	3.75	3.26
		CAS(12 $\pi e$ , 12 $\pi o$ )	-613.912130	-613.771275	-613.764713	3.83	4.01
EOM-CCSD		-613.927251	-613.763560	-613.786867	4.45	3.82	
TPPy	GMCSCF	MRX(2)	-1530.208096	-1529.939689	-1529.982544	7.30	6.14
		MRX(3)	-1530.214345	-1530.028781	-1530.075887	5.05	3.77
		MRX(4)	-1530.243303	-1530.040528	-1530.102935	5.52	3.82
	CASSCF	CAS(4 $\pi e$ , 4 $\pi o$ )	-1530.072126	-1529.887052	-1529.892707	5.04	4.88
		CAS(8 $\pi e$ , 8 $\pi o$ )	-1530.119736	-1529.934120	-1529.950080	5.05	4.62
		CAS(12 $\pi e$ , 12 $\pi o$ )	-1530.183896	-1529.992171	-1530.023859	5.22	4.35
	GMCQDPT	MRX(2)	-1535.272512	-1535.158154	-1535.163555	3.11	2.96
		MRX(3)	-1535.274668	-1535.154509	-1535.159934	3.27	3.12
		MRX(4)	-1535.280775	-1535.167838	-1535.161723	3.07	3.24
	MCQDPT	CAS(4 $\pi e$ , 4 $\pi o$ )	-1535.277130	-1535.169965	-1535.181531	2.92	2.60
		CAS(8 $\pi e$ , 8 $\pi o$ )	-1535.306796	-1535.191025	-1535.195163	3.15	3.04
		CAS(12 $\pi e$ , 12 $\pi o$ )	-1535.368049	-1535.232284	-1535.236305	3.69	3.58
EOM-CCSD		-1535.391457	-1535.247783	-1535.257238	3.91	3.65	
1,6-DPPy	GMCSCF	MRX(4)	-1071.121009	-1070.913546	-1070.978846	5.65	3.87
	GMCQDPT	MRX(4)	-1074.592114	-1074.467613	-1074.470366	3.39	3.31
2,7-DPPy	GMCSCF	MRX(4)	-1071.128369	-1070.917149	-1070.987240	5.75	3.84
	GMCQDPT	MRX(4)	-1074.592383	-1074.458462	-1074.471182	3.64	3.30



**Fig. S4** Molecular orbitals of pyrene, TPPy, 1,6-DPPy, and 2,7-DPPy obtained from the Hartee-Fock calculations.