

Operation Range Extension via Hot Spot Control for Fixed-Bed CO₂ Methanation Reactors

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A Supplementary Material

A.1 Heat transport correlations

Jacket

The heat transport coefficient for the reactor jacket k_{jac} in eqn (15) is obtained via

$$k_{\text{jac}} = \left(\frac{1}{\lambda_{\text{jac}}} \ln((R + \delta_{\text{jac}})/R) \right)^{-1},$$

to compensate radial mismatch between inner and outer jacket surface. Its impact on the overall heat transport is illustrated in [Fig. A.6](#).

Cooling channel

The heat transport inside the cooling channel (considered as an annular gap) is calculated via the correlations from Gnielinski [[Gni10](#)]. As heat transfer medium we selected the synthetic oil *Marlotherm SH* and used the corresponding thermo-physical properties as described in [[Pre10](#)]. [Fig. A.1](#) illustrates our results for the coolant Nusselt number over a broad coolant Reynolds number range and for different technically relevant coolant temperatures.

Furthermore, we assume technically relevant values for coolant velocity and hydraulic cooling channel diameter as:

$$v_{\text{cool}} = 1 - 2 \frac{\text{m}}{\text{s}} \quad \text{and} \quad d_h = 0.01 - 0.02 \text{ m}.$$

The resulting cooling regime in [Fig. A.1](#) relevant for our study is shaded in red. Consequently, two limiting cases can be identified to estimate a reasonable range for the coolant heat transfer coefficient α_{cool} :

Max. case:

$T_{\text{cool}} =$	573	K	$\Delta p_{\text{cool}} =$	0.3	bar
$d_h =$	0.02	m	$\dot{V}_{\text{cool}} =$	2.1	l/s
$v_{\text{cool}} =$	2	m/s			

$$\begin{aligned} \text{Re}_{\text{cool}} &= 8.9 \times 10^4 \Rightarrow \text{Nu}_{\text{cool}} = 560 \\ \Rightarrow \alpha_{\text{cool}} &= 2632 \frac{\text{W}}{\text{m}^2 \text{K}}, \end{aligned}$$

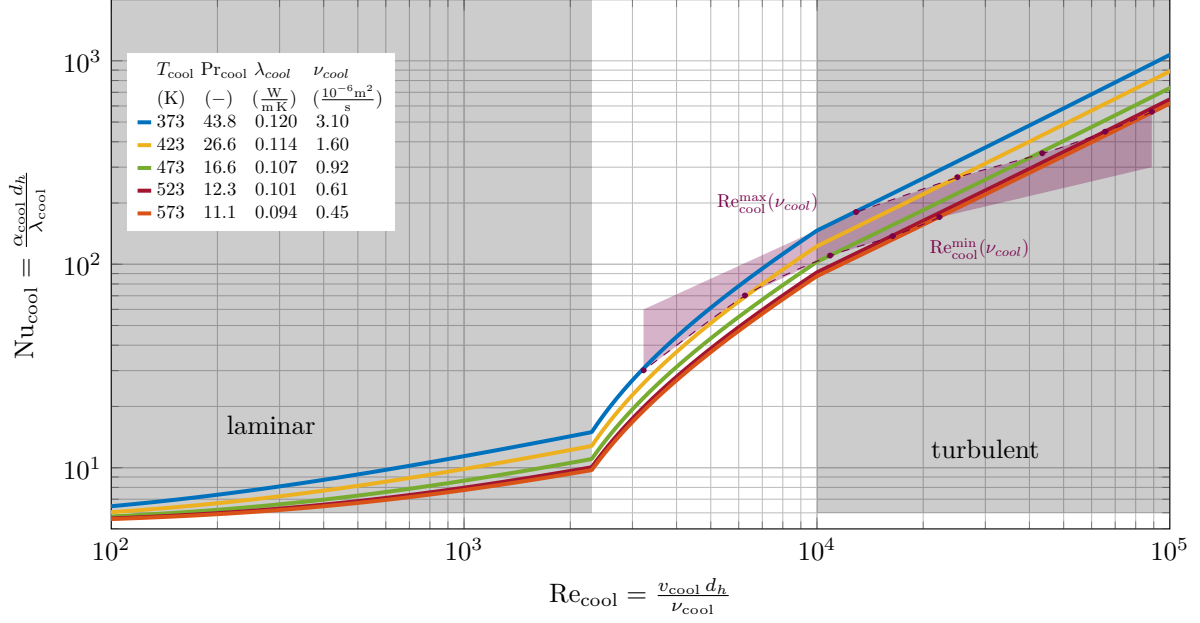


Figure A.1: Nu-Re-dependency for the heat transfer medium *Marlotherm SH*; $d_h = 0.01 \text{ m}$ and $L = 2.5 \text{ m}$; thermo-physical data from [Pre10].

Min. case:

$T_{\text{cool}} =$	373	K	$\Delta p_{\text{cool}} =$	0.04	bar
$d_h =$	0.01	m	$\dot{V}_{\text{cool}} =$	0.45	l/s
$v_{\text{cool}} =$	1	m/s			

$$\text{Re}_{\text{cool}} = 3.2 \times 10^3 \Rightarrow \text{Nu}_{\text{cool}} = 30$$

$$\Rightarrow \alpha_{\text{cool}} = 360 \frac{\text{W}}{\text{m}^2 \text{K}}.$$

Thus, the reference heat transfer coefficient α_{cool} of $500 \text{ W/m}^2 \text{K}$ used in this study is relatively moderate, so that the coolant supply is rather not a limiting factor of our proposed control approach.

A.2 Rate expressions

The rate expressions used in our model are adapted from Xu and Froment [Xu89] and Koschany et al. [Kos16], which have been implemented via the following correlations.

Xu and Froment

Xu and Froment [Xu89] considered three rate equations including the water-gas-shift (WGS) reaction:

$$r_1 = \frac{k_1}{p_{H_2}^{2.5}} \left(p_{CH_4} p_{H_2O} - \frac{p_{H_2}^3 p_{CO}}{K_1} \right) / \text{DEN}^2, \quad (\text{A.1})$$

$$r_2 = \frac{k_2}{p_{H_2}} \left(p_{CO} p_{H_2O} - \frac{p_{H_2} p_{CO_2}}{K_2} \right) / \text{DEN}^2, \quad (\text{A.2})$$

$$r_3 = \frac{k_3}{p_{H_2}^{3.5}} \left(p_{CH_4} p_{H_2O}^2 - \frac{p_{H_2}^4 p_{CO_2}}{K_3} \right) / \text{DEN}^2, \quad (\text{A.3})$$

where p_α is the partial pressure of the respective component in bar and DEN is a dimensionless parameter defined as

$$\text{DEN} = 1 + K_{CO} p_{CO} + K_{H_2} p_{H_2} + K_{CH_4} p_{CH_4} + \frac{K_{H_2O} p_{H_2O}}{p_{H_2}}.$$

K_α is the respective adsorption constant for CH_4 , CO , H_2O and H_2 and b_β are rate coefficients exponentially depending on temperature via:

$$K_\alpha = \mathcal{A}_\alpha \exp\left(-\frac{\Delta H_\alpha}{\mathcal{R}T}\right),$$

$$k_\beta = \mathcal{A}_\beta \exp\left(-\frac{E_\beta}{\mathcal{R}T}\right).$$

\mathcal{A}_β , E_β , \mathcal{A}_α , ΔH_α are constant kinetic parameters stated in [Tab. A.1](#).

Table A.1: Kinetic parameters for [Eqs. \(A.1\) to \(A.3\)](#); each pre-exponential factor contains a multiplier of 1.225 (see Xu and Froment [\[Xu89\]](#))

α	Formula	\mathcal{A}_α	$[\mathcal{A}_\alpha]$	ΔH_α	$[\Delta H_\alpha]$	β	\mathcal{A}_β	$[\mathcal{A}_\beta]$	E_β	$[E_\beta]$
1	CH_4	8.15×10^{-4}	bar^{-1}	-38.28	$\frac{\text{kJ}}{\text{mol}}$	1	5.176×10^{15}	$\frac{\text{kmol bar}^{0.5}}{\text{kg}_{\text{cat}} \text{ h}}$	240.10	$\frac{\text{kJ}}{\text{mol}}$
2	CO	10.08×10^{-5}	bar^{-1}	-70.65	$\frac{\text{kJ}}{\text{mol}}$	2	2.395×10^6	$\frac{\text{kmol}}{\text{kg}_{\text{cat}} \text{ h bar}}$	67.13	$\frac{\text{kJ}}{\text{mol}}$
4	H_2O	2.17×10^{-5}		88.68	$\frac{\text{kJ}}{\text{mol}}$	3	1.250×10^{15}	$\frac{\text{kmol bar}^{0.5}}{\text{kg}_{\text{cat}} \text{ h}}$	243.90	$\frac{\text{kJ}}{\text{mol}}$
5	H_2	7.50×10^{-9}	bar^{-1}	-82.90	$\frac{\text{kJ}}{\text{mol}}$					

The temperature dependent equilibrium constants K_1 , K_2 and K_3 are based on the Gibbs reaction energy (STP) as shown in Poling et al. [\[Pol01\]](#).

Finally, a unit conversion is required to adequately implement these rate equations to eqn (4) and (5):

$$\tilde{r}_\beta = r_\beta \rho_{\text{cat}} 1000/3600.$$

Koschany et al.

Koschany et al. [\[Kos16\]](#) exclusively considered CO_2 methanation to describe they experimental kinetic data. The corresponding rate equation is:

$$r_{\text{meth}} = k p_{\text{CO}_2}^{0.5} p_{\text{H}_2}^{0.5} \left(1 - \frac{p_{\text{CH}_4} p_{\text{H}_2\text{O}}^2}{K_{\text{eq}} p_{\text{CO}_2} p_{\text{H}_2}^4}\right) / \text{DEN}^2, \quad (\text{A.4})$$

$$\text{DEN} = 1 + K_{\text{OH}} \frac{p_{\text{H}_2\text{O}}}{p_{\text{H}_2}^{0.5}} + K_{\text{H}_2} p_{\text{H}_2}^{0.5} + K_{\text{mix}} p_{\text{CO}_2}^{0.5}, \quad (\text{A.5})$$

which is determined by the following correlations for rate coefficient k , adsorption constant K_x and equilibrium constant K_{eq} :

$$k = k_{0,\text{ref}} \exp\left(\frac{E_A}{\mathcal{R}} \left(\frac{1}{T_{\text{ref}}} - \frac{1}{T}\right)\right), \quad (\text{A.6})$$

$$K_x = K_{x,0,\text{ref}} \exp\left(\frac{\Delta H_x}{\mathcal{R}} \left(\frac{1}{T_{\text{ref}}} - \frac{1}{T}\right)\right), \quad (\text{A.7})$$

$$K_{\text{eq}} = 137 T^{-3.998} \exp\left(\frac{158.7 \text{ kJ/mol}}{\mathcal{R} T}\right). \quad (\text{A.8})$$

Again, a unit conversion is required to adequately implement this rate equation to eqn (4) and (5):

$$\tilde{r}_{\text{meth}} = r_{\text{meth}} \rho_{\text{cat}} 1000.$$

Table A.2: Kinetic parameters for Eqs. (A.6) to (A.8); (see Koschany et al. [Kos16])

T_{ref}	550	K
$k_{0,\text{ref}}$	3.46e-4	mol/(bar s g _{cat})
E_A	77.5	kJ/mol
$K_{\text{OH},0,\text{ref}}$	0.5	bar ^{-0.5}
ΔH_{OH}	22.4	kJ/mol
$K_{\text{H}_2,0,\text{ref}}$	0.44	bar ^{-0.5}
ΔH_{H_2}	-6.2	kJ/mol
$K_{\text{mix},0,\text{ref}}$	0.88	bar ^{-0.5}
ΔH_{mix}	-10	kJ/mol

A.3 Reference case details

In order to enable a simple replication of our results, we outline detailed information on the reference reactor setting in Table 1 and the corresponding steady state assuming a coolant temperature of $T_{\text{cool}} = 550$ K. Furthermore, surface plots illustrate the finite volume mesh density and provide a clearer visualization of our chosen PDE discretization.

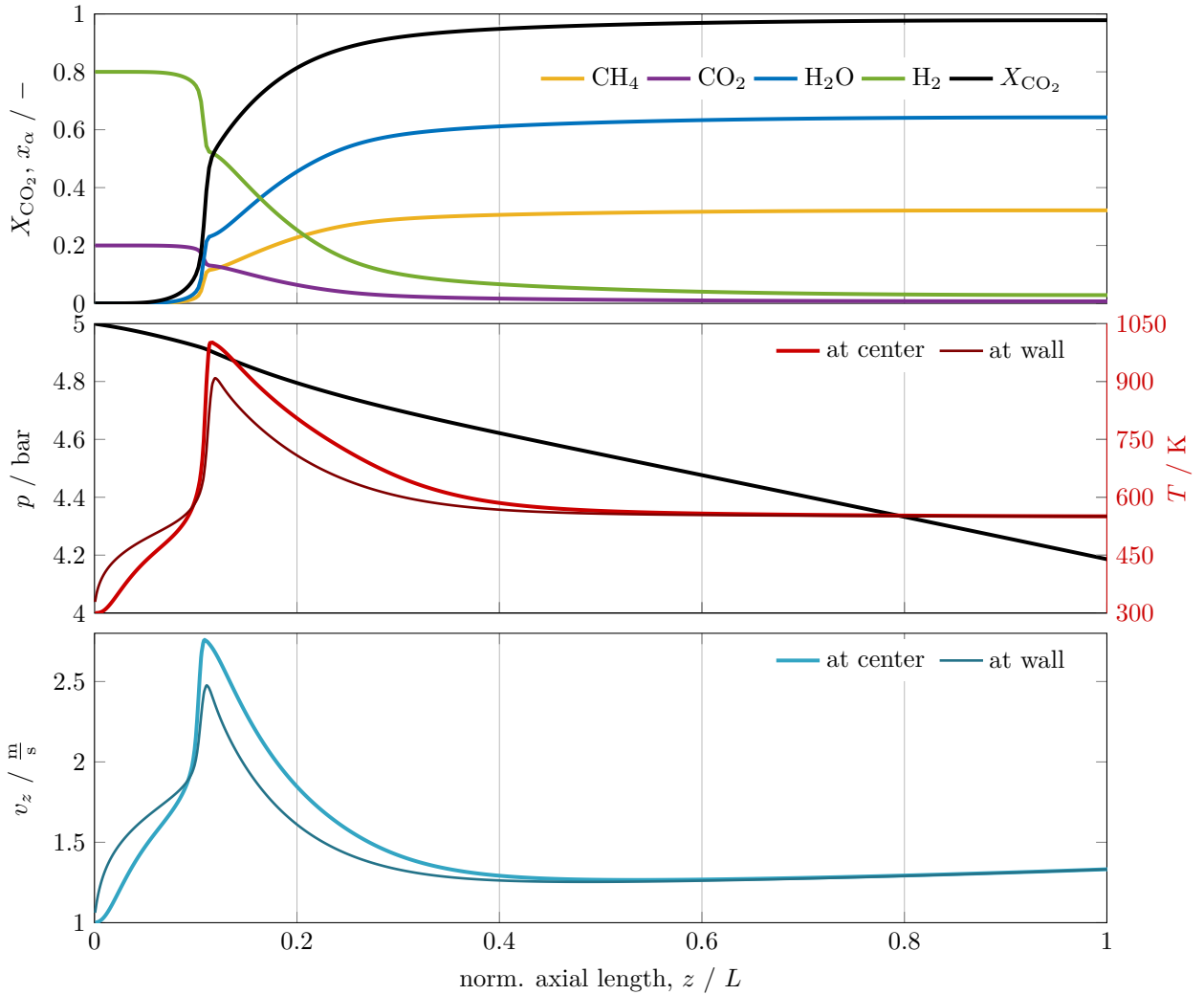


Figure A.2: Conversion, composition, temperature, pressure and velocity changes along the entire reactor length; reactor setting according to Table 1 and at $T_{\text{cool}} = 550$ K

Reaction

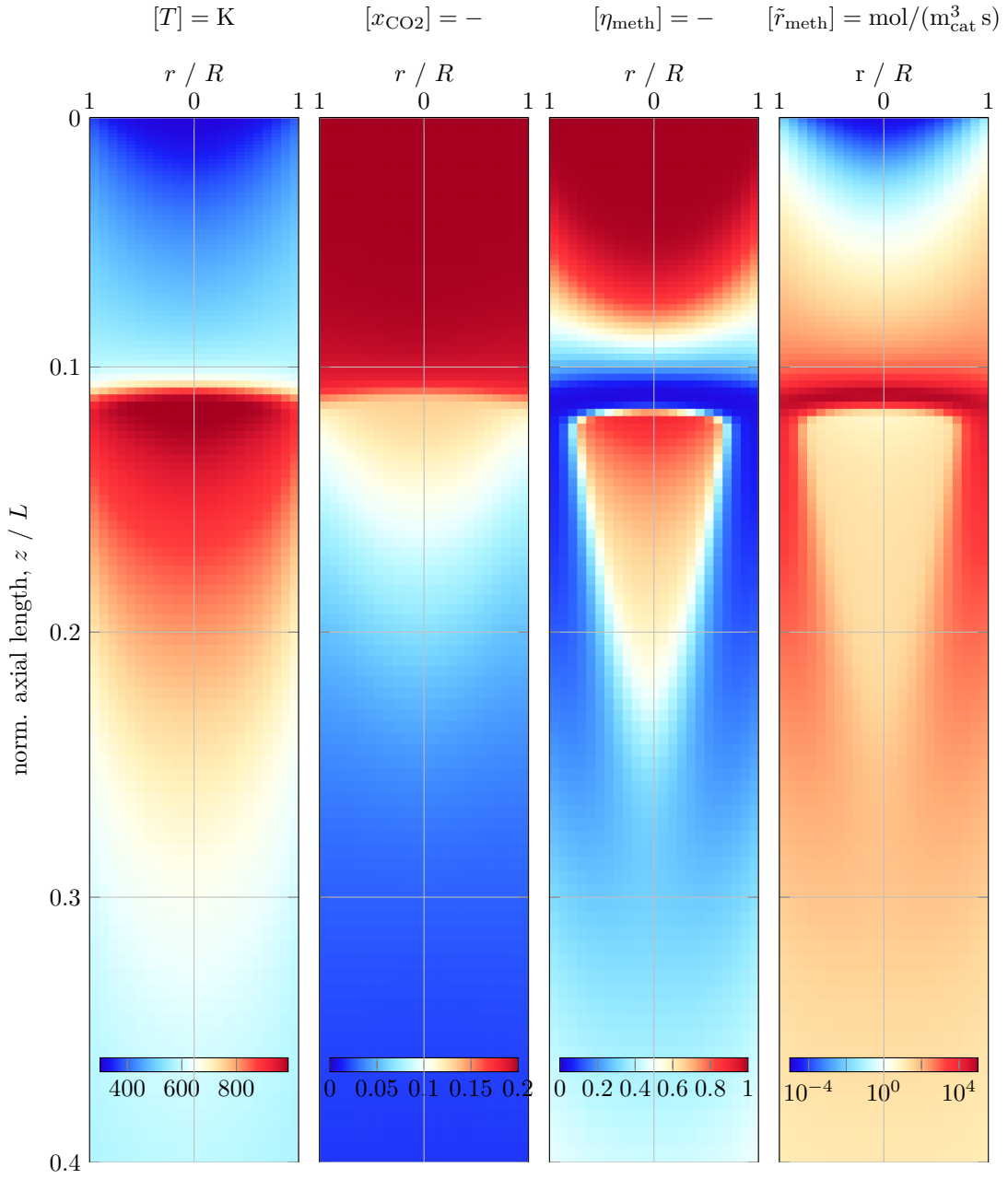


Figure A.3: Temperature, CO_2 -composition, effectiveness factor and reaction rate changes around the reactive zone; reactor setting according to Table 1 and at $T_{\text{cool}} = 550 \text{ K}$

Heat and mass transport

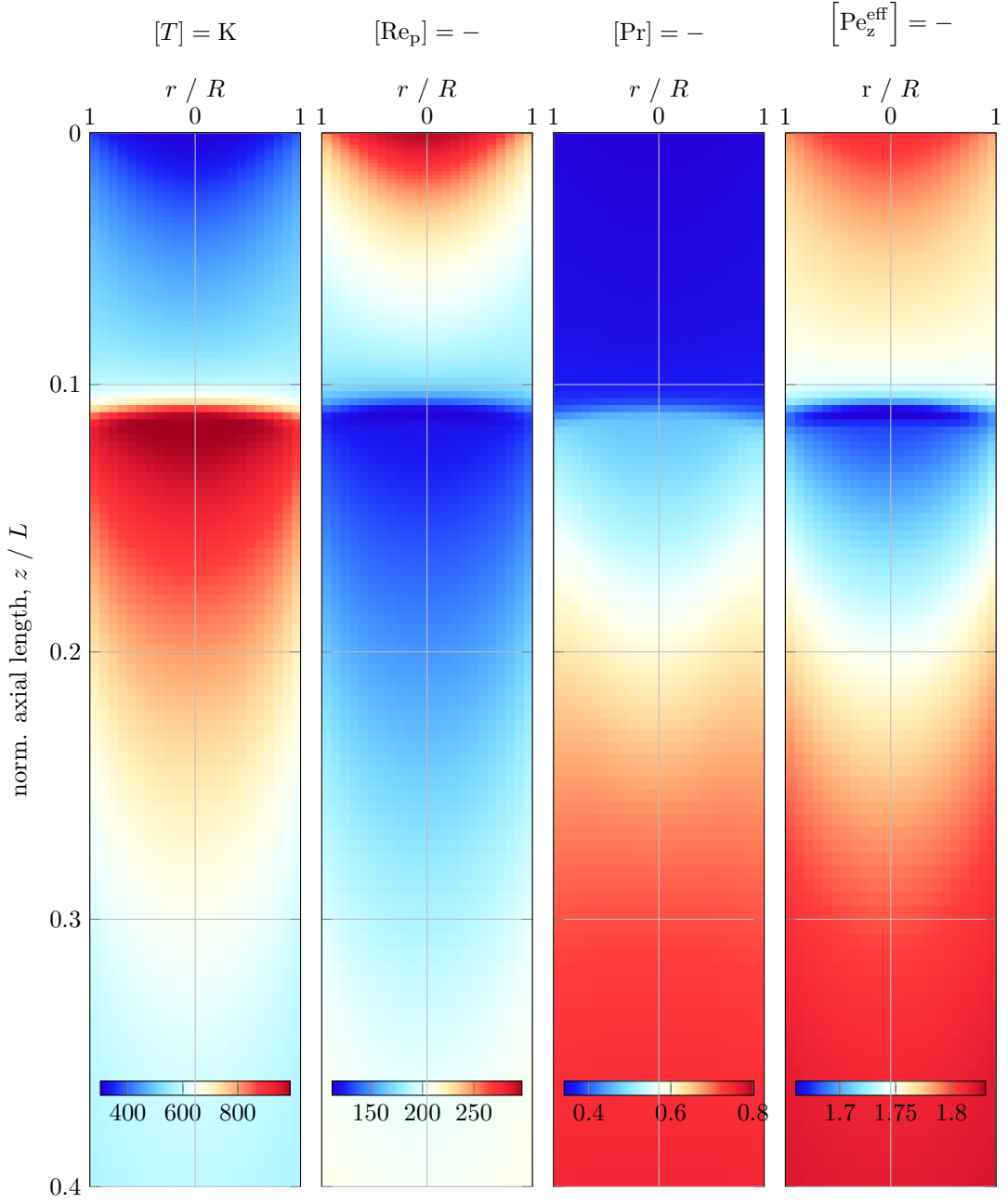


Figure A.4: Temperature, Reynolds number, Prandtl number and effective axial Péclet number around the reactive zone; reactor setting according to Table 1 and at $T_{cool} = 550$ K

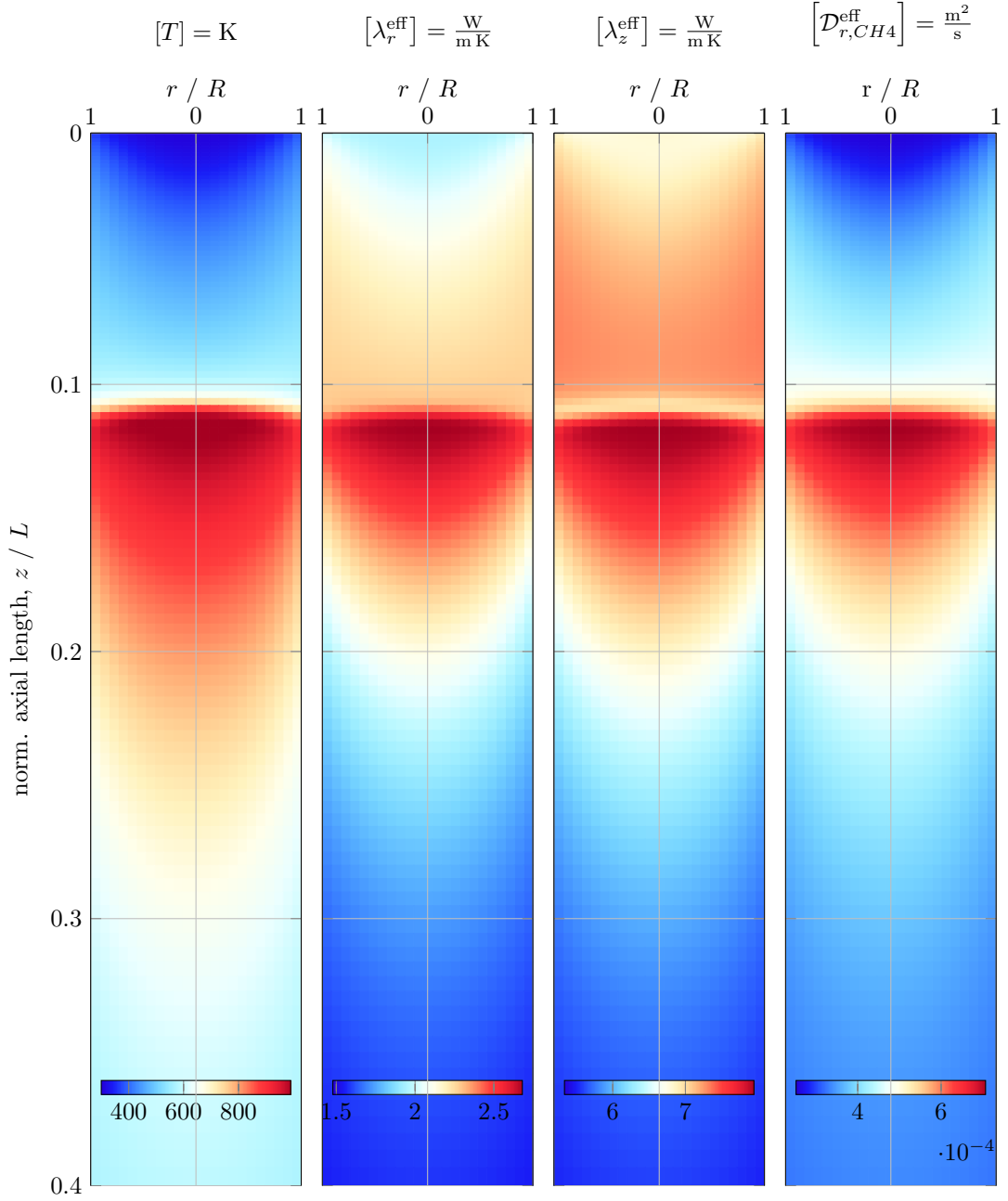


Figure A.5: Temperature, effective radial conductivity, effective axial conductivity and effective CH_4 diffusion coefficient around the reactive zone; reactor setting according to Table 1 and at $T_{\text{cool}} = 550 \text{ K}$

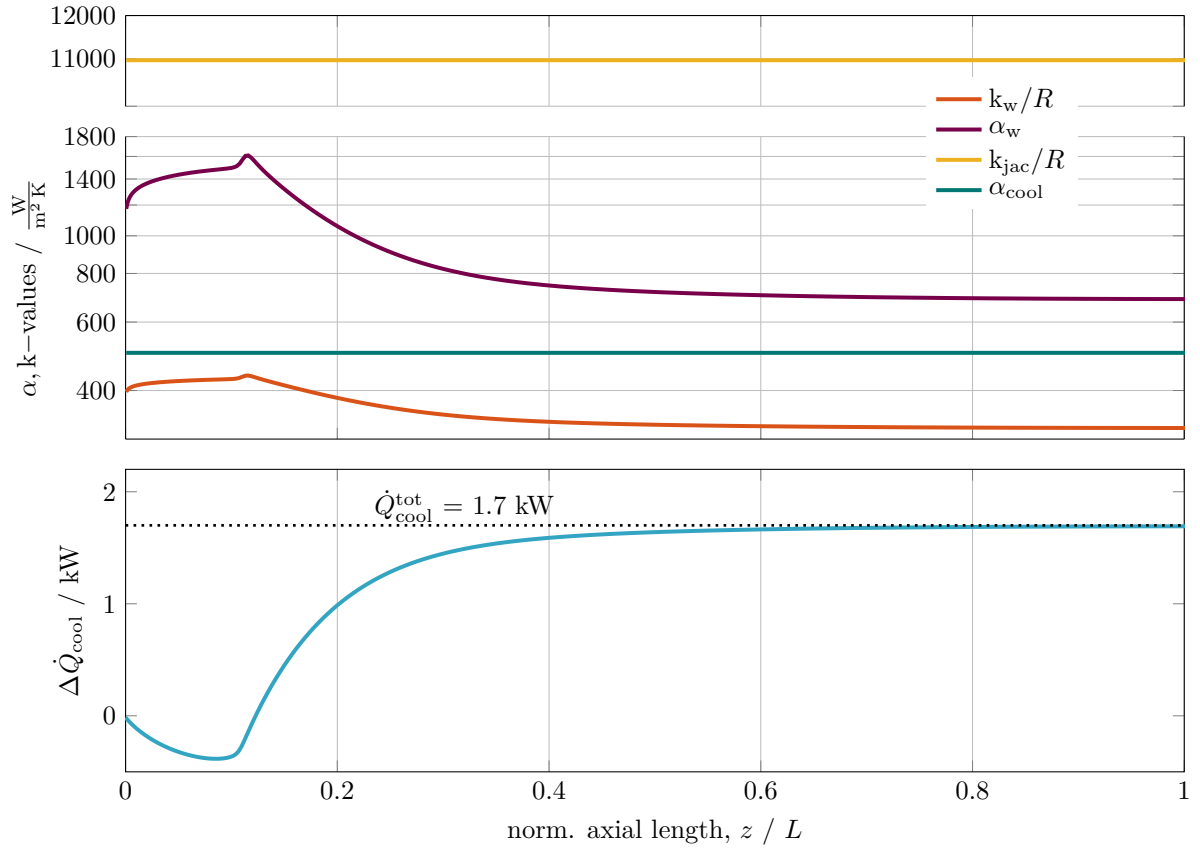


Figure A.6: Heat transport coefficients and cumulative heat transfer from reactor to coolant along the entire reactor length; reactor setting according to Table 1 and at $T_{cool} = 550 \text{ K}$

A.4 Influence of axial heat dispersion

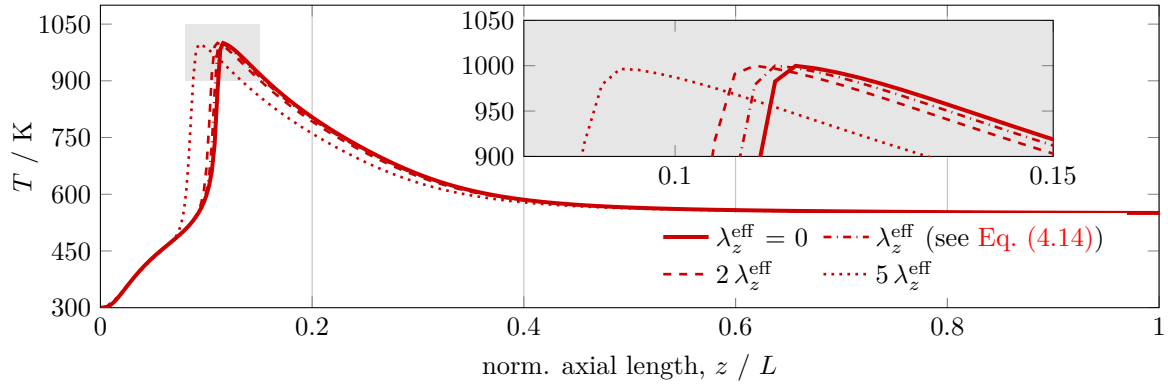


Figure A.7: Influence of axial heat dispersion on steady-state temperature profile (at center); reactor setting according to Table 1 and at $T_{\text{cool}} = 550$ K

References

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- [Kos16] F. Koschany et al. “On the kinetics of the methanation of carbon dioxide on coprecipitated $\text{NiAl}(\text{O})_x$ ”. In: *Applied Catalysis B: Environmental* 181 (2016), pp. 504–516 (cit. on pp. 2–4).
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