

Identification of Optimal Active Boron Site for N₂ Reduction

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Free Energy Calculations

The associated free energy change (ΔG) of each step was determined according to a computational hydrogen electrode model proposed by Nørskov et al.,¹ and is calculated by taking gas-phase N_2 and H_2 as reference states

$$\Delta G = \Delta E + \Delta ZPE - T\Delta S + \Delta G_U + \Delta G_{pH}$$

where ΔE , ΔZPE , and ΔS represent the reaction energy, zero point energy difference and entropy change of each step, respectively. The temperature (T) is set to be 298.15 K. ΔG_U is the effect of an operating bias U , and equals $-neU$ with n being the number of electrons involved in the reaction. ΔG_{pH} is the correction of the H^+ concentration in electrolytes, and was calculated as $\Delta G_{pH} = 0.059 \times \text{pH}$. Since the overpotential remains the same with increasing pH value, pH was assumed to be zero.

The entropies and zero-point energy were calculated based on the vibrational frequencies. The entropy is calculated as

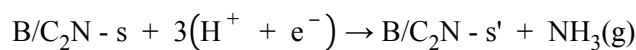
$$S(T) = \sum_{i=1}^{3N} \left[-R \ln \left(1 - e^{-\frac{hv_i}{k_B T}} \right) + \frac{N_A h v_i}{T} \frac{e^{-\frac{hv_i}{k_B T}}}{1 - e^{-\frac{hv_i}{k_B T}}} \right]$$

in which R , h , k_B , N_A , v_i , N and T is the universal gas constant, Planck's constant, Boltzmann's constant, Avogadro's number, frequency of the normal mode, number of adsorbed atoms and temperature (298.15 K), respectively. Entropies of the gas-phase N_2 and H_2 were taken from the NIST database. The zero point energy is defined as

$$E_{ZPE} = \frac{1}{2} \sum_{i=1}^{N_{\text{modes}}} hv_i$$

where N_{modes} is the number of vibrational modes. Then, ΔE_{ZPE} and ΔS are the differences in zero point energy and entropy, respectively, between the adsorbed species and gas-phase molecules. The operating bias U_L is the applied potential required to eliminate the energy barrier of the potential-limiting step and is calculated as $-\Delta G_{\text{pls}}/e$, where ΔG_{pls} is the free energy difference of the potential-limiting step according to the standard hydrogen electrode (SHE).²

The decomposition of N-doped substrate to release NH_3 can be expressed as:



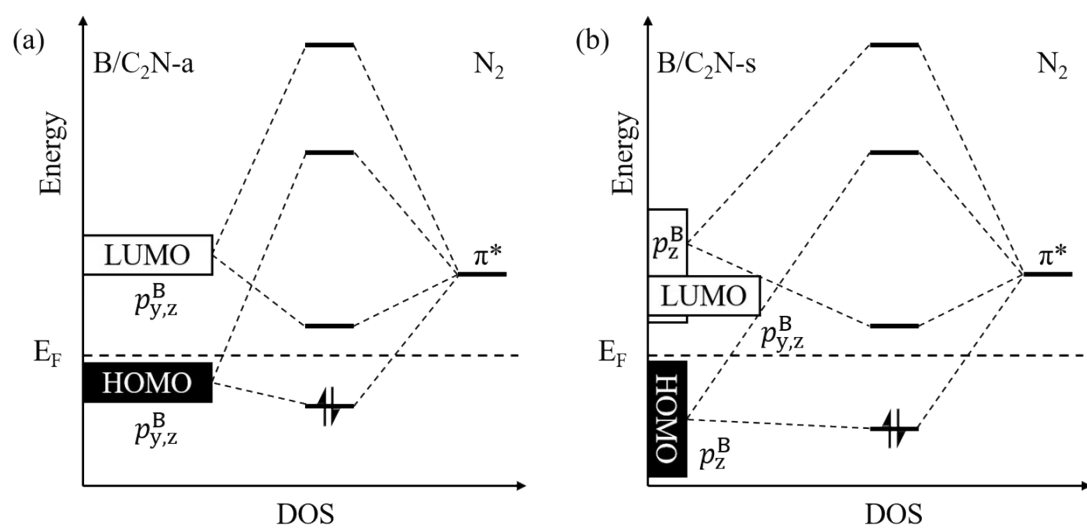
where B/C₂N-s' is the structure of B/C₂N-s after losing one nitrogen atom. Hence, the required potential (U_d vs. SHE) to form NH₃ by the decomposition of catalysts can be expressed as:
 $U_d = \Delta G_d/3e$

Table S1. The free energies of each step via alternating and distal mechanisms on B/C₂N-a and B/C₂N-s in a 2 × 2 supercell and those on B/C₂N-s in a 1 × 1 supercell.

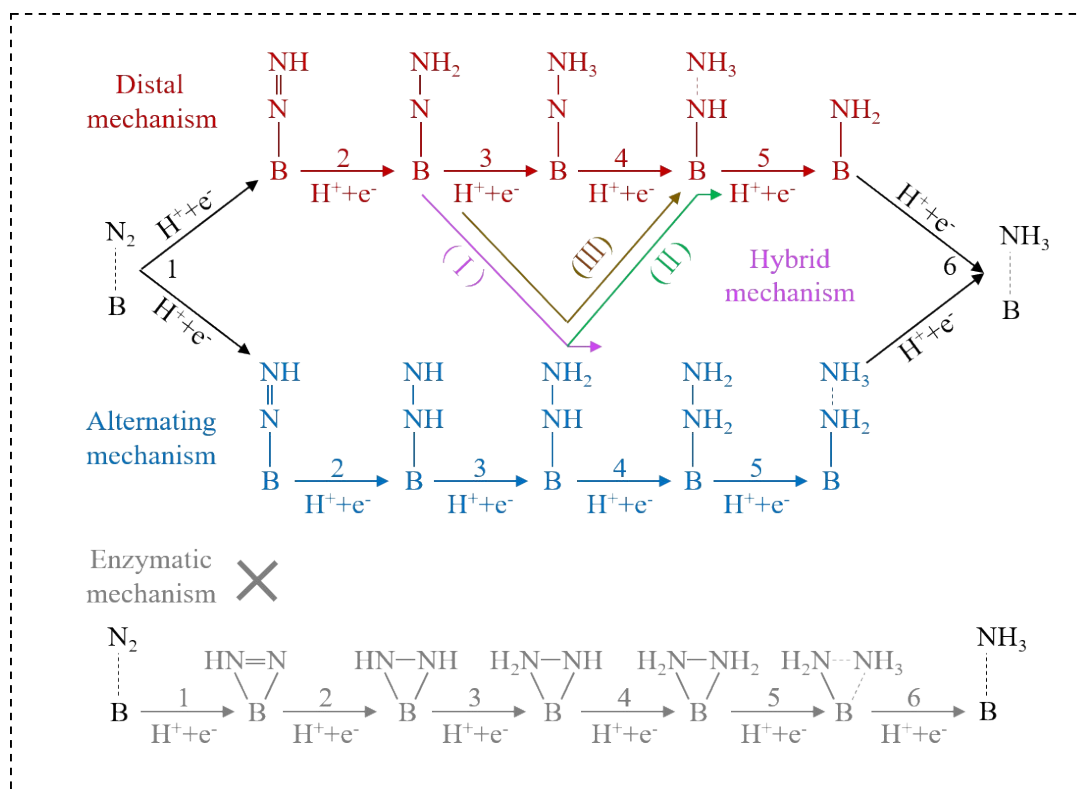
Distal mechanism			Alternating mechanism			
species	ΔG (eV)	ΔG (eV)	species	ΔG (eV)	ΔG (eV)	ΔG (eV)
	B/C ₂ N-a (2 × 2)	B/C ₂ N-s (2 × 2)		B/C ₂ N-a (2 × 2)	B/C ₂ N-s (2 × 2)	B/C ₂ N-s (1 × 1)
N ₂	0	0	N ₂	0	0	0
*N ₂ H	-0.77	-0.37	*N ₂ H	-0.77	-0.37	-0.58
*NNH ₂	-1.41	-0.77	*NHNH	-1.69	-0.57	-0.86
*NNH ₃	-1.43	-0.48	*NH ₂ NH	-2.43	-1.40	-1.39
*NH+NH ₃	-2.48	-2.39	*NH ₂ NH ₂	-2.13	-2.05	-2.07
*NH ₂ +NH ₃	-4.96	-2.88	*NH ₂ +NH ₃	-4.96	-2.88	-2.89
*NH ₃ +NH ₃	-4.83	-3.96	*NH ₃ +NH ₃	-4.83	-3.96	-3.91

Table S2. B-C bond length in NRR via the alternating pathway.

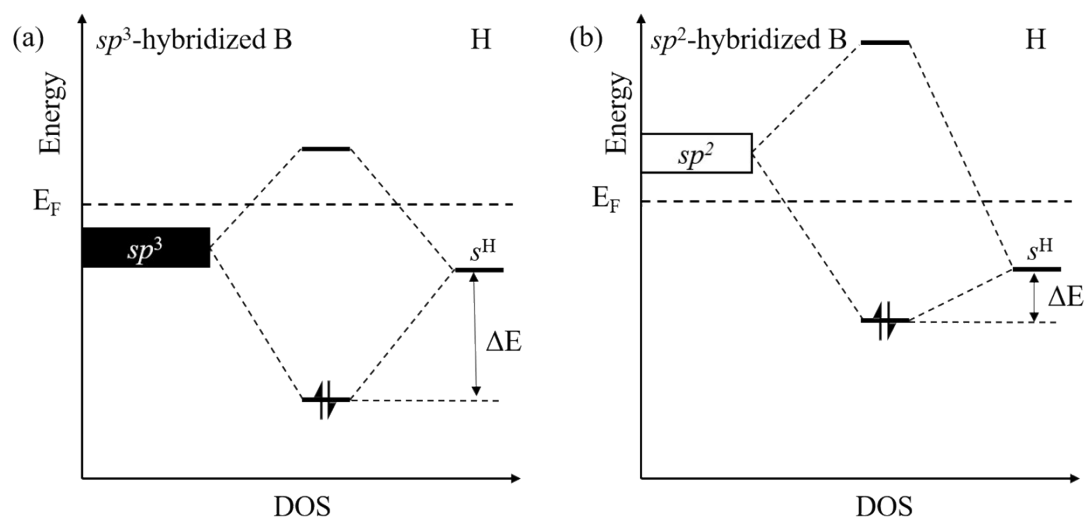
Adsorbed species	*N ₂	*N ₂ H	*NHNH	*NH ₂ NH	*NH ₂ NH ₂	*NH ₂	*NH ₃
B-C bond length	1.49	1.51	1.50	1.53	1.50	1.54	1.50



Scheme S1. Schematic diagrams of the orbital interaction for N₂ adsorption on (a) B/C₂N-a and (b) B/C₂N-s.



Scheme S2. Schematic illustration of possible reaction paths for N_2 reduction to NH_3 .



Scheme S3. Schematic diagrams of the orbital interaction for H bonding with sp^3 - and sp^2 -hybridized B.

$$\Delta E = \frac{|H_{ij}|^2}{E_i^0 - E_j^0} \quad \text{Equation S1}$$

where E_i^0 is an unperturbed orbital energy before a perturbation or interaction is turned on. H_{ij} represents the matrix element of the perturbation.³⁻⁴

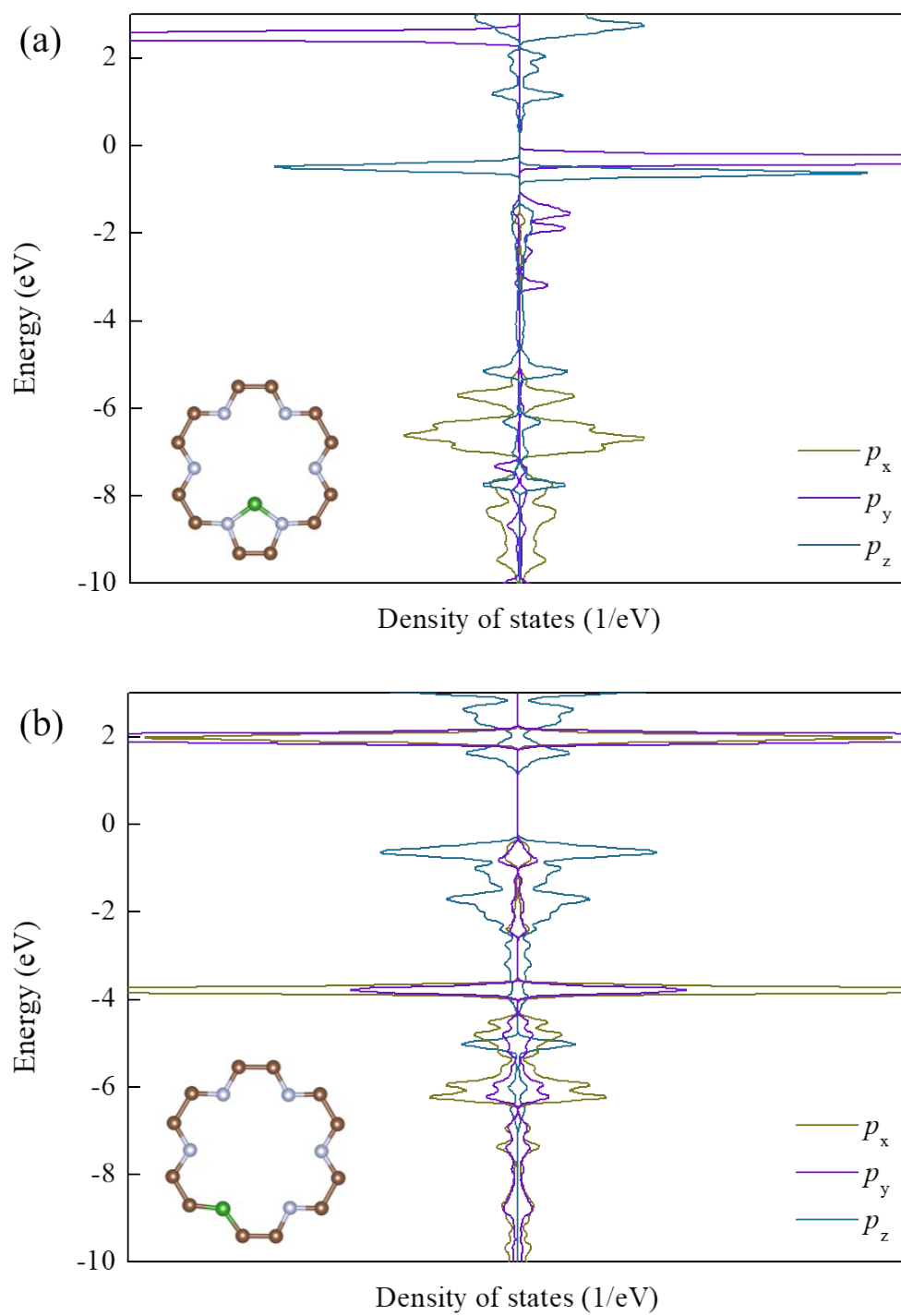


Figure S1. The pDOS of B atoms in (a) B/C₂N-a and (b) B/C₂N-s.

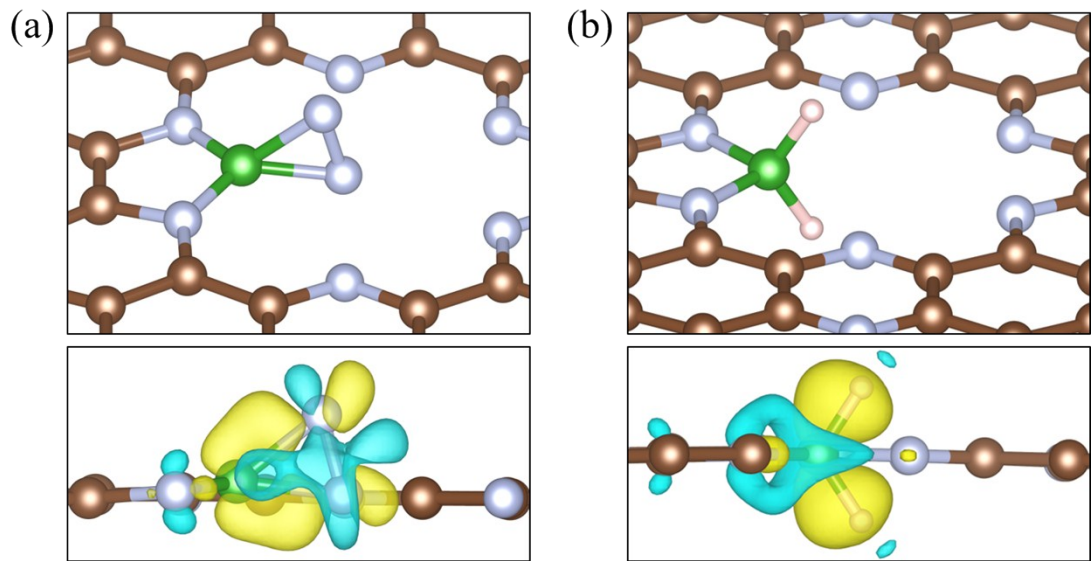
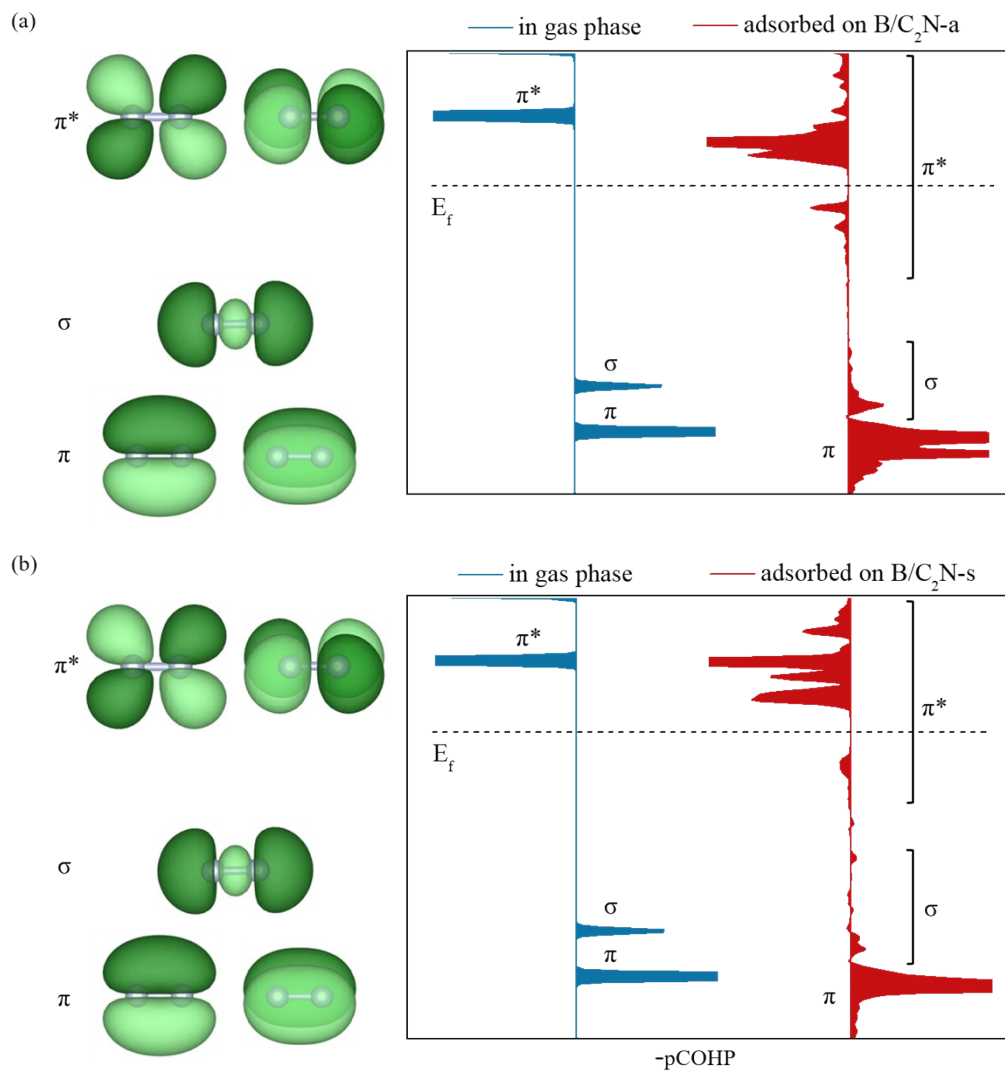


Figure S2. The geometry structure (upper panel) and differential charge density (lower panel) of (a) N₂ adsorption in side-on mode and (b) two H atoms co-adsorption on B/C₂N-a.



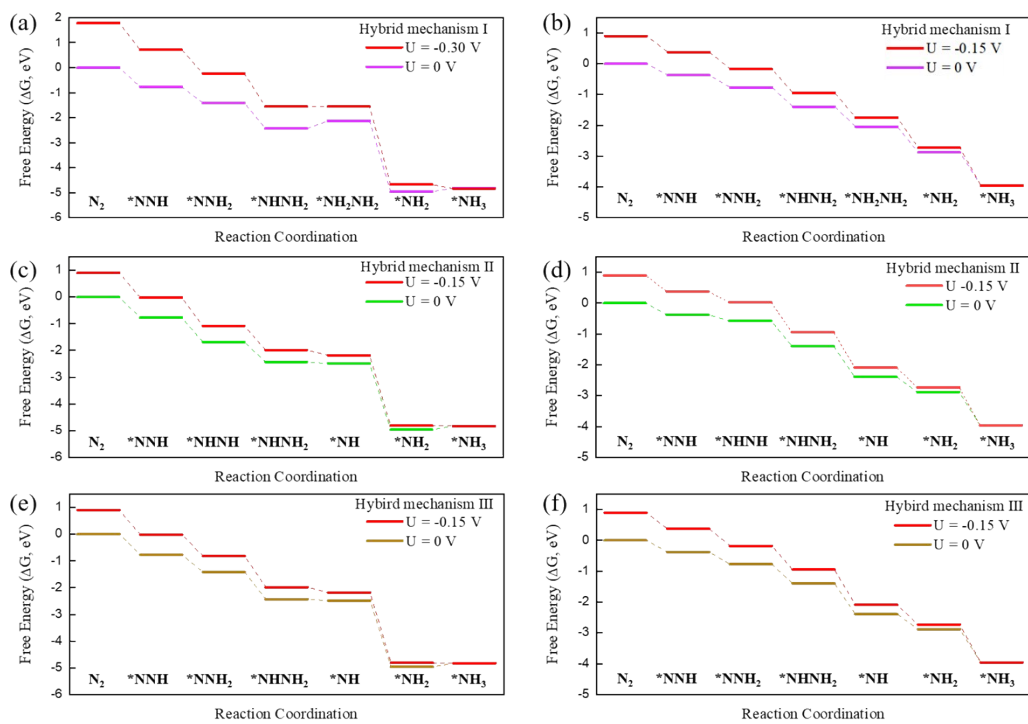


Figure S4 Free energy landscape of N_2 reduction at 0 V and the applied potential on (a, c and e) B/C₂N-a and (b, d and f) B/C₂N-s.

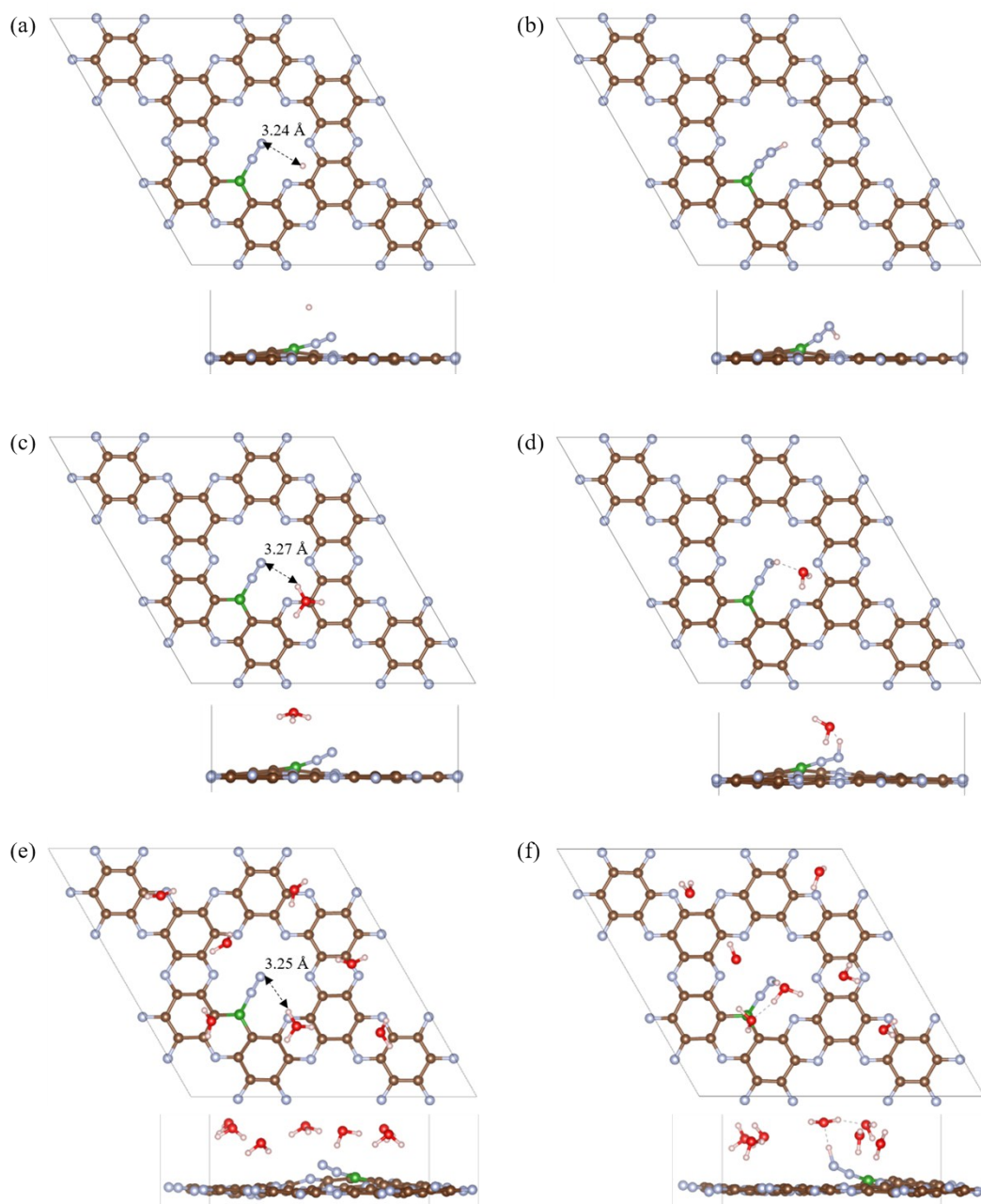


Figure S5. Initial structures of N_2 adsorption on B/C₂N-s with (a) a H atom, (c) a H₃O molecule and (e) a H₃O and several H₂O molecules in the vicinity. (b), (d) and (f) are the corresponding structure after optimization.

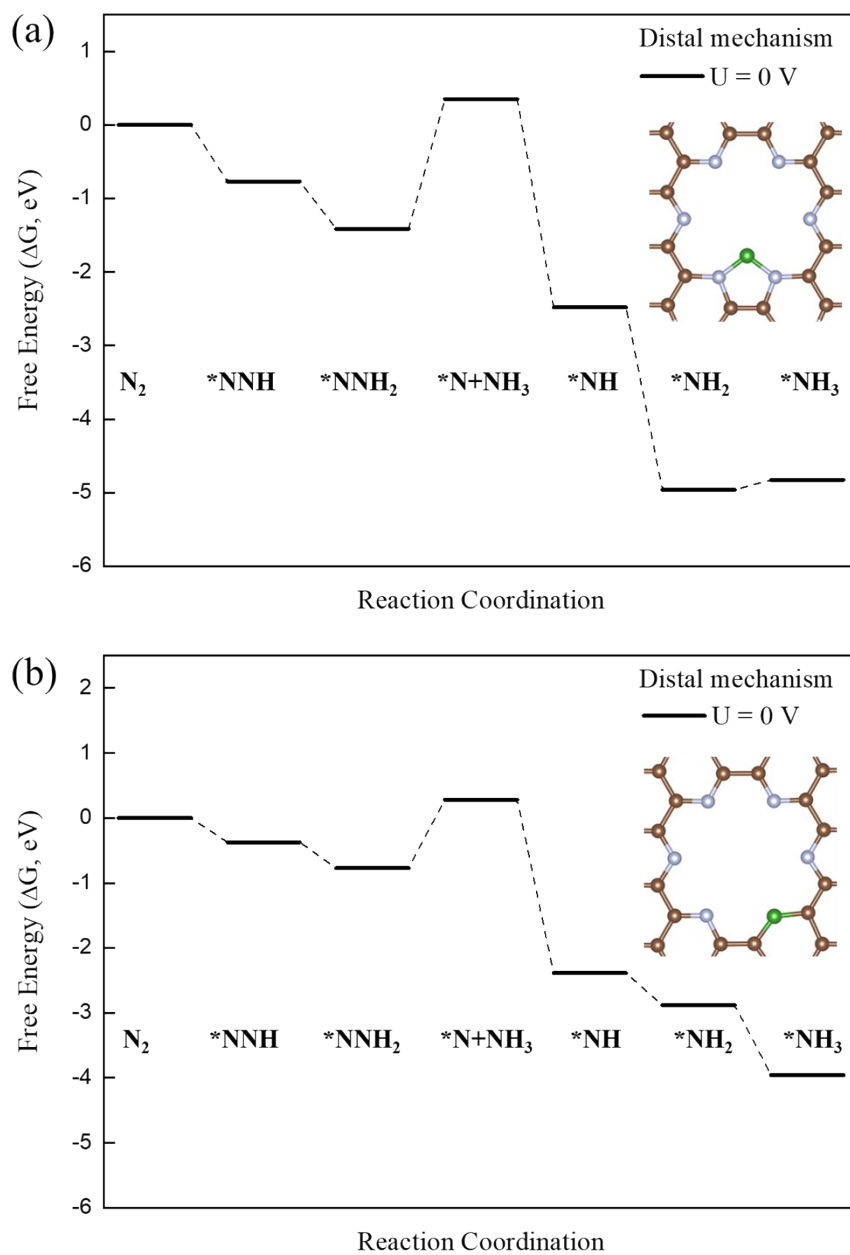


Figure S6. Free energy landscape of N_2 reduction at 0 V on (a) B/C₂N-a and (b) B/C₂N-s through distal pathway where the first NH_3 is formed by N-N bond cleavage of NNH_3 .

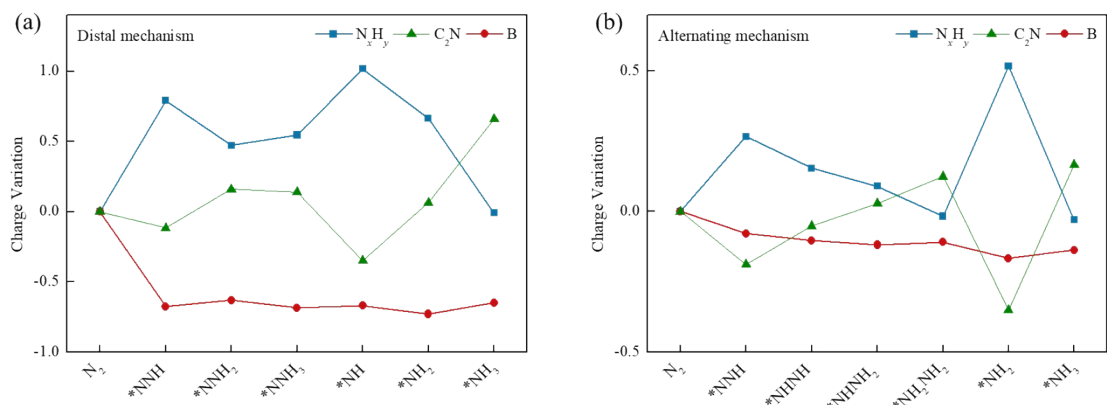


Figure S7. Bader charge of each entity in NRR process via (a) distal and (b) alternating mechanism on B/C₂N-s.

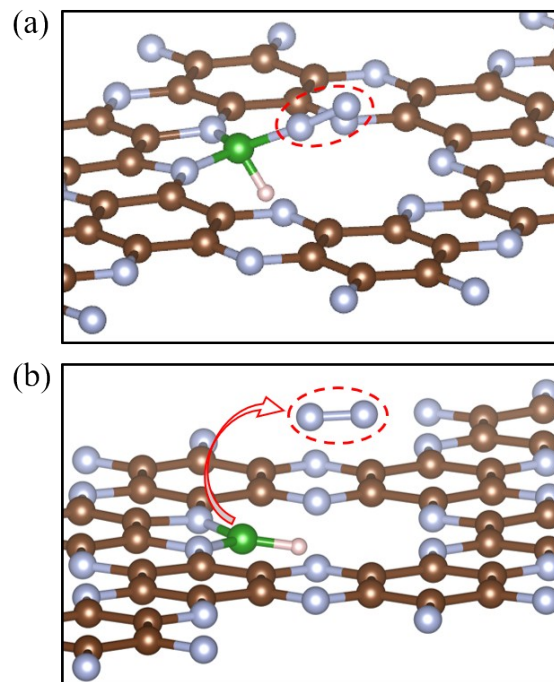


Figure S8. The geometries of N_2 and H coadsorption on B/C₂N-a (a) before and (b) after structural optimization.

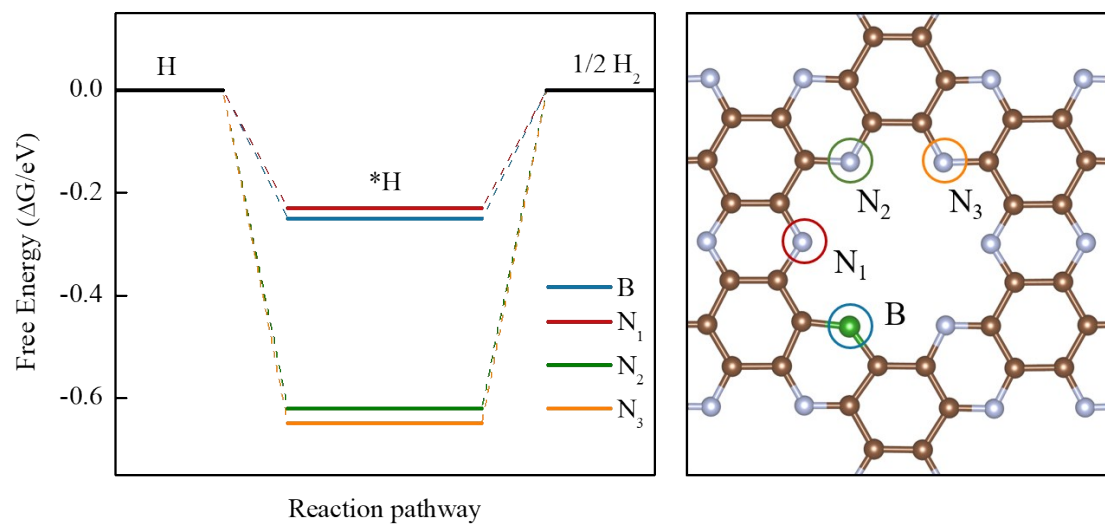


Figure S9. Free energy diagram for HER at different sites on B/C₂N-s.

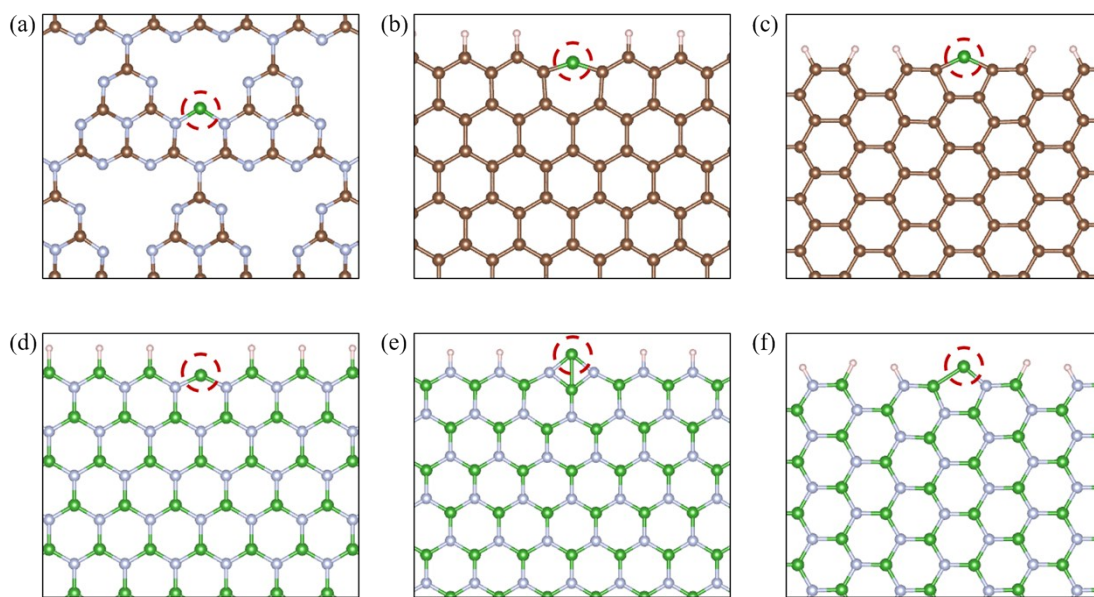


Figure S10. The optimized structures of (a) B/C₃N₄-a, (b) B/Gz-s, (c) B/Ga-a, (d) hBNz, (e) B/hBNz-a and (f) B/hBNa-a. The active B sites are marked by red circles.

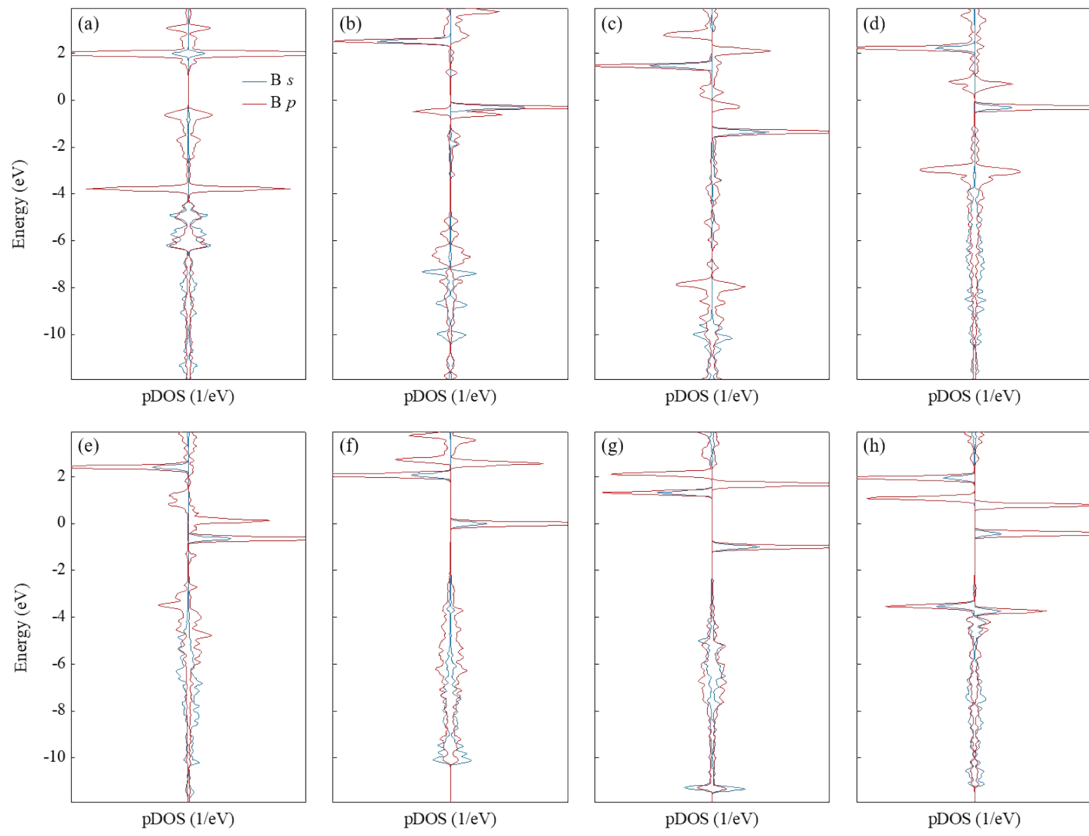


Figure S11. The pDOS of B in (a) B/C₂N-s, (b) B/C₂N-a, (c) B/C₃N₄-a, (d) B/Gz-s, (e) B/Ga-a, (f) hBNz, (g) B/hBNz-a and (h) B/hBNa-a.

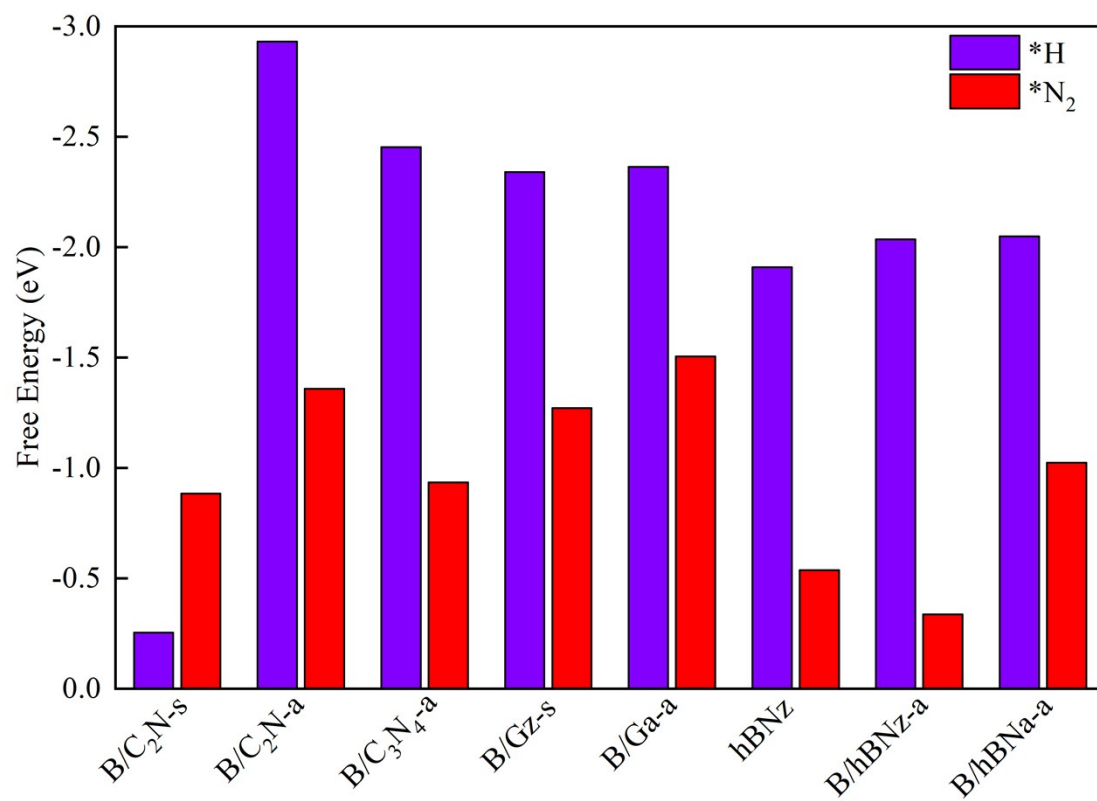


Figure S12. Free energy of H (blue) and N₂ (red) adsorption on B/C₂N-a, B/C₂N-s, B/C₃N₄-a, B/Gz-s, B/Ga-a, hBNz, B/hBNz-a and B/hBNA-a.

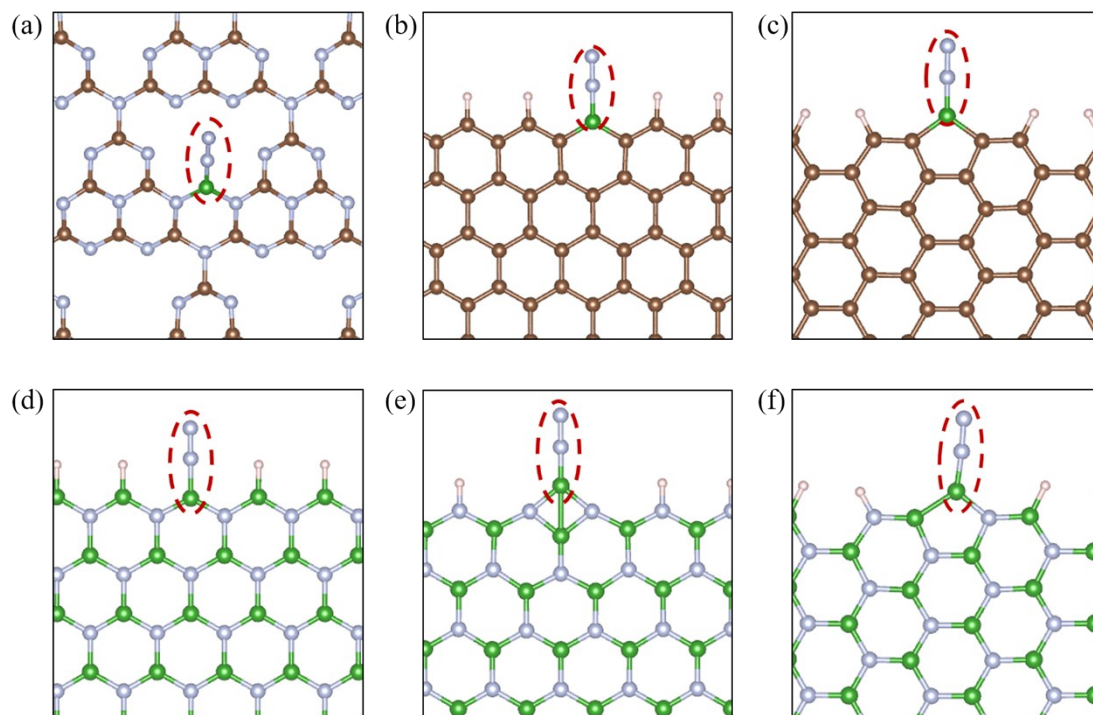


Figure S13. The optimized structures of N_2 adsorption on (a) B/C_3N_4 -a, (b) B/Gz -s, (c) B/Ga -a, (d) $hBNz$, (e) $B/hBNz$ -a and (f) $B/hBNa$ -a.

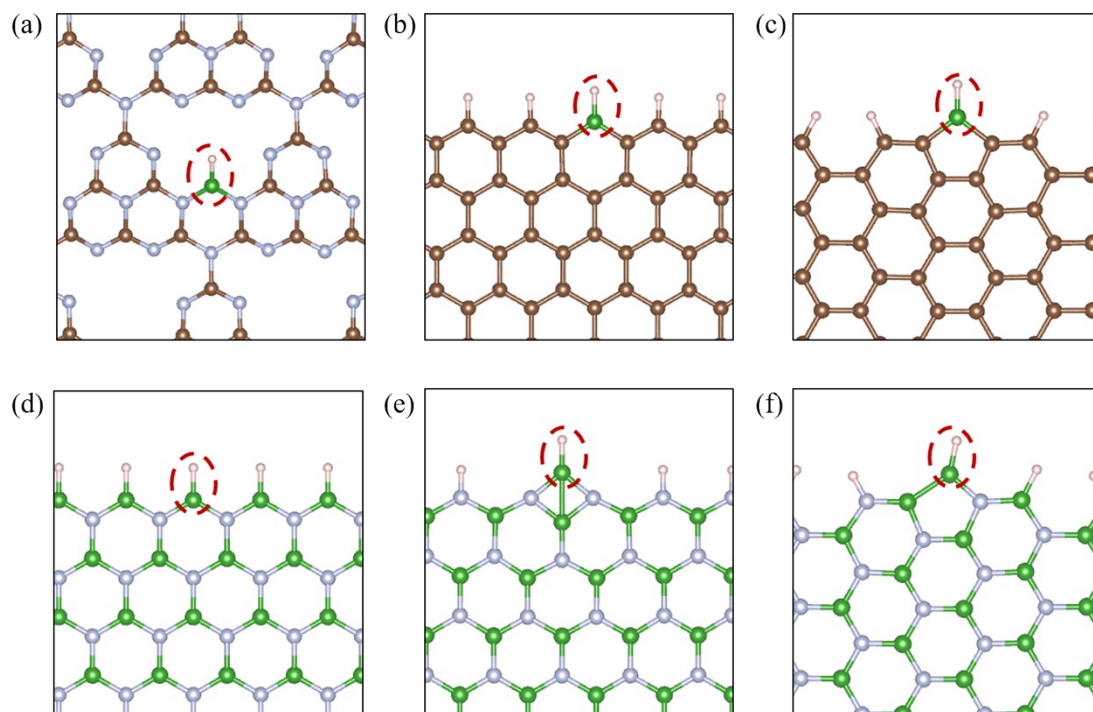


Figure S14. The optimized structure of H adsorption on (a) B/C_3N_4 -a, (b) B/Gz -s, (c) B/Ga -a, (d) $hBNz$, (e) $B/hBNz$ -a and (f) $B/hBNa$ -a.

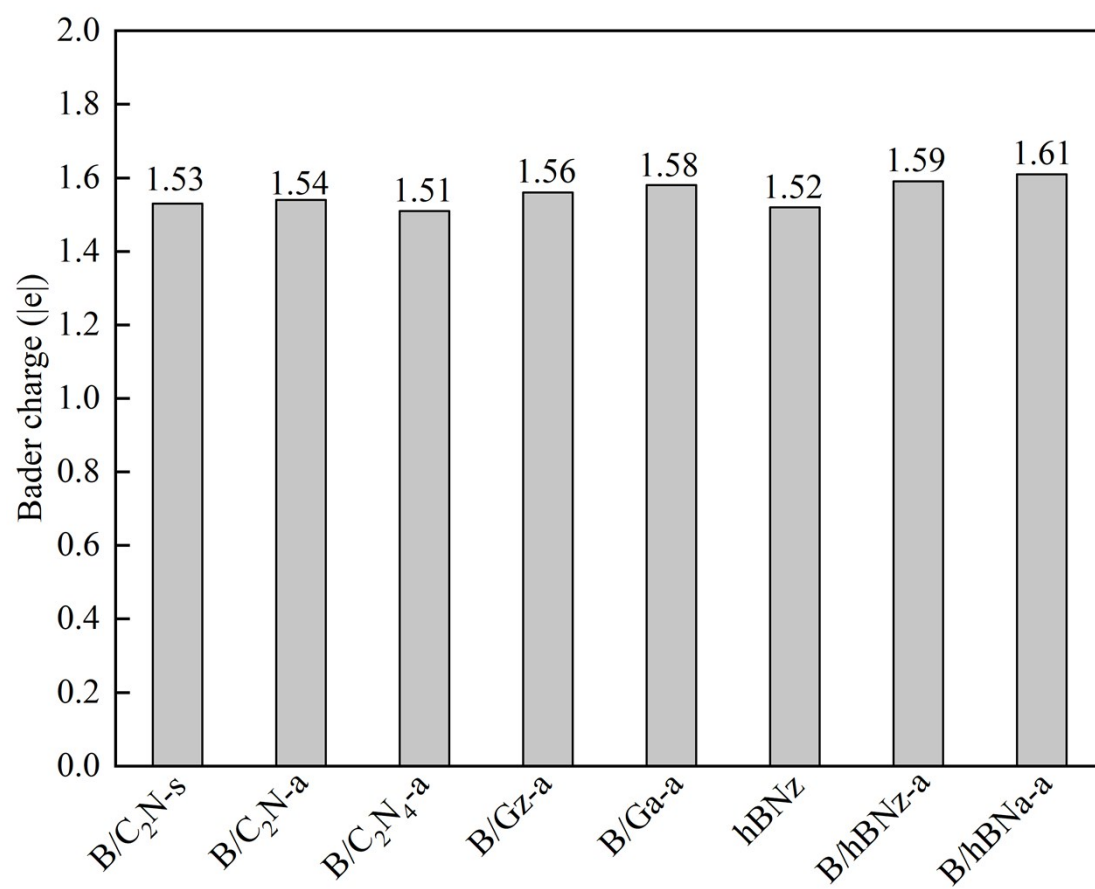


Figure S15. Bader charge of H adsorption on B/C₂N-s, B/C₂N-a, B/C₃N₄-a, B/Gz-s, B/Ga-a, hBNz, B/hBNz-a and B/hBNa-a.

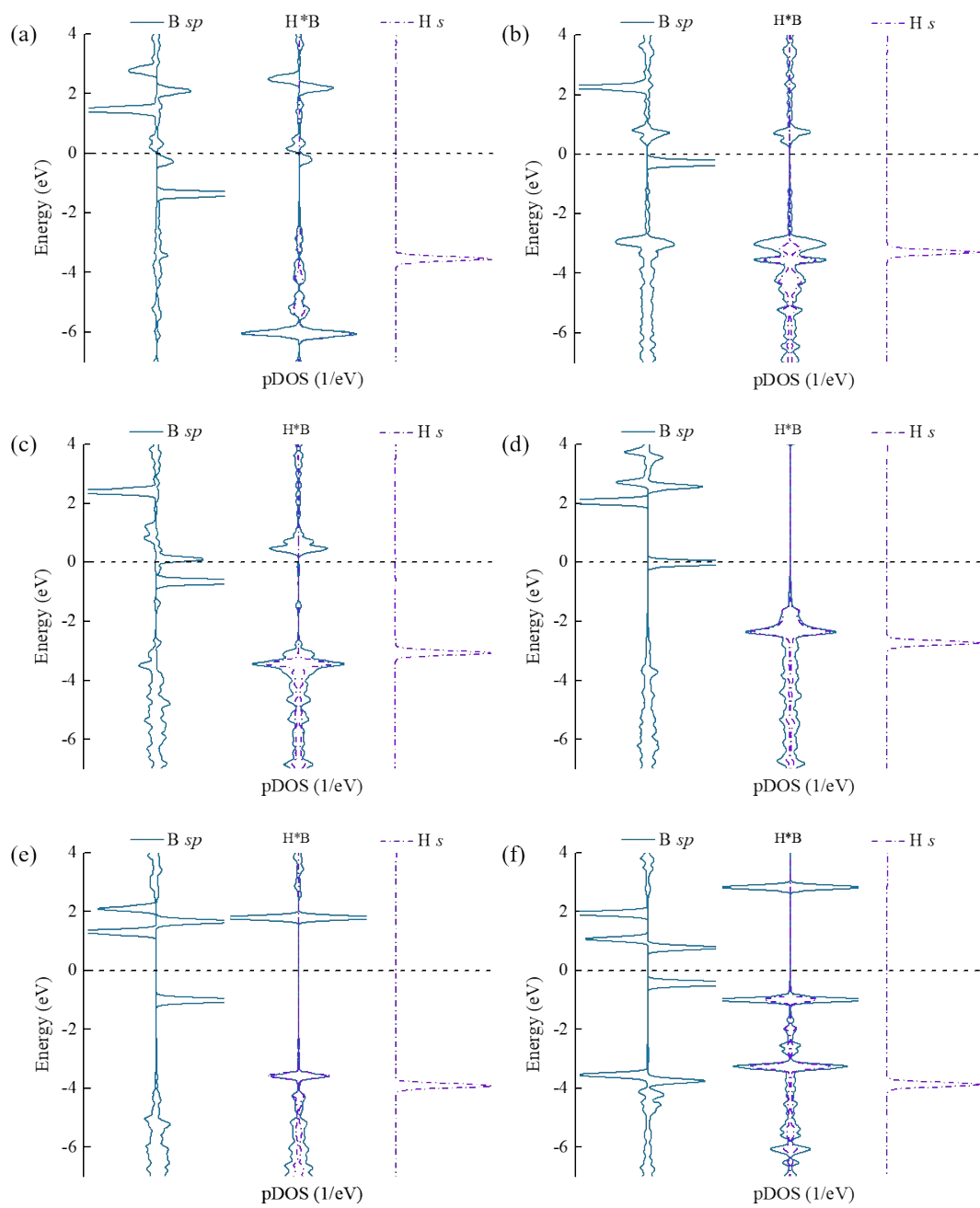


Figure S16. The pDOS of B and H atom in (a) B/C₃N₄-a, (b) B/Gz-s, (c) B/Ga-a, (d) hBNz, (e) B/hBNz-a and (f) B/hBNa-a before and after H adsorption.

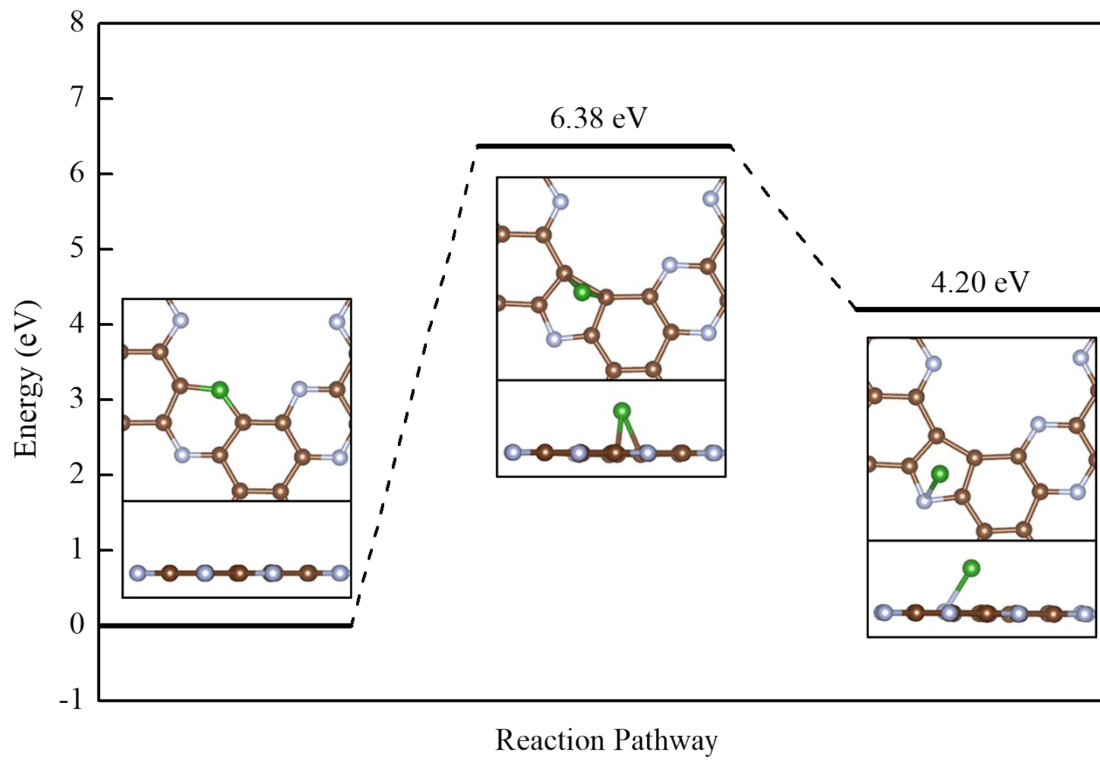


Figure S17. The minimum energy path for B hopping out of the trapping center in B/C₂N-s.

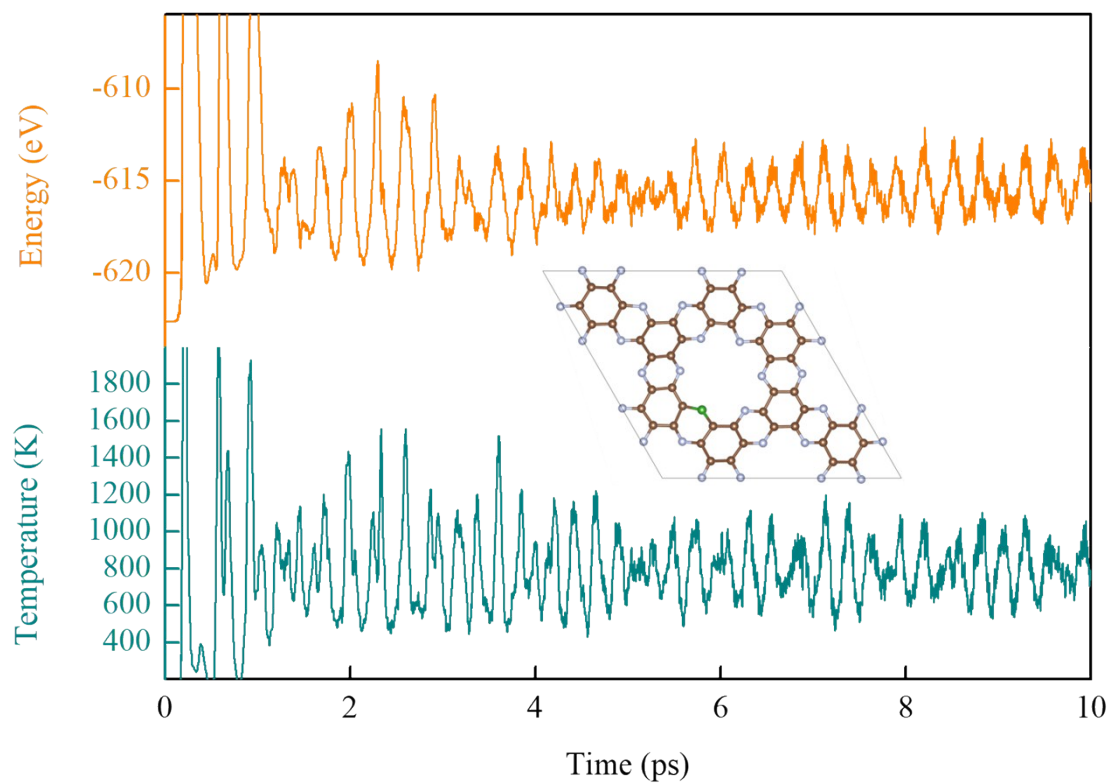


Figure S18. Variations of energy (orange) and temperature (olive) against the time in *ab initio* molecular dynamics simulations for B/C₂N-s. Insert shows the structure of B/C₂N-s after 10-ps simulation. The temperature is set to be 800 K and the time step is 2 fs.

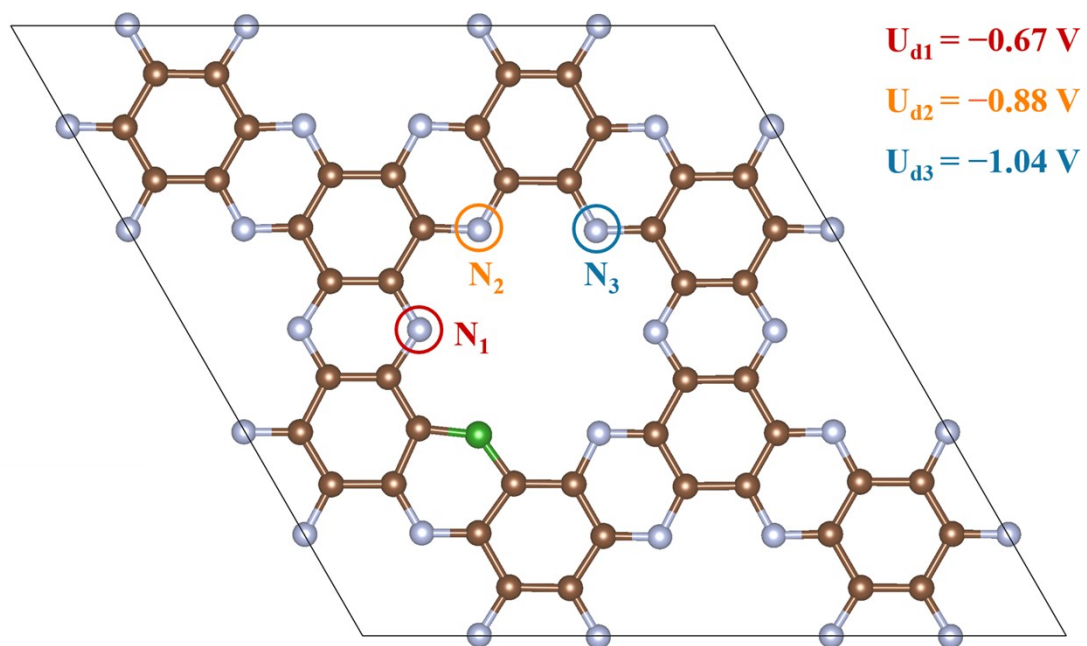


Figure S19 The decomposition potentials at three nonequivalent N sites in B/C₂N-s.

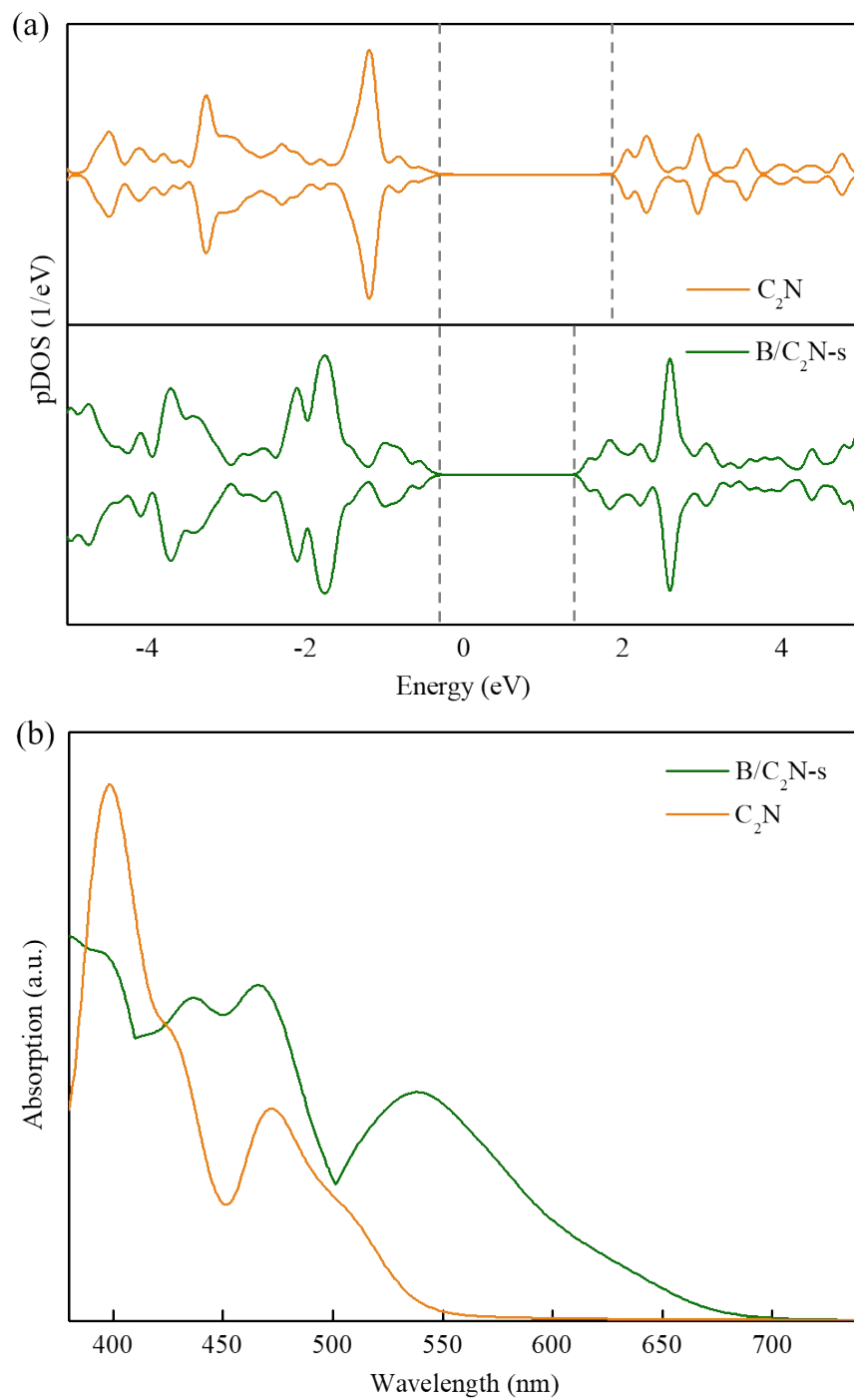


Figure S20. Comparison of (a) pDOS and (b) optical adsorption spectra for pristine C_2N and B/C_2N-s .

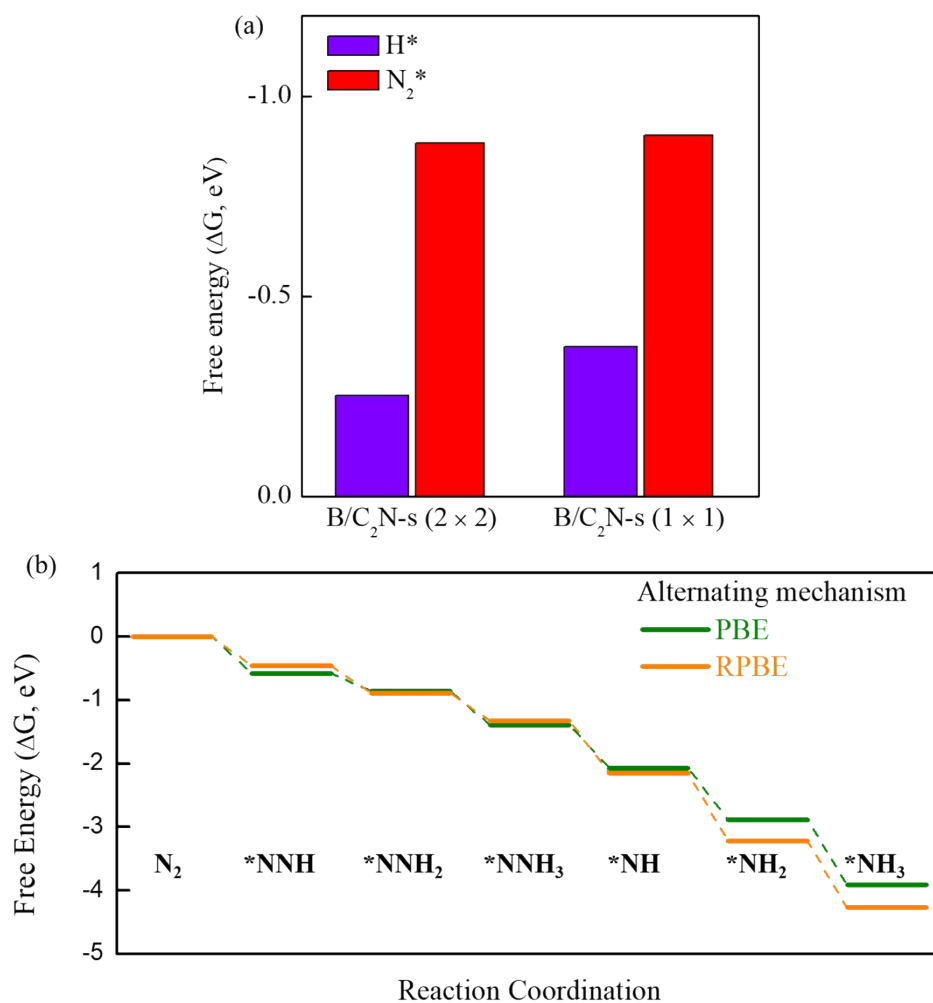


Figure S21. (a) The adsorption free energy of N_2 and H adsorption on B/C_2N-s in a 2×2 and 1×1 supercell. (b) The free energy diagram of NRR on B/C_2N-s in a 1×1 supercell, using Perdew-Burke-Ernzerh (PBE) and revised Perdew-Burke-Ernzerhof (RPBE) functionals, respectively.

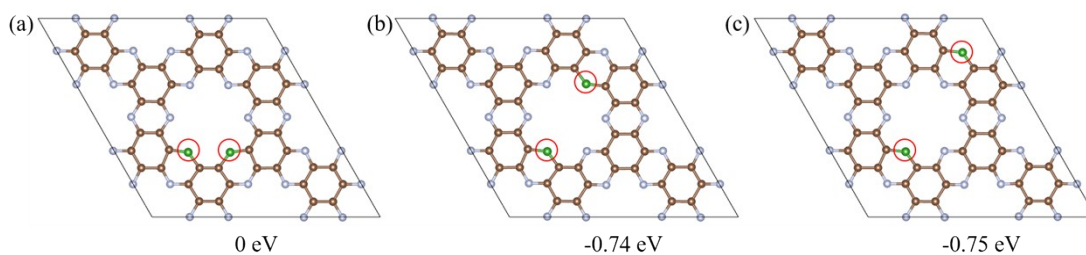


Figure S22. Relative energies of C_2N with two (a) adjacent and (b) diagonal N atoms in one cave and (c) two N atoms in two caves substituted by two B atoms.

References

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