

*Supplementary Information for*

High Quality Two-Photon Pumped Whispering-Gallery-Mode Lasing from  
Ultrathin CdS Microflakes

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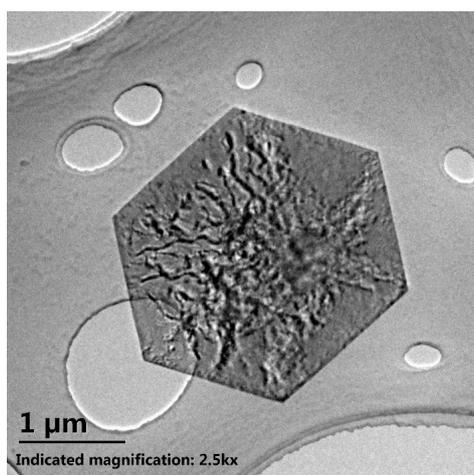
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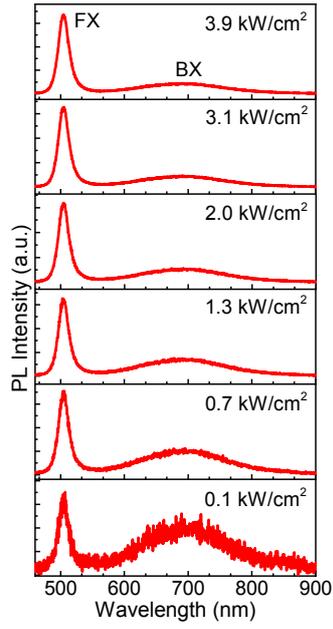
**Tab.1** Comparison of TPP lasing dimension and threshold values reported semiconductor lasers with active CdS cavity.

Materials	Thickness	$\lambda$ (nm)	Threshold (mJ/cm <sup>2</sup> )	Excitation sources	Ref.
CdSe/CdS NP film	-----	534	4.4-8.3	800 nm, 1 kHz, 120 fs	1
CdSe/CdS NR film	Thickness: 500 nm	550-600	1.5 -3.4	800 nm, 1 kHz, 150 fs	2
CdS MW	Dimeter: 1 $\mu$ m Length: 28 $\mu$ m	523	3.3	800nm, 1 kHz, 80 fs	3
CdS NW	Dimeter: ~100 nm	513	3.15	780nm, 1 kHz, 1.6 ps	4

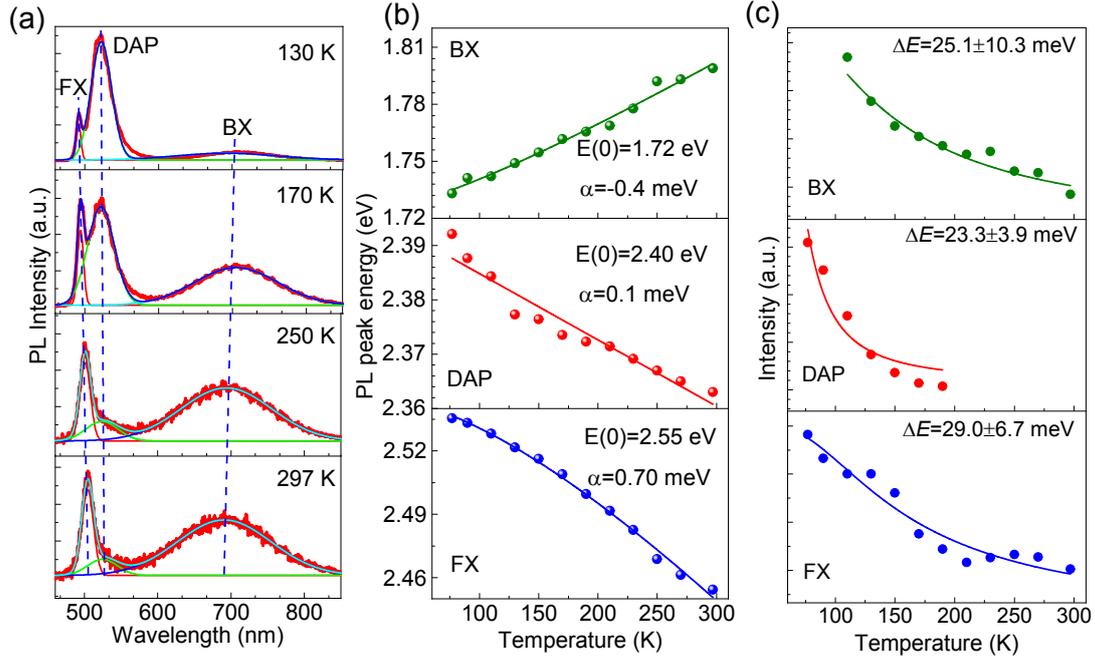
\*Abbreviations: NP, nanoplatelet; NR, nanorod; MW, microwire; NW, nanowire.<sup>1-4</sup>



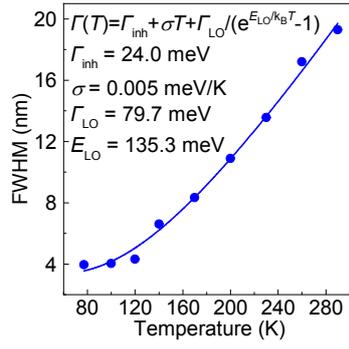
**Fig. S1** Low-magnification TEM image of a hexagonal CdS microflake.



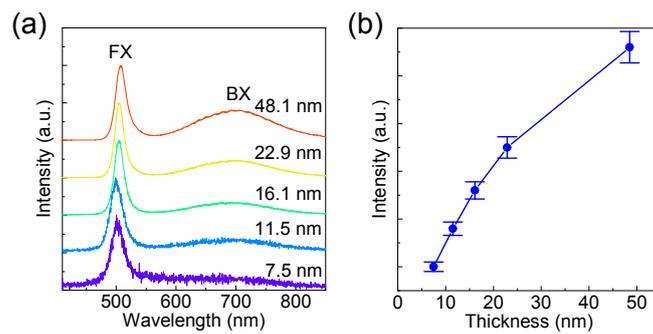
**Fig. S2** PL spectroscopy of a CdS microflake at power density of 0.1, 0.7, 1.3, 2.0, 3.1 and 3.9 kW/cm<sup>2</sup>, respectively. Excitation source is a CW laser with a wavelength of 405 nm.



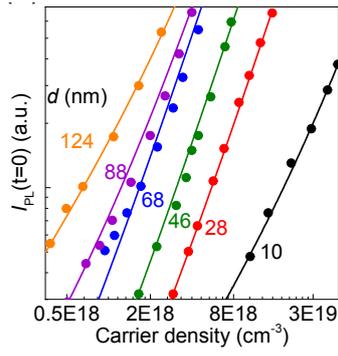
**Fig. S3** (a) PL spectroscopy of the CdS microflake at 297, 250, 170, and 130 K. (b) Energy shifts of FX, DAP and BX emission with temperature. Scatters: data points; solid lines: fitting curves using function of  $E(T) = E(0) - \alpha T^2 / (T + \delta)$ , where  $E(0)$  is the bandgap at 0 K,  $\alpha$  represents the linear shift of  $E(T)$  at high temperature, and  $\delta$  stands for the quadratic variation of  $E(T)$  at low temperature. (c) PL intensity of FX, DAP and BX emission as a function of temperature. Scatters: data points; solid lines: fitting curve using a function of  $I(T) = I_0 / (1 + C e^{-\Delta E / k_B T})$ , where  $I_0$ ,  $C$  and  $k_B$  represent the PL intensity at 0 K, a constant and the Boltzmann constant, respectively. The activate energies  $\Delta E$  of FX, DAP and BX are  $29.0 \pm 6.7$ ,  $23.3 \pm 3.9$  and  $25.1 \pm 10.3$  meV, respectively.



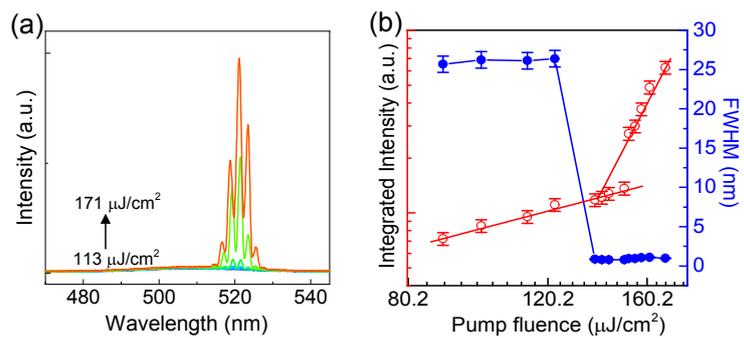
**Fig. S4** Temperature-dependence FWHM of a typical CdS microflake. Scatters: data points; solid and dashed lines: fitting curve using Boson model  $\Gamma(T) = \Gamma_{\text{inh}} + \sigma T + \Gamma_{\text{LO}} / (e^{E_{\text{LO}}/k_B T} - 1)$ , where  $\Gamma_{\text{inh}}$  the inhomogeneous broadening factor,  $\sigma$  is exciton-longitudinal acoustic phonon coupling coefficient,  $\Gamma_{\text{LO}}$  is exciton-longitudinal optical (LO) phonon coupling coefficient, and  $E_{\text{LO}}$  is phonon energy.



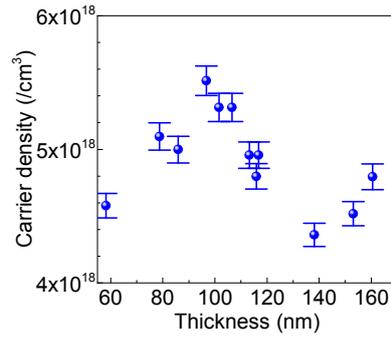
**Fig. S5** (a) Normalized PL spectra of CdS microflakes with thickness from 7.5 to 48.1 nm at a fixed average power density of  $1.0 \text{ MW/cm}^3$  under 405 nm laser. (b) Plot of integrated PL intensity of BX emission of the CdS microflakes in (a).



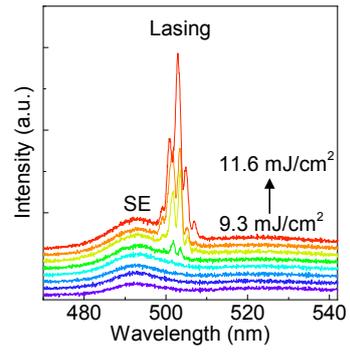
**Fig. S6** Photon-generated carrier density dependence of the initial time PL intensity ( $I_{PL}(t=0)$ ) of CdS with thickness of 10, 28, 46, 68, 88, and 124 nm, respectively, following excitation at 400 nm (80 MHz, 140 fs).



**Fig. S7** (a) The evolution from spontaneous emission to lasing in a typical CdS microflake using 400 nm pulse laser as excitation source. The pumping fluence increased from 113 to 171  $\mu\text{J}/\text{cm}^2$ . (b) Power-dependence of the integrated PL intensity and FWHM of the microflake as a function of power fluence, which gives a threshold of  $\sim 137.8 \mu\text{J}/\text{cm}^2$ .



**Fig. S8** The calculated photo-generated carrier density under pulsed 800 nm laser at lasing threshold for CdS microflakes with different thicknesses (blue scatters).



**Fig. S9** Emission spectra of microflake (thickness:  $46.0 \pm 0.3$  nm) with a threshold of  $10.8$  mJ/cm<sup>2</sup> at pump fluences from  $9.3$  to  $11.6$  mJ/cm<sup>2</sup>.

### Supplementary Note 1: Estimation of average power density, carrier density and defect density

The average power density  $P_{ave}$  in CdS microflakes can be expressed as:

$$P_{ave} = P(1 - R)(1 - \exp(-\alpha d))/(\pi r^2 d)$$

where  $P$  is excitation power,  $r = 1 \mu\text{m}$  is laser spot,  $R = 0.2$  is the reflection coefficient of CdS,  $d$  is the thickness of the microflakes, and  $\alpha \sim 1.2 \times 10^5 \text{ cm}^{-1}$  is the absorption coefficient of CdS at 405 nm. For a fixed average power density of  $1.0 \text{ MW/cm}^3$ , the  $P$  are 30.3, 46.5, 66.7, 92.7, and  $196.9 \mu\text{W}$  for CdS microflakes with thicknesses of 7.5, 11.5, 16.5, 22.9, and 48.1 nm, respectively.

For photon-generated carrier density excitation by pulsed laser,<sup>5</sup>

$$N = \frac{E_{ave} \cdot (1 - R)}{2 \cdot \hbar \cdot \omega \cdot d} \cdot (1 - \exp(-\alpha P_{peak} \cdot d))$$

where  $R = 0.2$  is the reflection coefficient of CdS,  $d$  is the thickness of the microflakes,  $\hbar\omega$  is the incident photon energy,  $E_{ave}$  is average pump energy ( $\text{mJ/cm}^2$ ),  $P_{peak} = P_{ave} f_{pump} / \Delta t$  is peak pump power ( $\text{GW/cm}^2$ ),  $P_{ave}$  is average pump power,  $f_{pump}$  is repetition rate,  $\Delta t$  is pulse duration, and  $\alpha$  is absorption coefficient ( $2.7 \text{ cm/GW}$  for two photon absorption at 800 nm).<sup>6</sup> The photon-generated carrier density is an order of  $10^{18} \text{ cm}^{-3}$  at threshold under pulsed 800 nm laser (1 kHz, 80 fs) (Fig. S8).

The initial time PL intensity ( $I_{PL}(t = 0)$ ) could be expressed as:<sup>7</sup>

$$I_{PL}(t = 0) = k_1 n(0) + \frac{k_2 n^2(0)}{n_t} + n(0)(k_1 - k_2) e^{-n(0)/n_t}$$

where  $n(0)$  is the photo-generated carrier density,  $n_t$  is the defect density,  $k_1$  and  $k_2$  are the exciton and defect recombination coefficients. Fitting the  $I_{PL}(t = 0)$  with the equation, as shown in Fig. S6, the defect density of CdS microflakes with thickness of 10, 28, 46, 68, 88, 124 nm are estimated to be around  $1.0 \times 10^{15}$ ,  $1.2 \times 10^{15}$ ,  $2.2 \times 10^{15}$ ,  $3.9 \times 10^{15}$ ,  $4.1 \times 10^{15}$  and  $4.2 \times 10^{15} \text{ cm}^{-3}$ , respectively.

## References

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