

# **An optical perspective on the thermal-activated ionic migration state and ionic jumping distance in glass**

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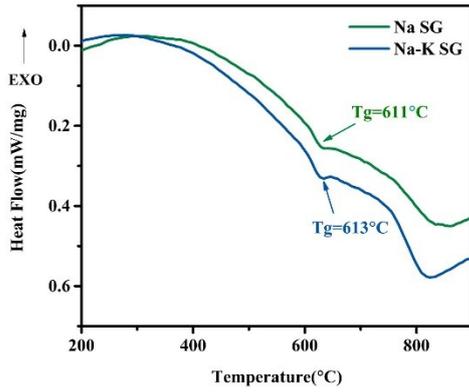


Fig. S1 DSC curves of the Na SG and the K-Na SG.

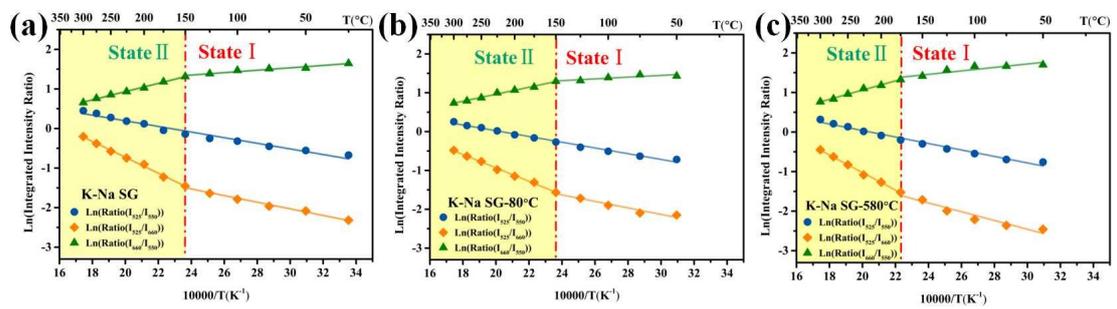


Fig. S2 The Ln~1/T plot of the (a) K-Na SG, (b) K-Na SG-80 °C and (c) K-Na SG-580 °C.

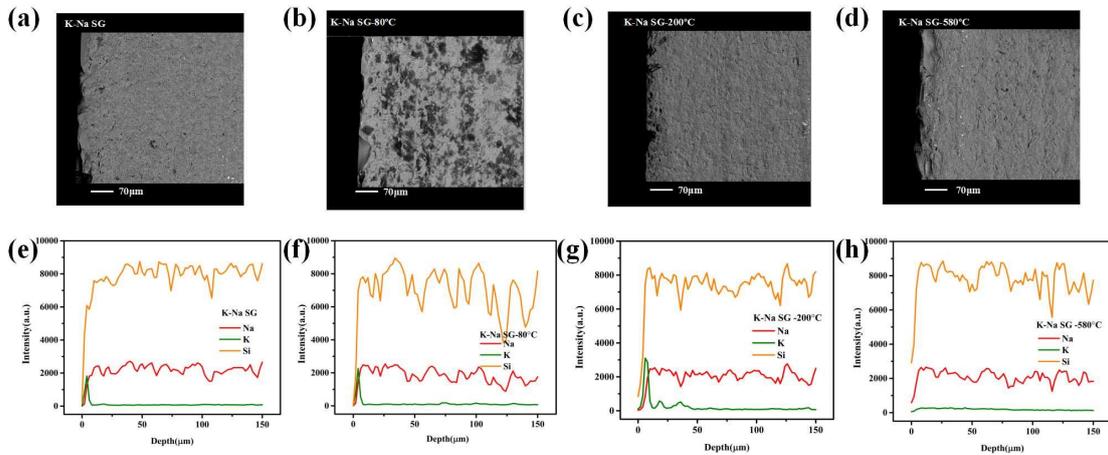


Fig. S3 EPMA images and the elemental line-scanning images of the (a, e) K-Na SG, (b, f) K-Na SG-80 °C, (c, g) K-Na SG-200 °C, and (d, h) K-Na SG-580 °C.

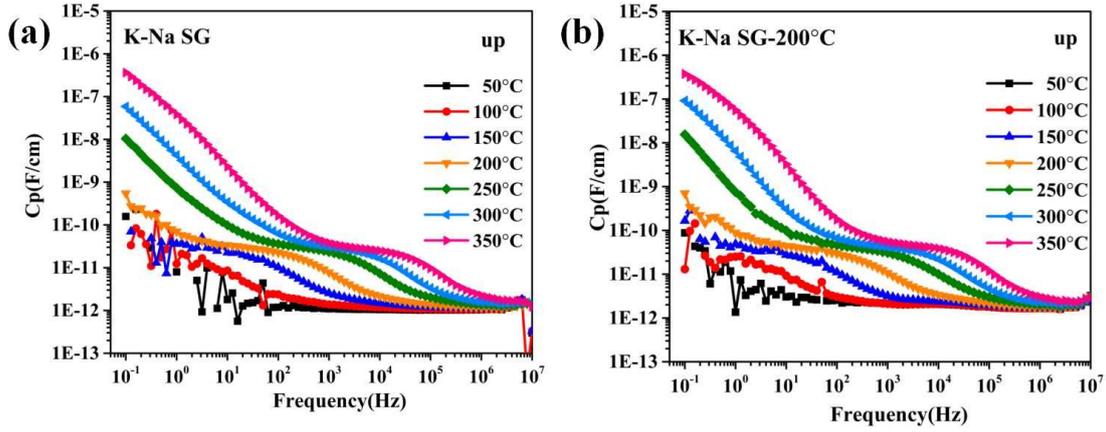


Fig. S4 Permittivity of (a) K-Na SG and (b) K-Na SG-200 °C as a function of frequency at different temperatures.

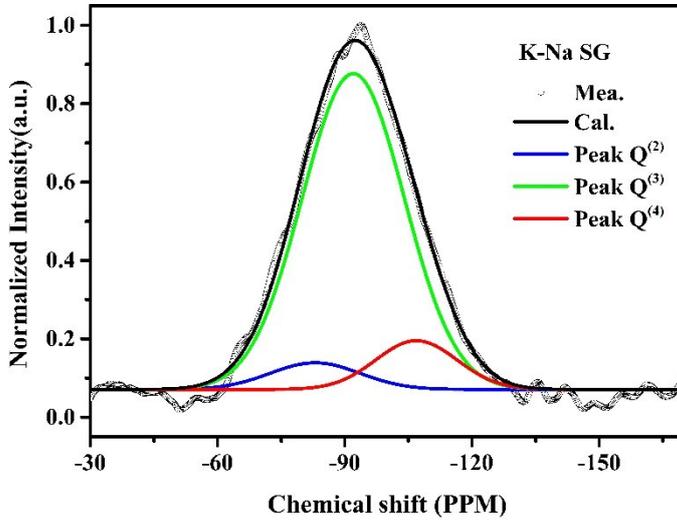


Fig. S5  $^{29}\text{Si}$  MAS NMR spectra of K-Na glass samples (circles), the integrated areas (black line) and the Gaussian fits for each site.

The specific calculation process for the initial distance  $D$  between mobile  $\text{Na}^+$  and  $\text{Er}^{3+}$ :

$$\begin{aligned}
 W(\text{K}_2\text{O}) &= 19.08\% & W(\text{Er}_2\text{O}_3) &= 2.85\% & \rho &= 2.79 \text{ g/cm}^3 \\
 N(\text{Na}^+) &= 2N_A \frac{\rho \cdot W(\text{Na}_2\text{O})}{M(\text{Na}_2\text{O})} \\
 &= 2 * 6.02 * 10^{23} (\text{/mol}) * \frac{2.79(\text{g/cm}^3) * 0.1908}{61.97(\text{g/mol})} \\
 &= 1.03 * 10^{22} (\text{ion/cm}^3) \\
 N(\text{Er}^{3+}) &= 2N_A \frac{\rho \cdot W(\text{Er}_2\text{O}_3)}{M(\text{Er}_2\text{O}_3)} \\
 &= 2 * 6.02 * 10^{23} (\text{/mol}) * \frac{2.79(\text{g/cm}^3) * 0.0285}{382.51(\text{g/mol})} \\
 &= 2.50 * 10^{20} (\text{ion/cm}^3) \\
 N(\text{Na}^+) + N(\text{Er}^{3+}) &= 1.06 * 10^{22} (\text{ion/cm}^3)
 \end{aligned}$$

$$\frac{1}{N(\text{Na}^+) + N(\text{Er}^{3+})} = 9.434 * 10^{-23}(\text{cm}^3/\text{ion}) = 94.34(\text{\AA}/\text{ion})$$

$$\frac{4}{3}\pi r^3 = 94.34(\text{\AA})$$

$$r = 2.8(\text{\AA})$$

$$D = 2r = 5.6(\text{\AA})$$

**Table S1** The jump distance  $d$  calculated by using the conductivity at different temperatures

| Glass sample          | The jump distance $d$ at different temperatures ( $\text{\AA}$ ) |       |       |       |       |       | average    |
|-----------------------|--|-------|-------|-------|-------|-------|------------|
|                       | 250°C  | 300°C | 350°C | 400°C | 450°C | 500°C |            |
| <b>Na SG</b>          | 1.9  | 1.7   | 1.4   | 1.5   | 1.7   | 2.3   | <b>1.8</b> |
| <b>K-Na SG</b>        | 2.0  | 1.7   | 2.0   | 1.9   | 1.8   | 1.8   | <b>1.9</b> |
| <b>K-Na SG-200 °C</b> | 2.1  | 1.9   | 2.1   | 2.0   | 2.0   | 2.0   | <b>2.0</b> |