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## Supplementary information: Geometric effects in random assemblies of ellipses

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1. Voronoi tessellation of randomly assembled ellipses at packing fraction  $\phi_g = 0.2$ .
2. Voronoi tessellation of randomly assembled ellipses at packing fraction  $\phi_g = 0.35$ .
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17. Distributions and standardised distributions of selected morphological measures for all studied ellipse assemblies.
18. Details of fits of gamma distribution to the cell elongation measure.
19. Comparison between shape-based and standard Voronoi tessellations.

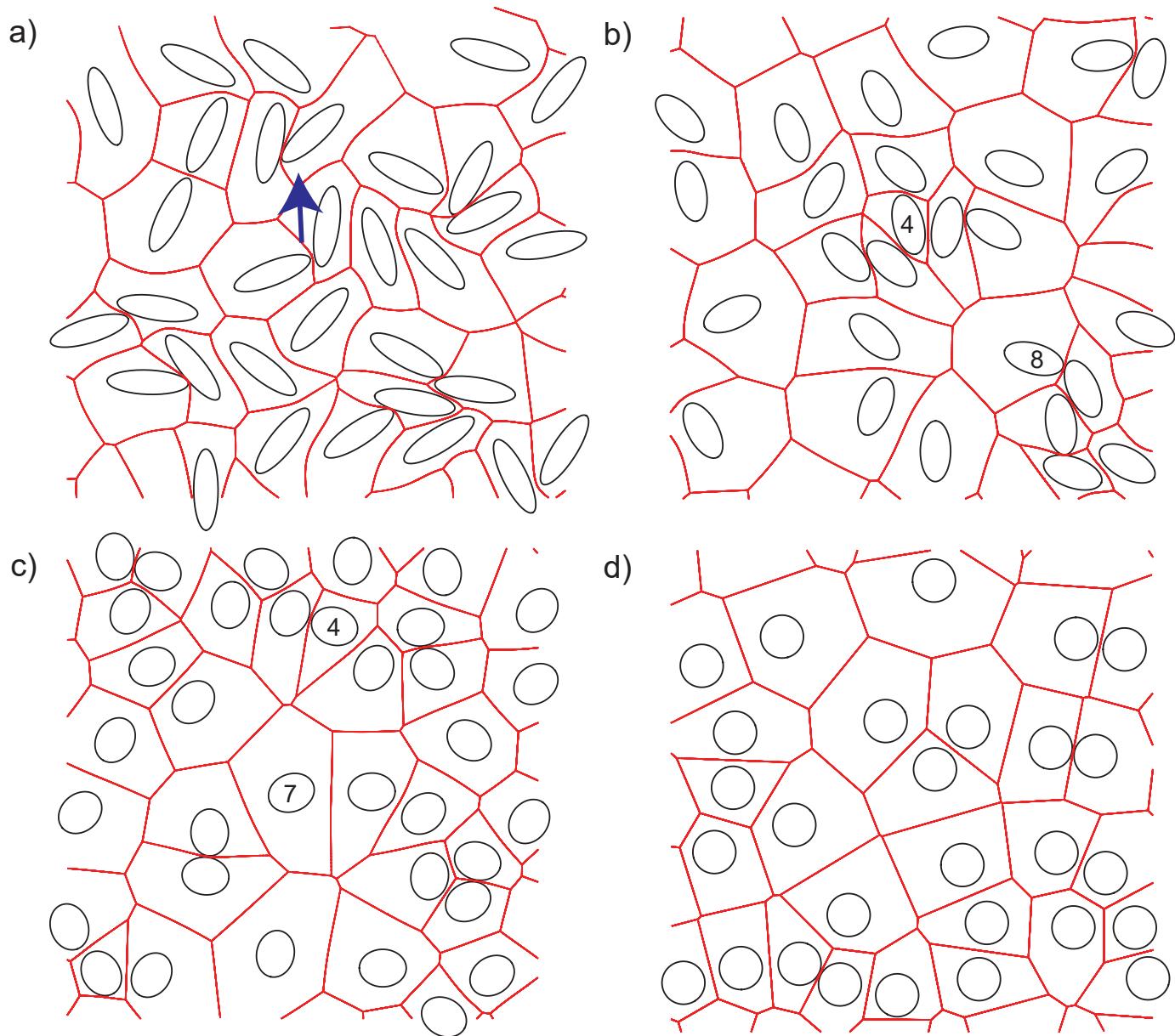
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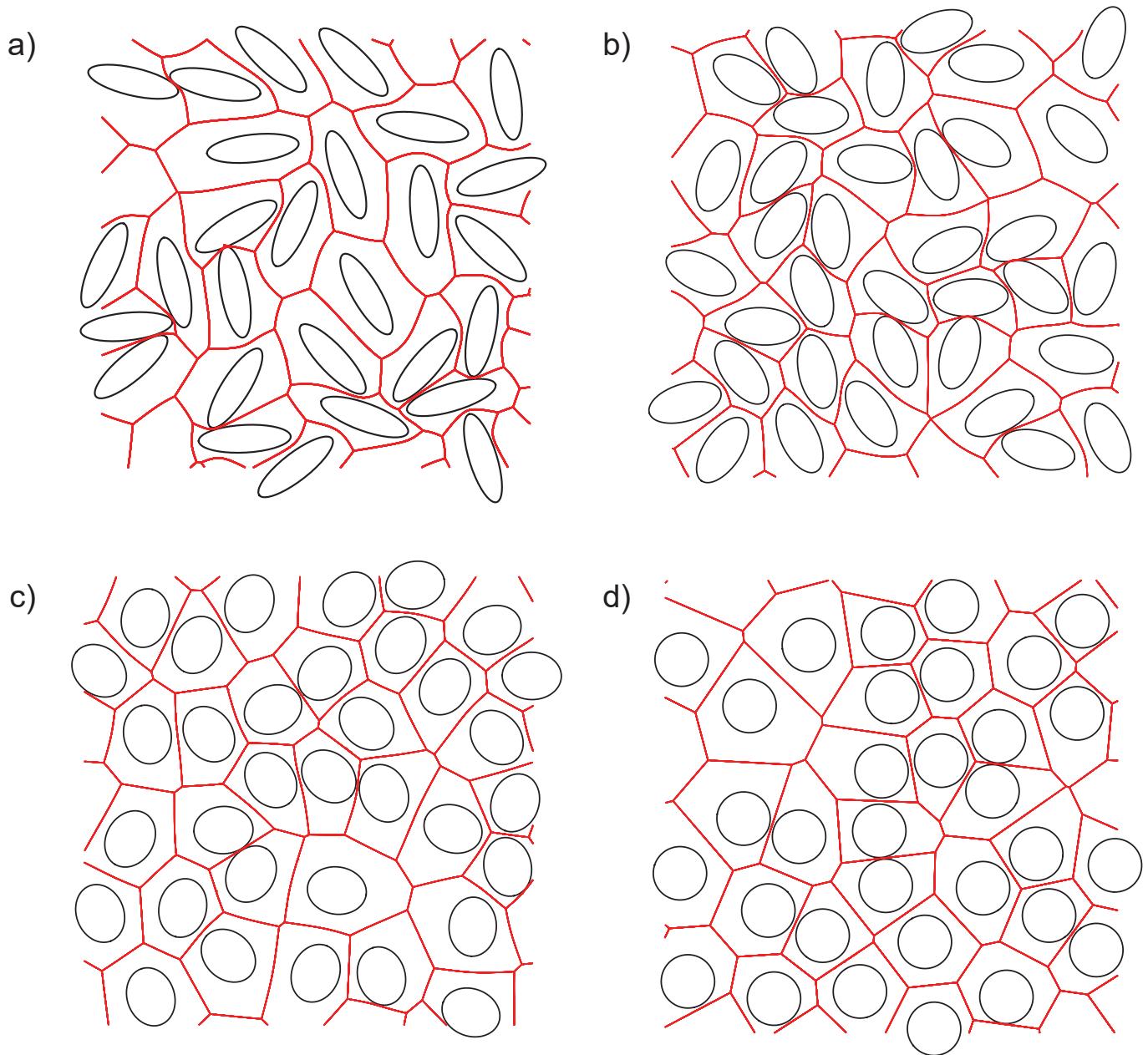
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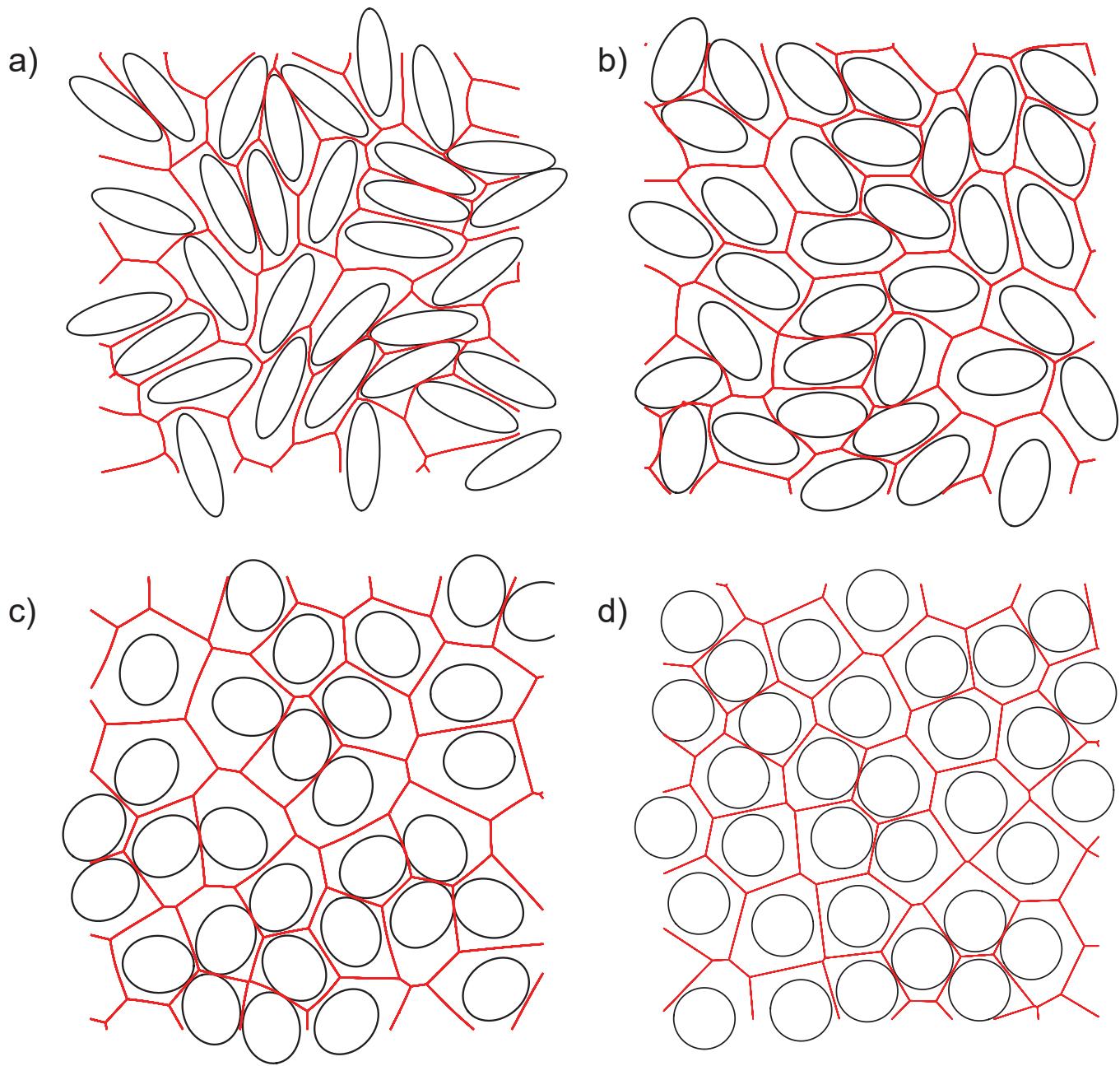
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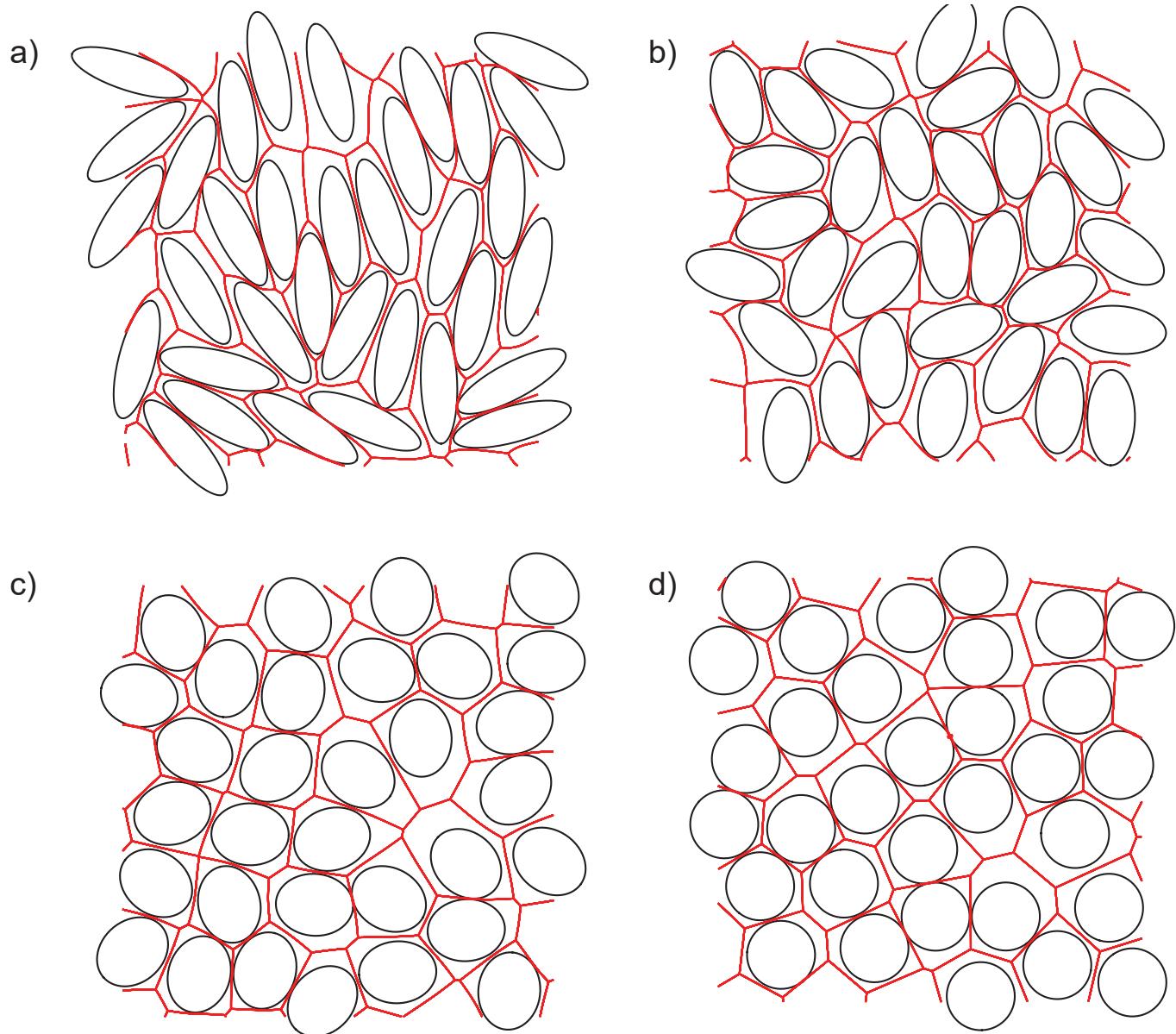
**Fig. 1** Voronoi tessellation of randomly assembled ellipses at packing fraction  $\phi_g = 0.2$ . **a)**  $e = 3.33$  **b)**  $e = 2$ , **c)**  $e = 1.25$ , **d)**  $e = 1$



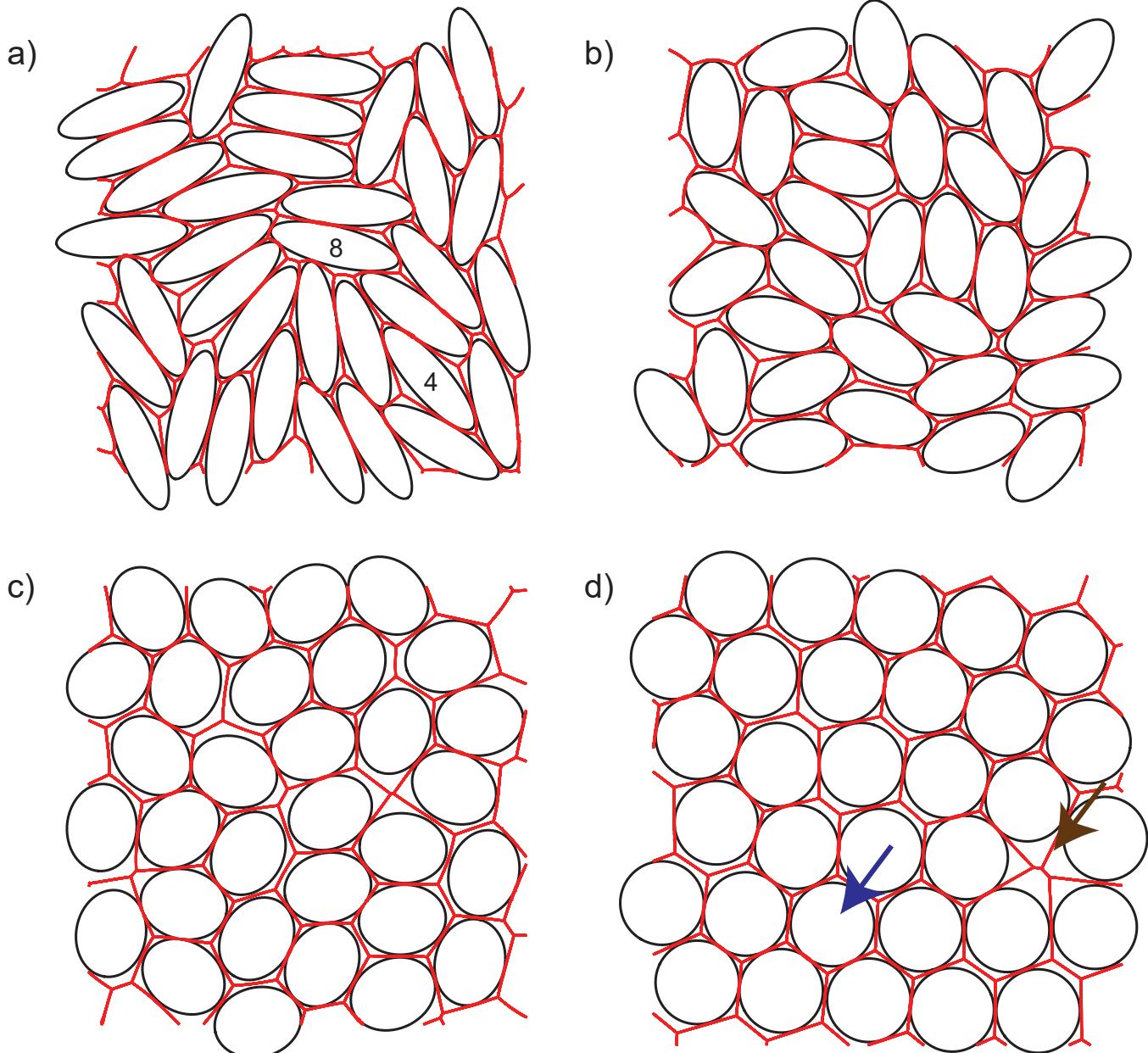
**Fig. 2** Voronoi tessellation of randomly assembled ellipses at packing fraction  $\phi_g = 0.35$ . a)  $e = 3.33$  b)  $e = 2$ , c)  $e = 1.25$ , d)  $e = 1$



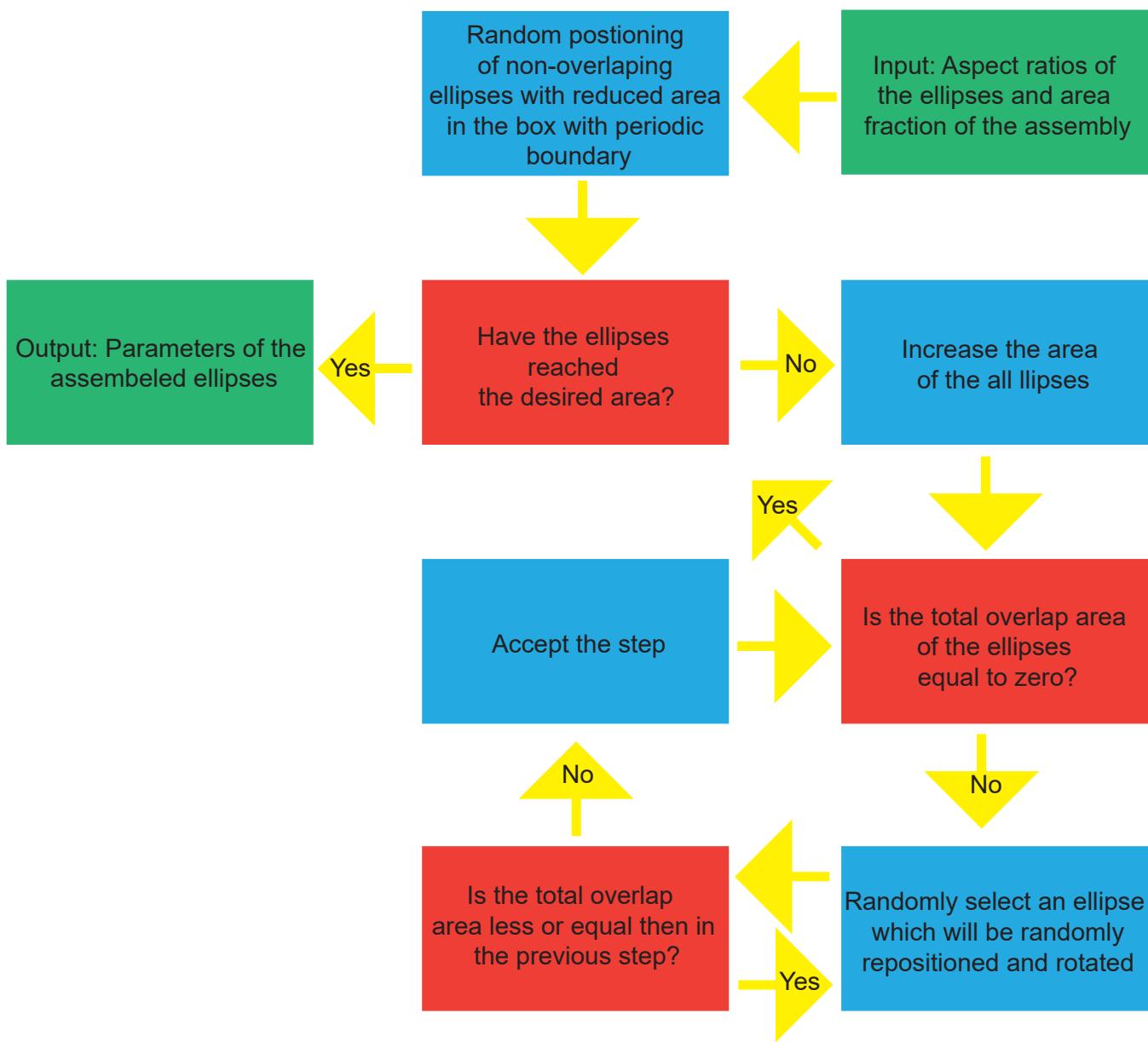
**Fig. 3** Voronoi tessellation of randomly assembled ellipses at packing fraction  $\phi_g = 0.5$ . a)  $e = 3.33$  b)  $e = 2$ , c)  $e = 1.25$ , d)  $e = 1$



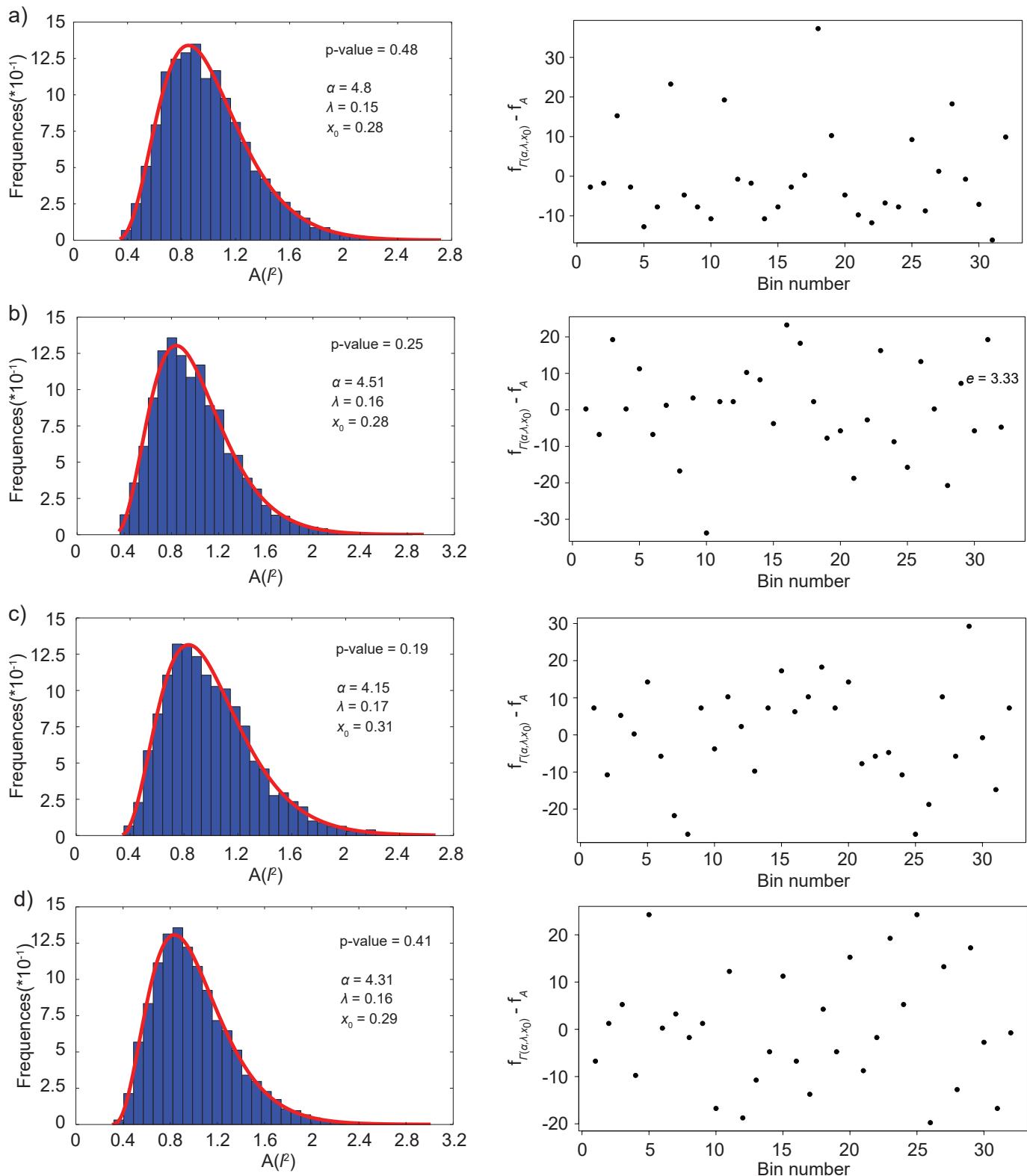
**Fig. 4** Voronoi tessellation of randomly assembled ellipses at packing fraction  $\phi_g = 0.65$ . a)  $e = 3.33$  b)  $e = 2$ , c)  $e = 1.25$ , d)  $e = 1$



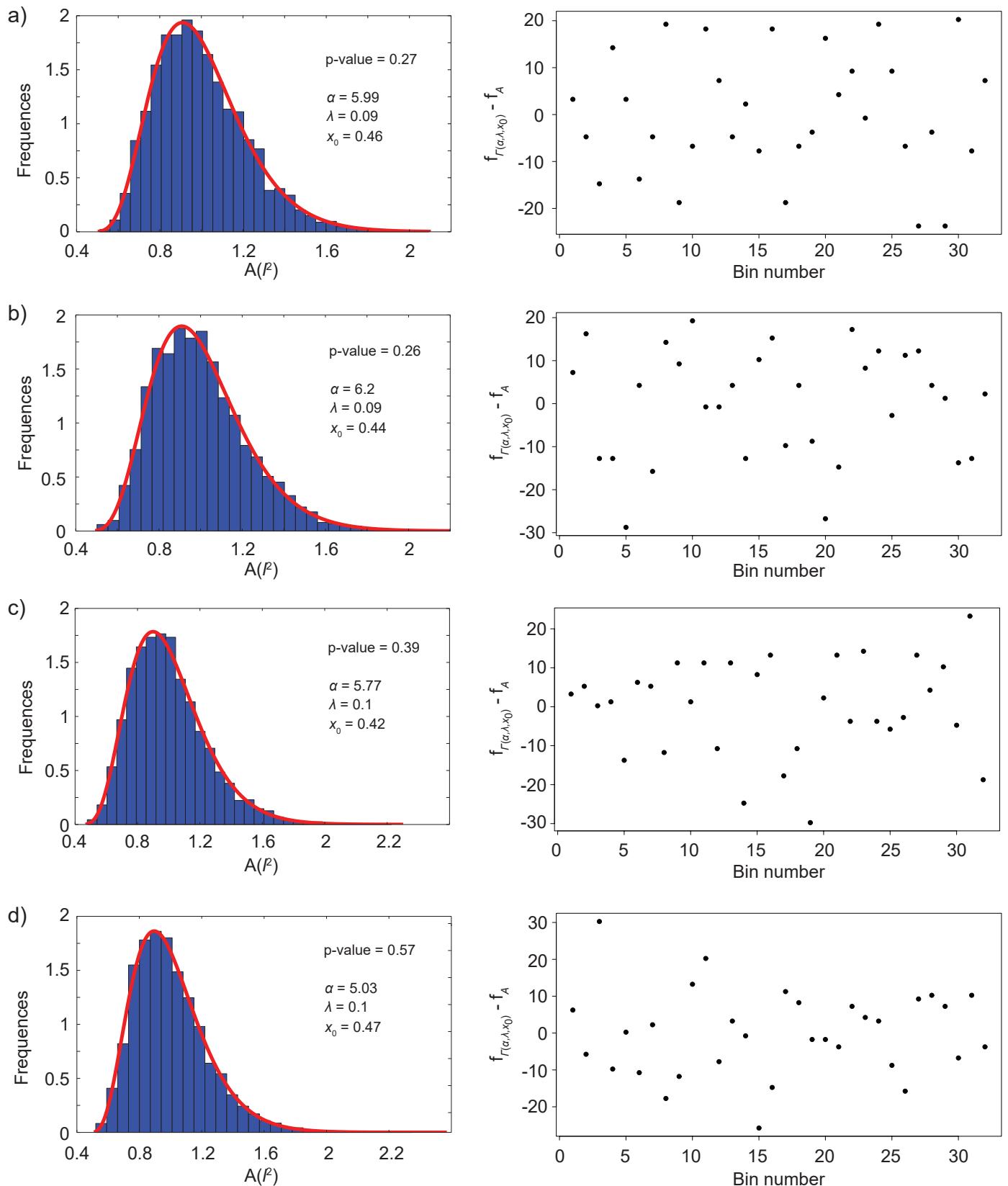
**Fig. 5** Voronoi tessellation of randomly assembled ellipses at packing fraction  $\phi_g = 0.8$ . a)  $e = 3.33$  b)  $e = 2$ , c)  $e = 1.25$ , d)  $e = 1$



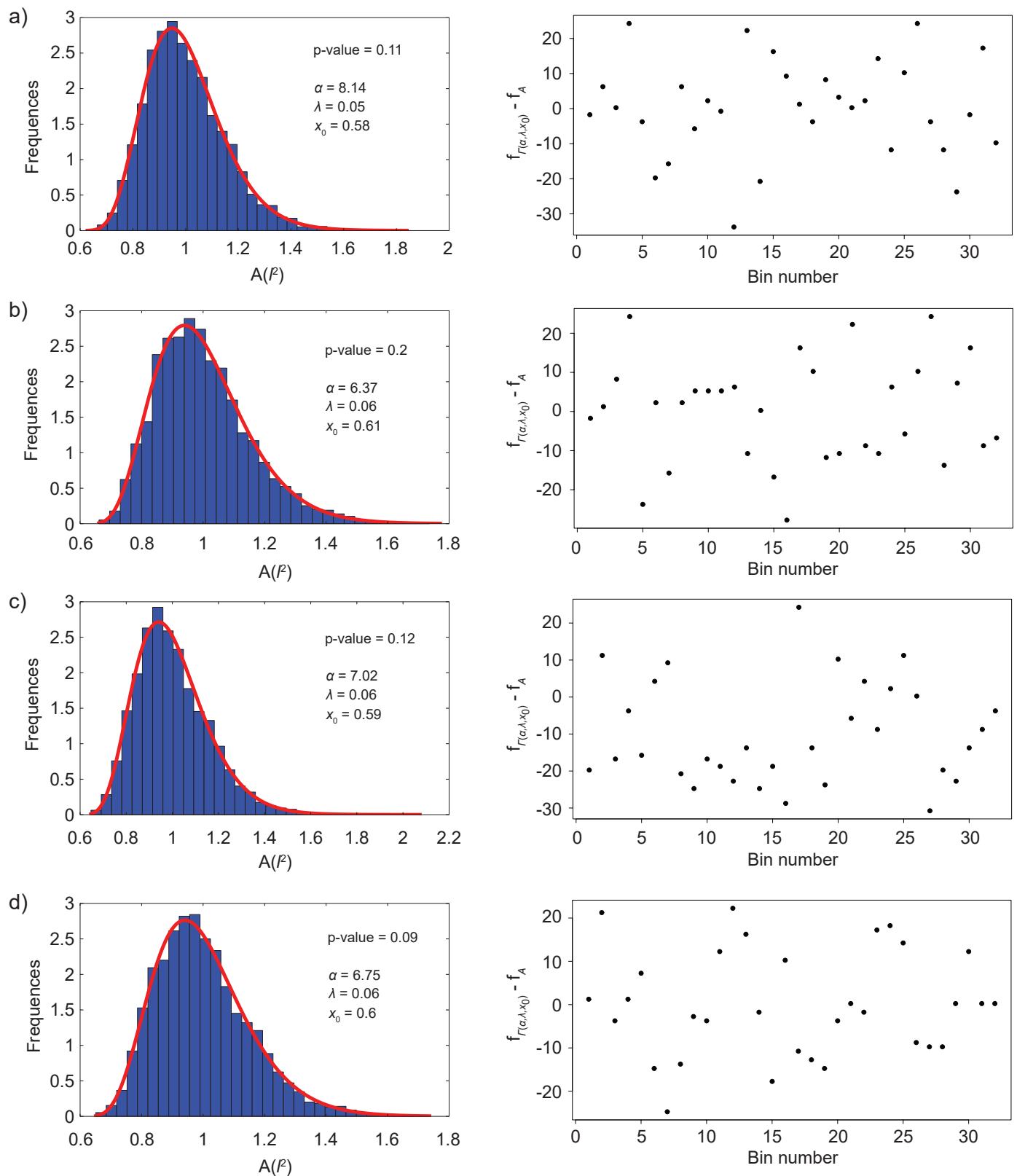
**Fig. 6** Flowchart of the algorithm used to generate assemblies.



**Fig. 7** Fits of gamma distribution to the cell area measure at packing fraction  $\phi_g = 0.2$ . Left figure shows fit together with p-value of  $\chi^2$  test and parameters of fitted distribution. Right figure shows difference between estimated(fitted) frequencies and observed frequencies for each bin in  $\chi^2$  test.  
 a)  $e = 3.33$  b)  $e = 2$ , c)  $e = 1.25$ , d)  $e = 1$

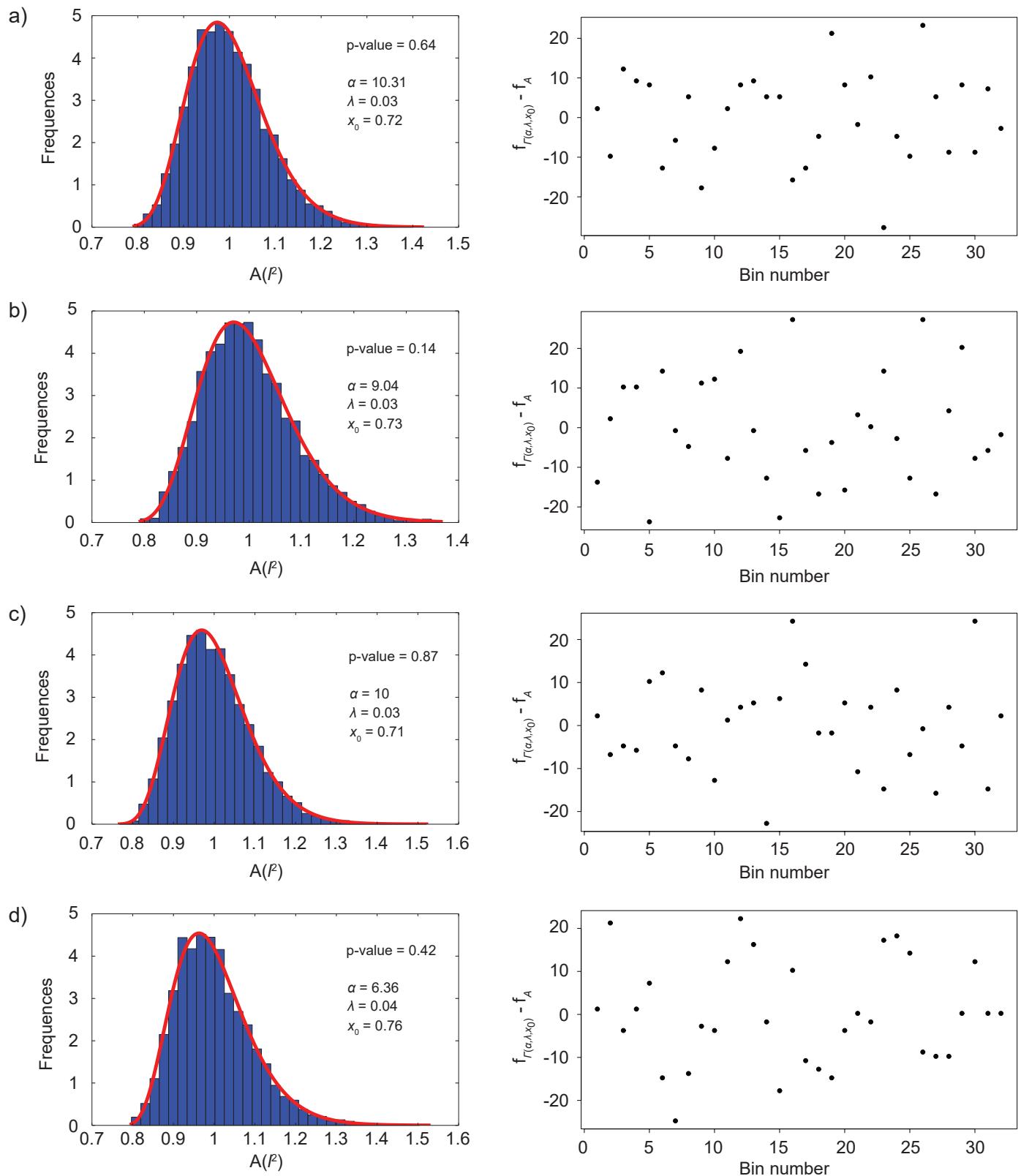


**Fig. 8** Fits of gamma distribution to the cell area measure at packing fraction  $\phi_g = 0.35$ . Left figure shows fit together with  $\chi^2$  test and parameters of fitted distribution. Right figure shows difference between estimated(fitted) frequencies and observed frequencies for each bin in  $\chi^2$  test.  
 a)  $e = 3.33$  b)  $e = 2$ , c)  $e = 1.25$ , d)  $e = 1$

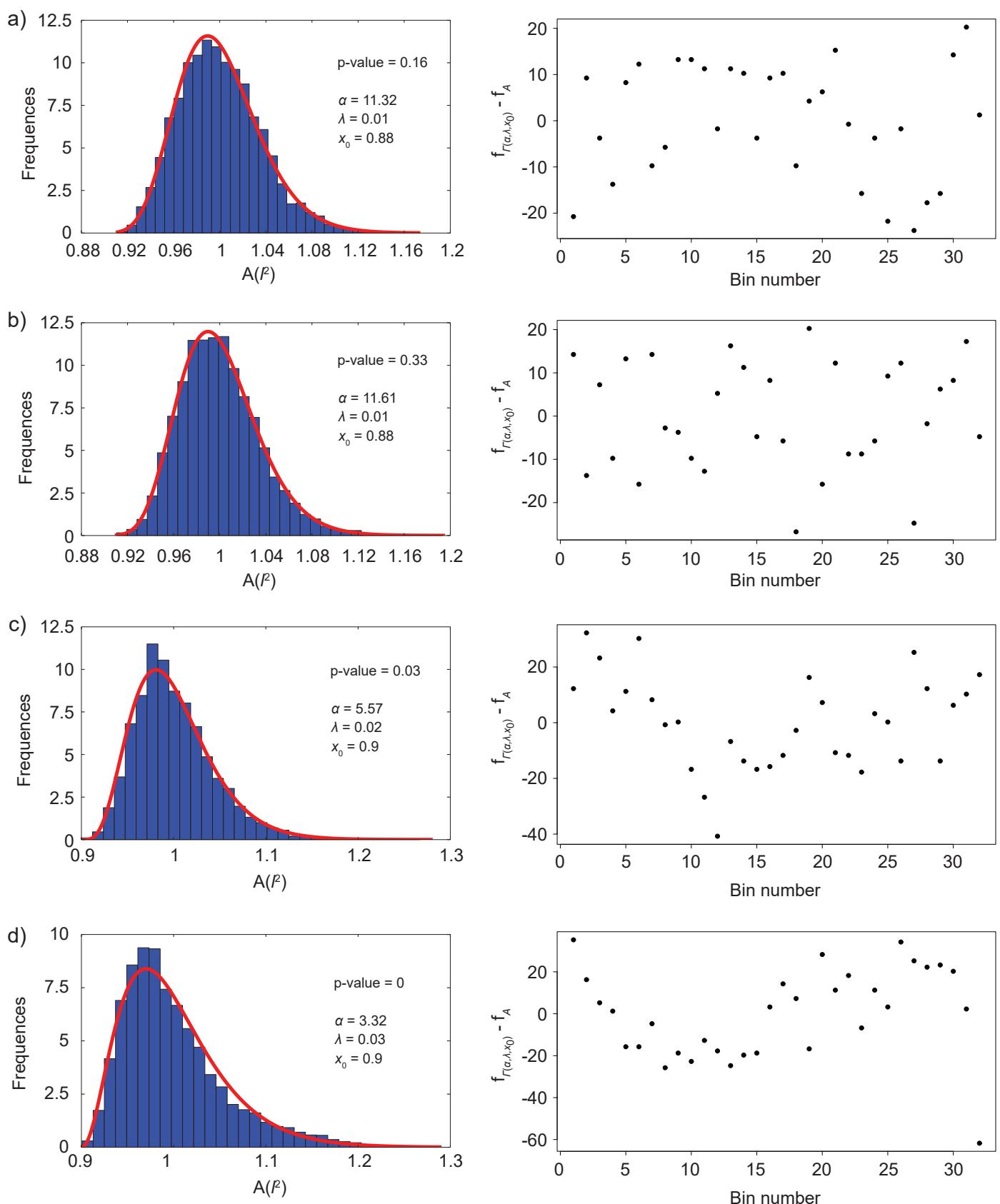


**Fig. 9** Fits of gamma distribution to the cell area measure at packing fraction  $\phi_g = 0.5$ . Left figure shows fit together with p-value of  $\chi^2$  test and parameters of fitted distribution. Right figure shows difference between estimated(fitted) frequencies and observed frequencies for each bin in  $\chi^2$  test.

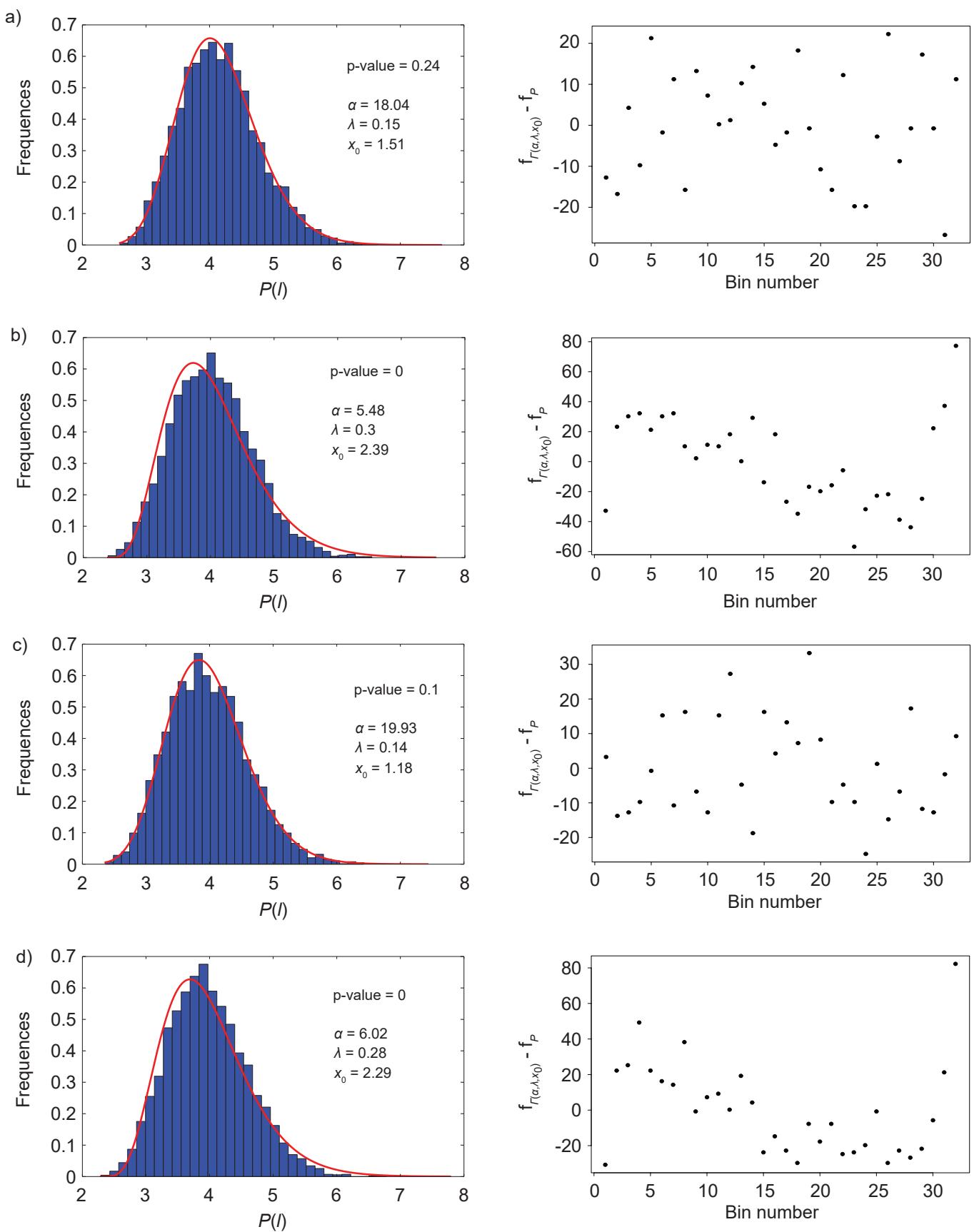
a)  $e = 3.33$  b)  $e = 2$ , c)  $e = 1.25$ , d)  $e = 1$



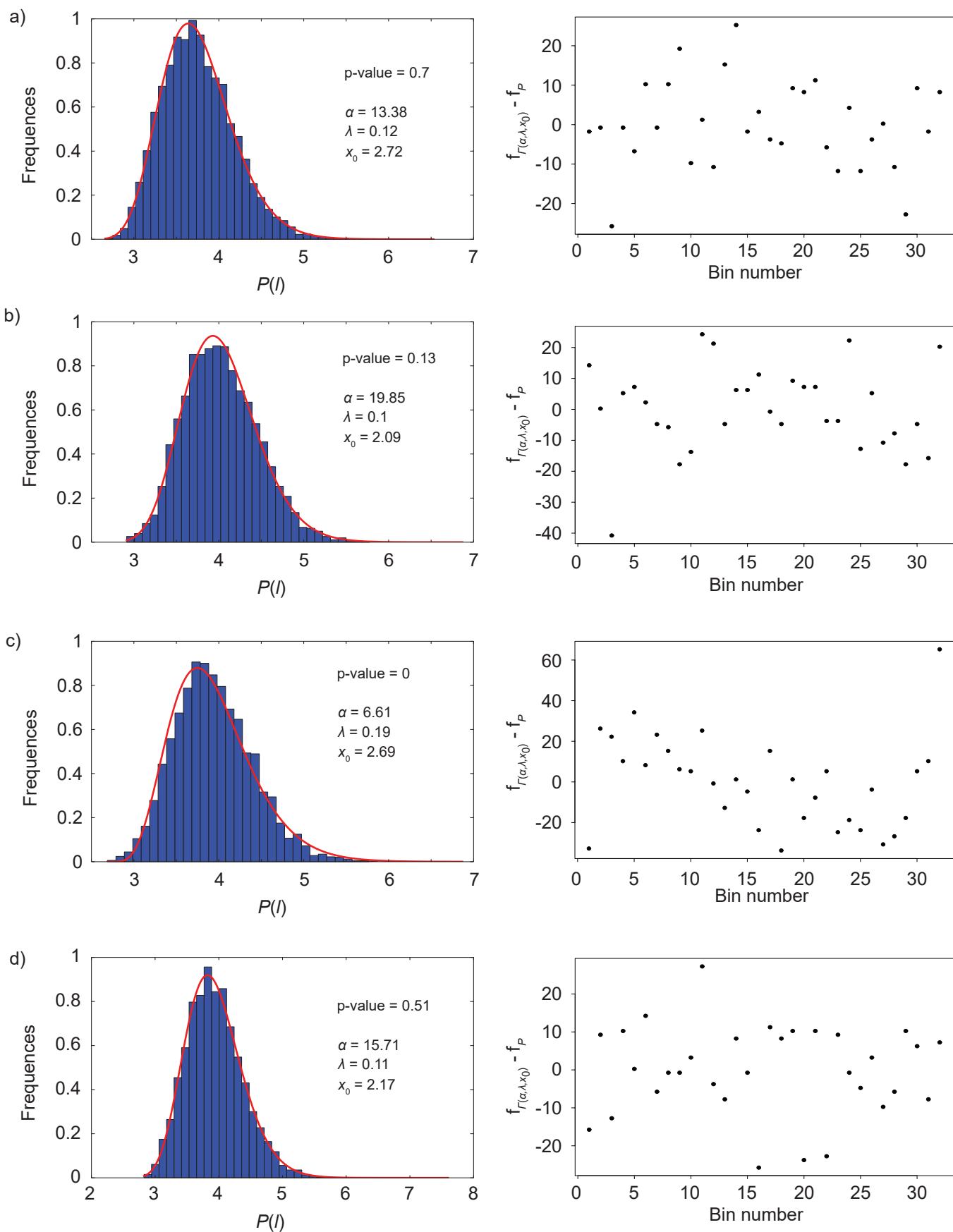
**Fig. 10** Fits of gamma distribution to the cell area measure at packing fraction  $\phi_g = 0.65$ . Left figure shows fit together with p-value of  $\chi^2$  test and parameters of fitted distribution. Right figure shows difference between estimated(fitted) frequencies and observed frequencies for each bin in  $\chi^2$  test.  
a)  $e = 3.33$  b)  $e = 2$ , c)  $e = 1.25$ , d)  $e = 1$



**Fig. 11** Fits of gamma distribution to the cell area measure at packing fraction  $\phi_g = 0.8$ . Left figure shows fit together with p-value of  $\chi^2$  test and parameters of fitted distribution. Right figure shows difference between estimated(fitted) frequencies and observed frequencies for each bin in  $\chi^2$  test.  
 a)  $e = 3.33$  b)  $e = 2$ , c)  $e = 1.25$ , d)  $e = 1$

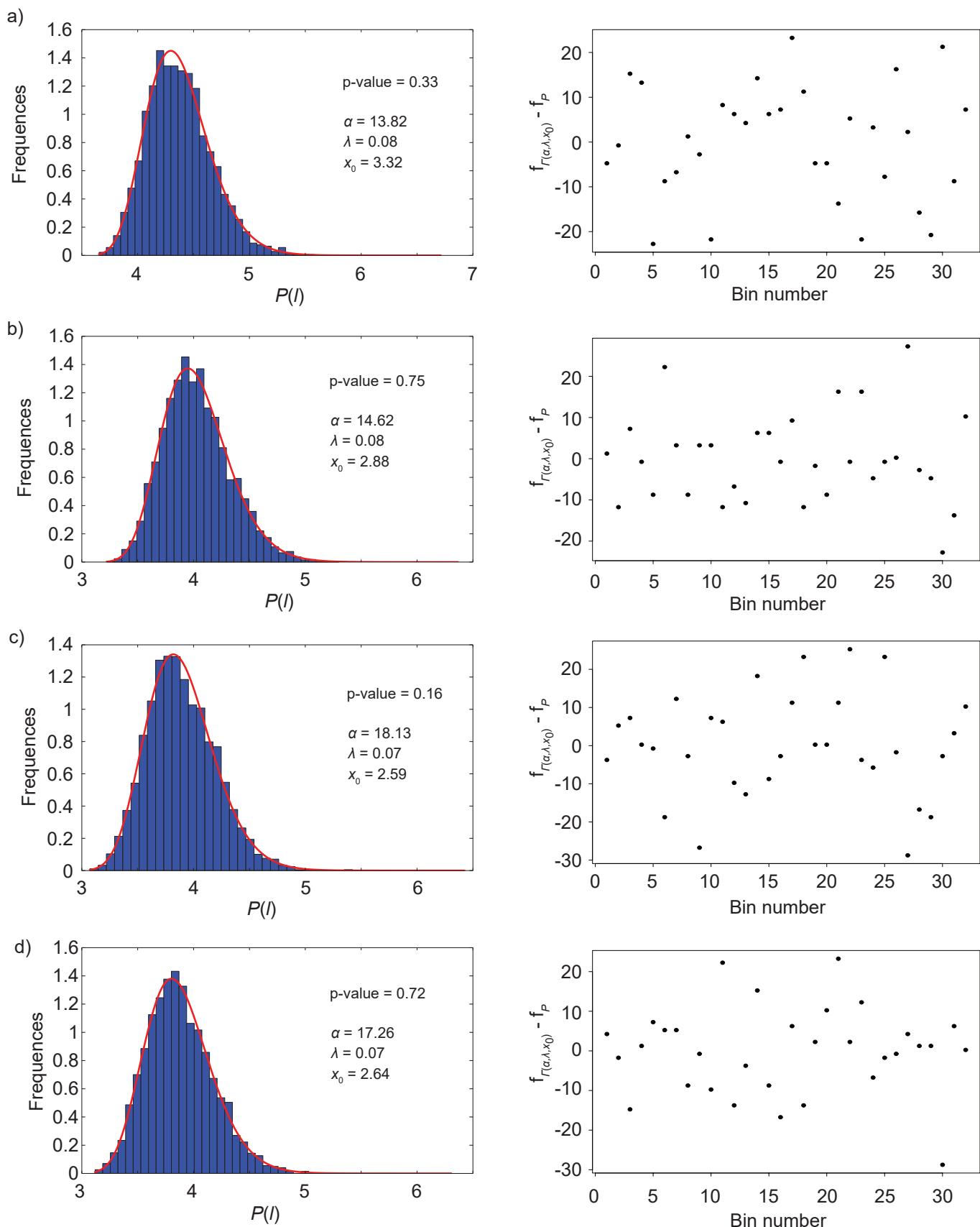


**Fig. 12** Fits of gamma distribution to the cell perimeter measure at packing fraction  $\phi_g = 0.2$ . Left figure shows fit together with p-value of  $\chi^2$  test and parameters of fitted distribution. Right figure shows difference between estimated(fitted) frequencies and observed frequencies for each bin in  $\chi^2$  test.  
 a)  $e = 3.33$  b)  $e = 2$ , c)  $e = 1.25$ , d)  $e = 1$



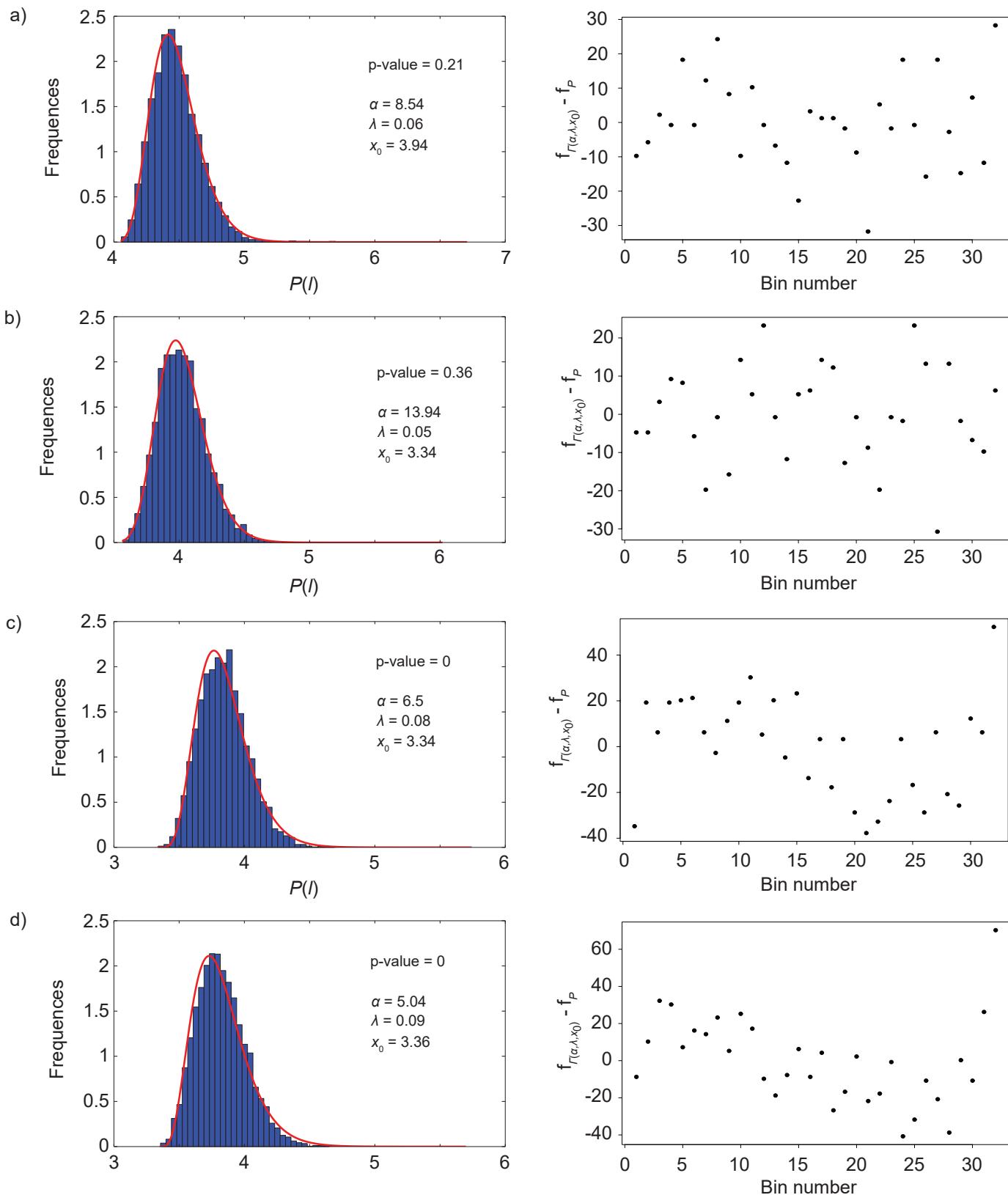
**Fig. 13** Fits of gamma distribution to the cell perimeter measure at packing fraction  $\phi_g = 0.35$ . Left figure shows fit together with p-value of  $\chi^2$  test and parameters of fitted distribution. Right figure shows difference between estimated(fitted) frequencies and observed frequencies for each bin in  $\chi^2$  test.

a)  $e = 3.33$ , b)  $e = 2$ , c)  $e = 1.25$ , d)  $e = 1$

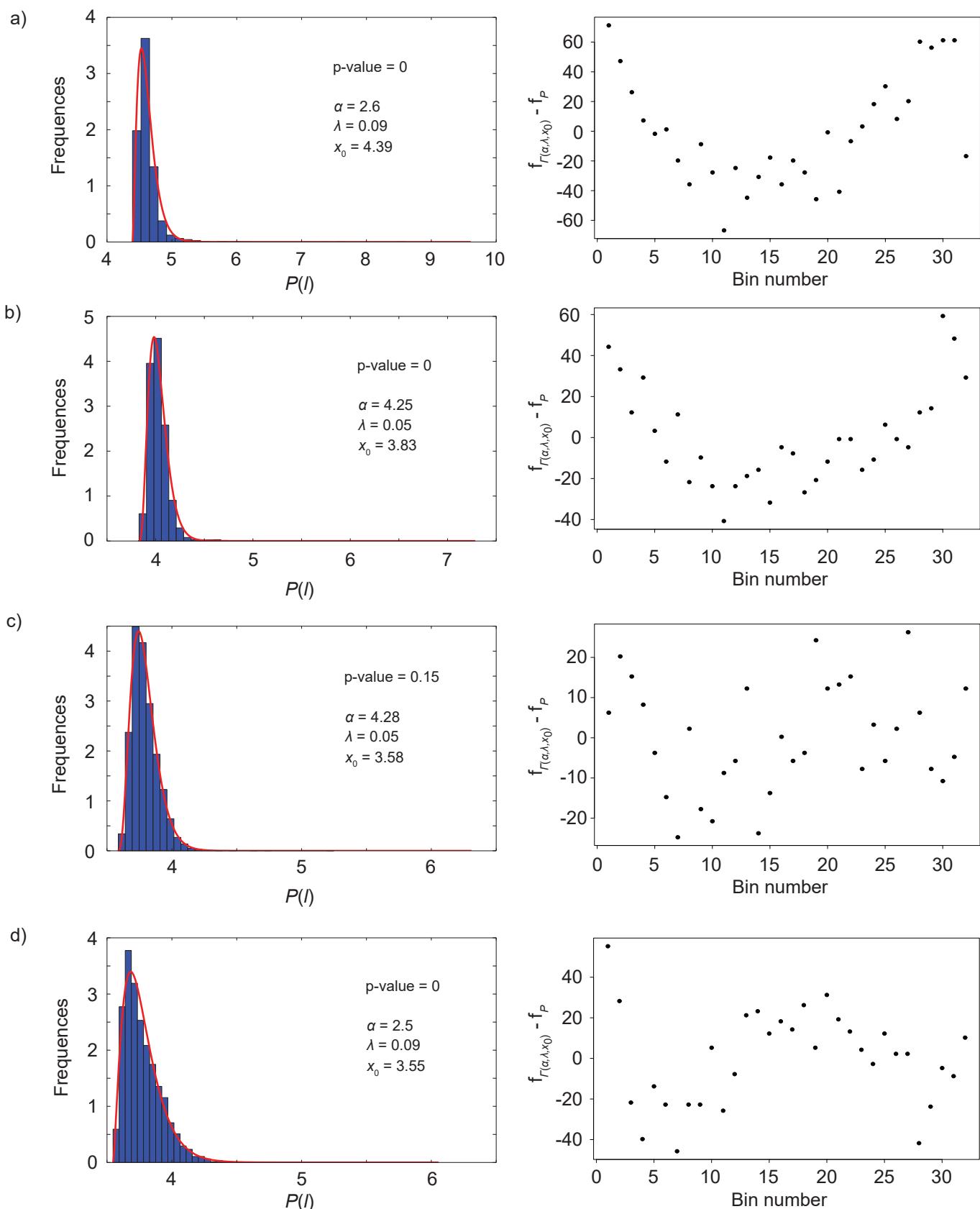


**Fig. 14** Fits of gamma distribution to the cell perimeter measure at packing fraction  $\phi_g = 0.5$ . Left figure shows fit together with p-value of  $\chi^2$  test and parameters of fitted distribution. Right figure shows difference between estimated(fitted) frequencies and observed frequencies for each bin in  $\chi^2$  test.

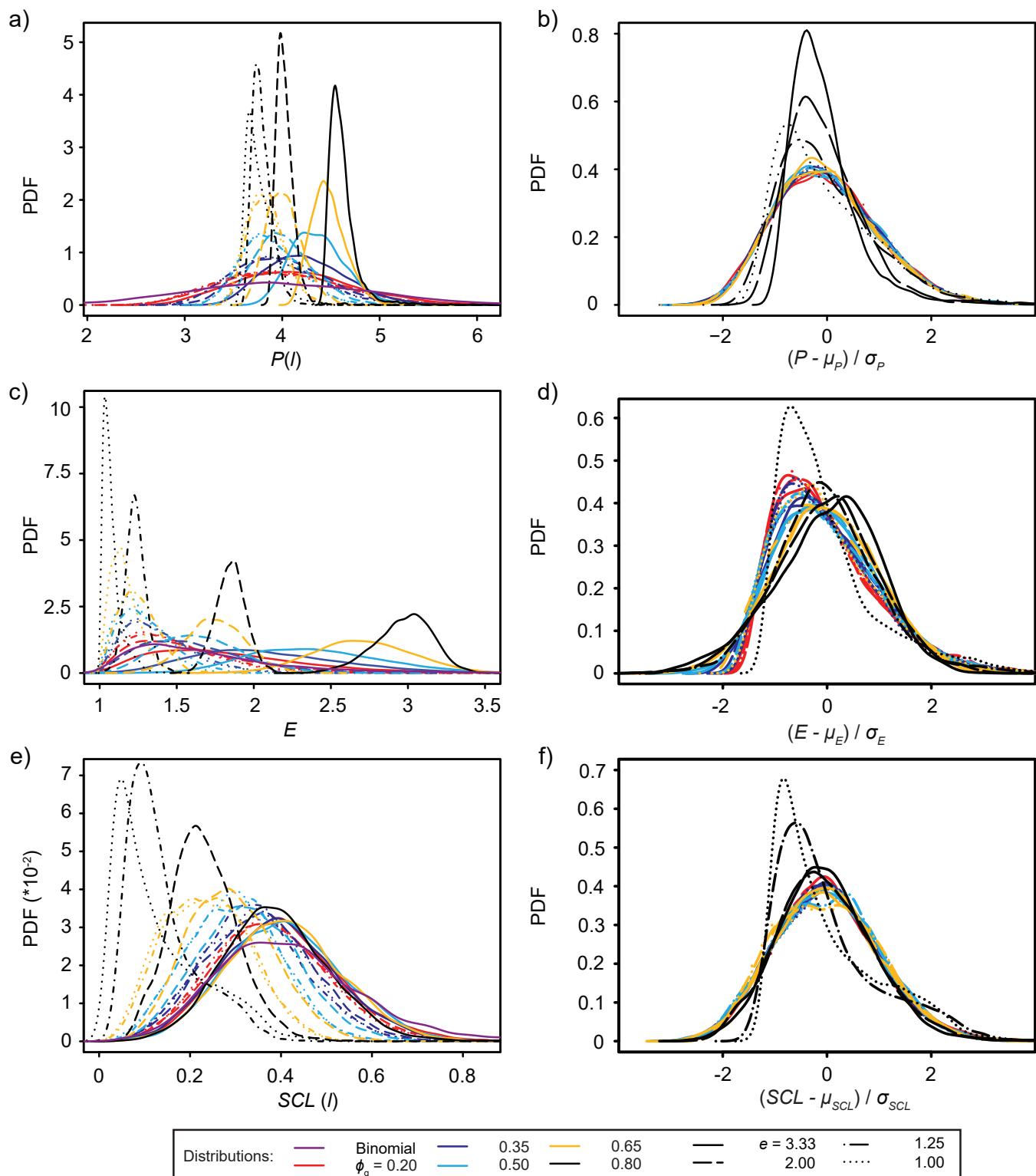
a)  $e = 3.33$  b)  $e = 2$ , c)  $e = 1.25$ , d)  $e = 1$



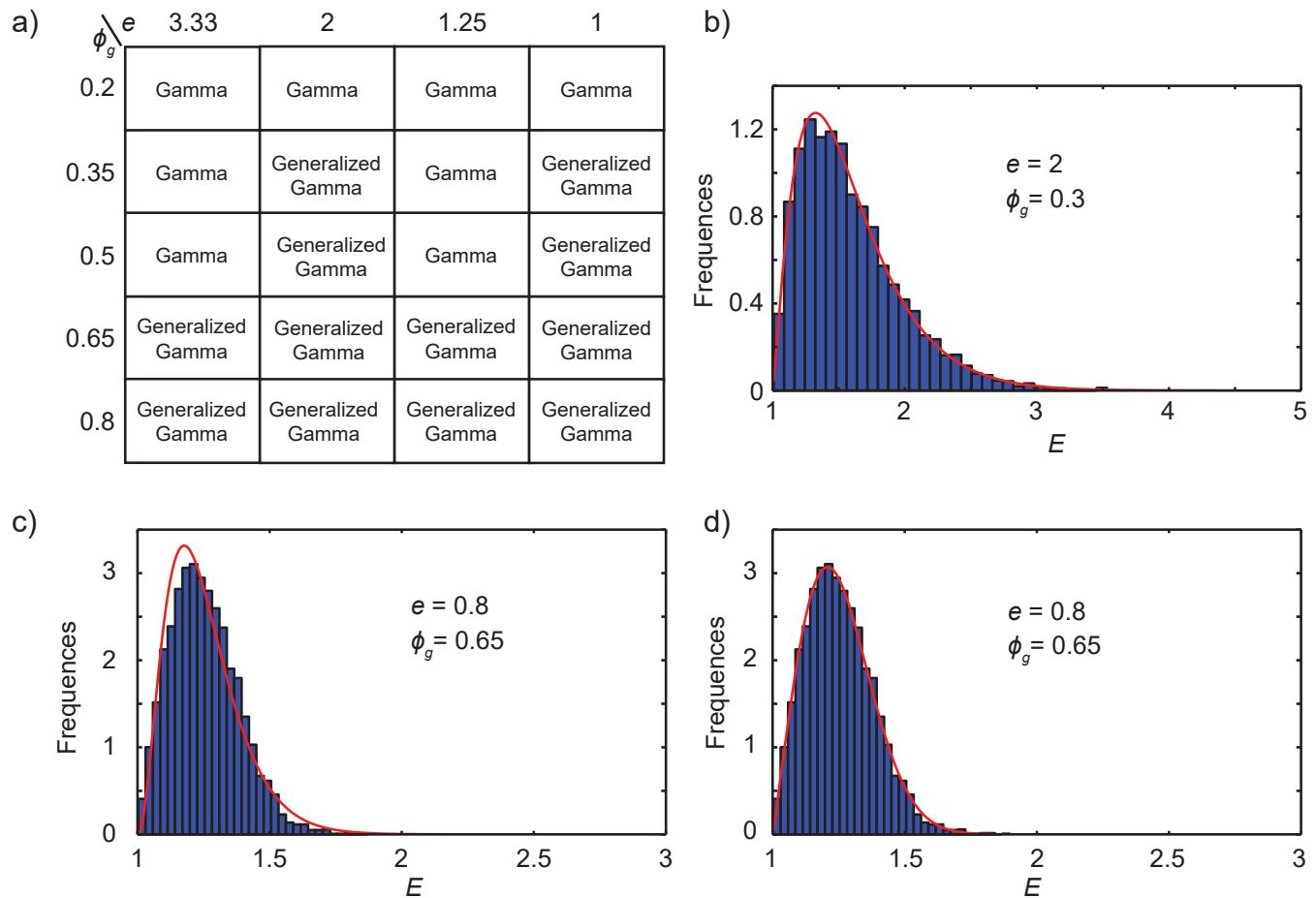
**Fig. 15** Fits of gamma distribution to the cell perimeter measure at packing fraction  $\phi_g = 0.65$ . Left figure shows fit together with p-value of  $\chi^2$  test and parameters of fitted distribution. Right figure shows difference between estimated(fitted) frequencies and observed frequencies for each bin in  $\chi^2$  test.  
 a)  $e = 3.33$  b)  $e = 2$ , c)  $e = 1.25$ , d)  $e = 1$



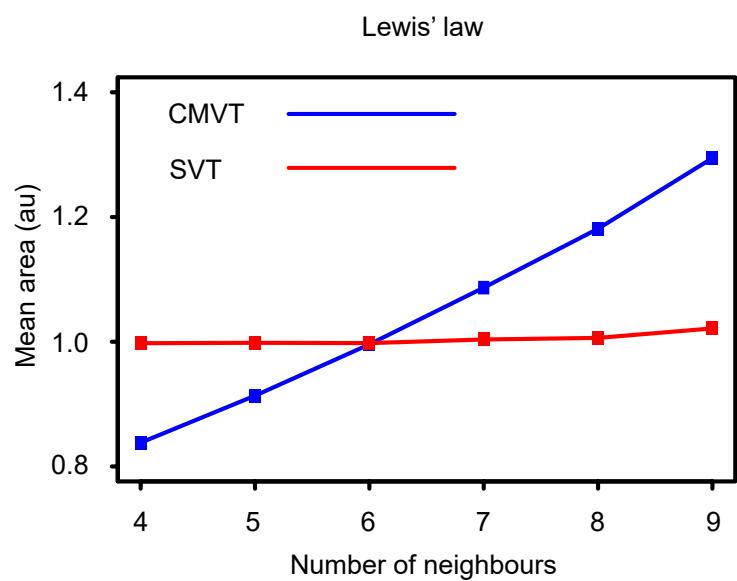
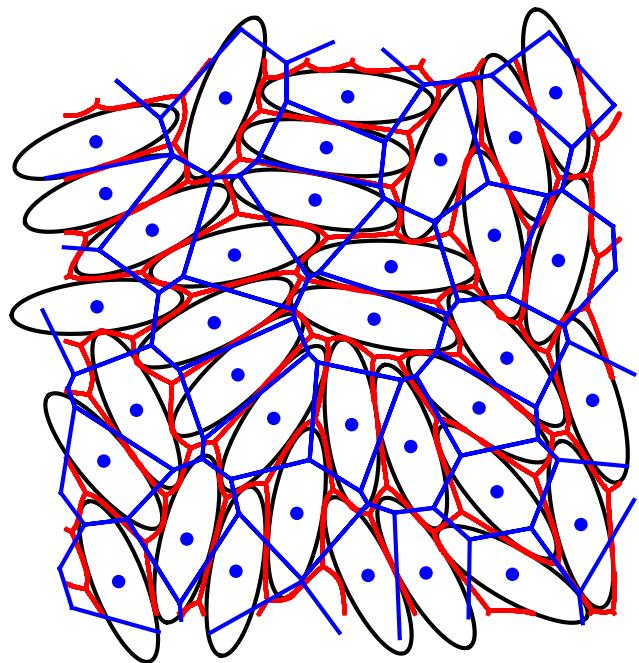
**Fig. 16** Fits of gamma distribution to the cell perimeter measure at packing fraction  $\phi_g = 0.8$ . Left figure shows fit together with p-value of  $\chi^2$  test and parameters of fitted distribution. Right figure shows difference between estimated(fitted) frequencies and observed frequencies for each bin in  $\chi^2$  test.  
a)  $e = 3.33$  b)  $e = 2$ , c)  $e = 1.25$ , d)  $e = 1$



**Fig. 17** Distributions and standardised distributions of selected morphological measures for all studied ellipse assemblies. a) Cell perimeter. b) Cell elongation. c) Standard deviation of contact lengths.



**Fig. 18** Details of fits of gamma distribution to the cell elongation measure. a) Table shows where gamma distributed was successfully fitted across whole phase space of studied assemblies. b) Example of a good fit of gamma distribution to cell elongation measure. c) Example of a bad fit of gamma distribution to cell elongation measure. d) Example of a good fit of generalized gamma distribution to cell elongation measure.



**Fig. 19** Comparison between shape-based and standard Voronoi tessellations. Difference between tessellations clearly emerge when Lewis' law lines are plotted.